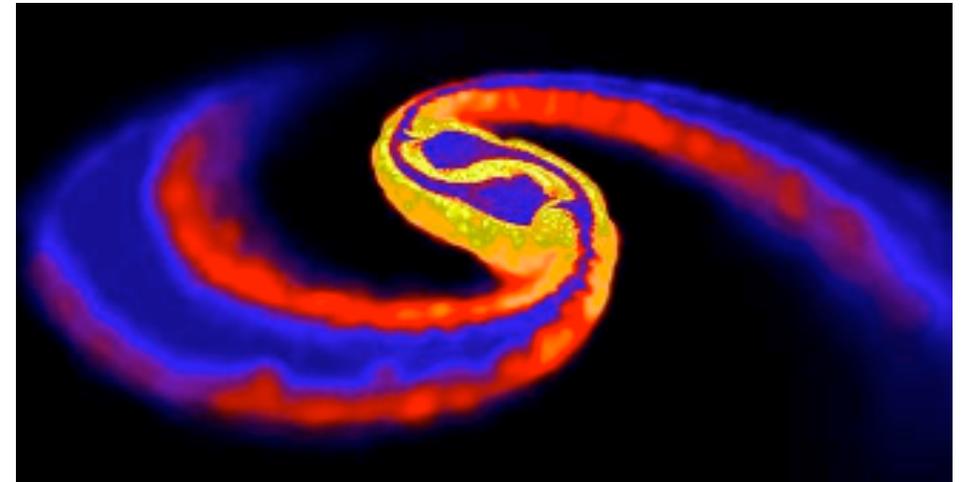


# Compact Binary Mergers, Nuclear EOS, and LIGO

- GWs and LIGO
- Compact binary mergers
- prospects for LIGO GW detection and EM counterparts
- Neutron stars
- Nuclear EOS
- Neutron star mass & radius
- BNS mergers
- BNS r-process nucleosynthesis
- BNS merger constrains on NEOS



*"Merging Neutron Stars" (Price & Rosswog)*

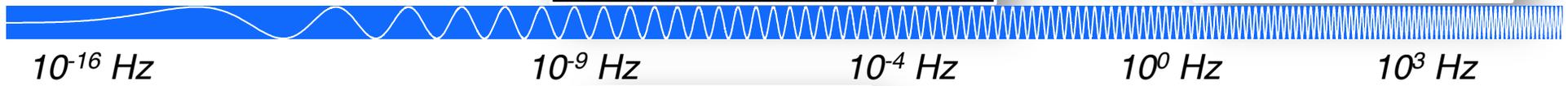
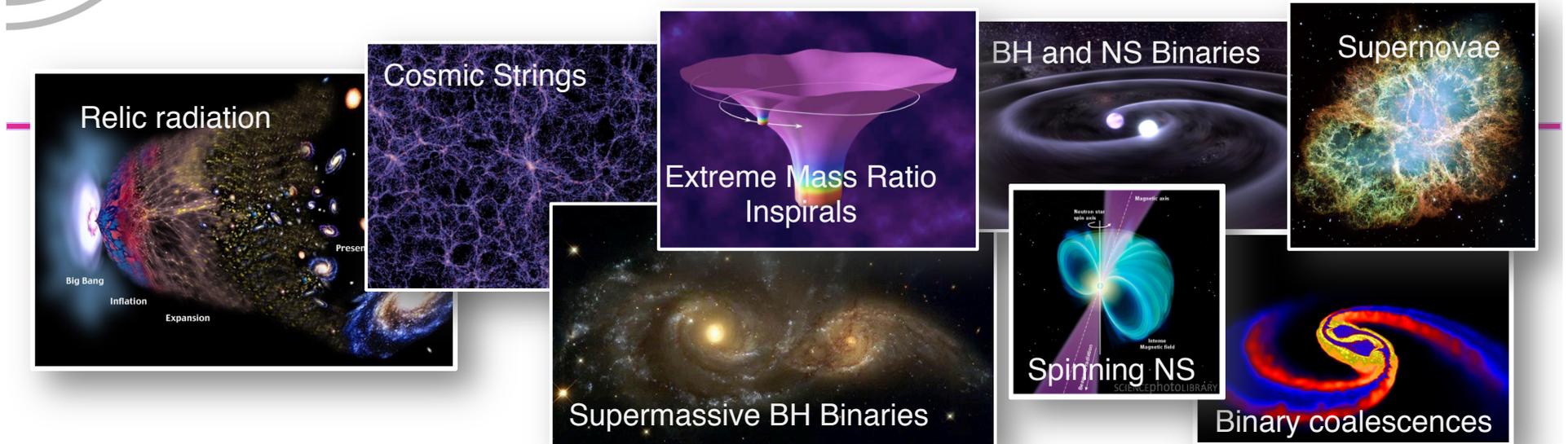


Alan Weinstein, Caltech  
for the LIGO Scientific Collaboration

DOE/NSF NSAC Meeting,  
Bethesda, March 23, 2016

LIGO-G1600723

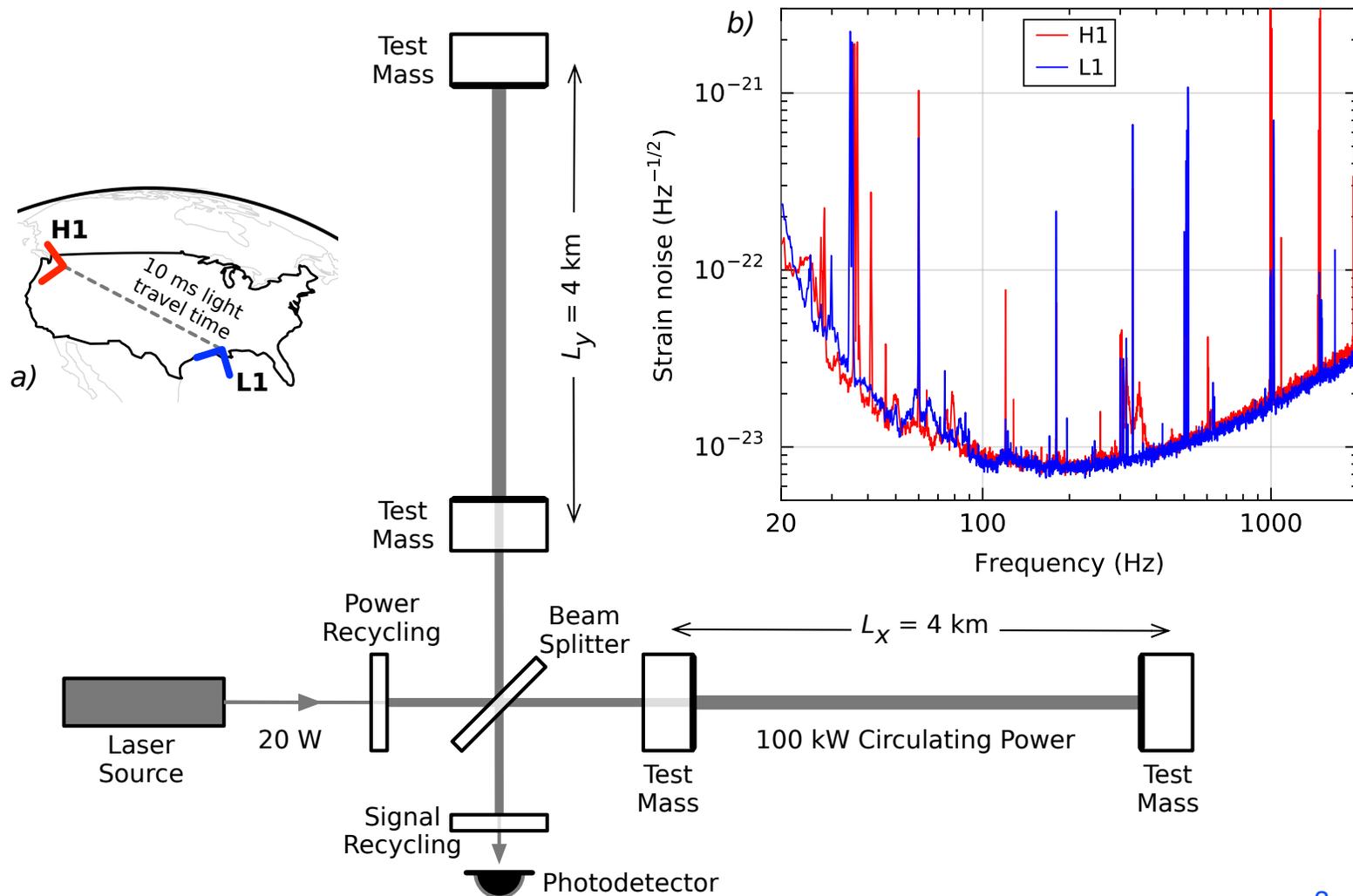
# The GW Spectrum



Inflation Probe      Pulsar timing      Space detectors      Ground interferometers



# The Advanced LIGO detectors



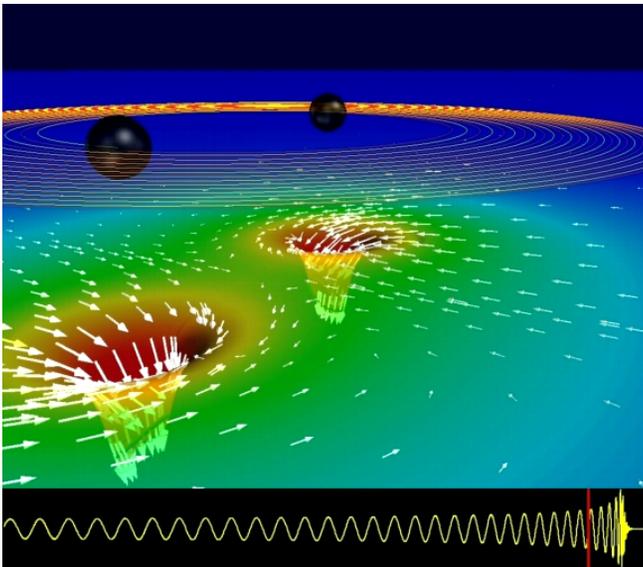
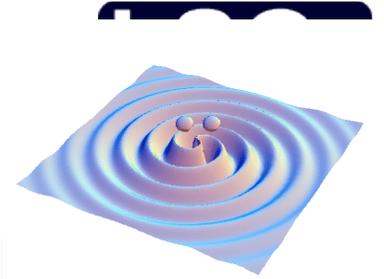




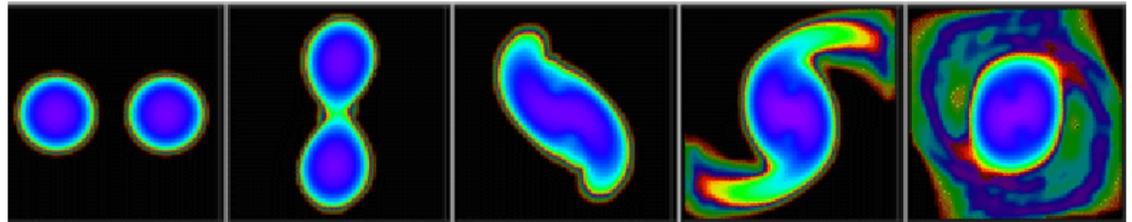


**LIGO**

# GWs from coalescing compact binaries (NS/NS, BH/BH, NS/BH)

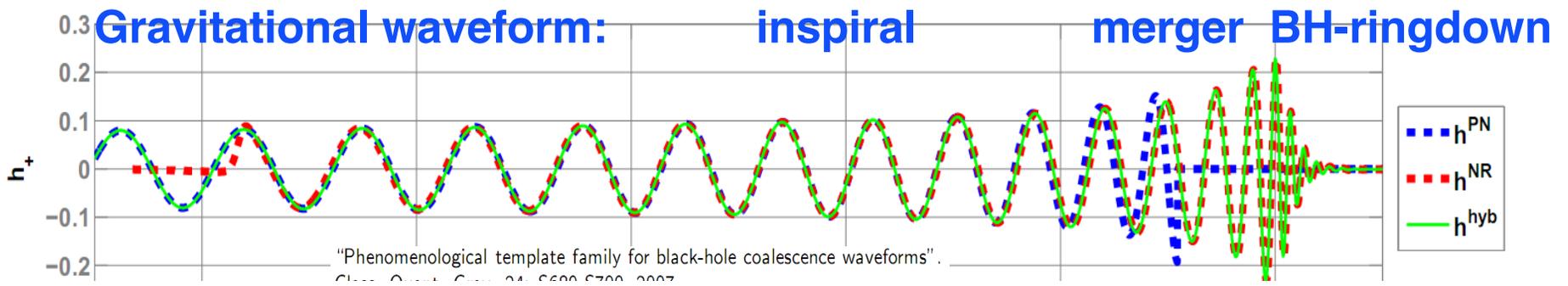


- Neutron star – neutron star (Centrella et al.)



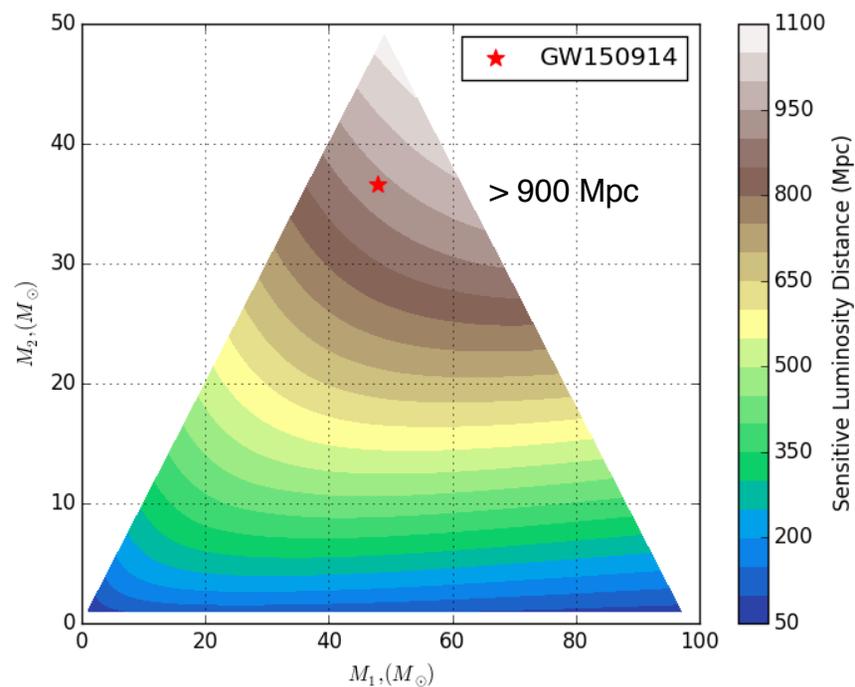
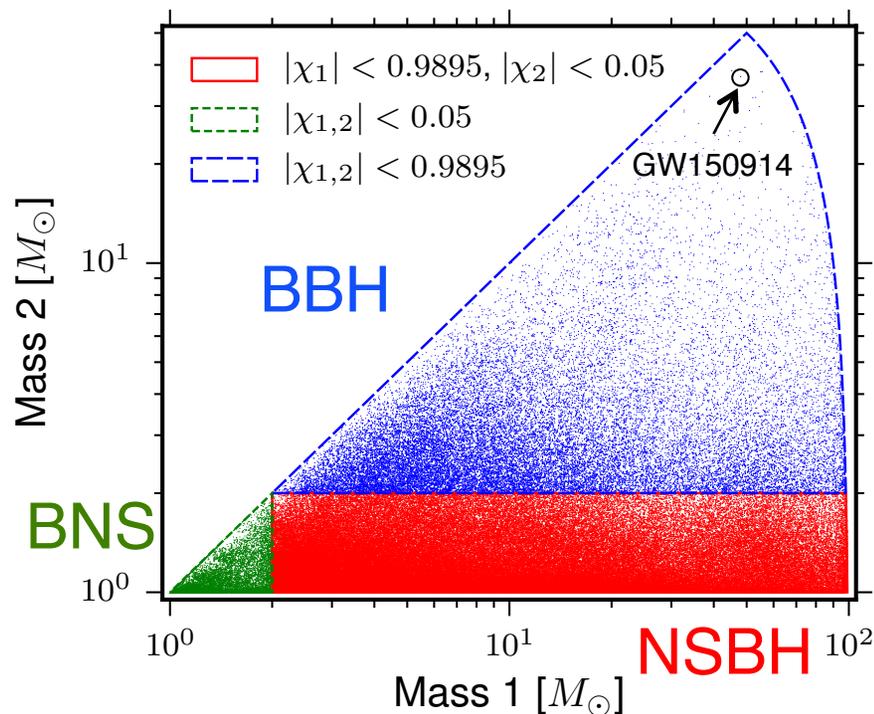
## Tidal disruption of neutron star

A unique and powerful laboratory to study strong-field, highly dynamical gravity and the structure of nuclear matter in the most extreme conditions



**Waveform carries lots of information about binary masses, orbit, merger**

# Template-based searches

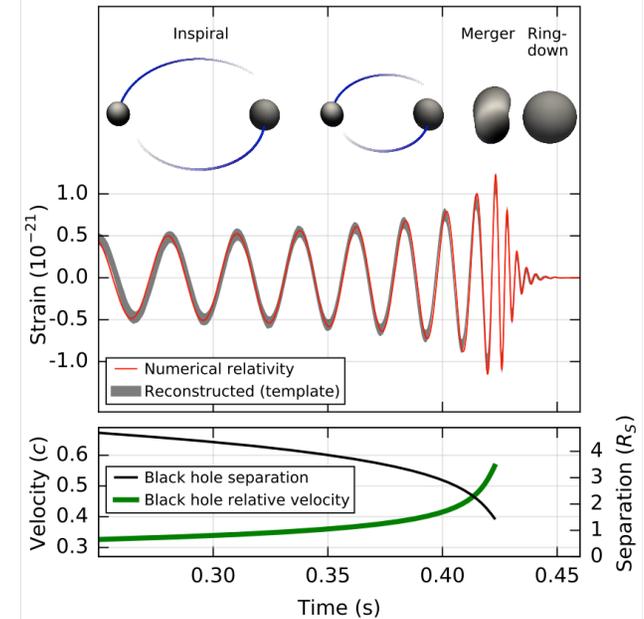
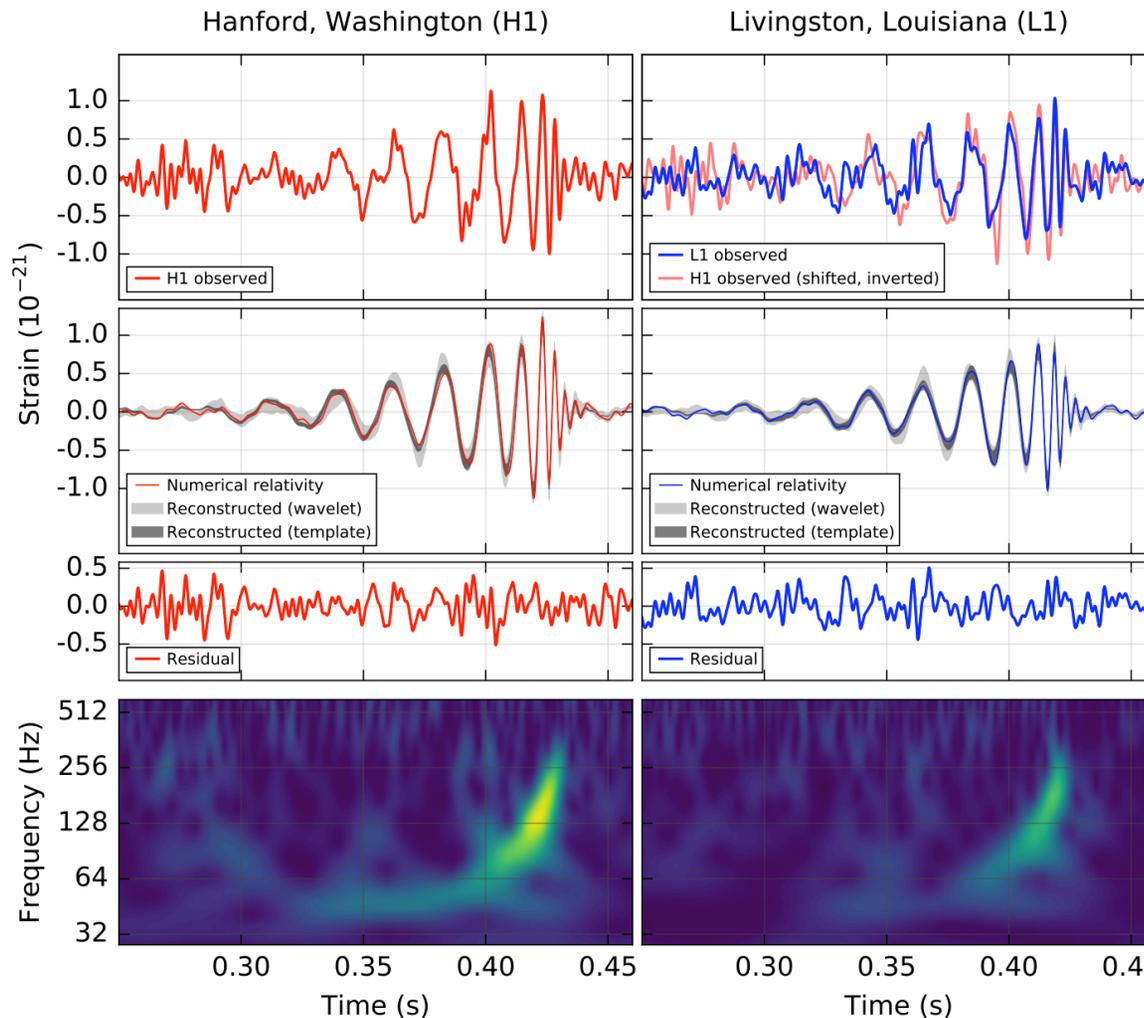


Masses and (aligned) spins  
 Templates spaced for  $< 3\%$   
 loss of SNR: 250K templates.

Sensitive distance in Mpc

# GW150914

Phys. Rev. Lett. 116, 061102 – Published 11 February 2016  
<https://dcc.ligo.org/LIGO-P150914/public/main>



## Reconstructed (no whitening)

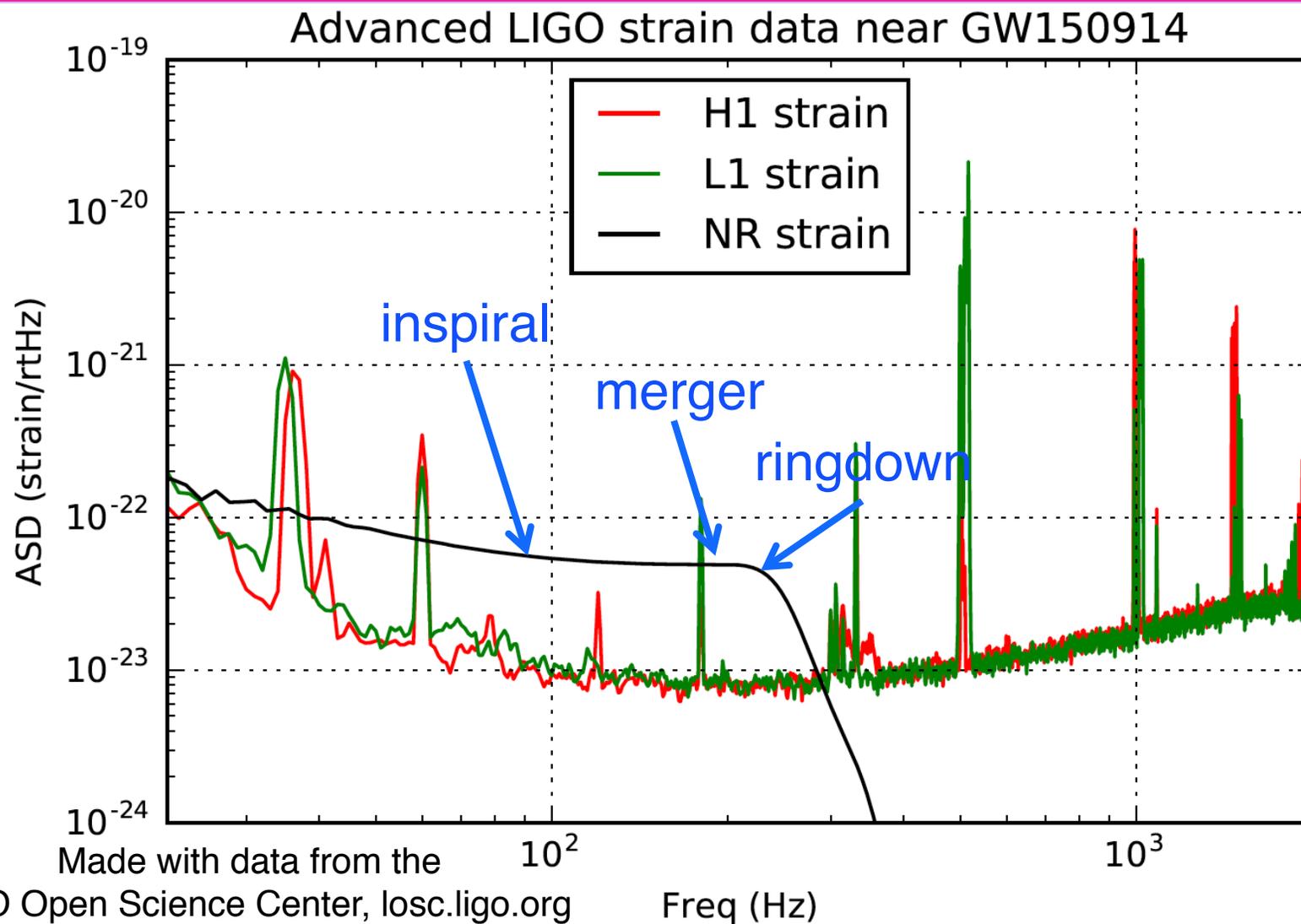
Audio:

- filtered data
- freq-shifted data
- reconstructed & shifted



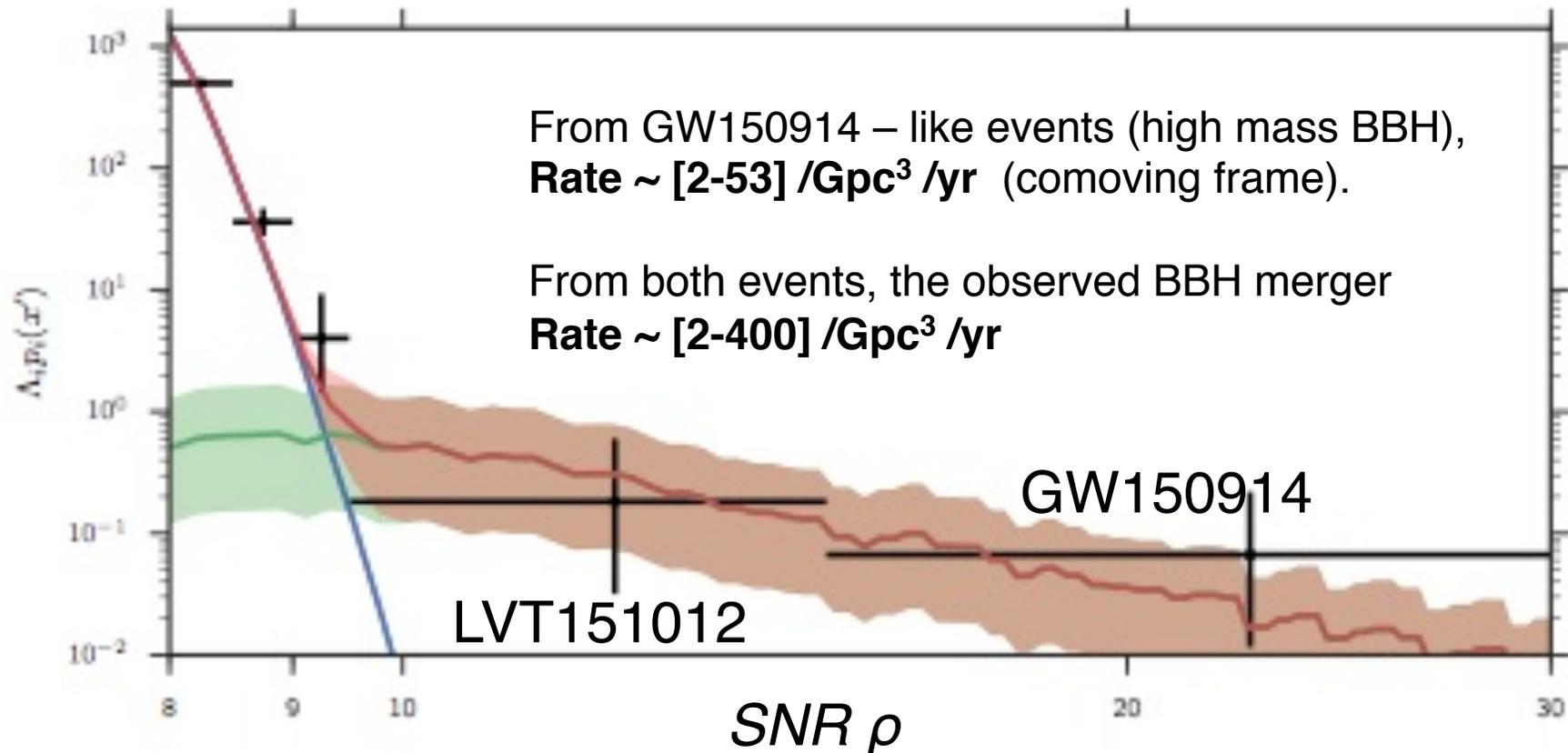
Whitened and band-passed [40-300] Hz

# GW150914 in the frequency domain



# Observed BBH merger rate

<https://dcc.ligo.org/LIGO-P1500217/public/main>

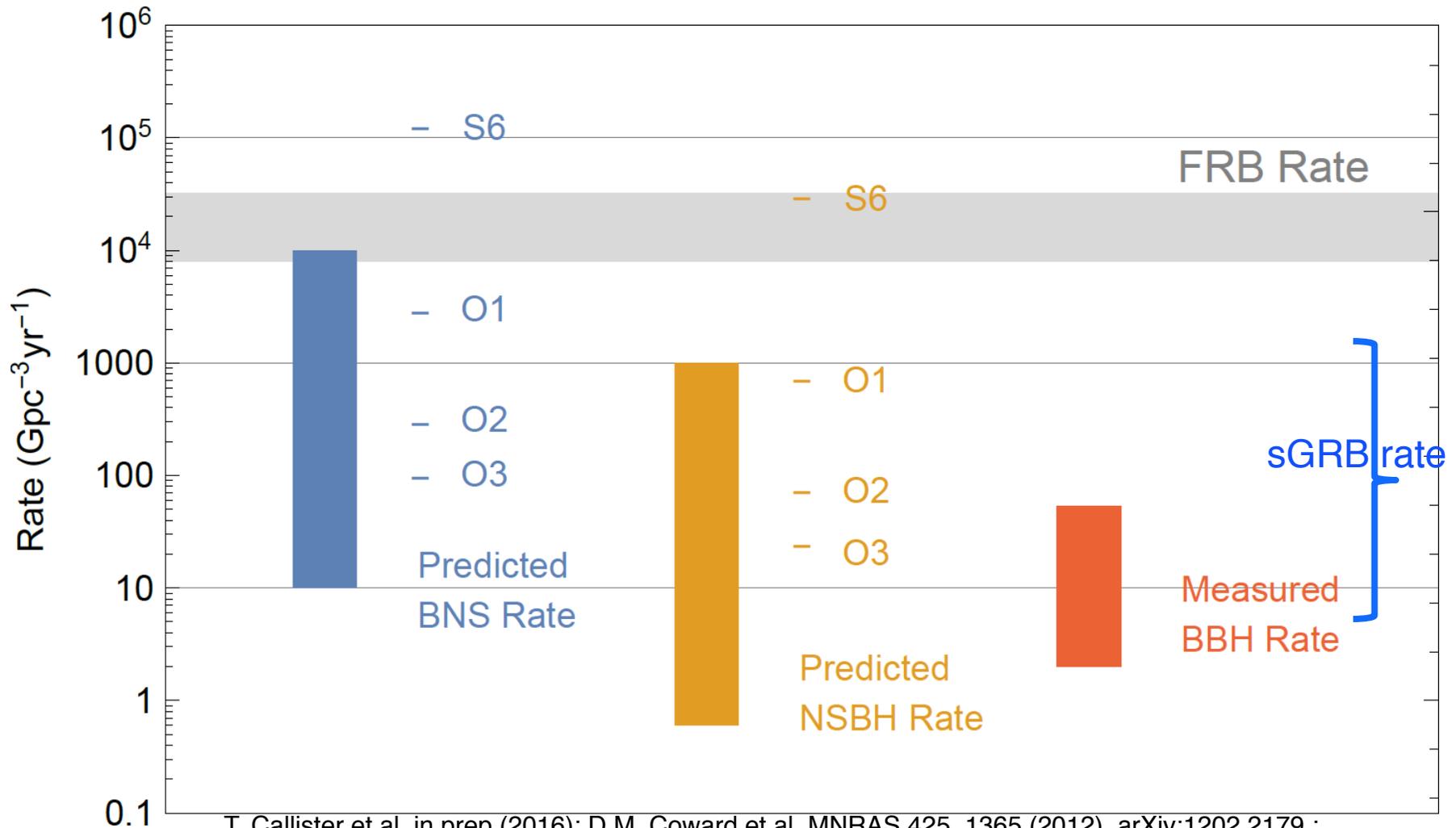


Same ballpark as population synthesis models, CCSN rate, etc

iLIGO+eLIGO BBH rate upper limit:  $\sim < 420 \text{ Gpc}^{-3} \text{ yr}^{-1}$



# Expected (and measured!) compact binary merger rates

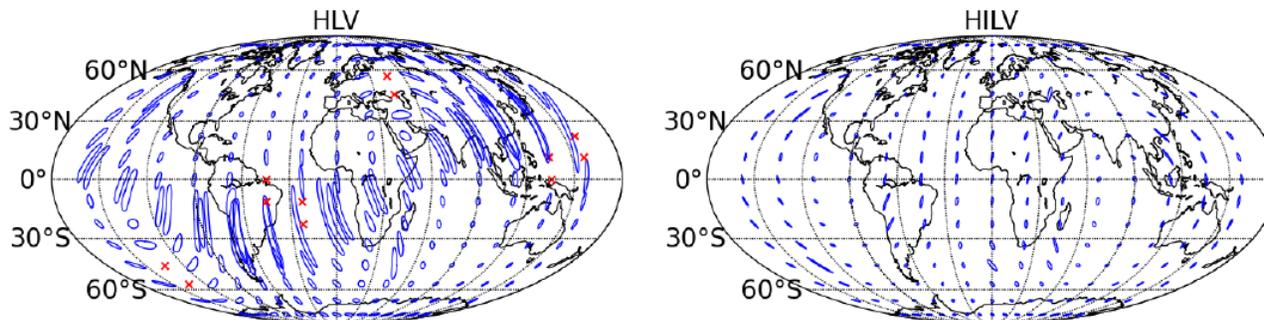


T. Callister et al, in prep (2016); D.M. Coward et al, MNRAS 425, 1365 (2012), arXiv:1202.2179 ;  
B. Abbott et al, Living Rev. Relativity, 19, 1 (2016) arXiv:1304.0670.

# Expected ranges of binary neutron star merger rates and detections

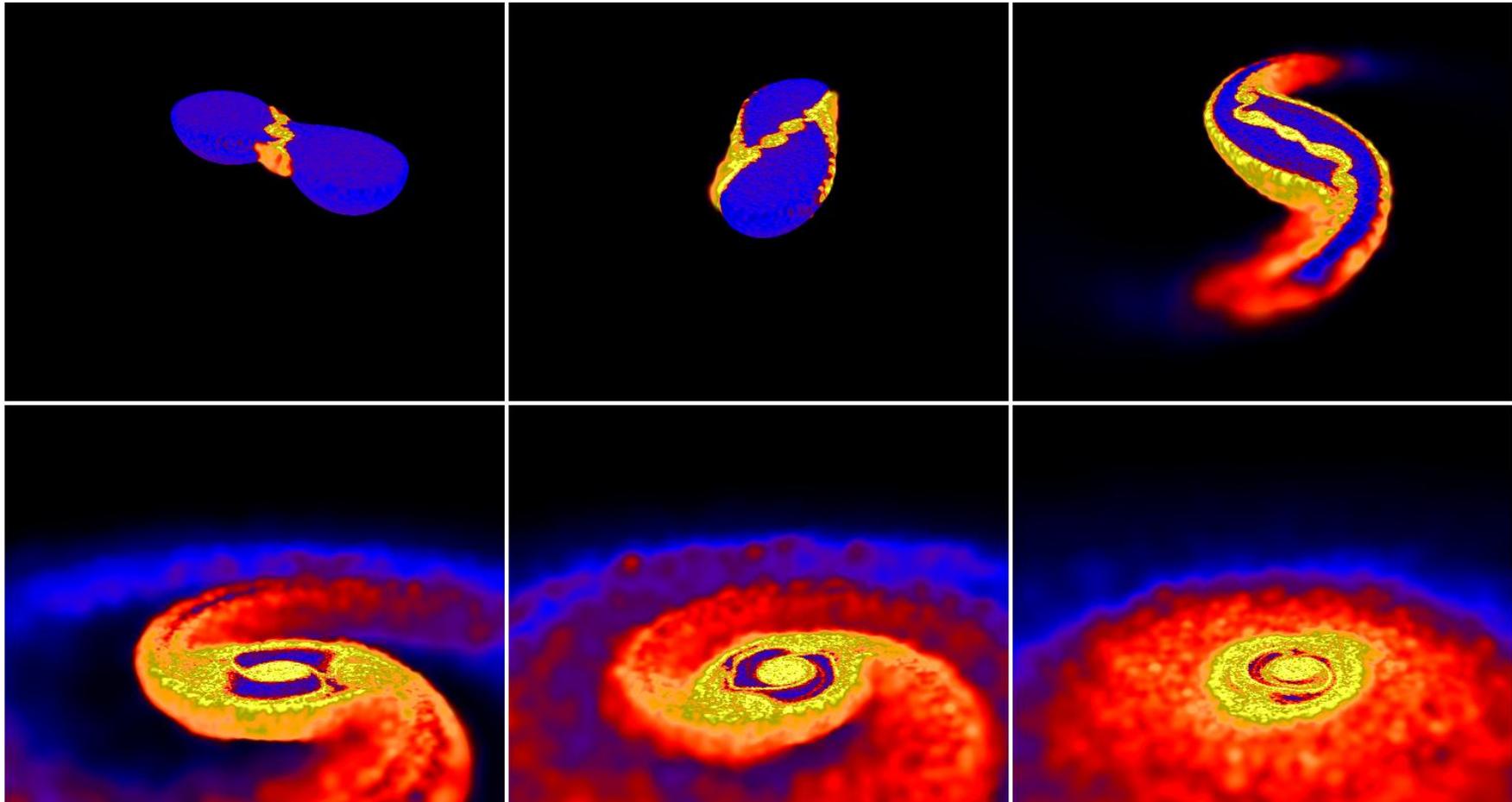
- “It’s tough to make predictions, especially about the future” (Yogi Berra)
- Estimated BNS rate:  $[10^1 - 10^4] \text{ Gpc}^{-3}\text{yr}^{-1}$

Epoch	Estimated Run Duration	BNS Range (Mpc)		Number of BNS Detections
		LIGO	Virgo	
2015	3 months	40 – 80	–	0.0004 – 3
2016–17	6 months	80 – 120	20 – 60	0.006 – 20
2017–18	9 months	120 – 170	60 – 85	0.04 – 100
2019+	(per year)	200	65 – 130	0.2 – 200
2022+ (India)	(per year)	200	130	0.4 – 400

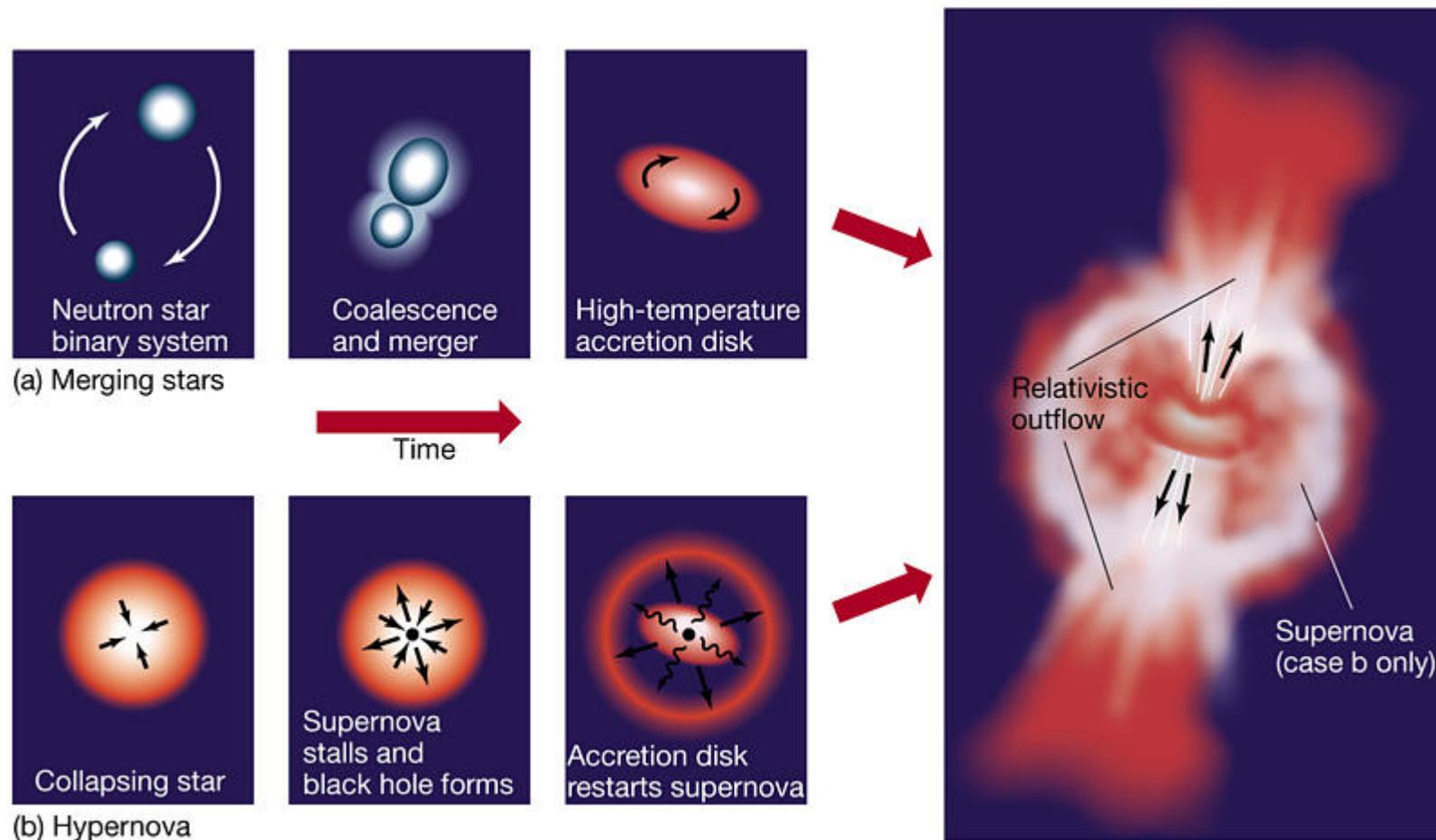


LIGO and Virgo Collaborations,  
 “Prospects for Observing and Localizing  
 Gravitational-Wave Transients with Advanced  
 LIGO and Advanced Virgo”  
*Living Rev. Relativity*, 19, 1 (2016)

# Binary neutron star mergers are a unique laboratory for nuclear (astro)-physics

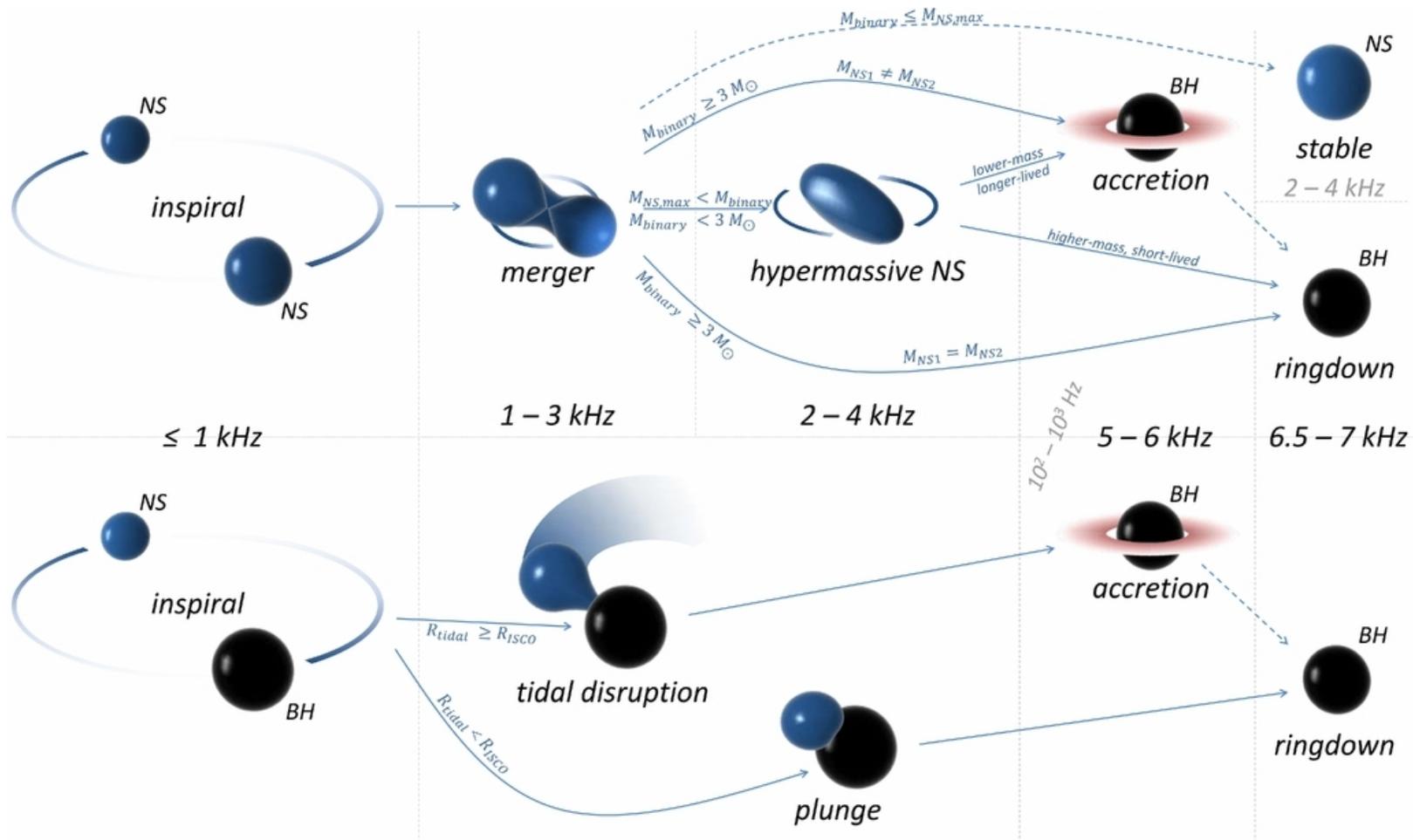


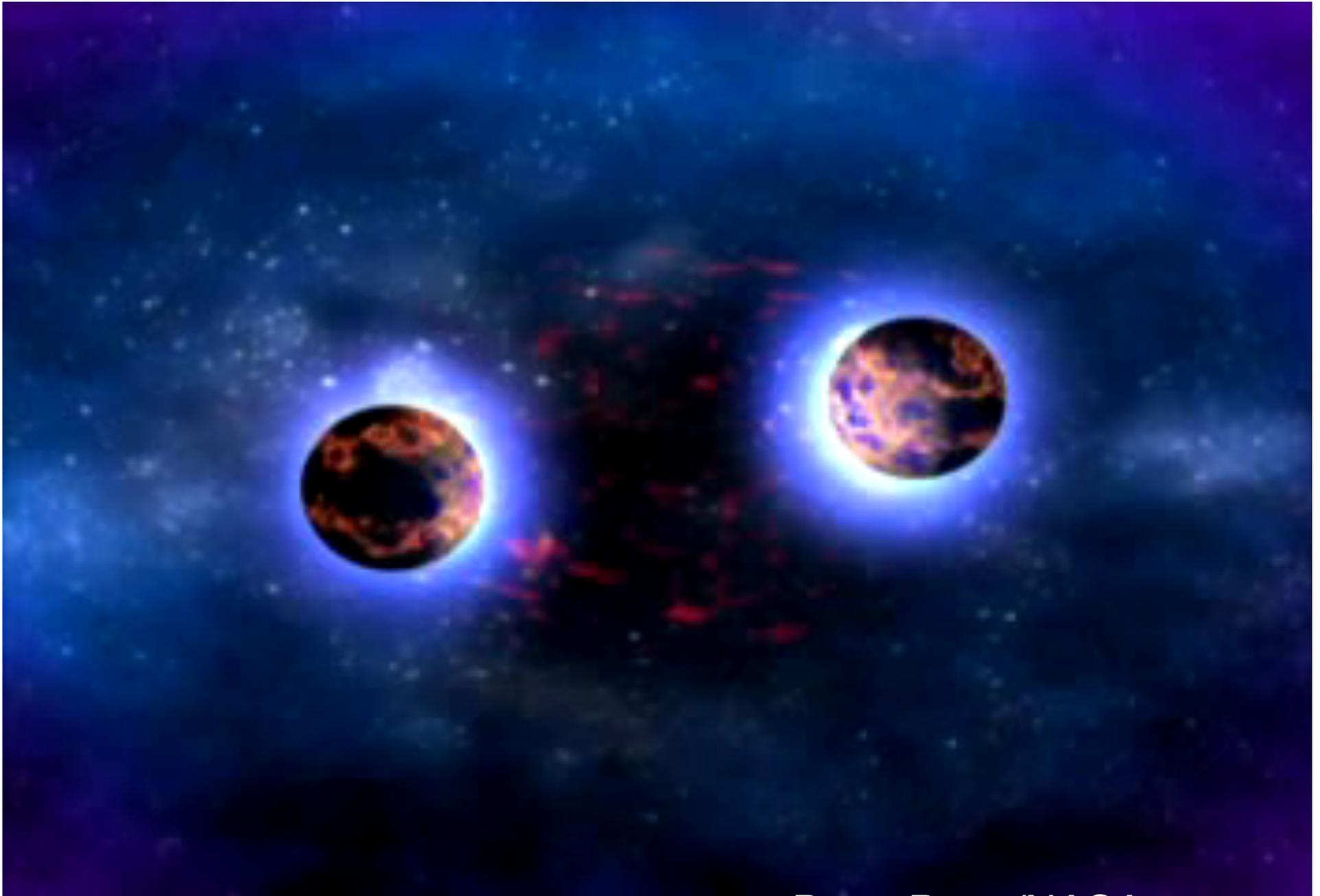
# Short-hard and Long-soft GRBs



# BNS and NSBH mergers

Figure 1 from I Bartos et al 2013 Class. Quantum Grav. 30 123001

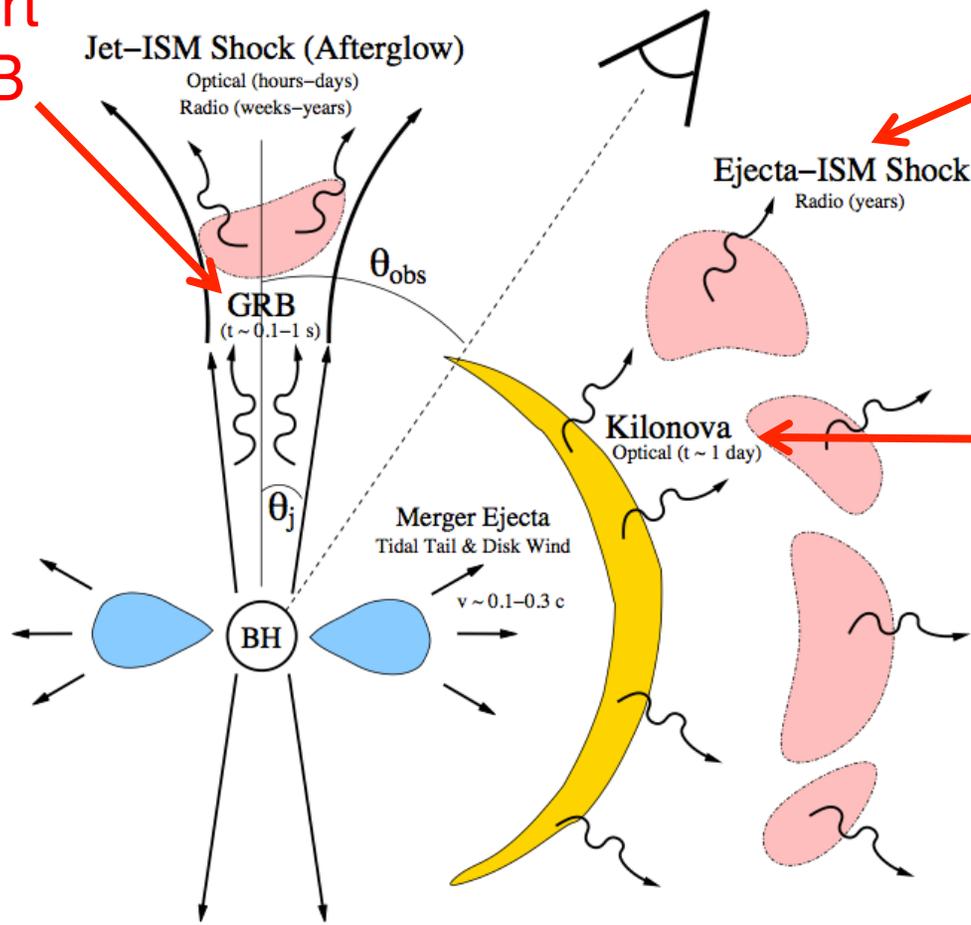




Dana Berry/NASA

# Electromagnetic radiation from sGRB progenitors

Short GRB



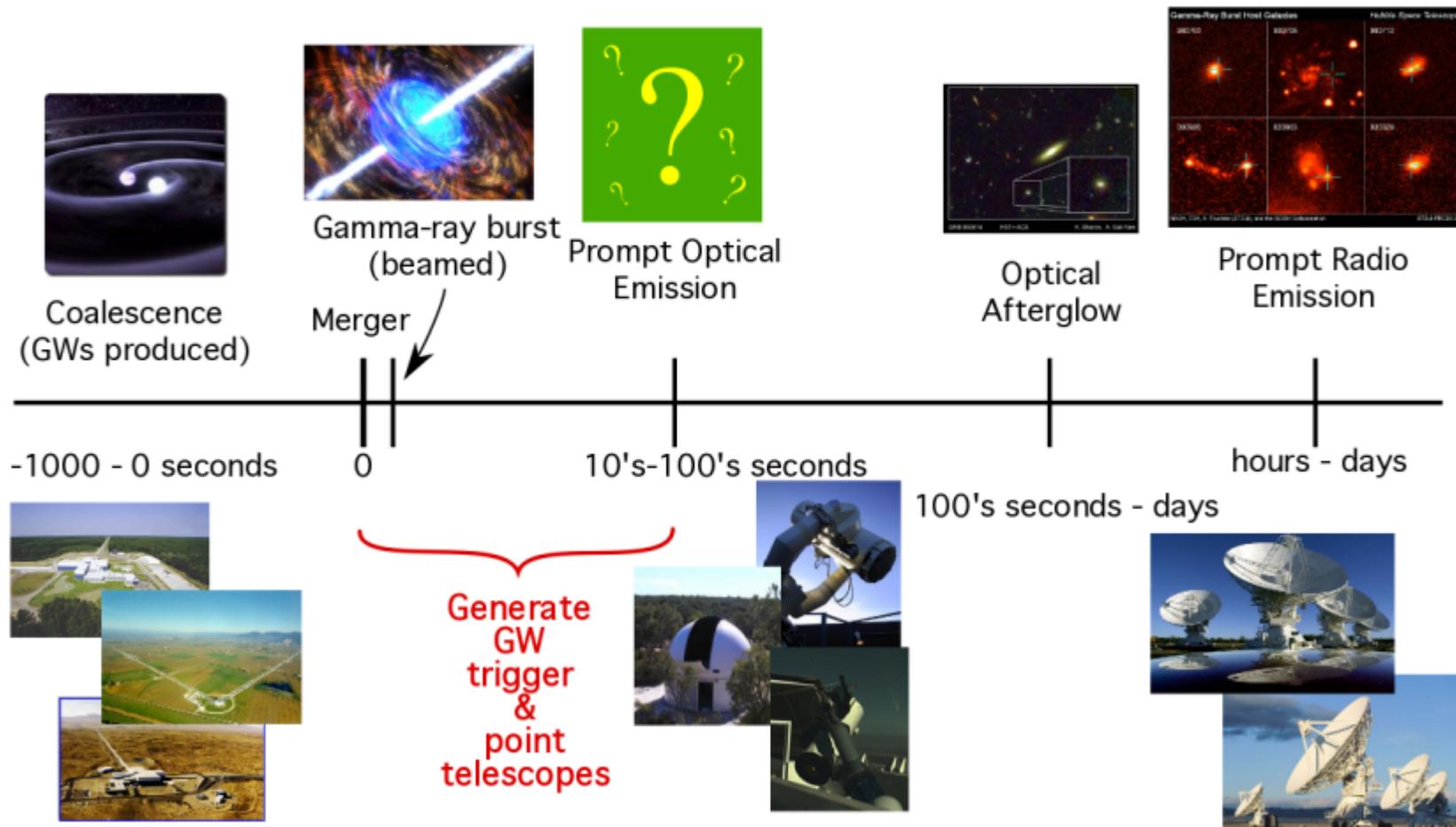
Ejecta-ISM shock  
radio emission  
from days to years

“kilonova”  
Prompt optical emission  
from seconds to days

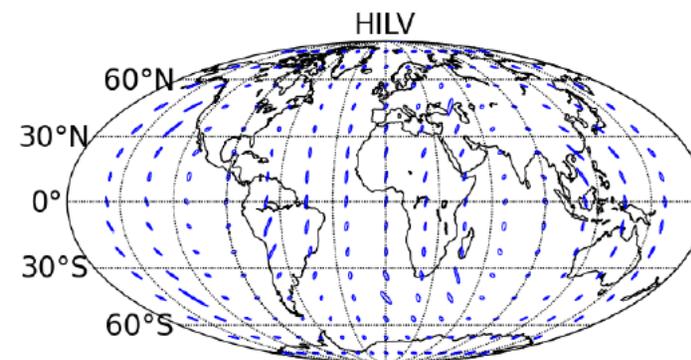
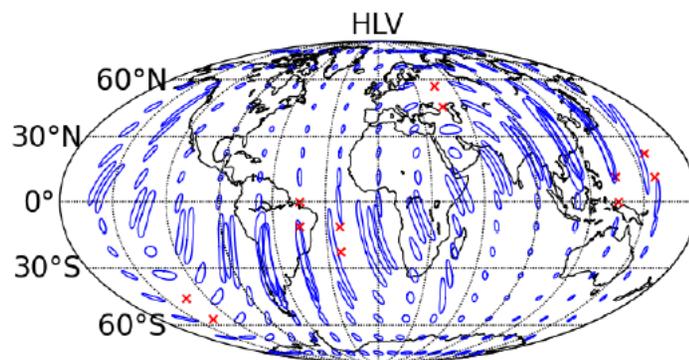
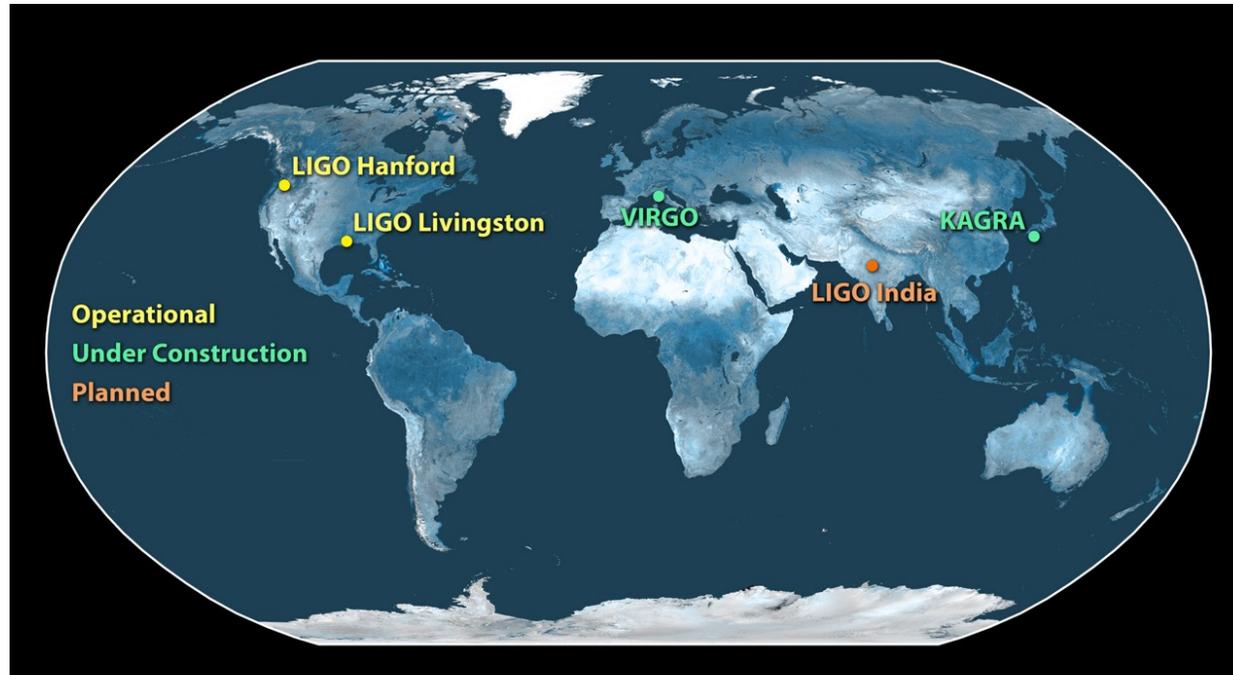
Metzger & Berger 2011

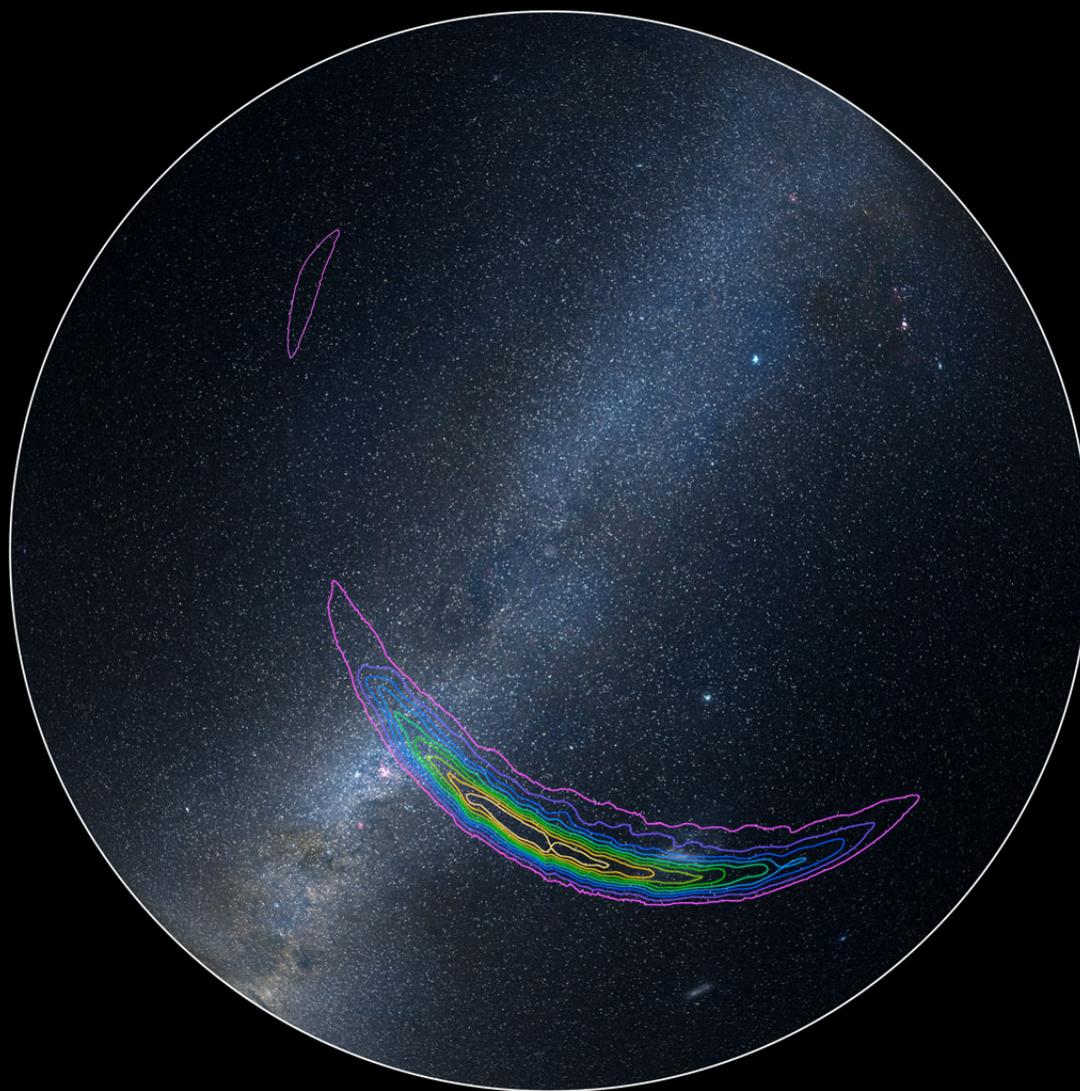
# Low-latency identification of transients for rapid ( $< \sim 100\text{s}$ ) followup

EM counterparts to GW sources (if any) are short-lived and faint

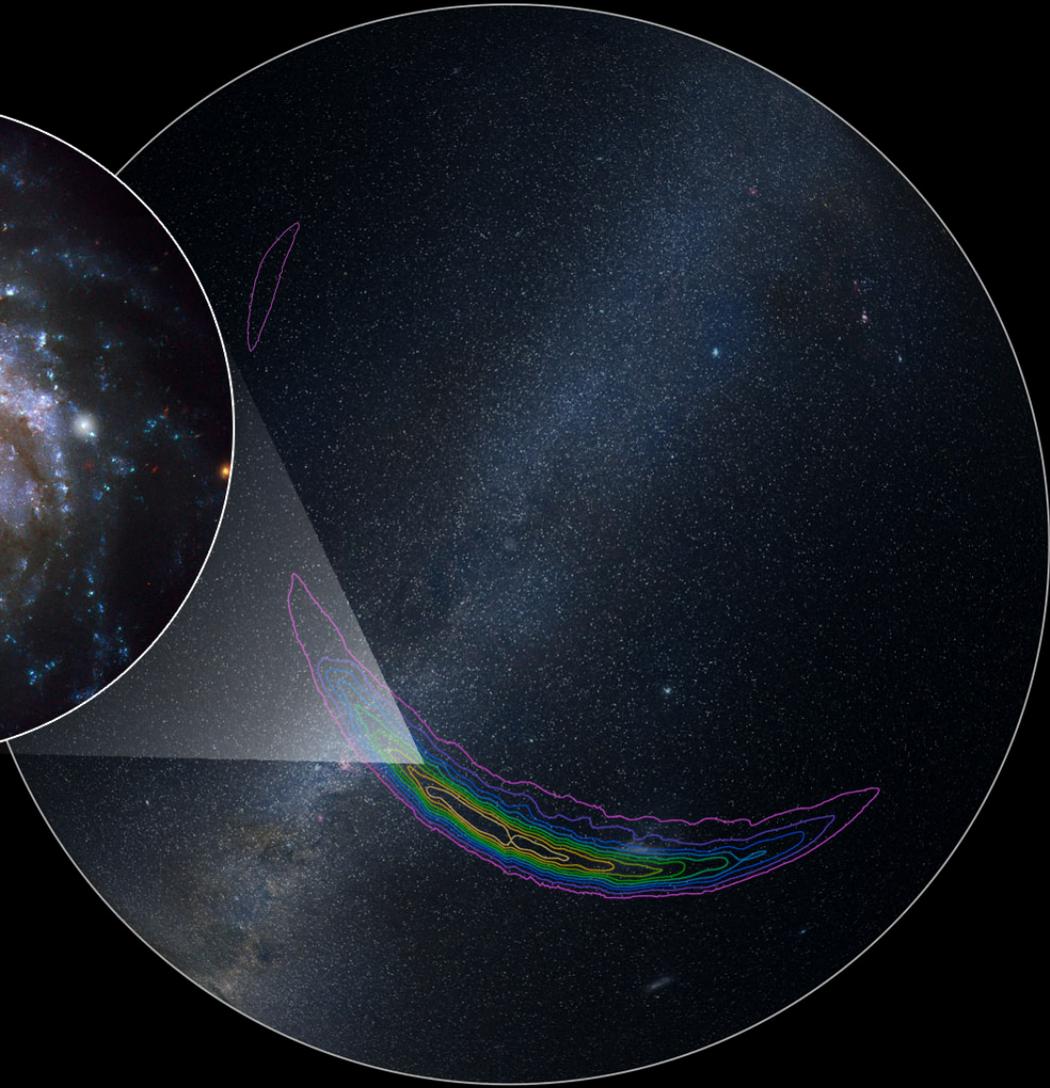


# sky localization with the GW detector network

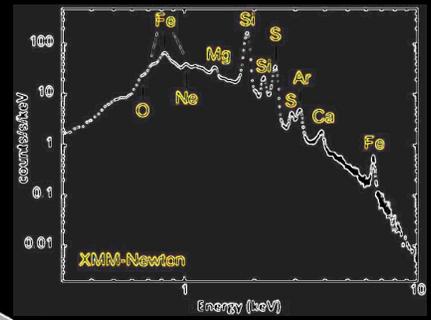
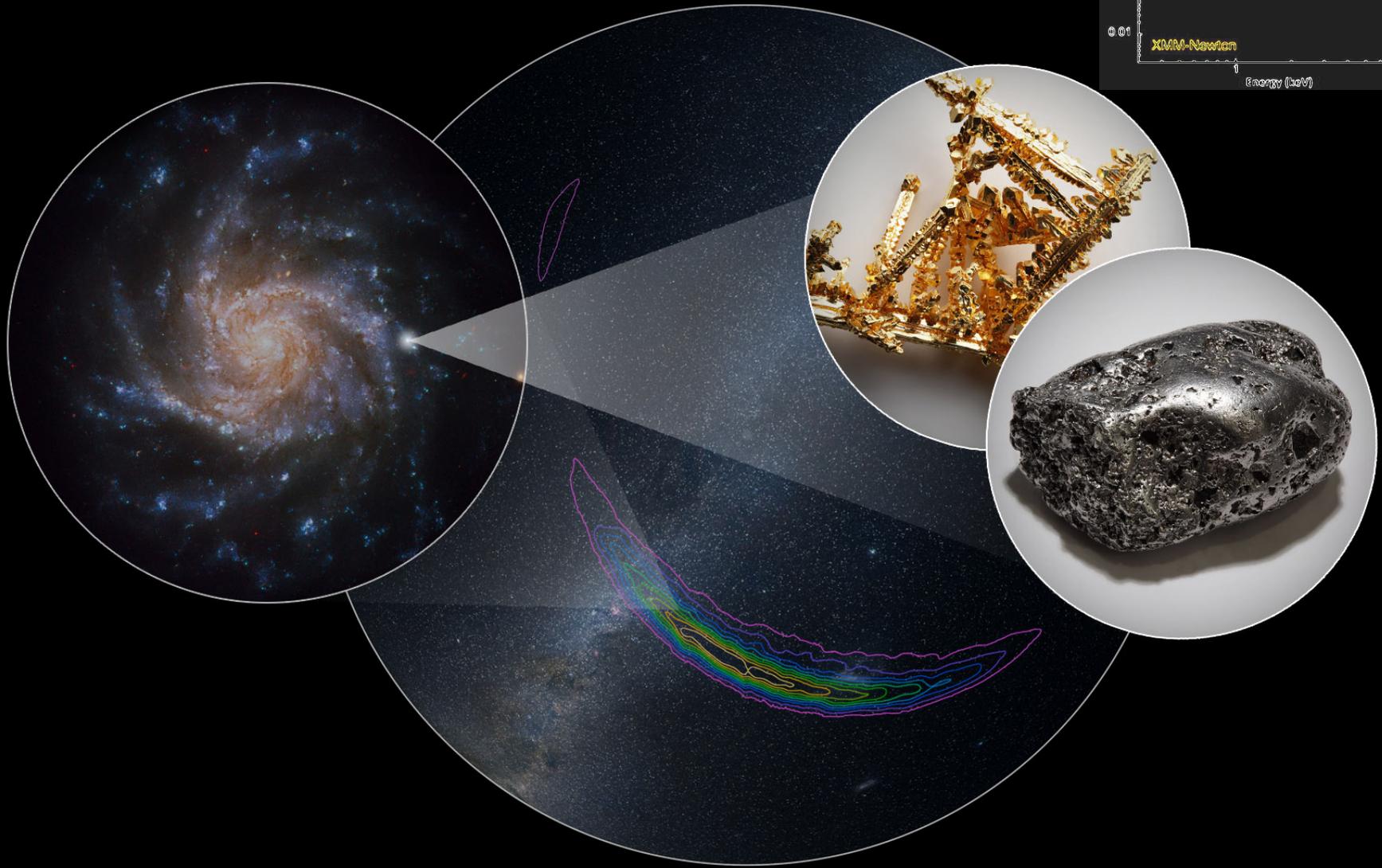




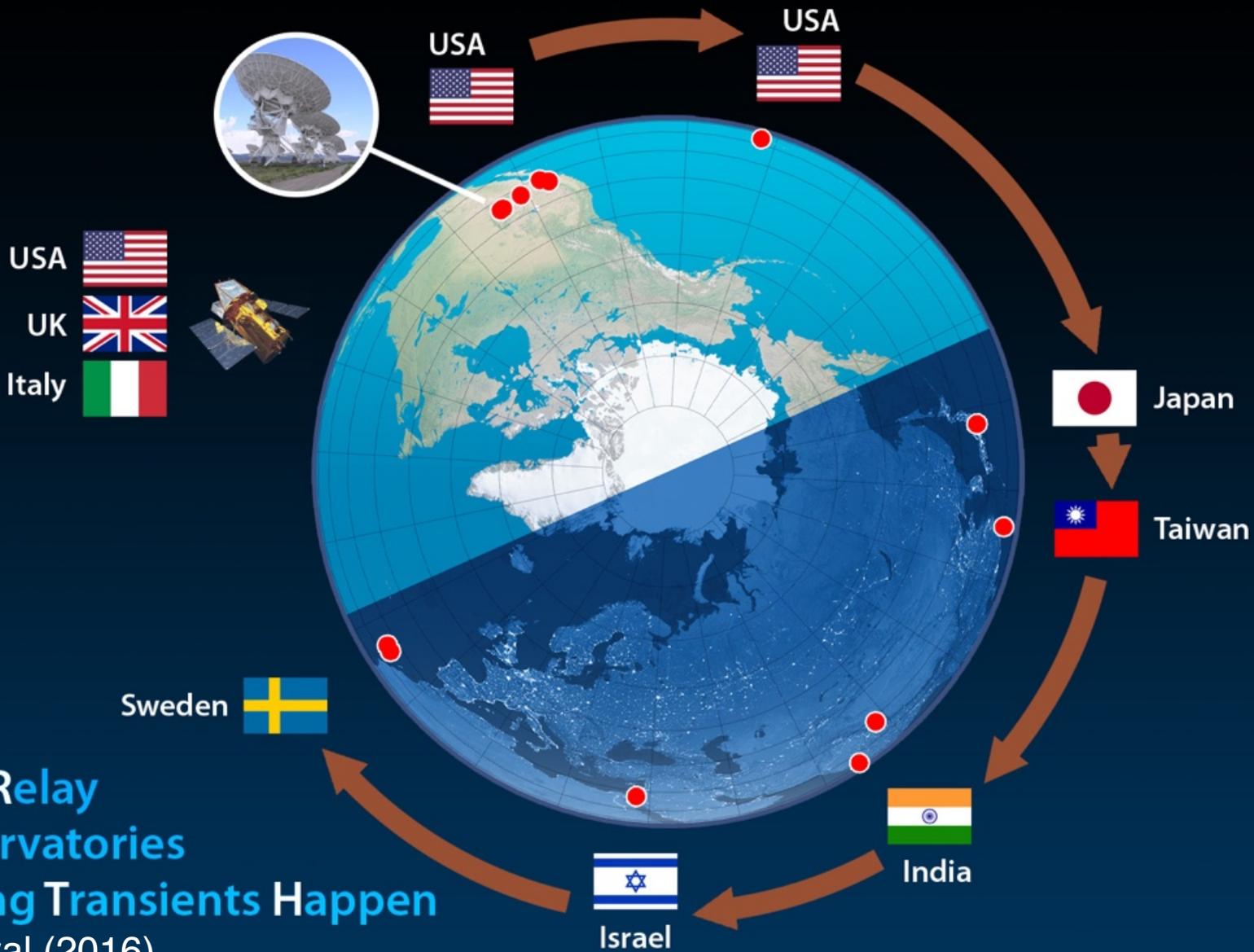
Kasliwal (2016)



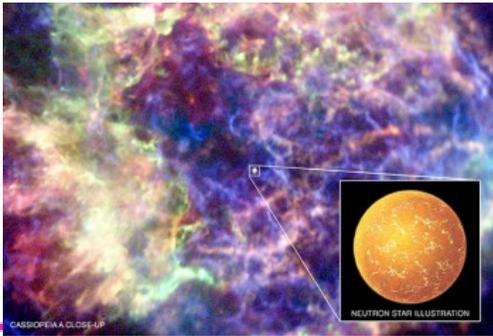
Kasliwal (2016)



Kasliwal (2016)

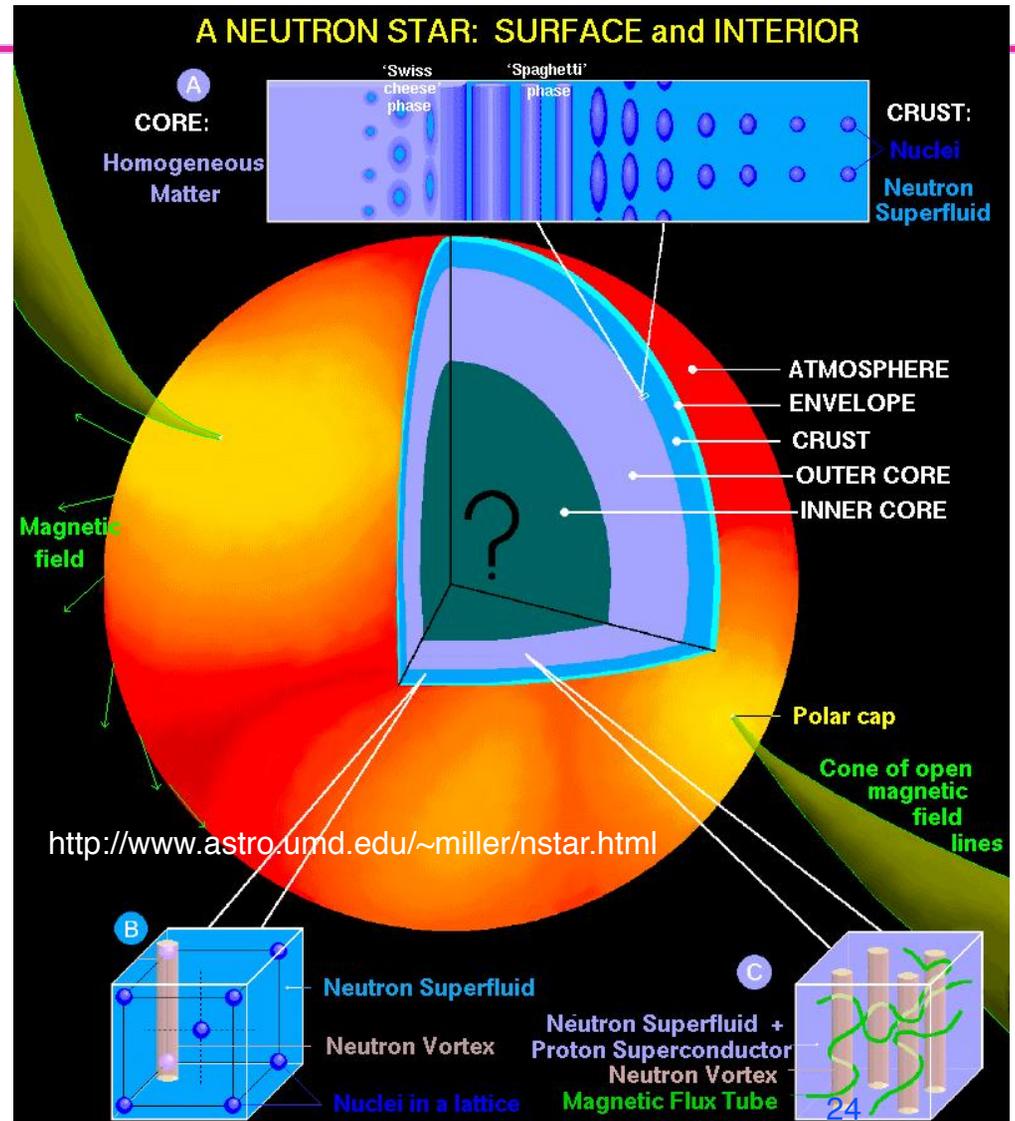
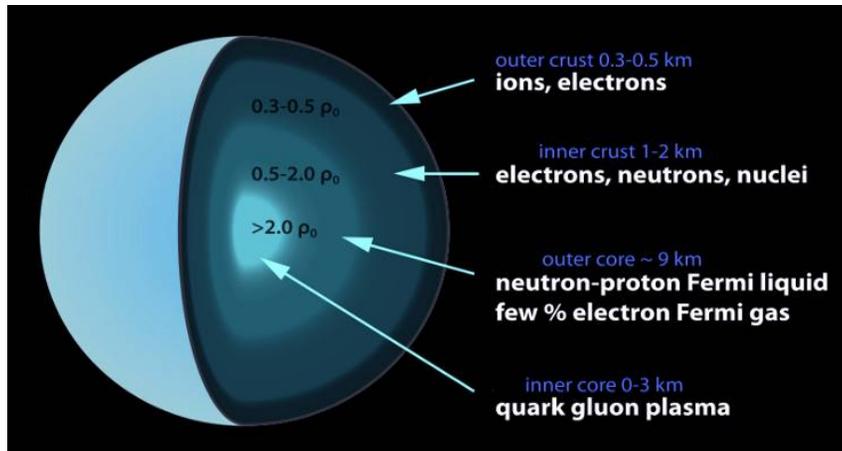


**Global Relay  
of Observatories  
Watching Transients Happen**  
Kasliwal (2016)



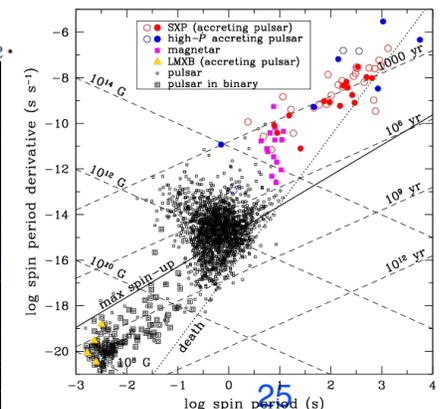
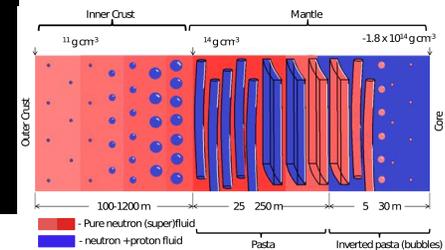
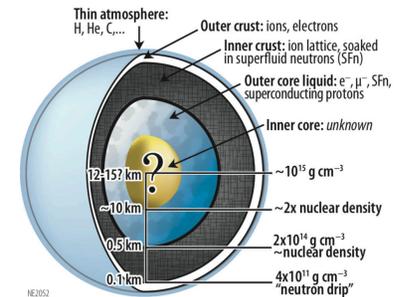
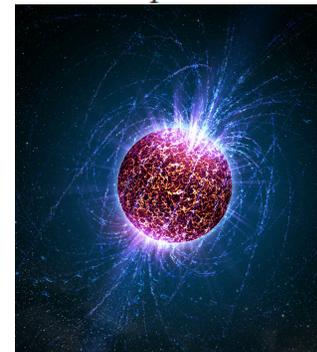
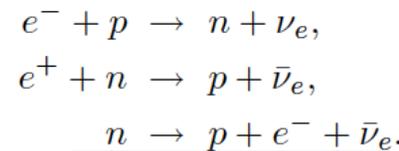
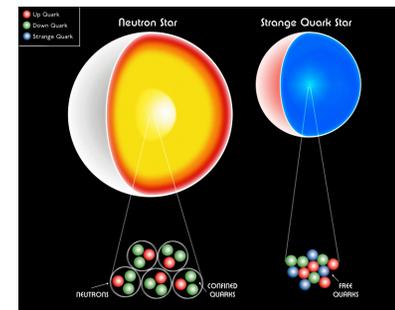
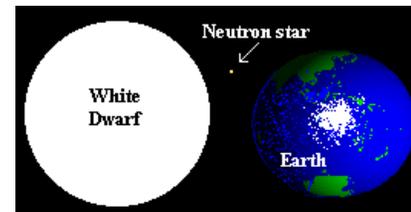
# Neutron stars

- Remnants of core collapse supernovae
- A unique laboratory for fundamental physics
- Strong, Weak, EM, gravity – all under the most extreme conditions
- Structure can be revealed through binary mergers



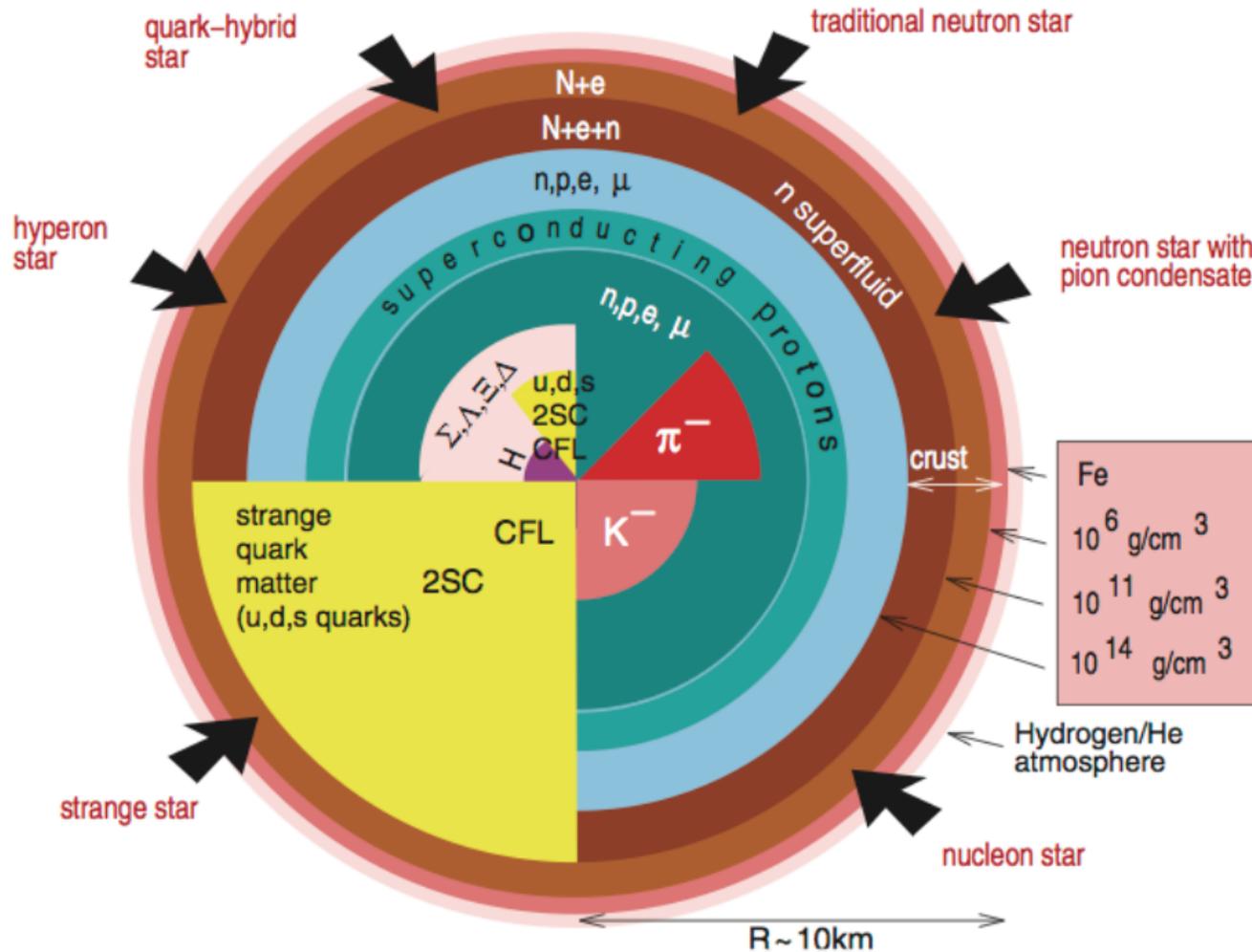
# All four fundamental forces under the most extreme conditions

- Gravity:** Compact stars have gravitational fields  $GM/c^2R \sim O(1)$ , strong tidal effects, strong curvature, highly relativistic
- Strong interaction at  $> 2x$  nuclear density in core**
  - » Hard repulsive core of nucleon-nucleon interaction plays crucial role
  - » Potential transition to hyperonic matter, strange quark matter, QGP
  - » Complex ionic crystal lattice structure in crust: “nuclear pasta”
- Weak interaction under extreme conditions with neutrino trapping -> beta equilibrium**
- EM:** Superfluid core supporting extreme magnetic fields (perhaps  $> 10^{15}$  Gauss at surface), flux tube pinning in core

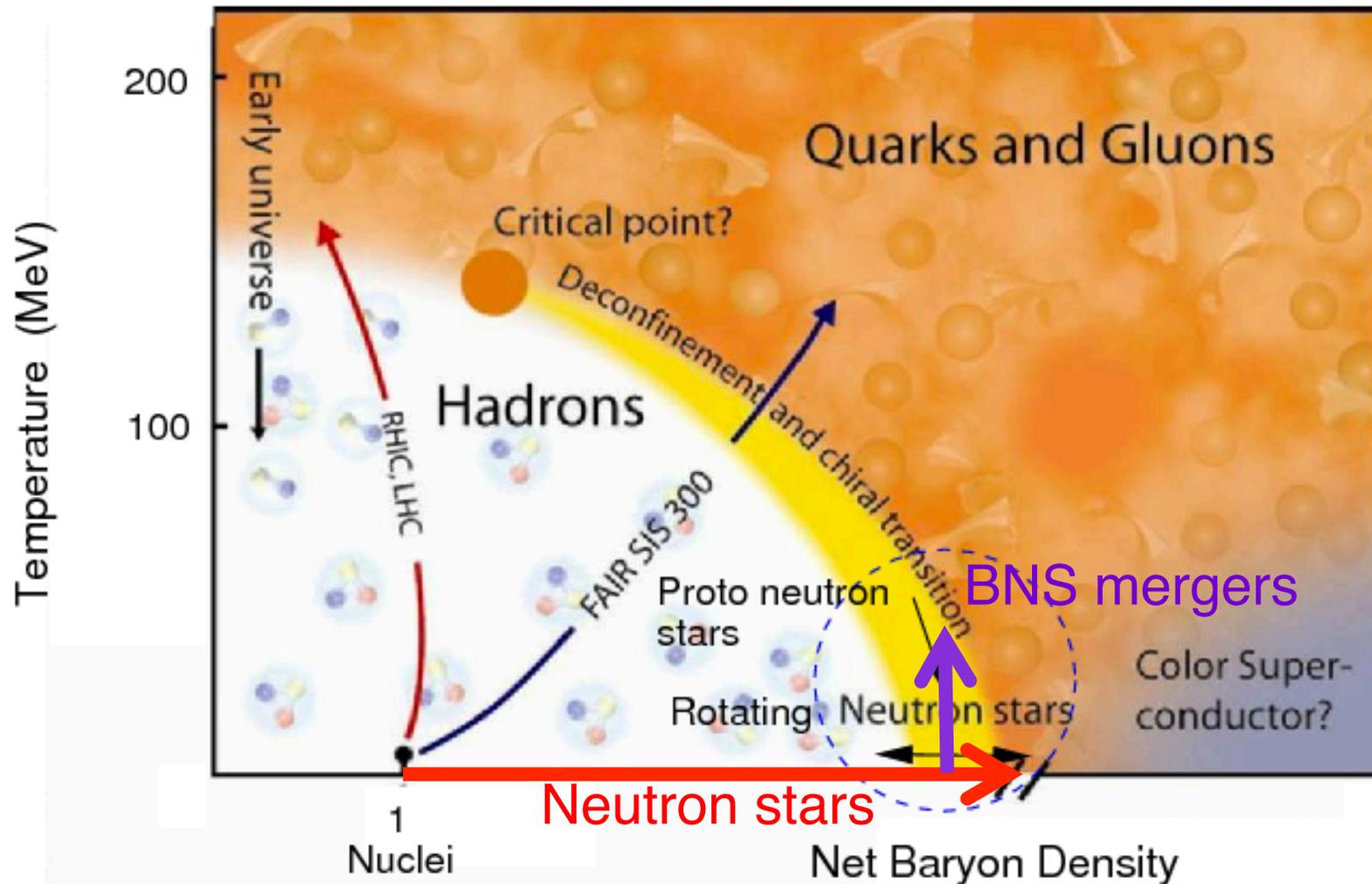


# Neutron Star Equation of State

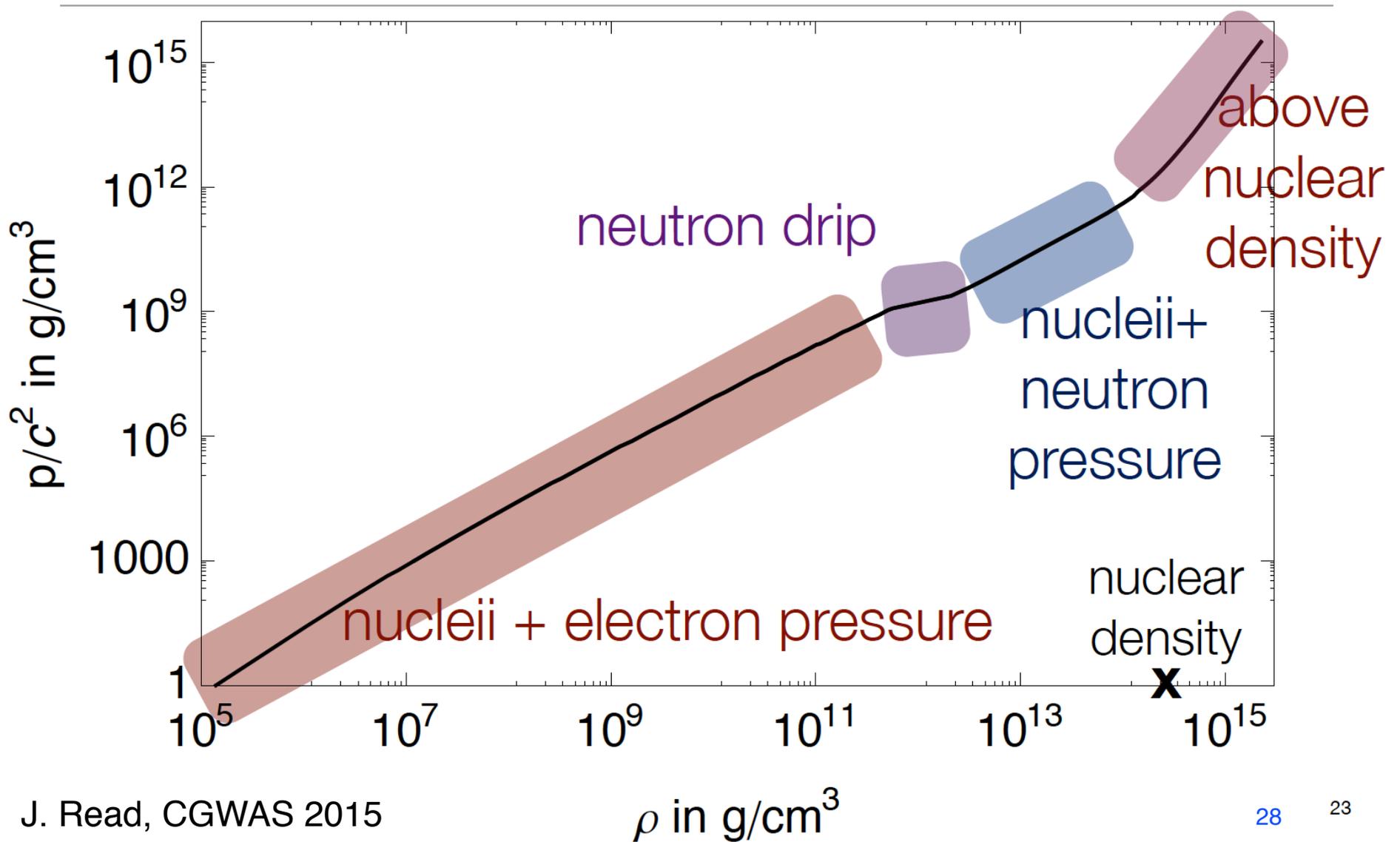
- Simplification:  $T=0$ , pure neutron & proton gas. Appropriate (?) for interior of cold neutron stars.



# Phase diagram of ground state



# Cold equation of state: pressure vs density



# Neutron Star Equation of State

- $T=0$ , pure neutron & proton gas.  $f = \epsilon$

$$\epsilon(n_n, n_p) = \frac{3}{5} \frac{p_{F,n}^2}{2m_n} \frac{n_n}{n} + \frac{3}{5} \frac{p_{F,p}^2}{2m_p} \frac{n_p}{n} \quad p_F = (3\pi^2 \hbar^3)^{1/3} n^{1/3}$$

$$P = n^2 \frac{\partial \epsilon}{\partial n} \propto n^{5/3}$$

$$\Gamma = \left. \frac{d \ln P}{d \ln \rho} \right|_s = \frac{5}{3}$$

$$P = K \rho^\Gamma$$

“polytrope”

$\Gamma = 5/3$  corresponds to a non-relativistic gas.

A relativistic gas has  $\Gamma = 4/3$ , which is unstable to collapse.

Note that (unlike ideal gas law  $P = nkT$ )

the result is independent of temperature.

In general,  $pv^n = \text{const}$  is polytropic, with  $\Gamma = 1 + 1/n$ ; here,

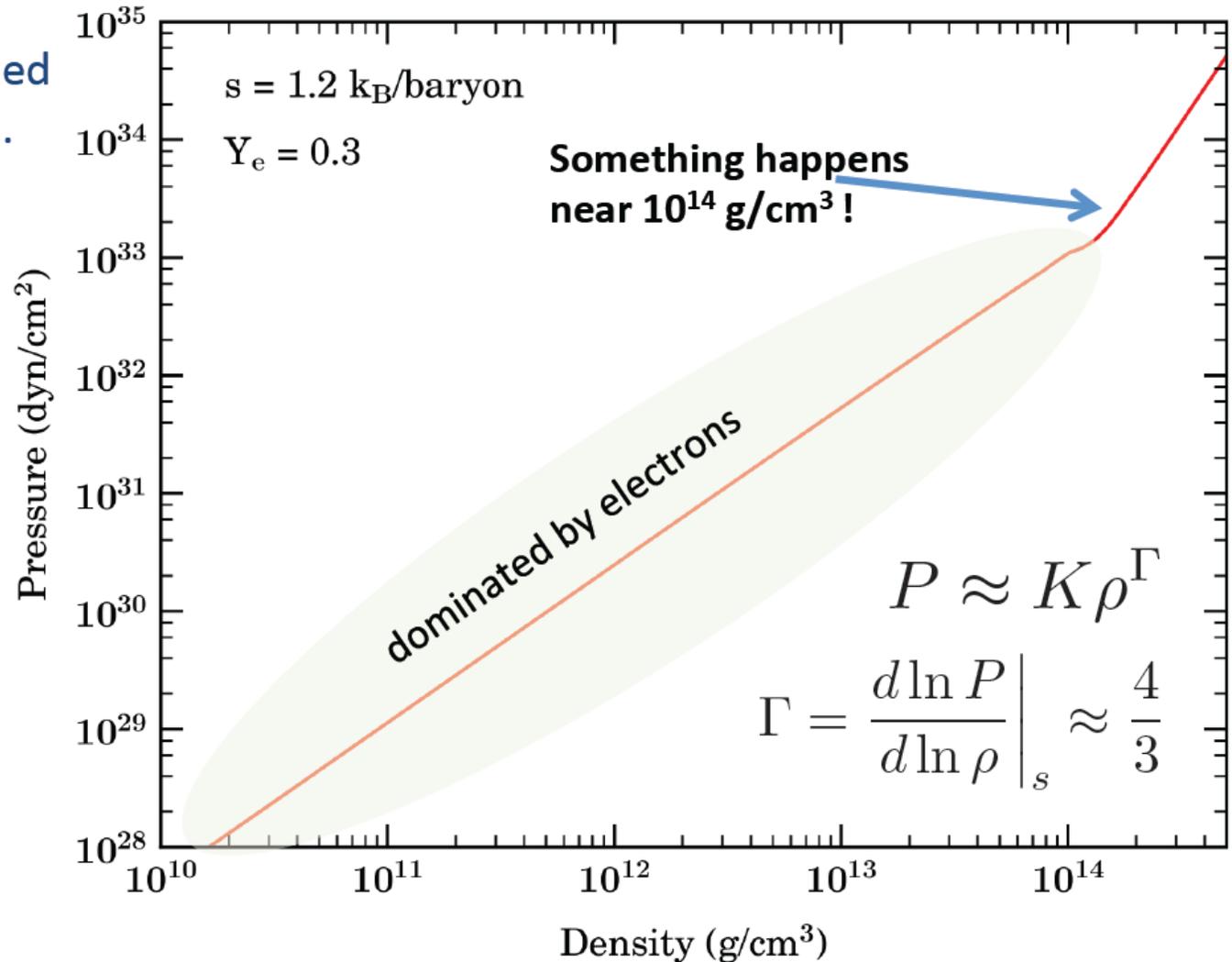
$n = \text{polytropic index (NOT } n = \rho/m_N)$

# Neutron Star Equation of State

Nuclear Statistical Equilibrium ( $\rho > 10^7 \text{ g/cm}^3$ ,  $T > 0.5 \text{ MeV}$ )

->  $P = P(\rho, T, Y_e)$

Composition determined  
by Saha-type equation.



# Neutron Star Equation of State

Nuclear Physics:

$$R_{\text{nuc}} = A^{1/3} r_0$$

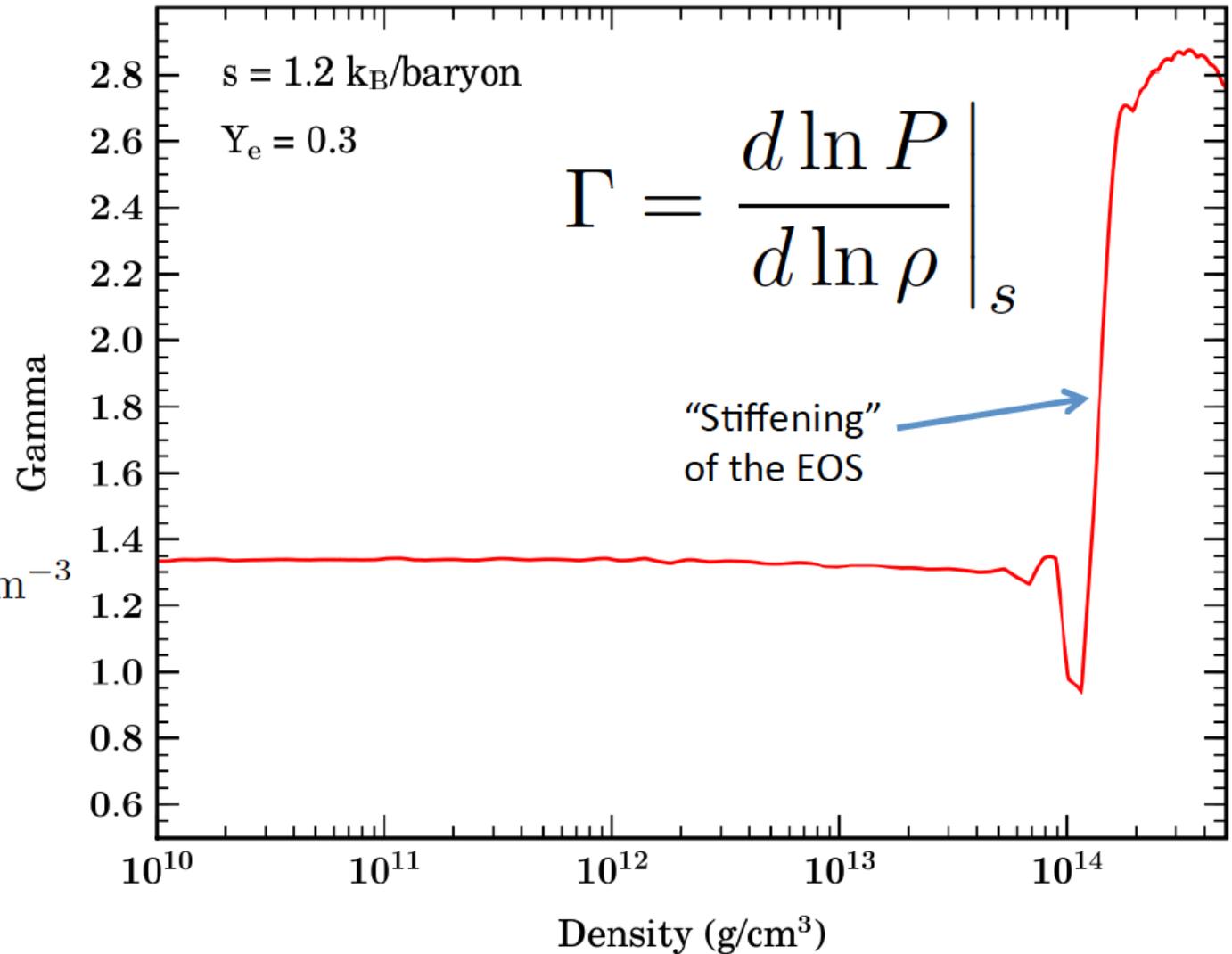
$$r_0 = 1.25 \text{ fm}$$

Nuclear Density:

$$\bar{\rho}_{\text{nuc}} = \frac{A m_b}{\frac{4}{3} \pi R_{\text{nuc}}^3}$$

$$\rho_{\text{nuc}} \sim 2.7 \times 10^{14} \text{ g cm}^{-3}$$

$$n_{\text{nuc}} \sim 0.16 \text{ fm}^{-3}$$



# Neutron Star Equation of State

Nuclear Physics:

$$R_{\text{nuc}} = A^{1/3} r_0$$

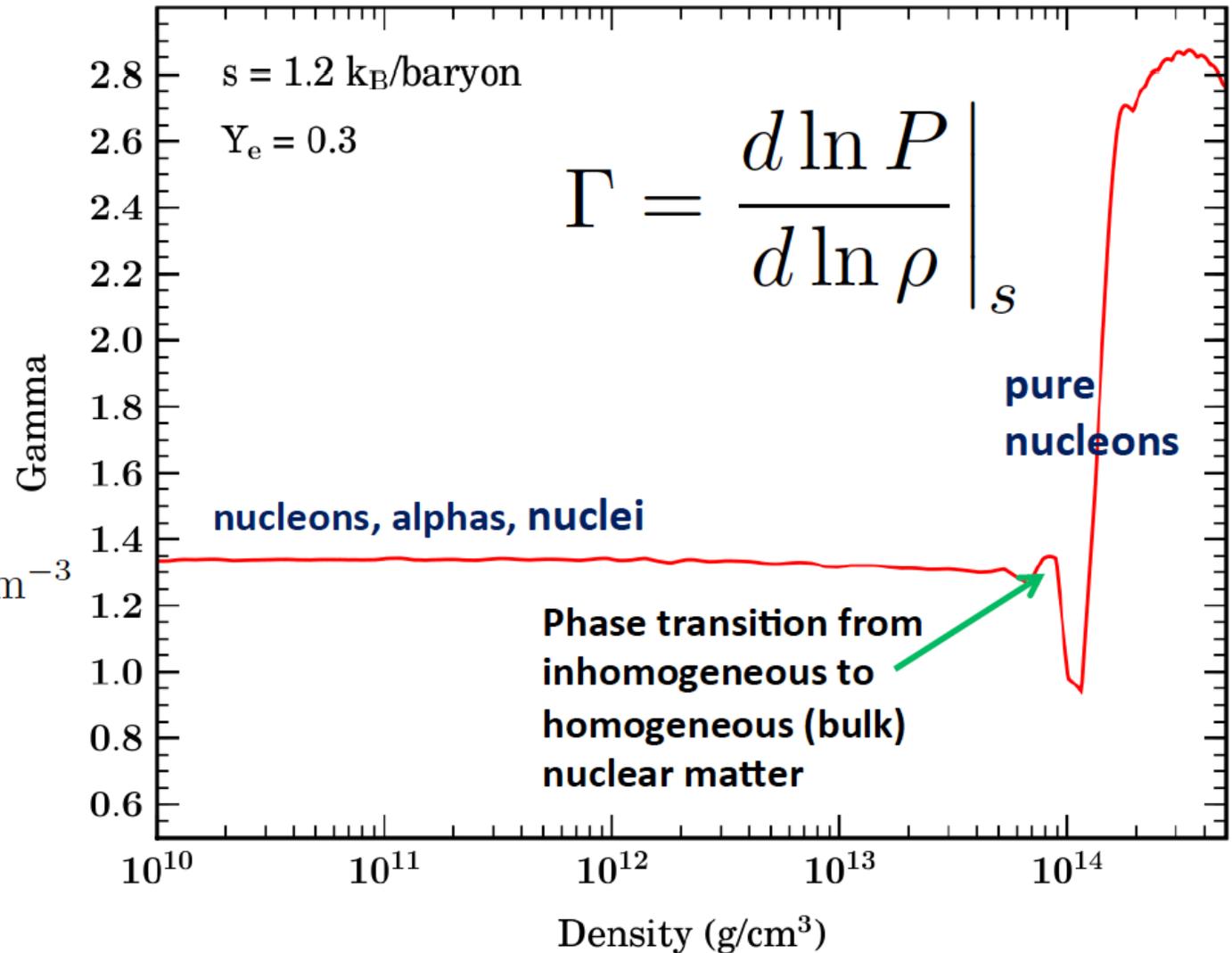
$$r_0 = 1.25 \text{ fm}$$

Nuclear Density:

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$$\rho_{\text{nuc}} \sim 2.7 \times 10^{14} \text{ g cm}^{-3}$$

$$n_{\text{nuc}} \sim 0.16 \text{ fm}^{-3}$$



**What is causing the stiffening of the nuclear EOS?**

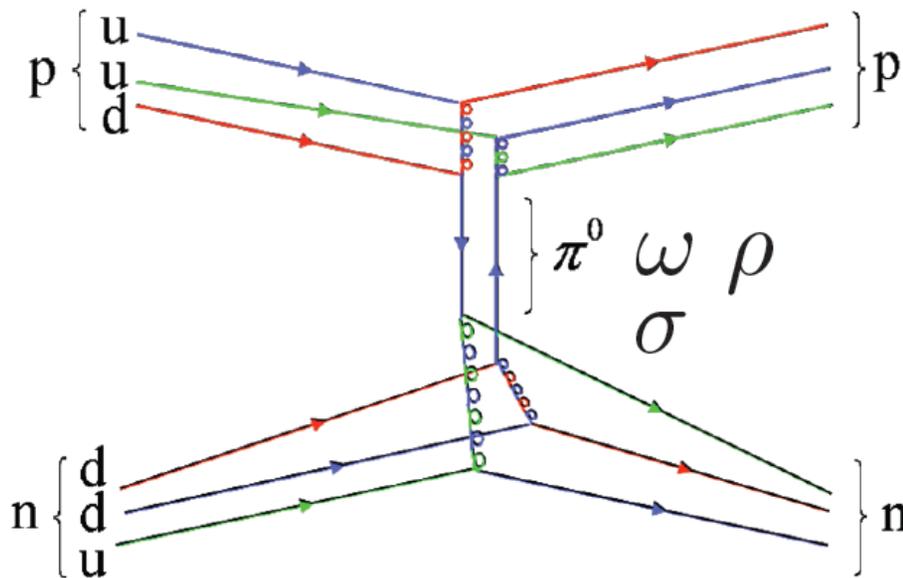
C. Ott, 2012

# Nuclear Equation of State

- $T=0$ , **interacting** pure neutron & proton gas.

$$\epsilon(n_n, n_p) = \frac{3}{5} \frac{p_{F,n}^2}{2m_n} \frac{n_n}{n} + \frac{3}{5} \frac{p_{F,p}^2}{2m_p} \frac{n_p}{n} + \frac{V_{np}(n_n, n_p)}{n}$$

nucleon-nucleon (NN) potential energy density



- Nuclear force is NN many-body interaction = “effective” strong force interaction.
- Mediated by mesons:  
 $\pi$  ( $s=0$ ),  $\sigma$  ( $s=0$ ),  $\omega$  ( $s=1$ ),  $\rho$  ( $s=1$ )
- Dependent on separation and spin orientation. **Scalar, vector, and tensor** components.  
**Vector component is repulsive.**

# Nucleon-Nucleon Interaction

Example: Bethe & Johnson 74

2-pion exchange attractive; omega-exchange repulsive

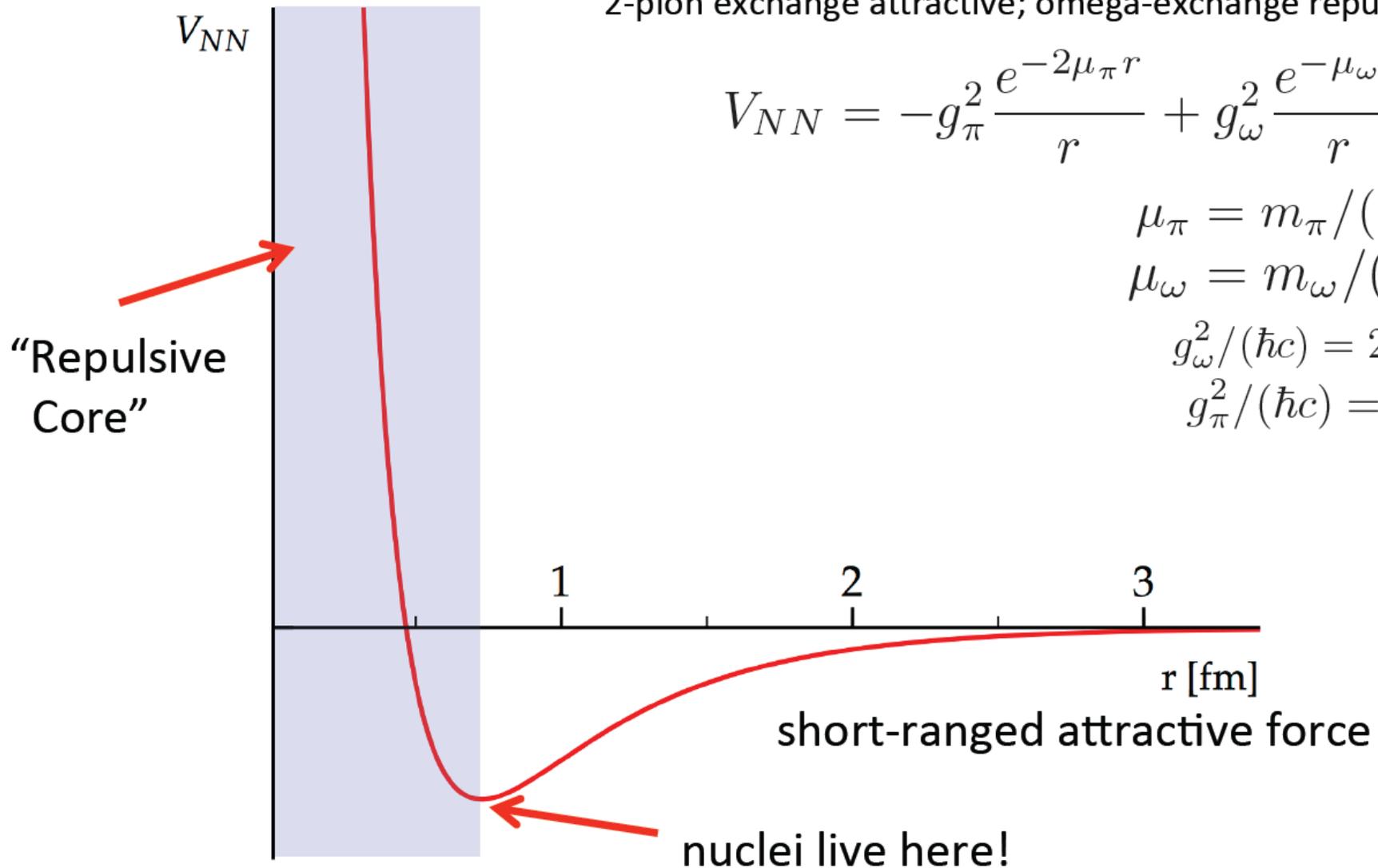
$$V_{NN} = -g_{\pi}^2 \frac{e^{-2\mu_{\pi}r}}{r} + g_{\omega}^2 \frac{e^{-\mu_{\omega}r}}{r}$$

$$\mu_{\pi} = m_{\pi}/(\hbar c)$$

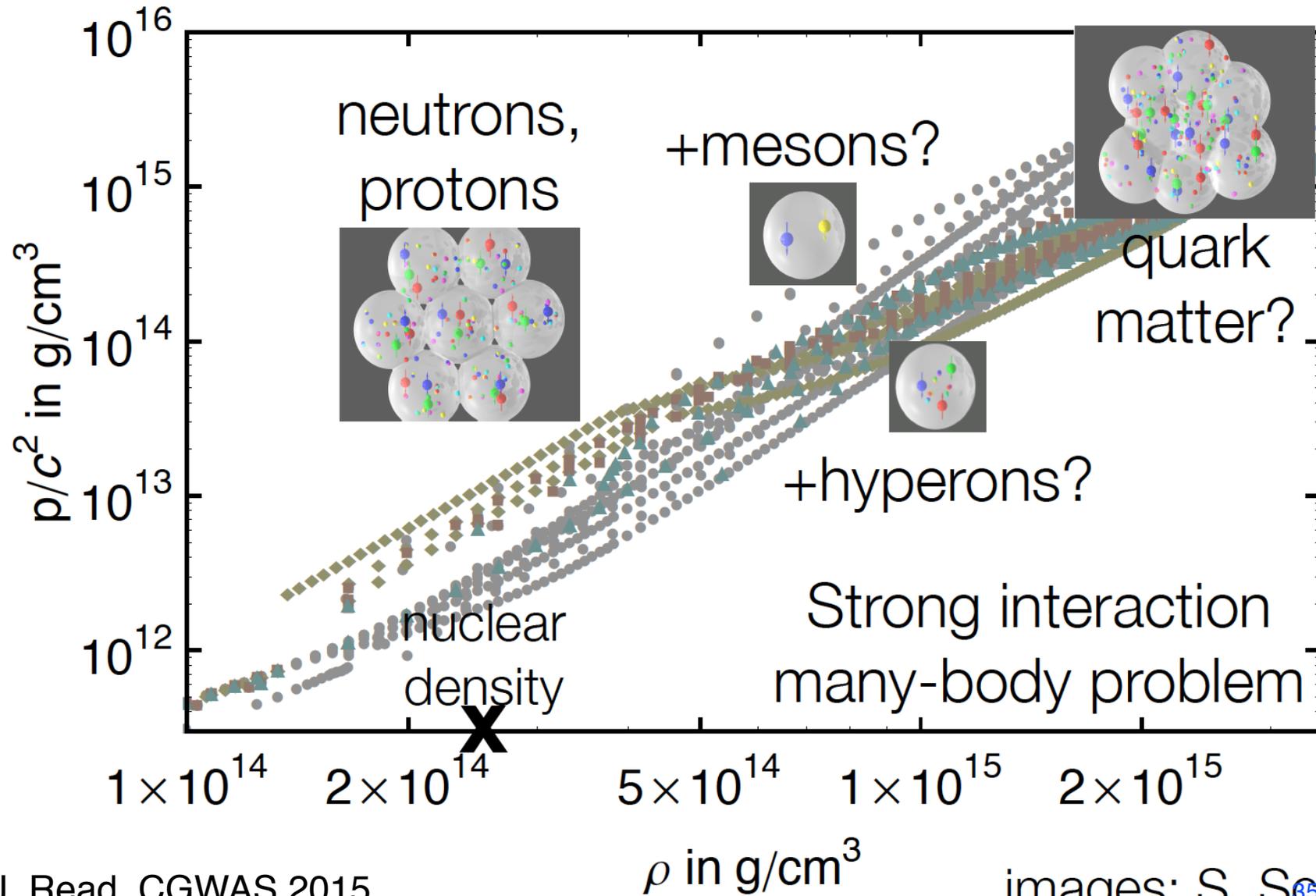
$$\mu_{\omega} = m_{\omega}/(\hbar c)$$

$$g_{\omega}^2/(\hbar c) = 29.6$$

$$g_{\pi}^2/(\hbar c) = 10$$



# What happens above nuclear density? Inside neutrons: quarks



# Neutron Star Structure

Newtonian:  $\frac{dP}{dr} = -\frac{GM\rho}{r^2}$      $\frac{dM}{dr} = 4\pi r^2 \rho$     (no maximum mass!)

GR: Tolman-Oppenheimer-Volkov (TOV) eqns

$$\frac{dP}{dr} = -G(\rho(1 + \epsilon/c^2) + P/c^2) \frac{M + 4\pi r^3 p/c^2}{r(r - 2GM/c^2)}$$

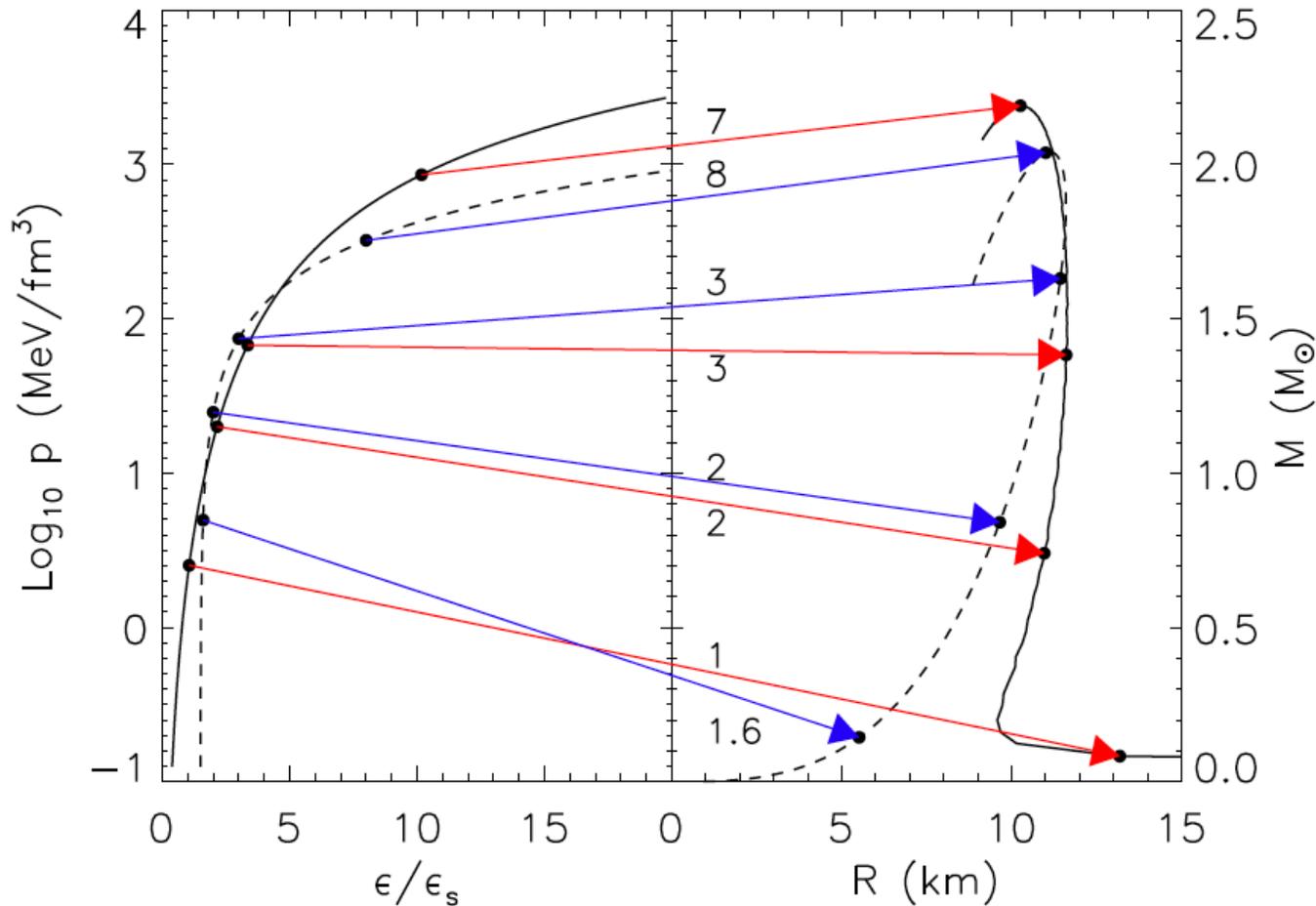
$$\frac{dM_g}{dr} = 4\pi r^2 \rho(1 + \epsilon/c^2) \quad \text{gravitational mass}$$

$$\frac{dM_b}{dr} = \frac{4\pi r^2}{\sqrt{1 - \frac{2GM}{rc^2}}} \rho \quad \text{baryonic mass}$$

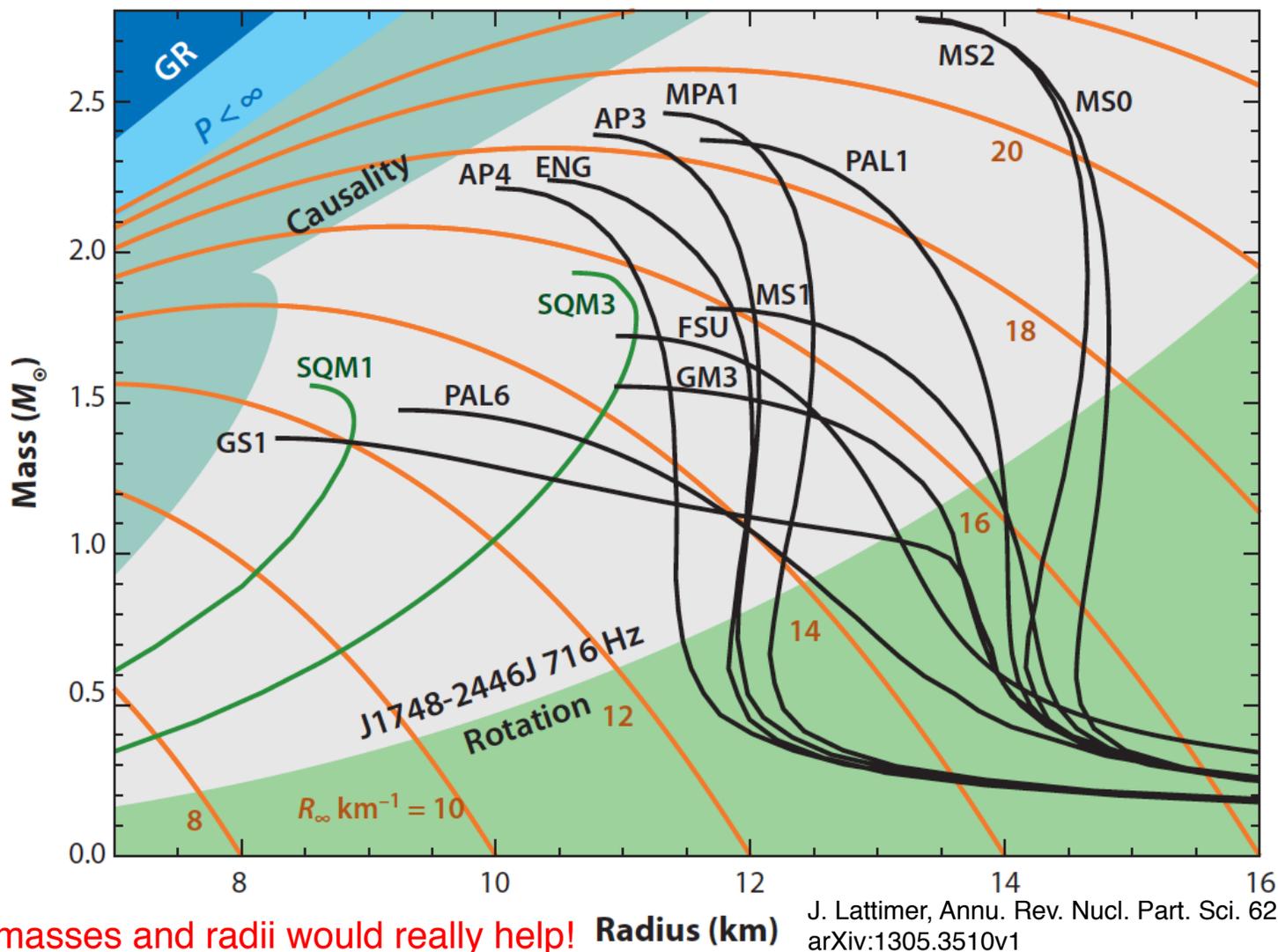
*Radius is circumferential radius!*

- Solve by ODE integration from  $r=0$ , invert  $P(\rho)$  at each step to obtain  $\rho$ .

# Building neutron star mass-radius relation with TOV and NEOS

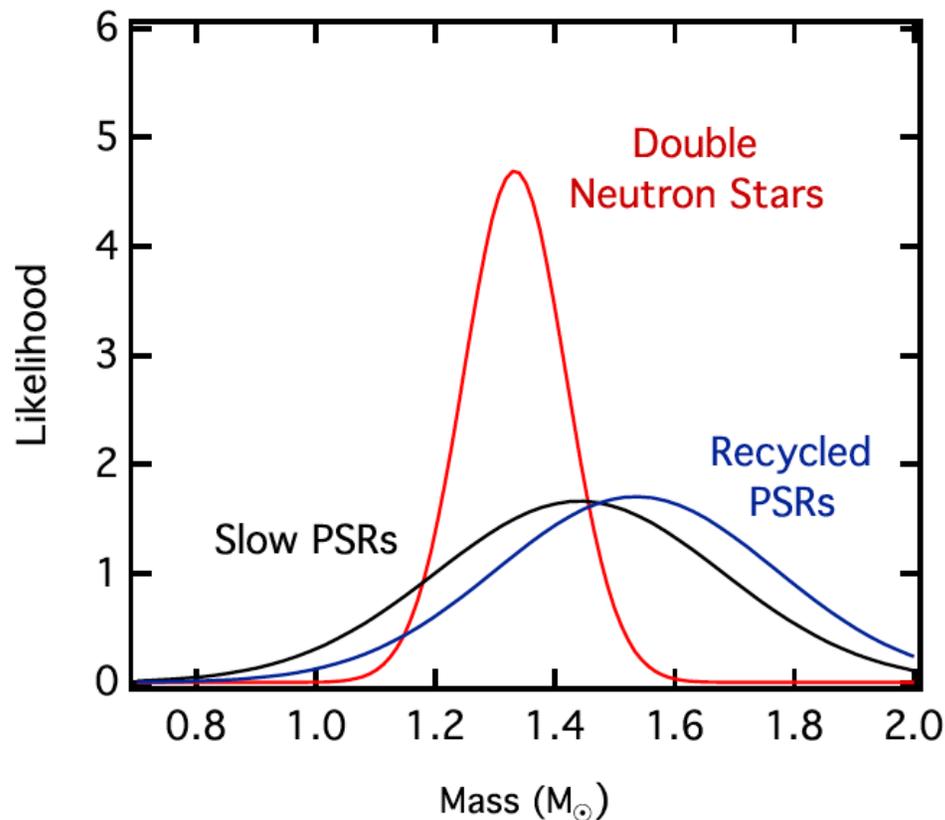
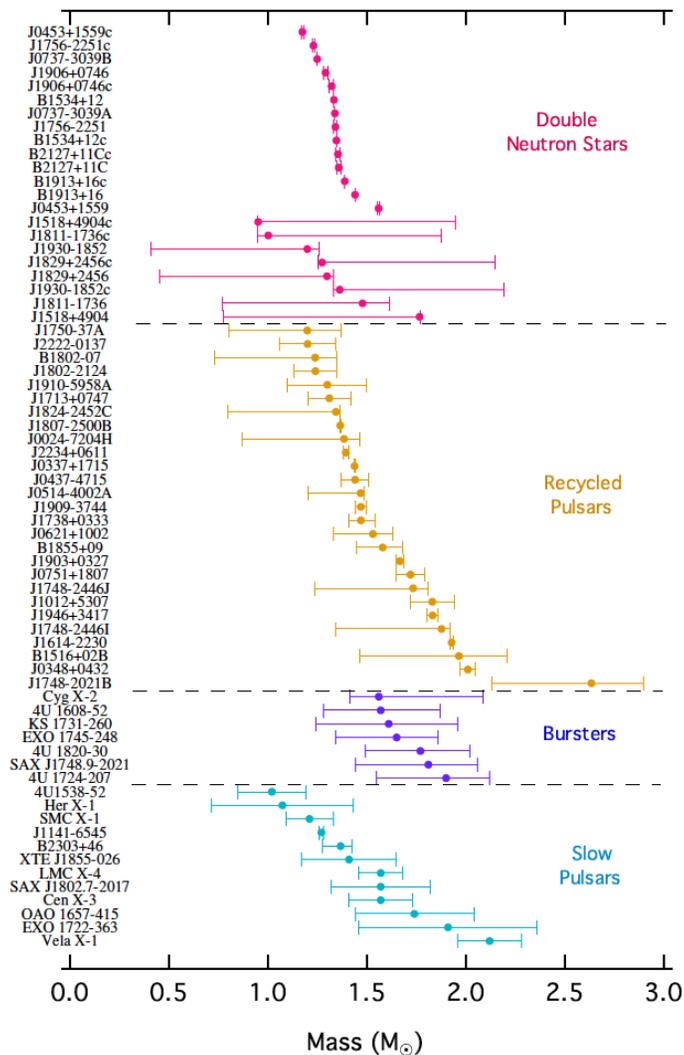


# EOS and Neutron star structure



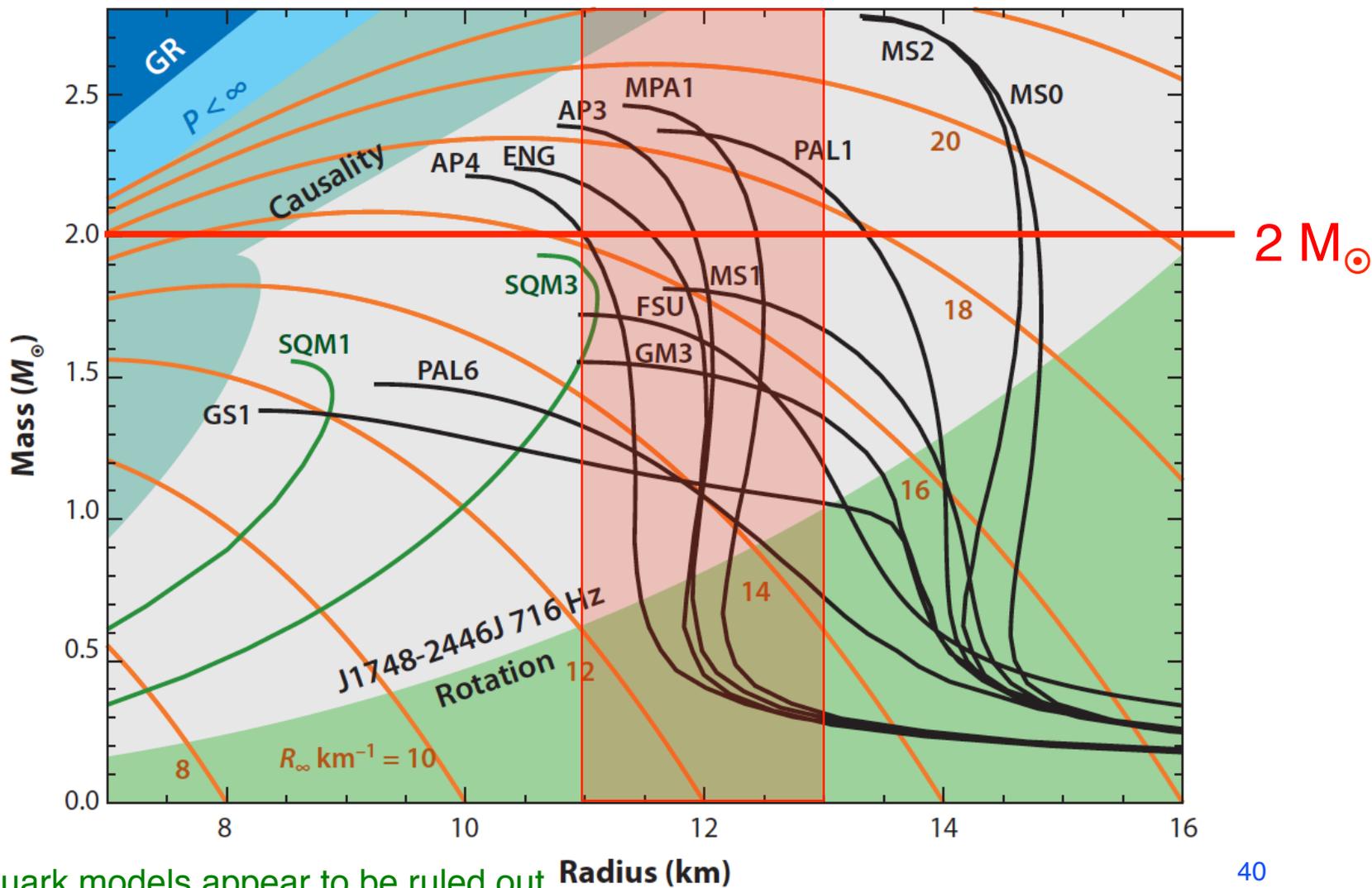
Knowing masses and radii would really help! **Radius (km)**

# Neutron star masses



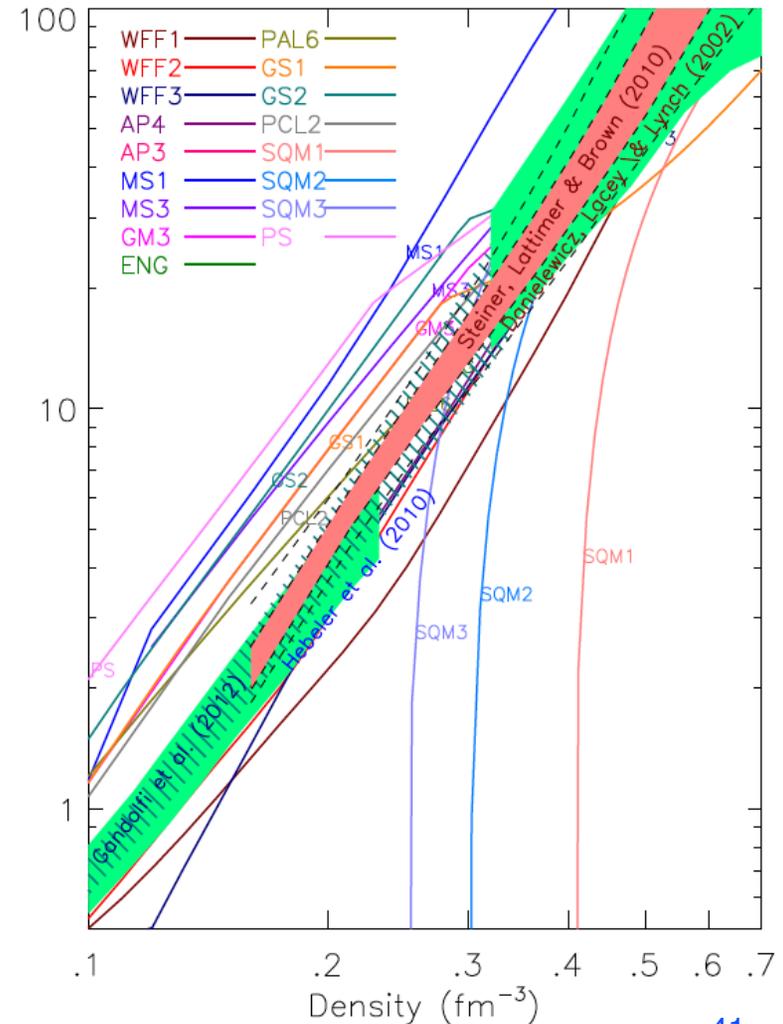
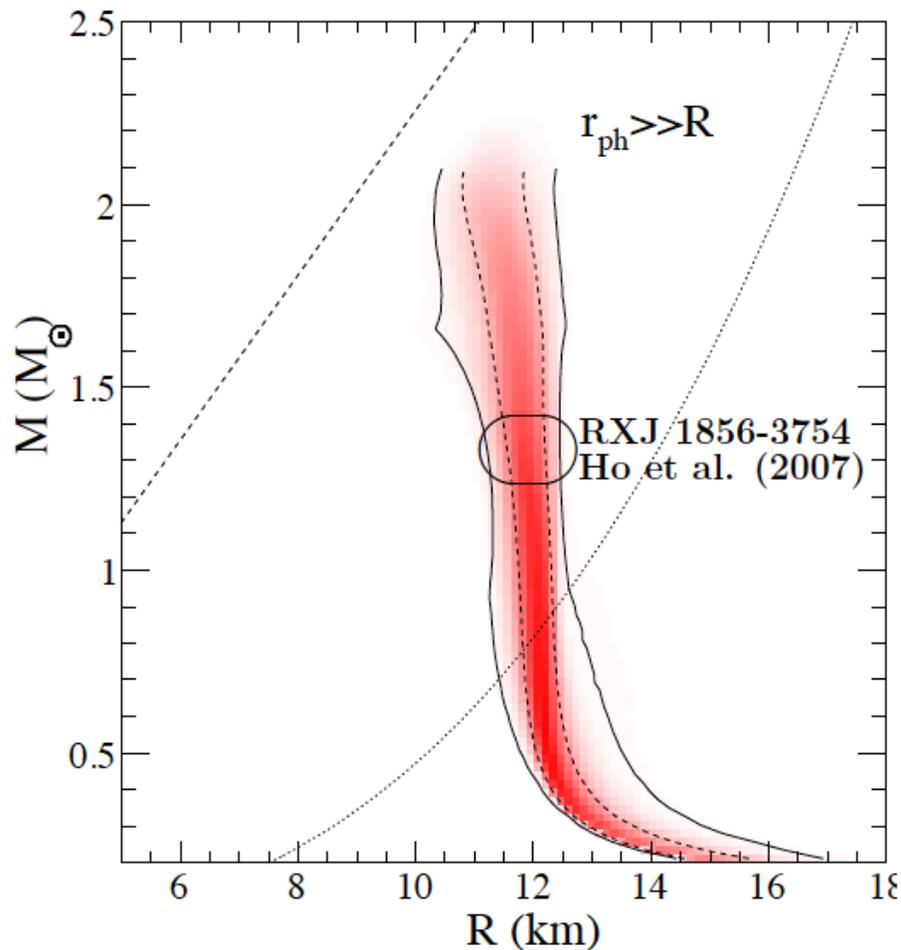
Feryal Ozel, Paulo Freire, <http://arxiv.org/abs/1603.02698v1>

# Mass and radius constraints



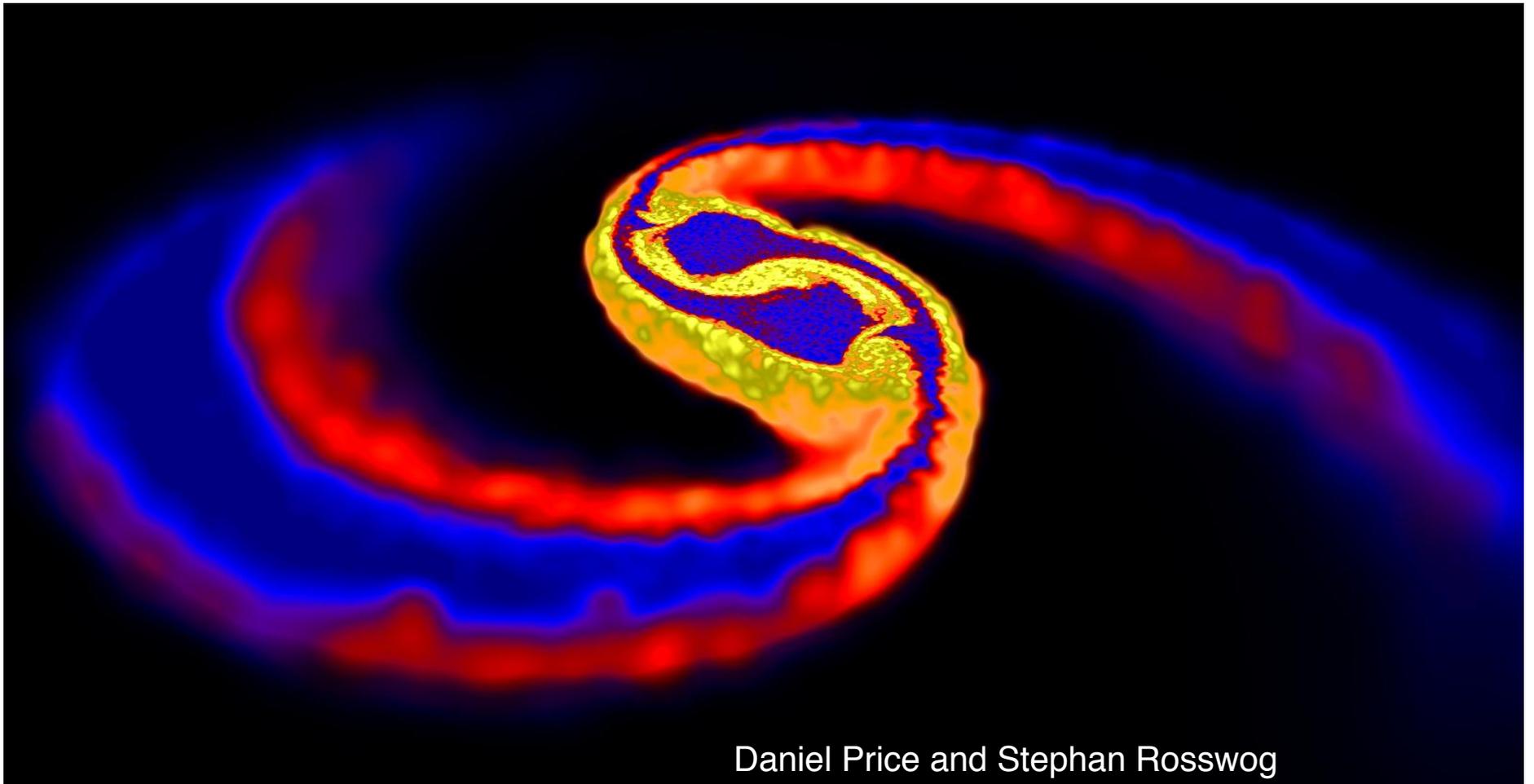
Strange quark models appear to be ruled out...

# Astrophysical constraints on masses and radii of NSs



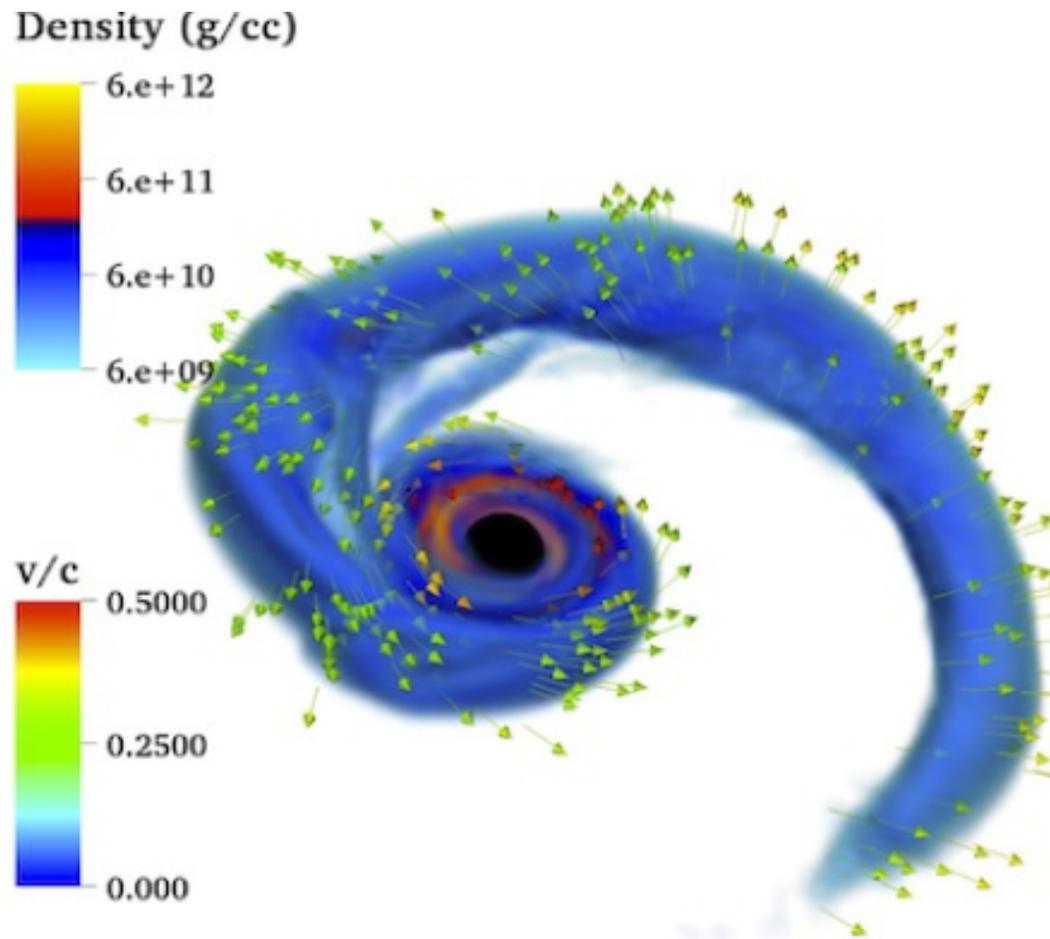
# Binary neutron star mergers

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Daniel Price and Stephan Rosswog

# Matter distribution during the disruption of the neutron star



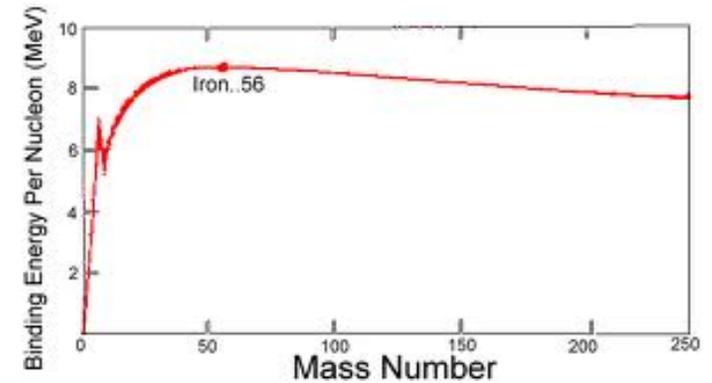
About half of the remnant material is unbound, while a relatively low mass hot disk forms.



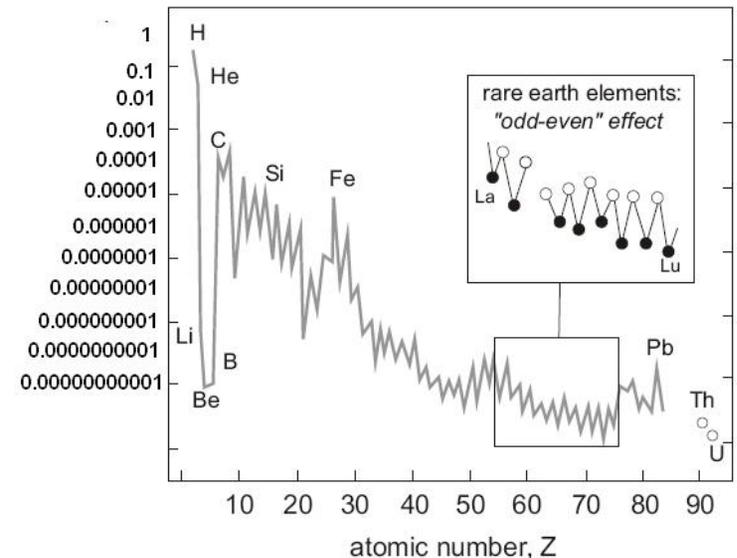
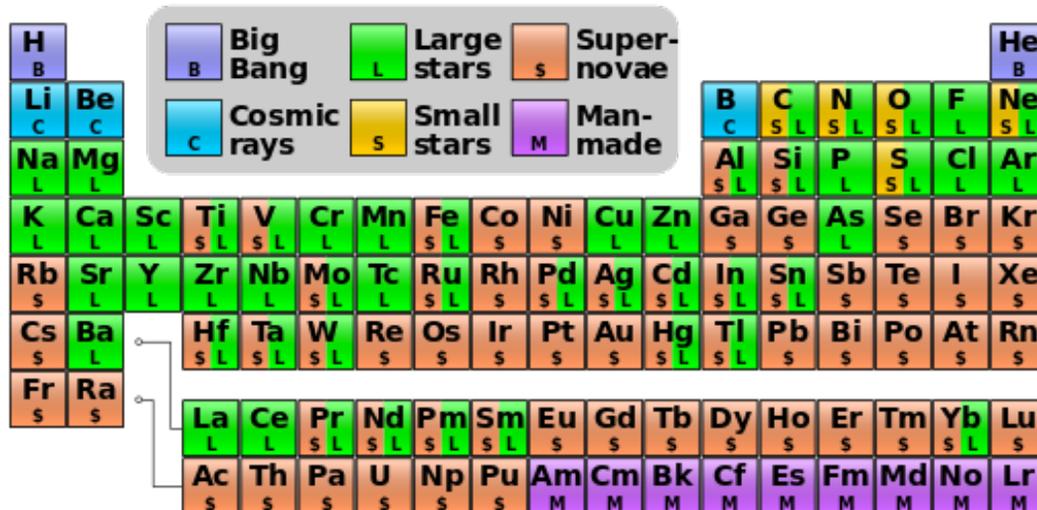
# The origin of the elements – astrophysical nucleosynthesis



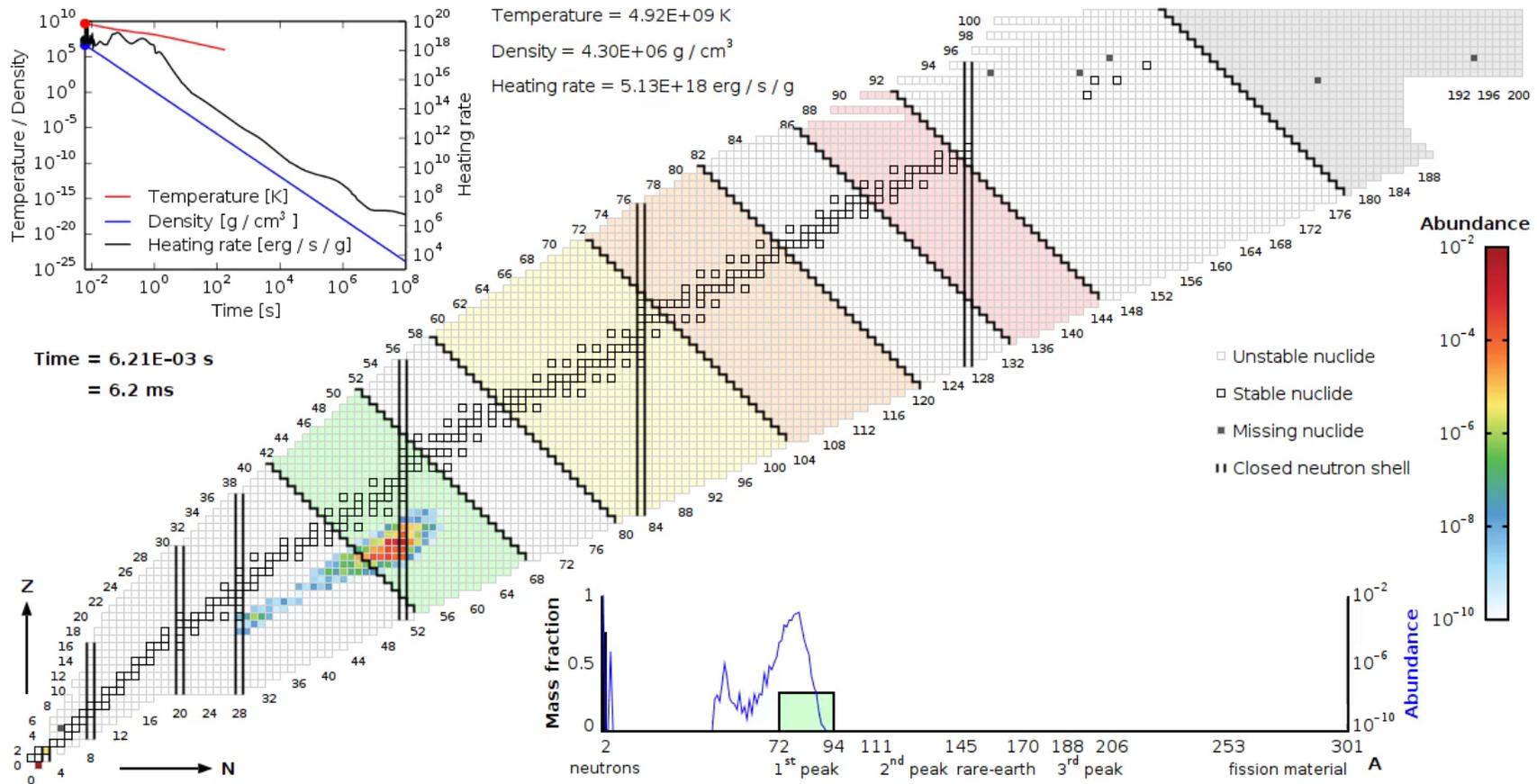
- Lightest elements (H, He, Li) forged in Big Bang
- Heavier elements (C, O, N, ... Fe) forged in the core of massive stars, distributed to ISM by core-collapse supernovae (star-death)
- Elements beyond Fe (like Cu, Au, Pb, Pt, U...) are forged during the SN (“r-process”)
- but many/most of them might come from binary neutron star mergers (second-death)



COSMIC ABUNDANCES of the elements

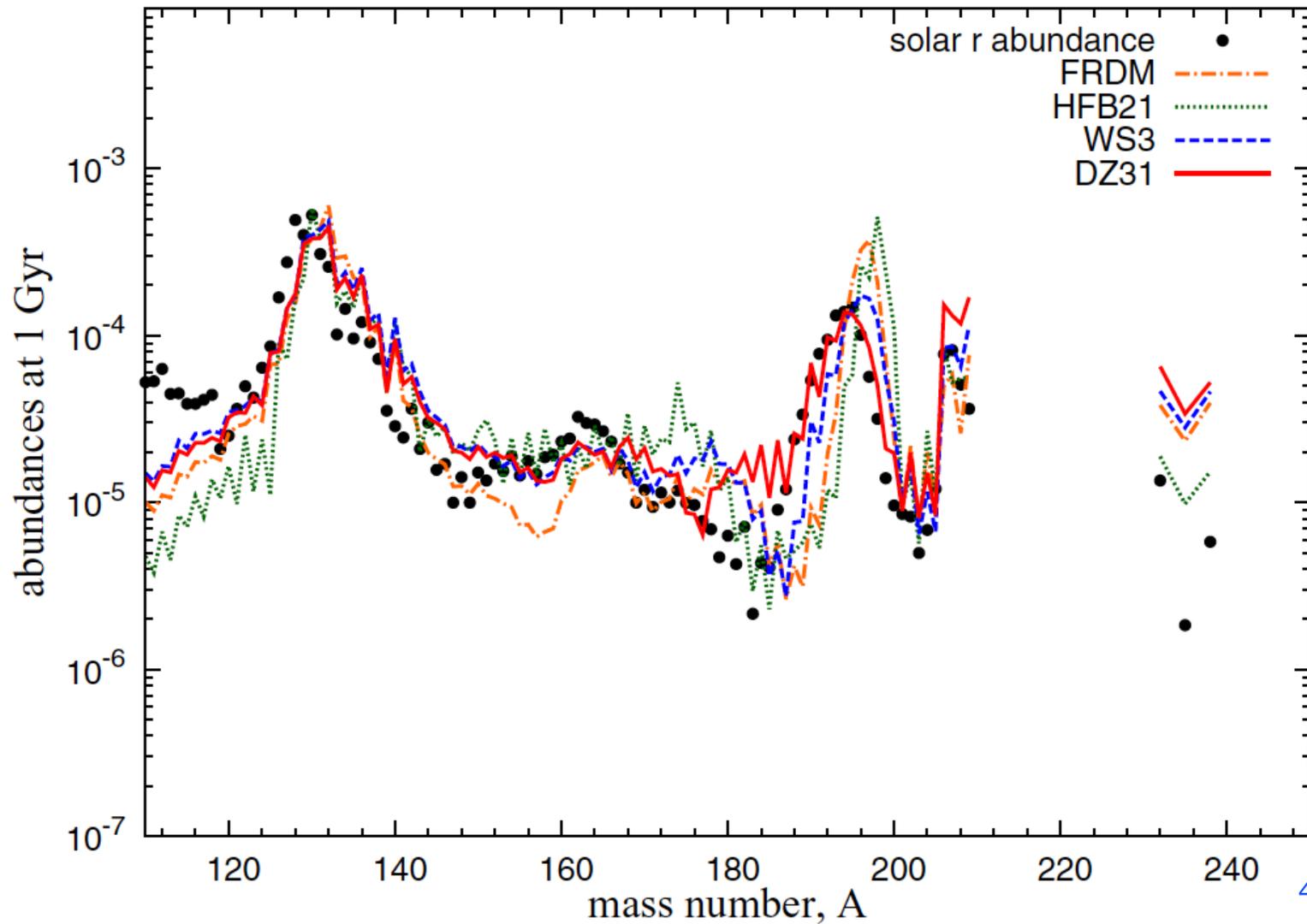


# Nucleosynthesis in binary neutron star collisions

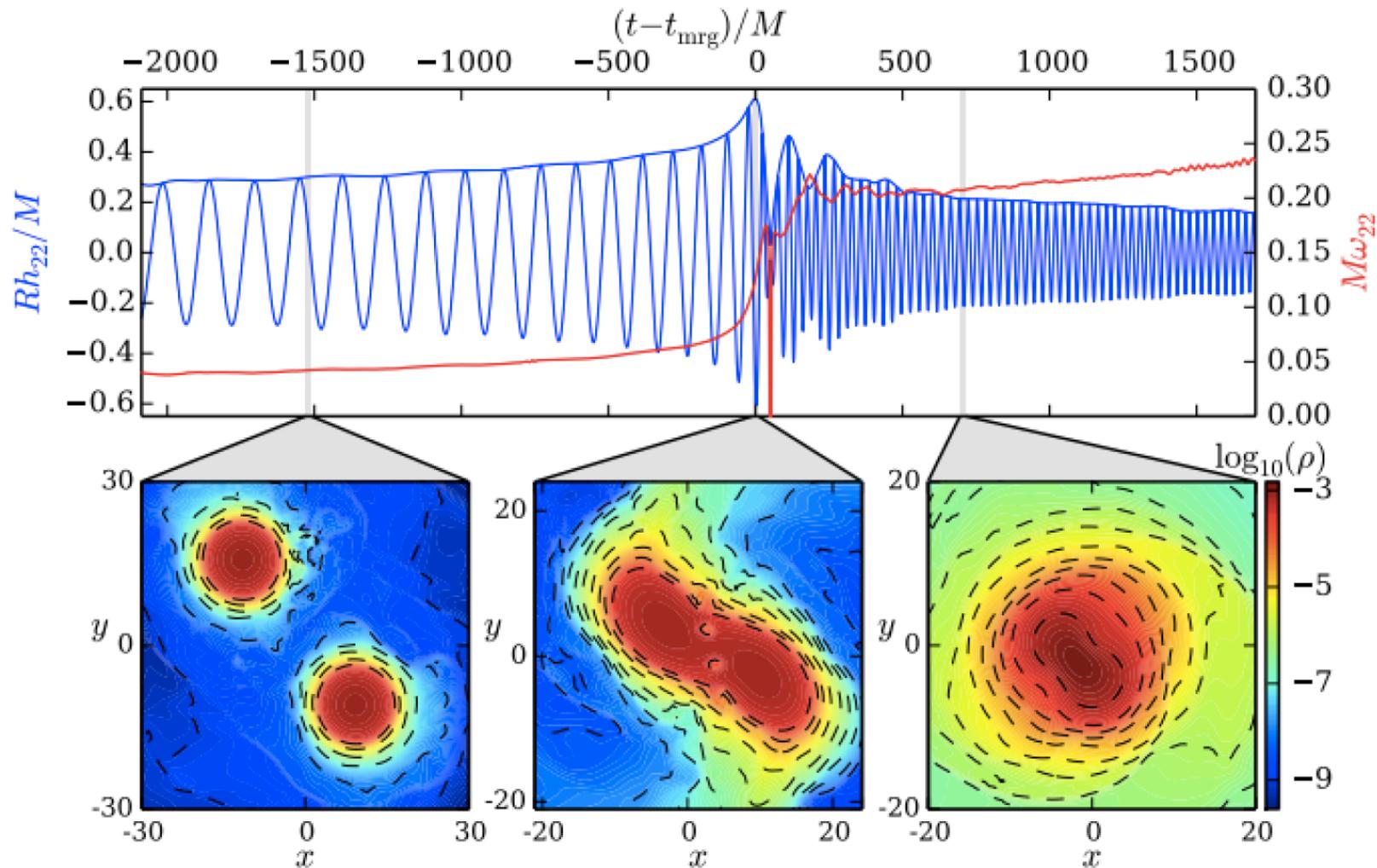


C. Ott; [http://www.lippuner.ca/files/nucleosynthesis\\_000\\_med.mp4](http://www.lippuner.ca/files/nucleosynthesis_000_med.mp4)

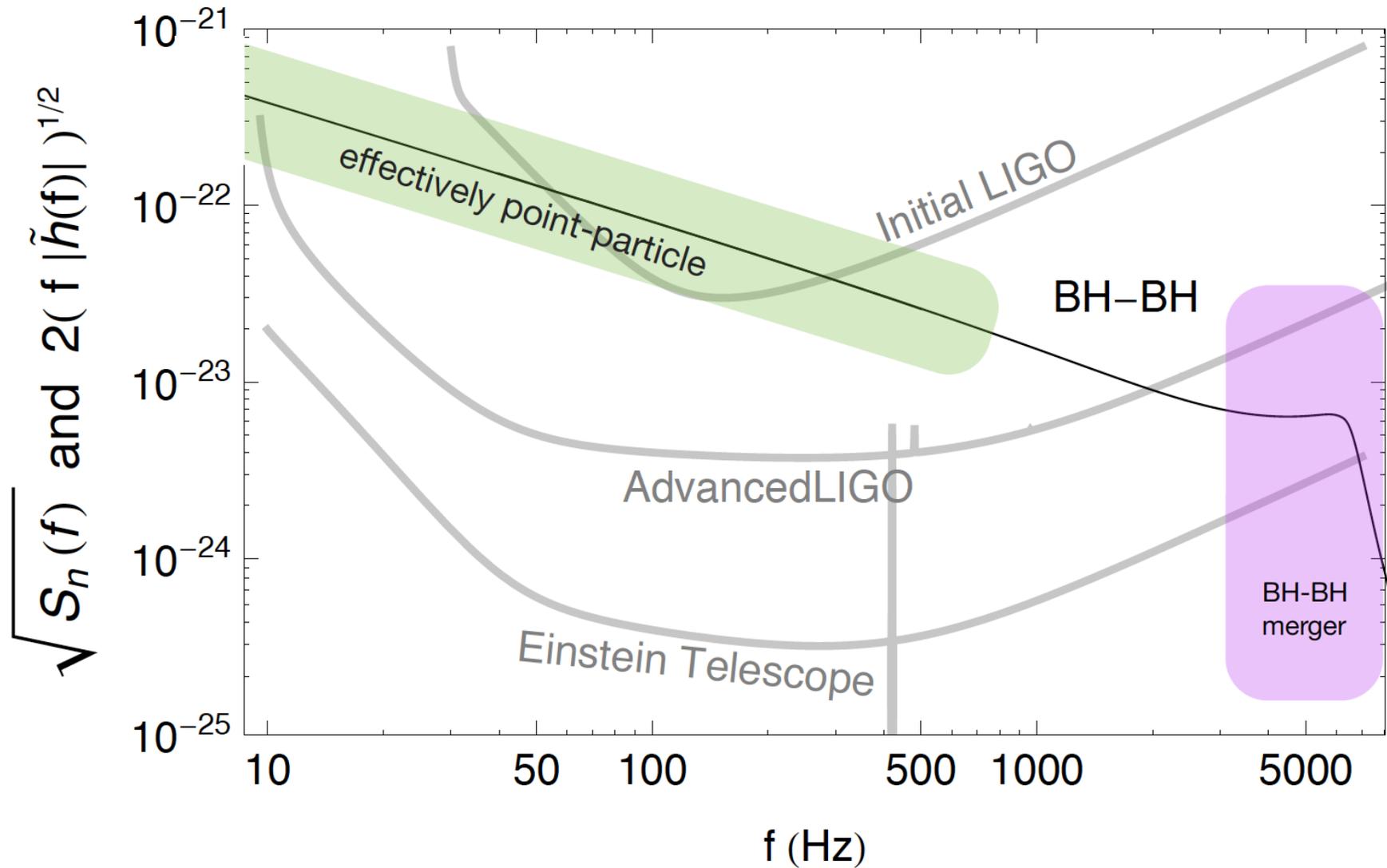
# Nuclear abundances from detailed simulations on BNS mergers



# GWs from BNS mergers

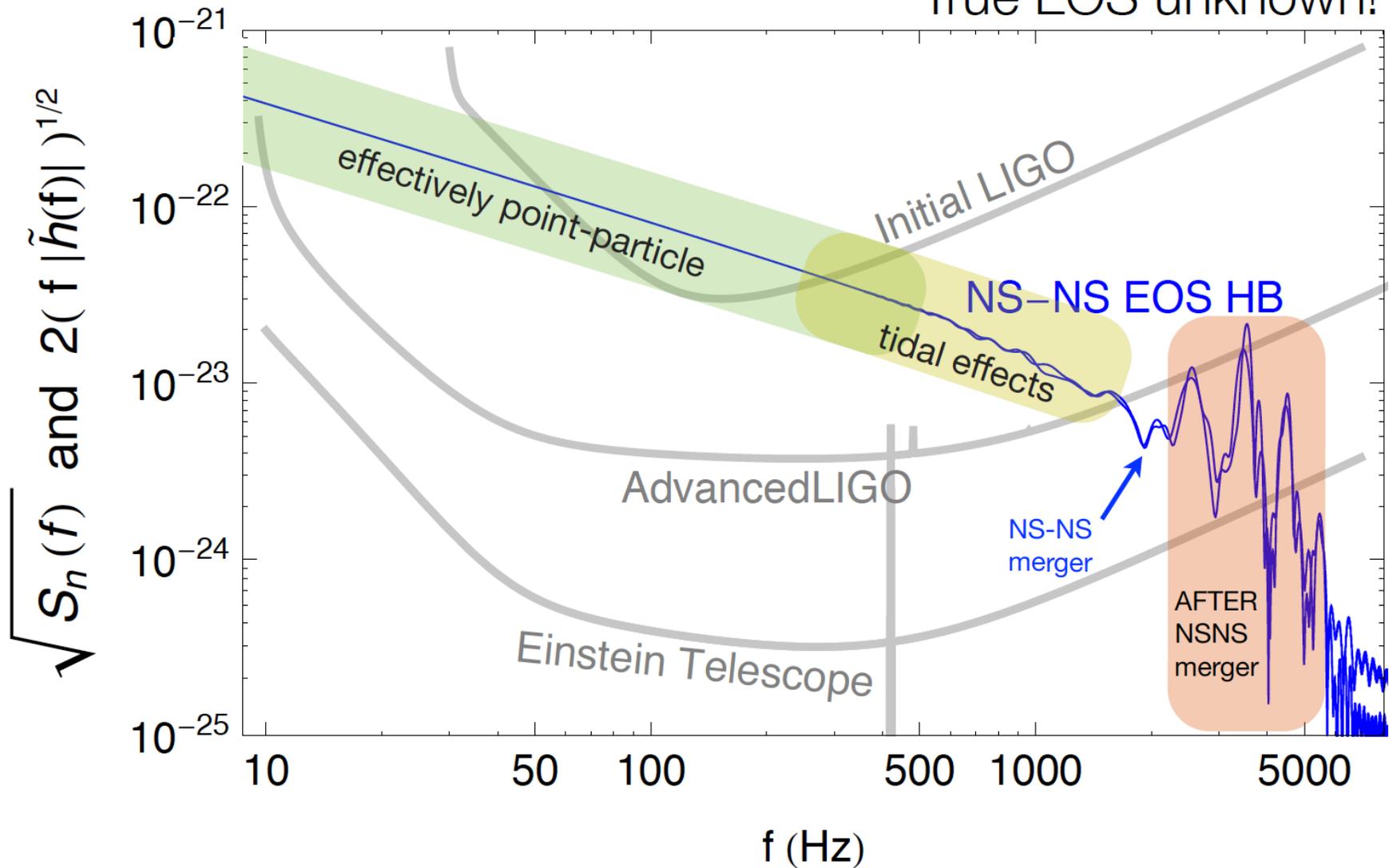


# Spectrum of BBH inspiral, scale to 1.35-1.35, 45 Mpc



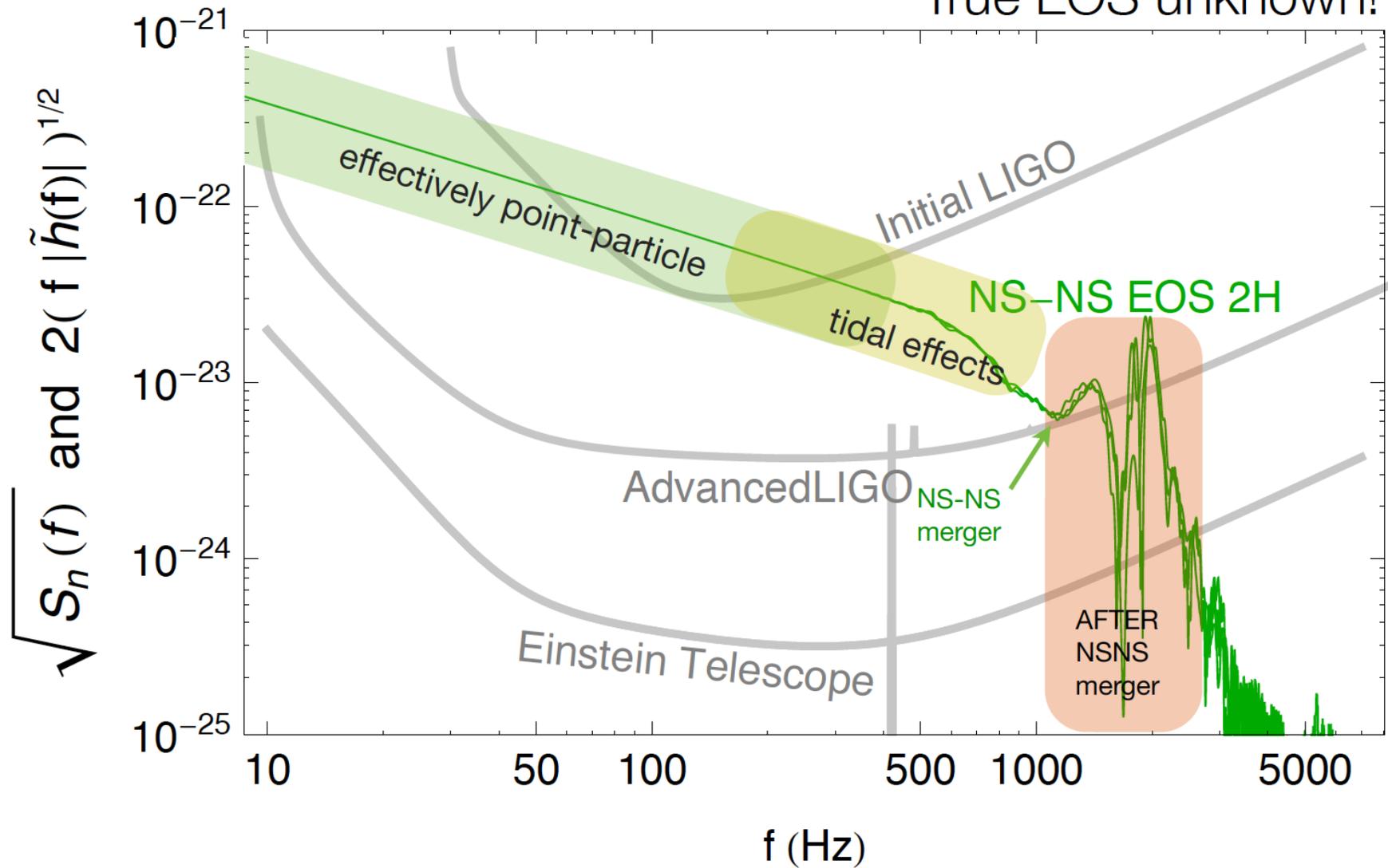
# Spectrum of NS-NS inspiral, 1.35-1.35, 45 Mpc

True EOS unknown!

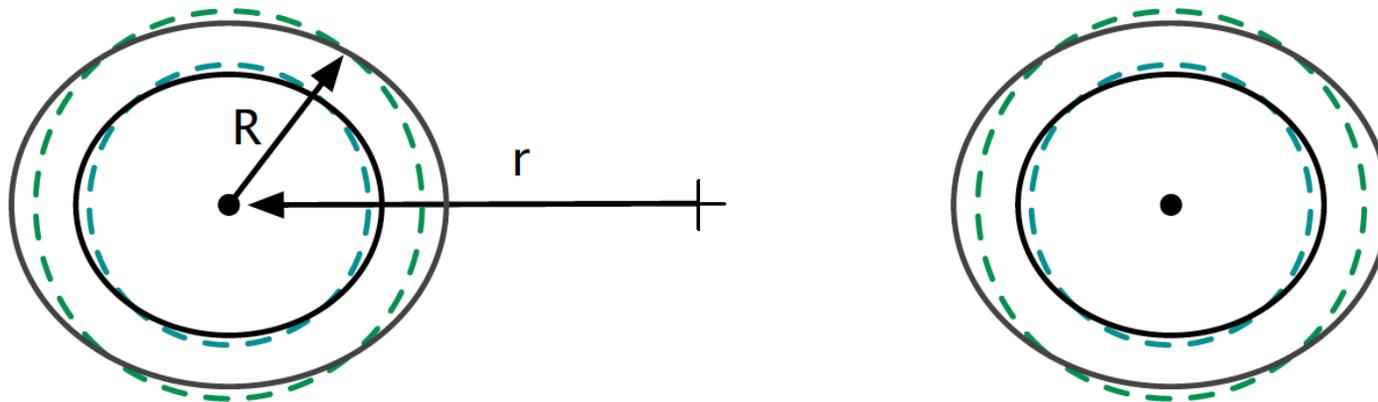


# Spectrum of NS-NS inspiral, 1.35-1.35, 45 Mpc

True EOS unknown!



Consider two extended bodies in orbit or free-fall:



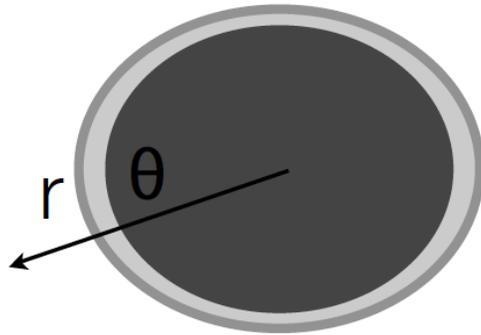
Residual gravitational effect is **tide**.

Amount of deformation depends on size and matter properties.

Deformation induces change in gravitational potential.

# Tides and the Quadrupole moment Q

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mass M radius R  
Love number k  
deformed by mass m  
distance a away

$$Q = \frac{2}{3} k R^5 \left( \frac{m}{d^3} \right)$$

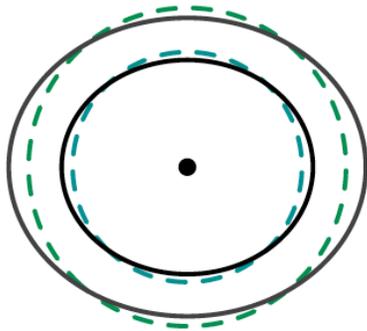
gives the gravitational potential  
around a deformed body

$$U = -\frac{M}{r} - \frac{3}{2} \frac{Q(\cos^2 \theta - 1)}{r^3}$$

This tells us about things like satellite movement, tidal locking (“back-reaction” on bulges), and **orbital dynamics in binary systems**

# Calculate in GR:

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Perturb a spherically symmetric neutron star  
impose quadrupole angular dependence  
look at scaling with distance from star  $r$

([0711.2420](#), [0906.1366](#), [0906.0096](#))

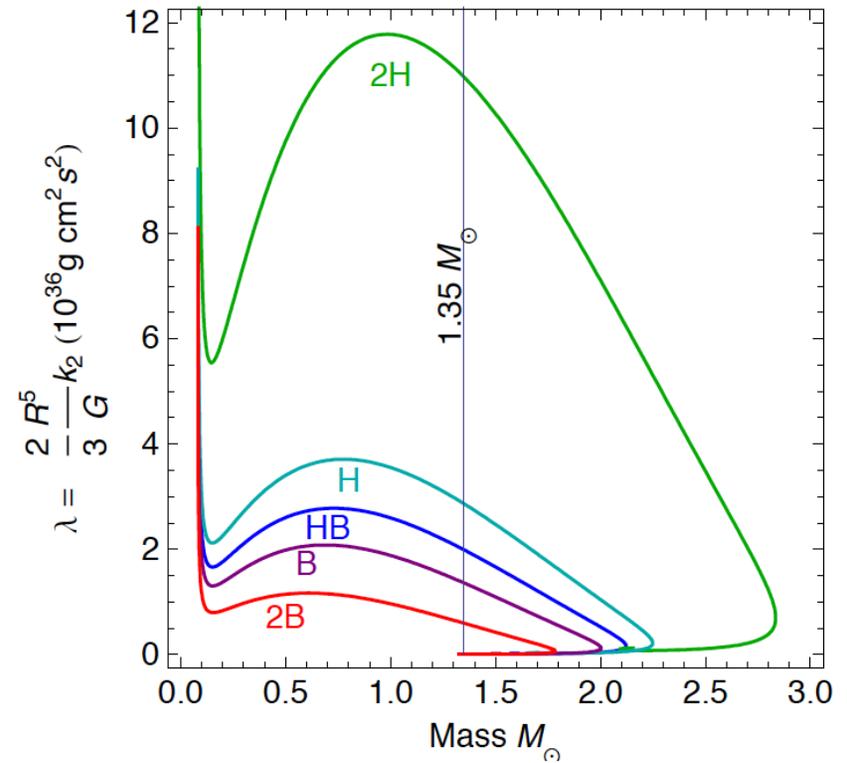
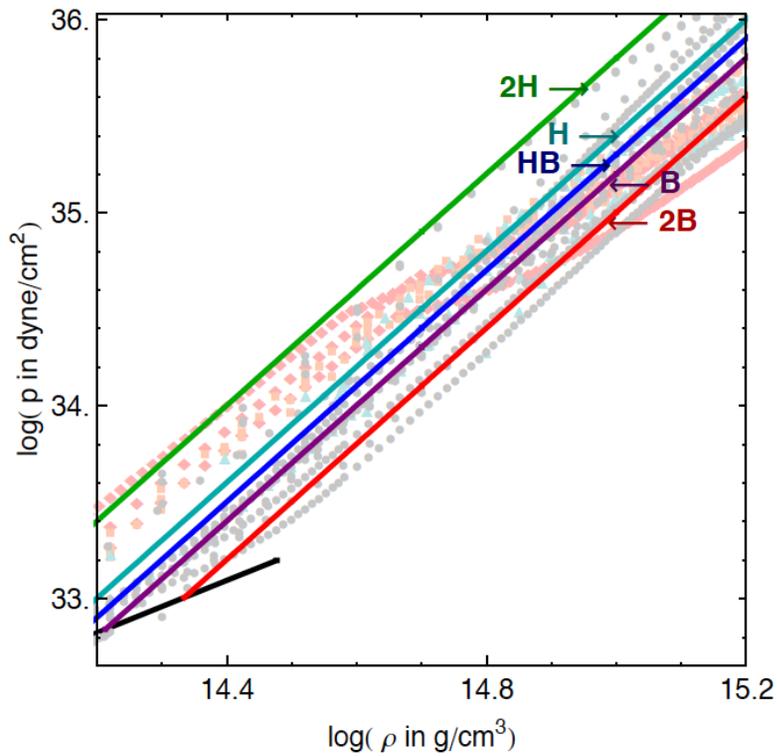
$$\lambda = \frac{Q}{\mathcal{E}} = \frac{\text{size of quadrupole deformation}}{\text{strength of external tidal field}} \quad \begin{array}{l} (\sim r^{-3}) \\ (\sim r^2) \end{array}$$

Love number  $k_2$

Radius  $R$

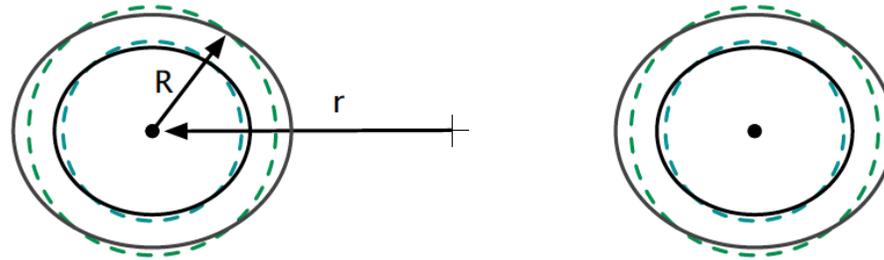
$$\lambda = \frac{2}{3} k_2 R^5 \quad (G = c = 1)$$

# Equation of state determines $\lambda$ for each M

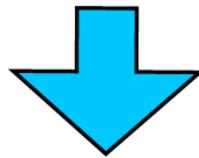


## Effect of tides on orbit:

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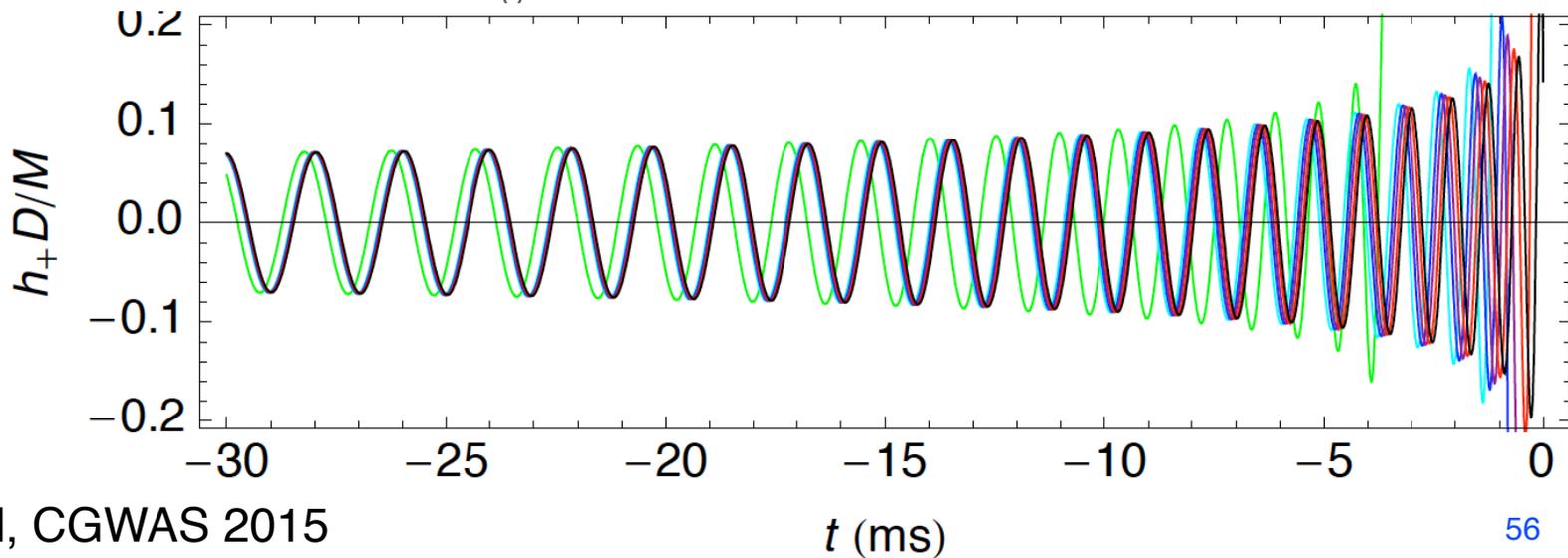
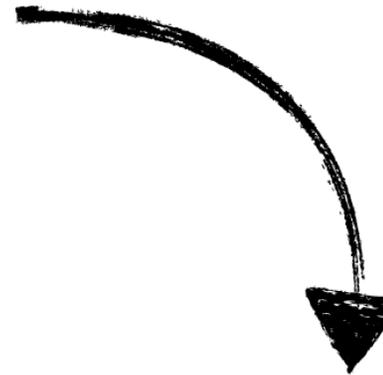
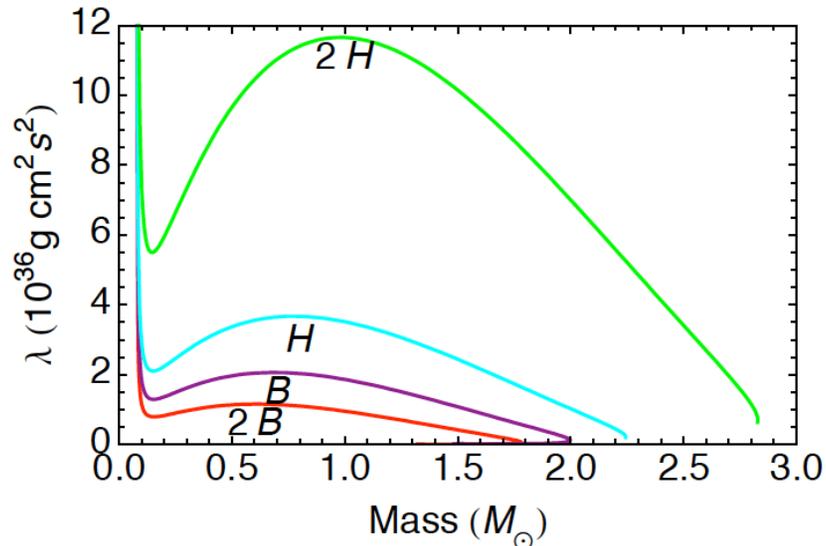


some energy into tides as stars come closer together  
a bit of extra GW luminosity from rotating quadrupoles

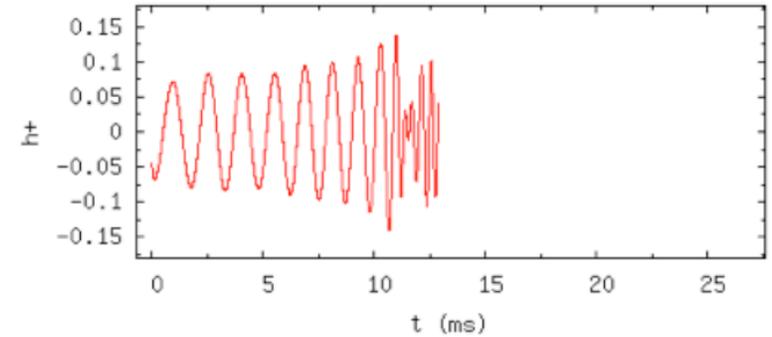
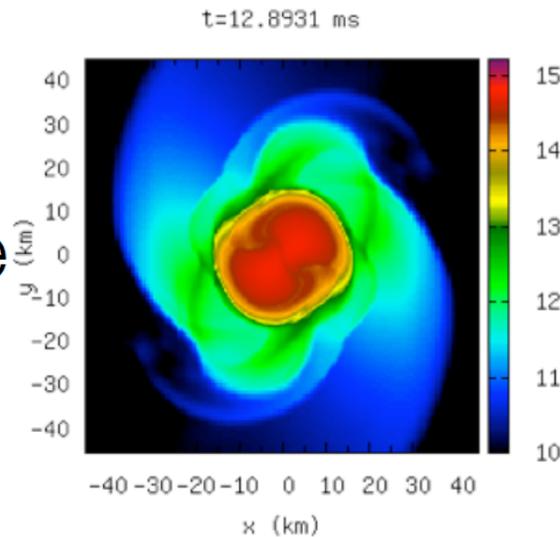


stars merge earlier

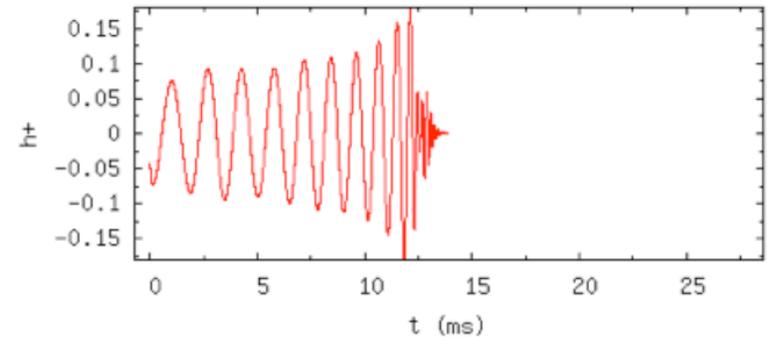
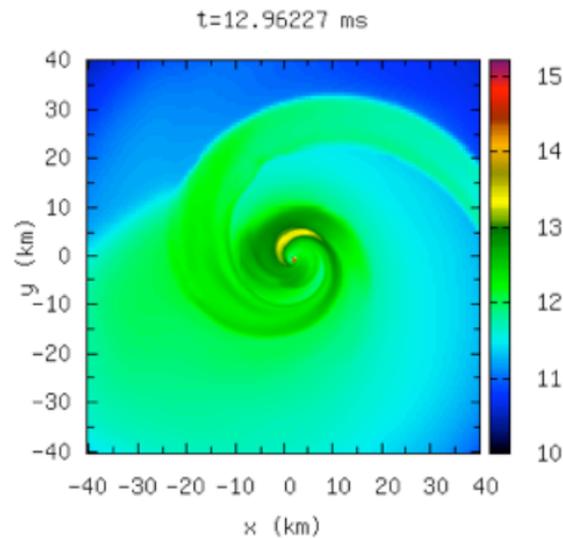
# Tidal effect on PN waveforms



Large stars,  
Hypermassive  
Remnant

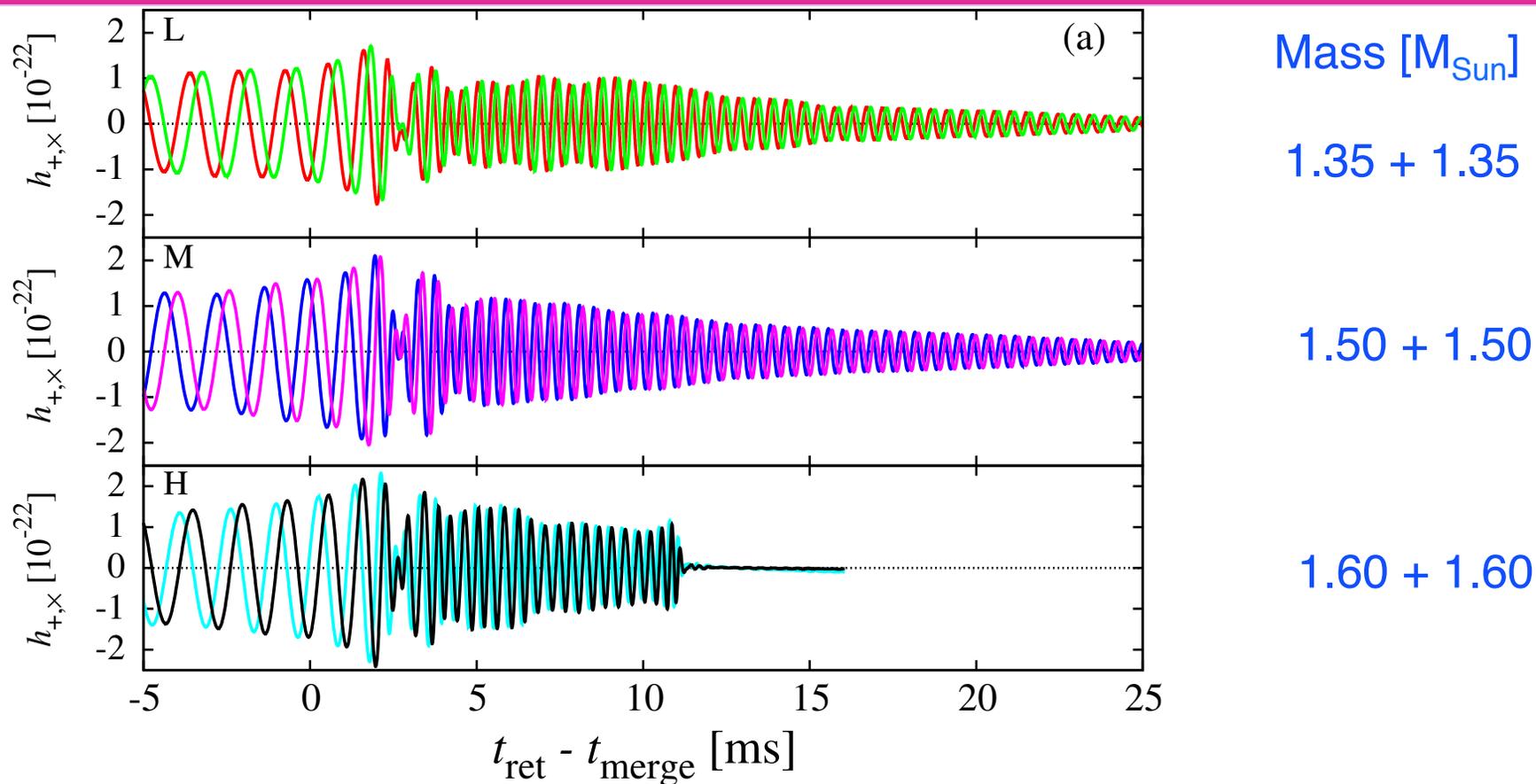


Compact  
stars,  
Prompt  
Collapse



Simulations & animations by K Hotokezaka

# Nuclear Astrophysics: NS-NS Mergers



Sekiguchi+ 11: First full GR NS-NS simulation with realistic microphysics, finite-temperature nuclear EOS of H. Shen+ '98, '11

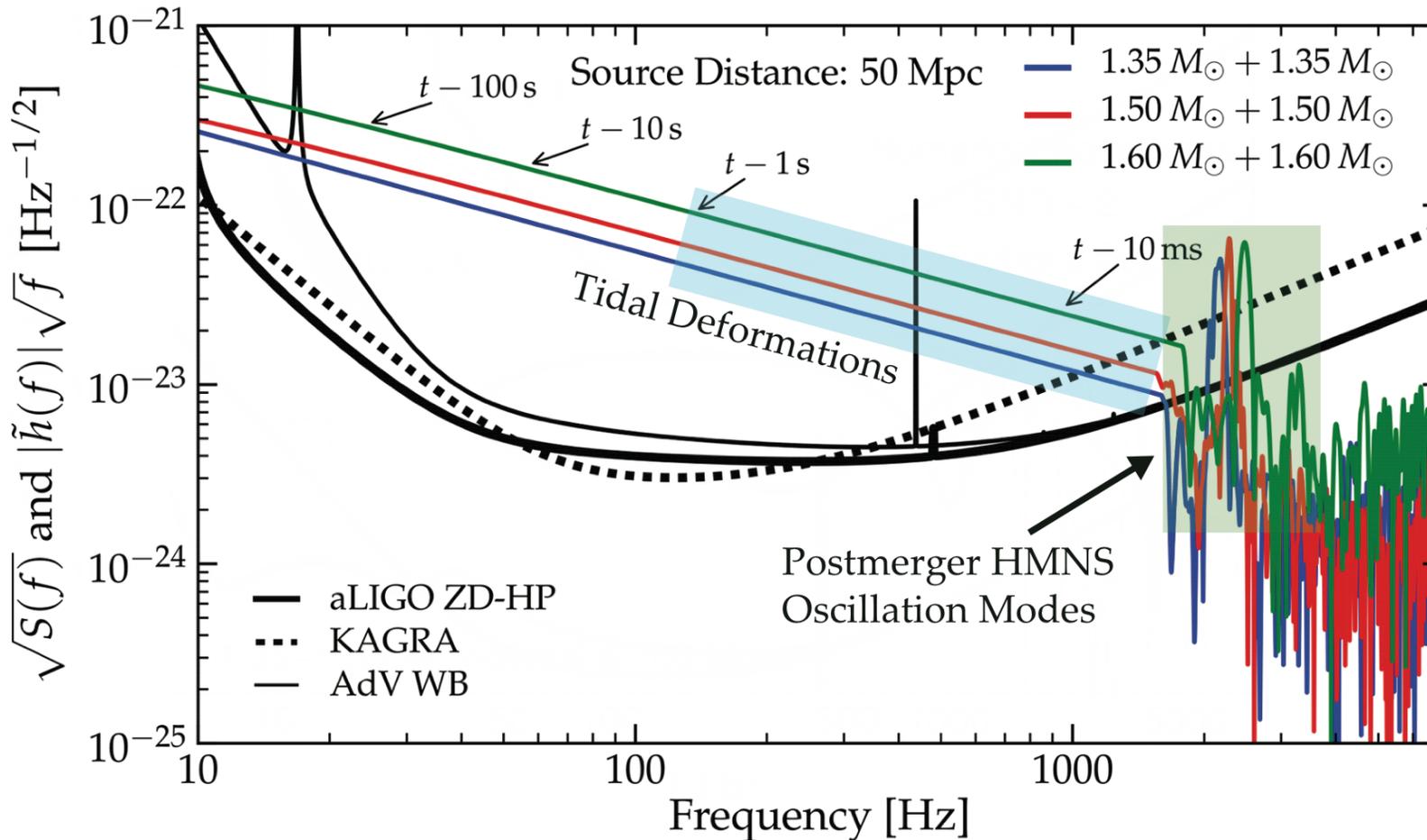


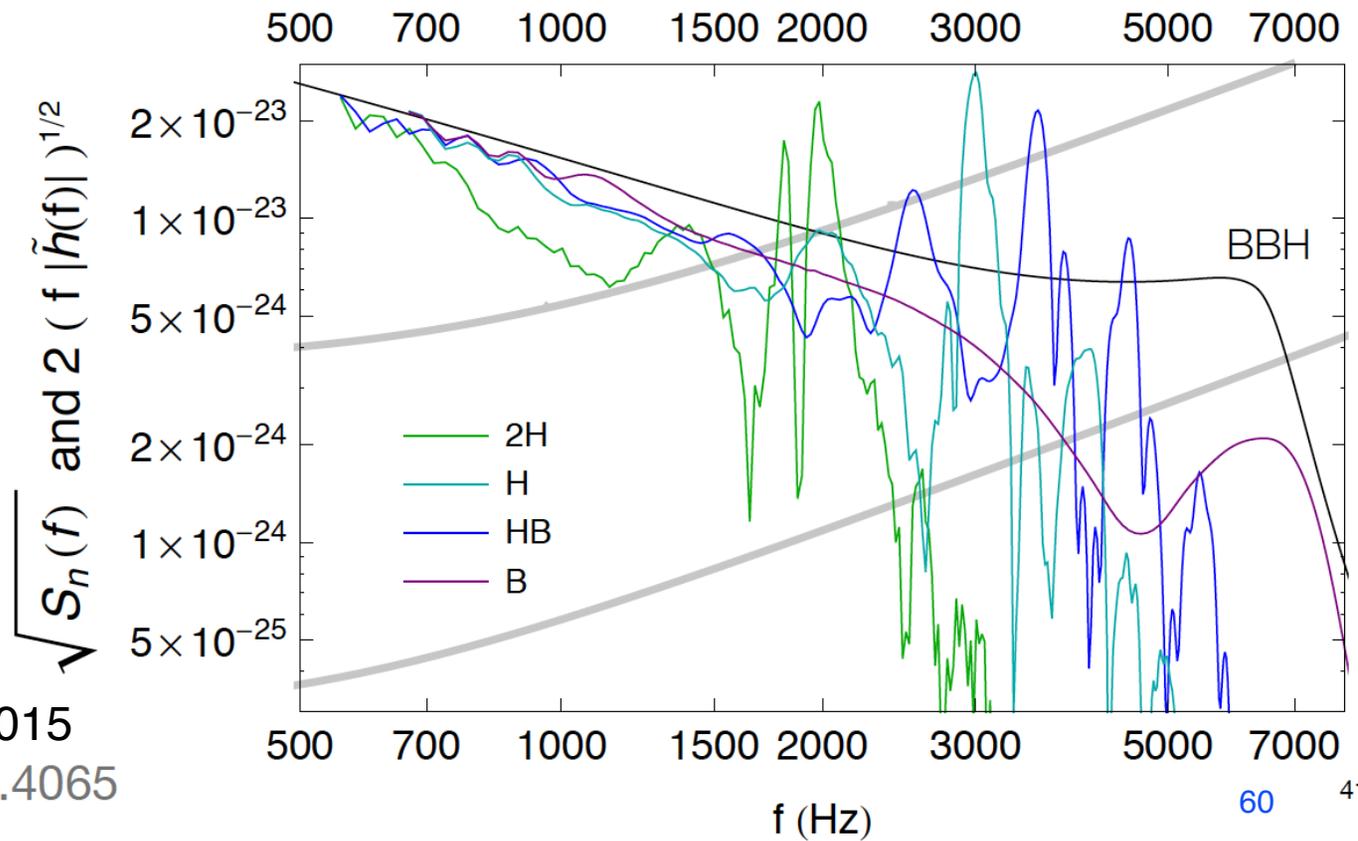
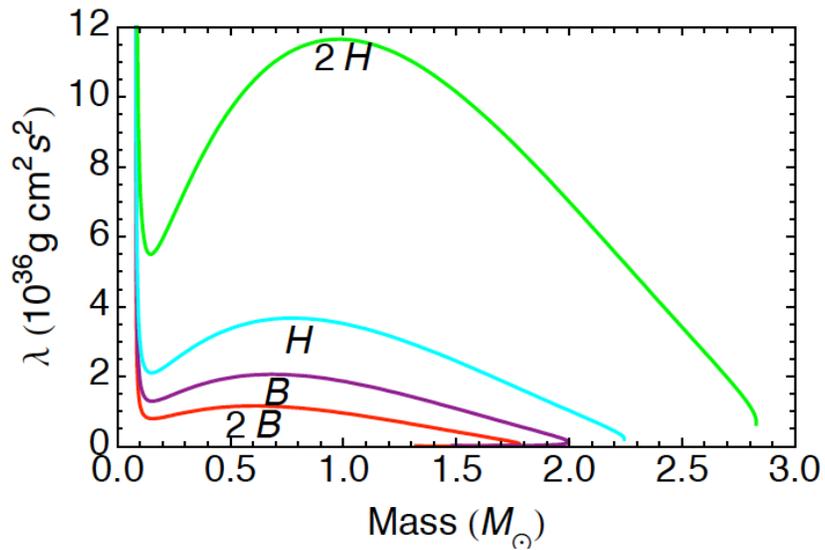
**LIGO**

# Effects of tidal disruption of neutron stars near merger



Credit: Daniel Price and Stephan Rosswog

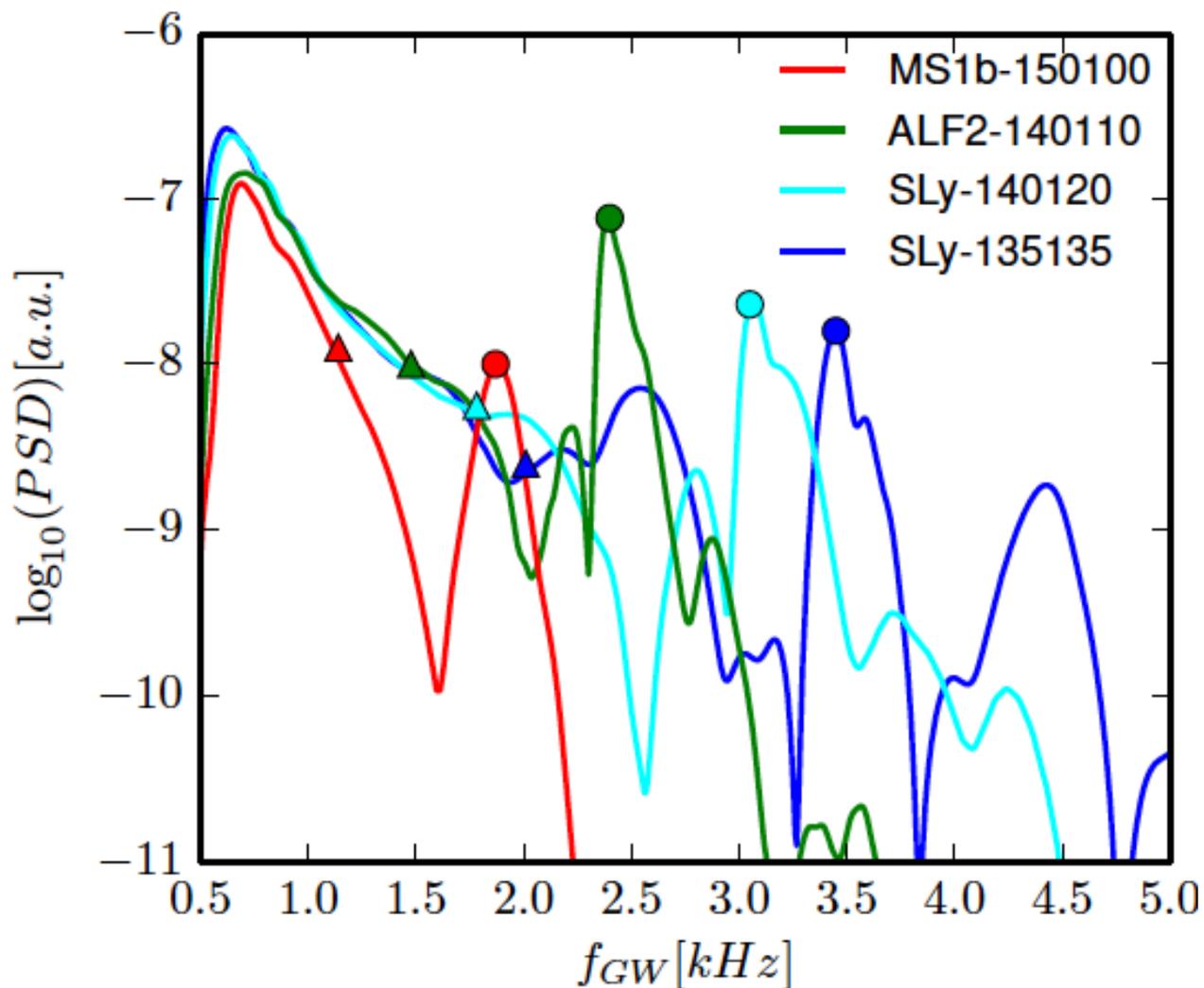




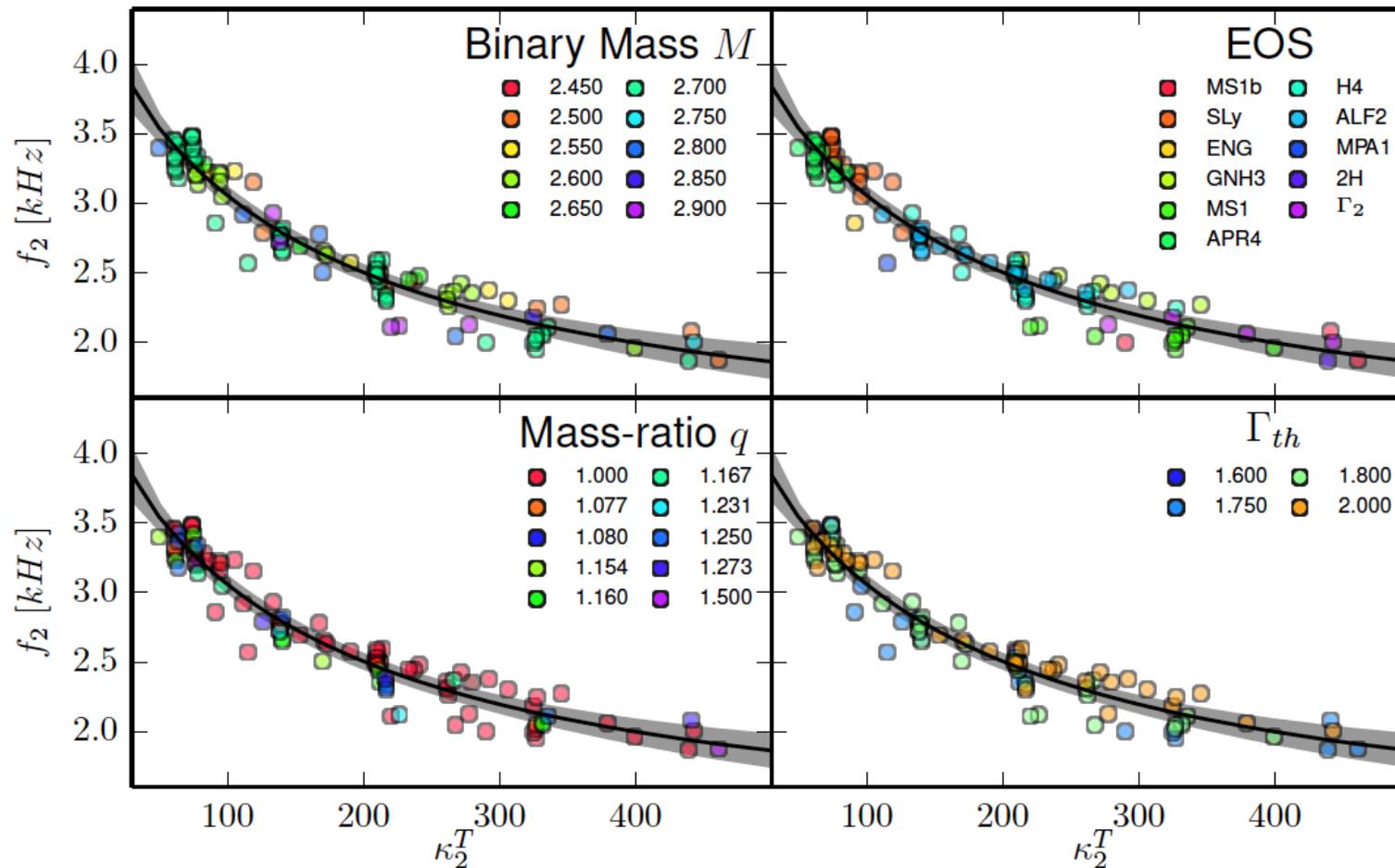
J. Read, CGWAS 2015

• [arxiv.org/abs/1306.4065](http://arxiv.org/abs/1306.4065)

# Frequency of peak of final hyper-massive NS resonance



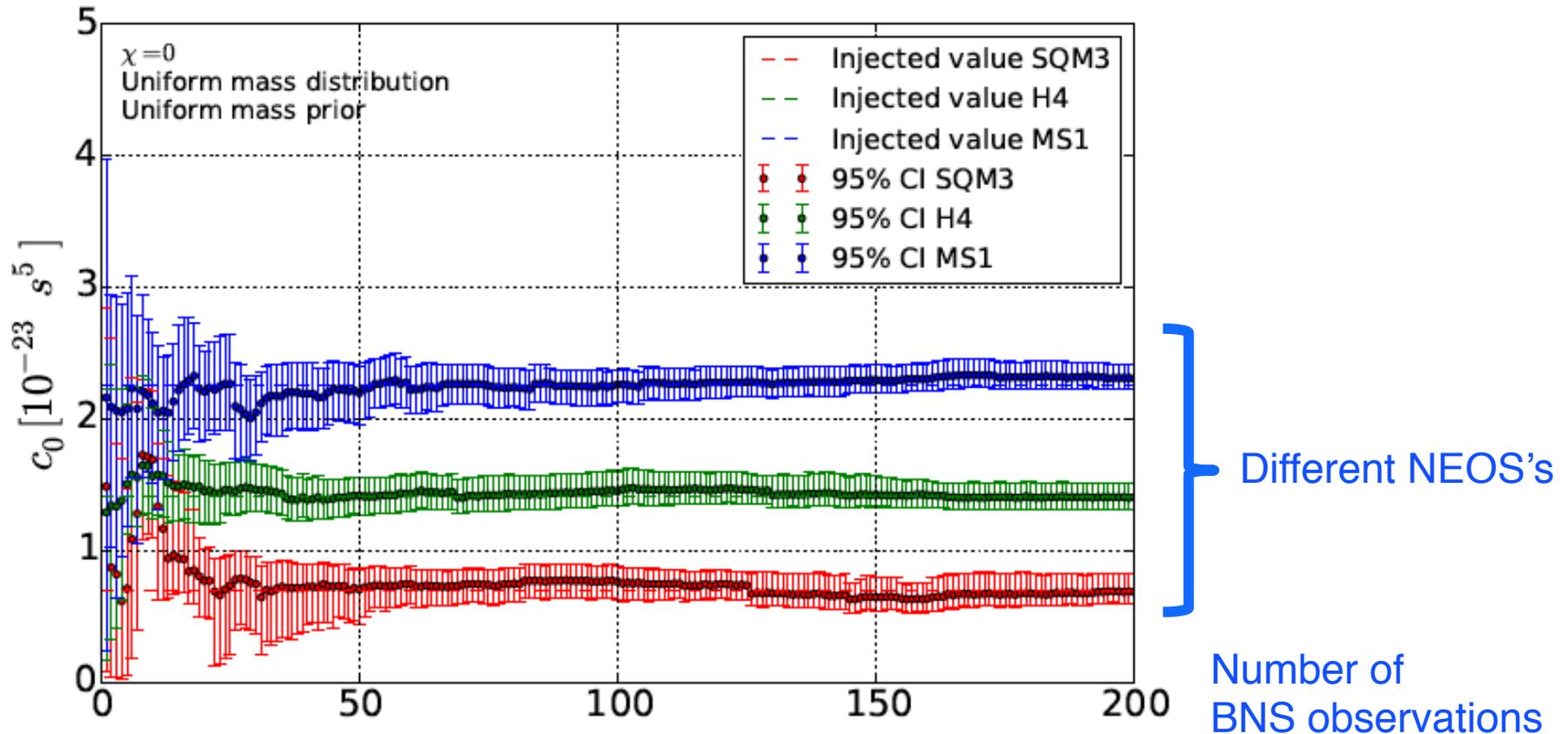
# Universality of peak frequency



$$\kappa_2^T = 2 \left( \frac{q^4}{(1+q)^5} \frac{k_2^A}{C_A^5} + \frac{q}{(1+q)^5} \frac{k_2^B}{C_B^5} \right)$$

S Bernuzzi, T Dietrich, A Nagar,  
Phys Rev Lett 115, 091101 (2015) arxiv.org:1504.01764

# Many observations required to constrain NEOS

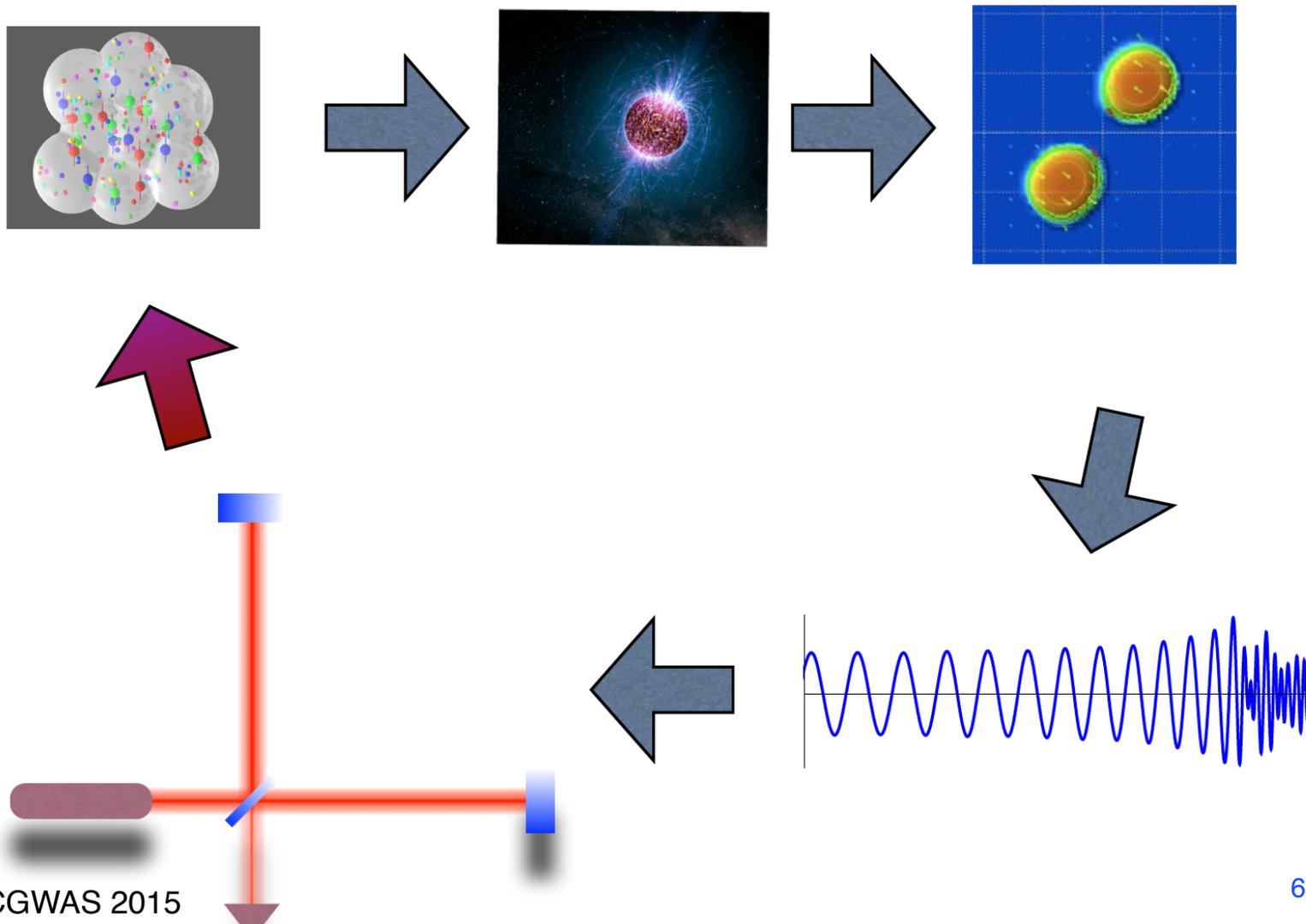


$$Q_{ij} = -\lambda(\text{EOS}; m) \mathcal{E}_{ij}$$

$$\lambda(m) = (2/3)k_2(m)R^5(m)$$

M. Agathos et al (LVC), Phys. Rev. D 92, 023012 (2015),  
 arXiv:1503.05405v1

# Constraining the NEOS using GWs from BNS





THANK YOU!

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Questions?