

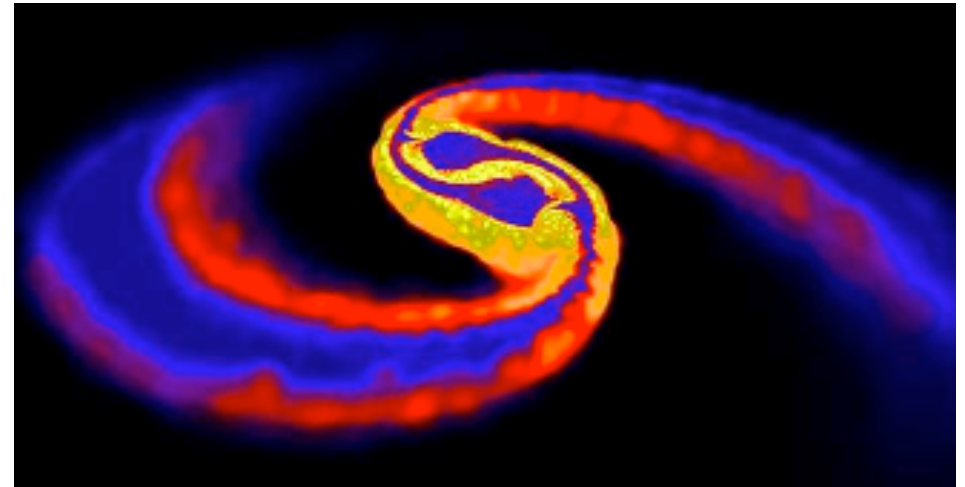
Compact Binary Mergers, Nuclear EOS, and LIGO

- GWs and LIGO
- Compact binary mergers
- prospects for LIGO GW detection and EM counterparts
- Neutron stars
- Nuclear EOS
- Neutron star mass & radius
- BNS mergers
- BNS r-process nucleosynthesis
- BNS merger constrains on NEOS

Alan Weinstein, Caltech
for the LIGO Scientific Collaboration

DOE/NSF NSAC Meeting,
Bethesda, March 23, 2016

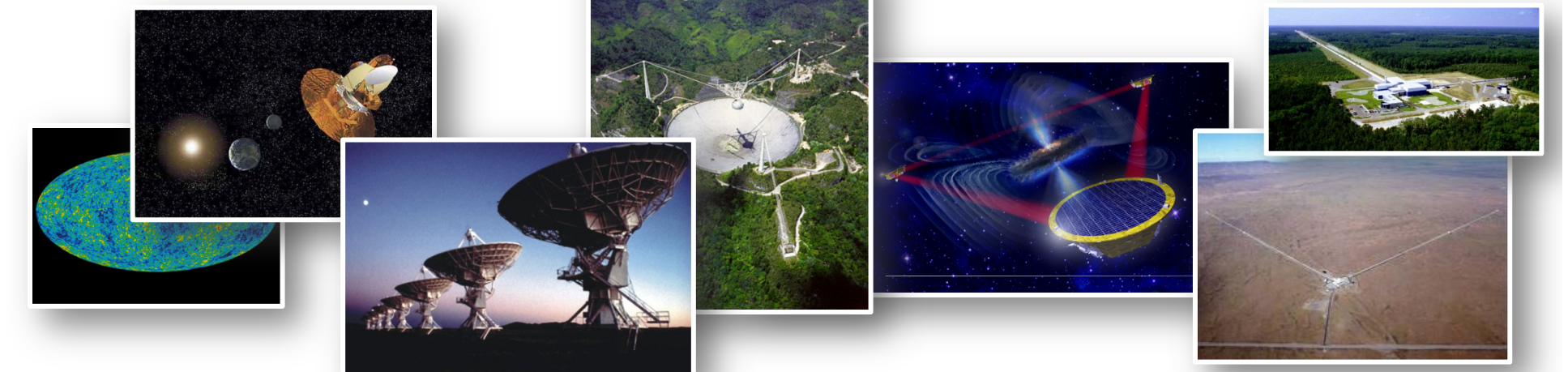
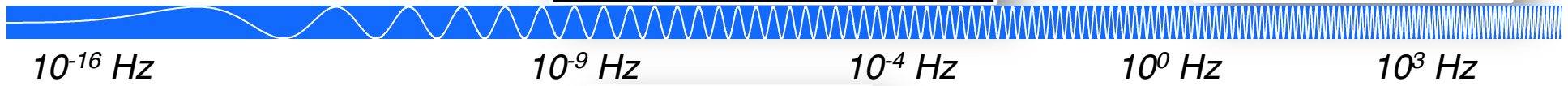
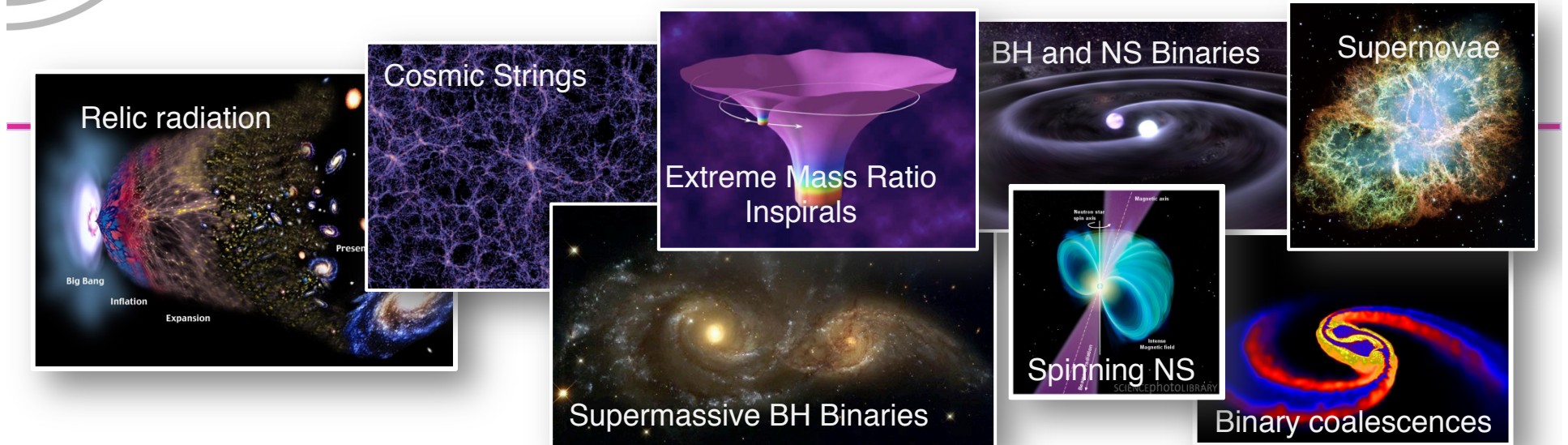
LIGO-G1600723



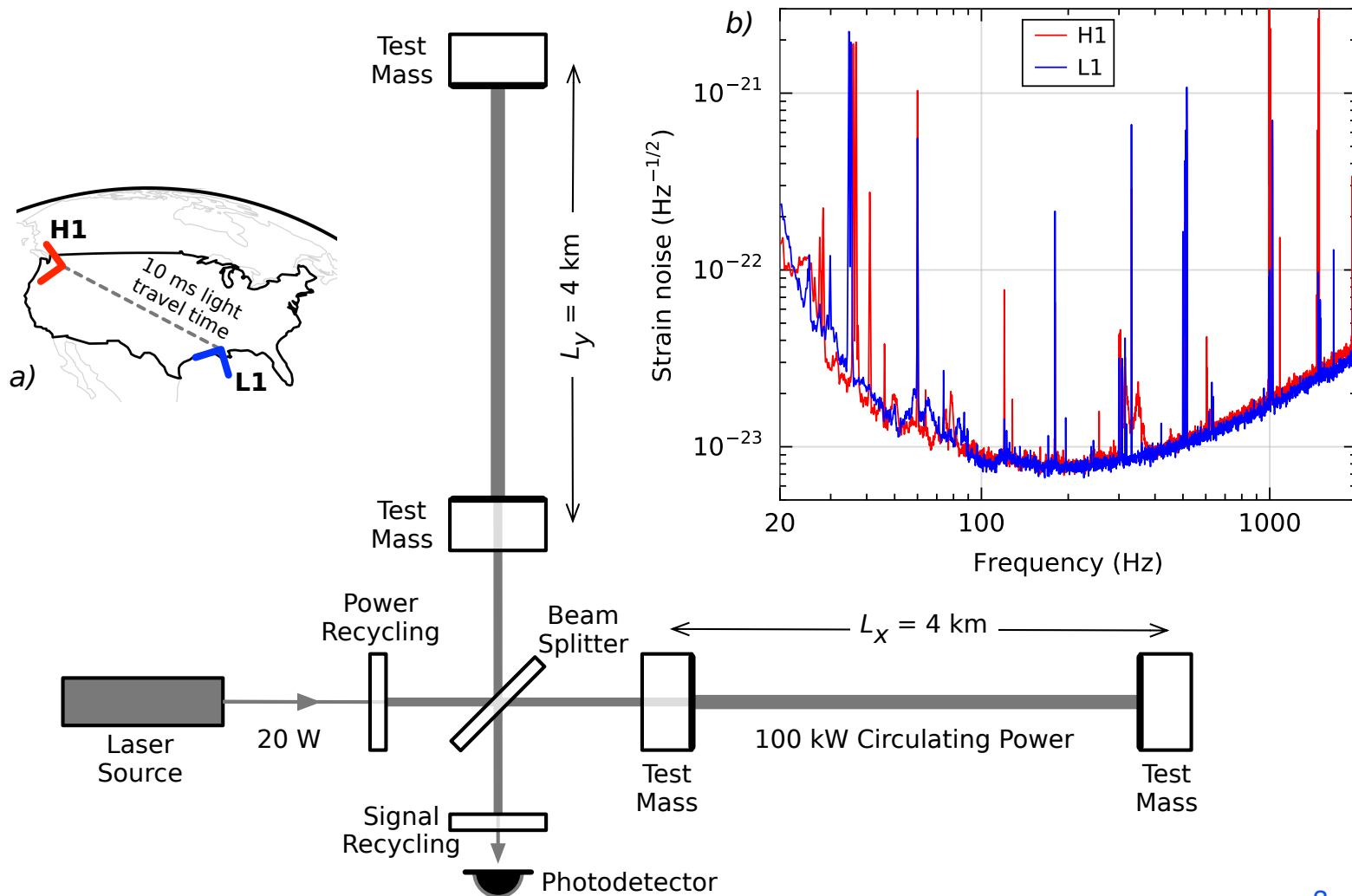
"Merging Neutron Stars" (Price & Rosswog)



The GW Spectrum



The Advanced LIGO detectors



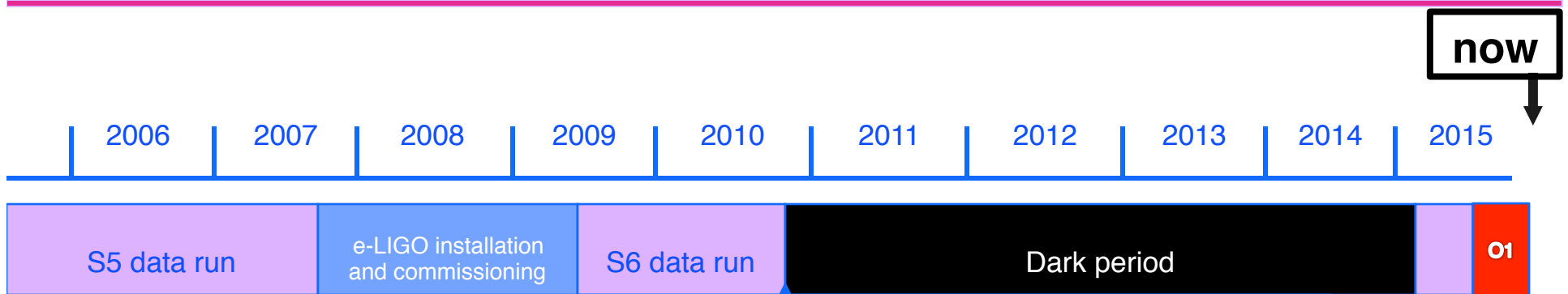


LIGO Scientific Collaboration





iLIGO → eLIGO → aLIGO

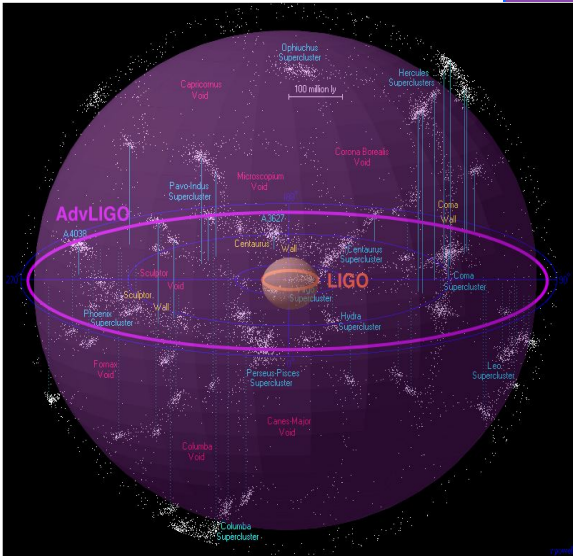


S6 data analysis & preparations for Advanced LIGO commissioning and open data

Advanced LIGO Project

Adv LIGO Installation begins

Commissioning & initial data With Advanced LIGO

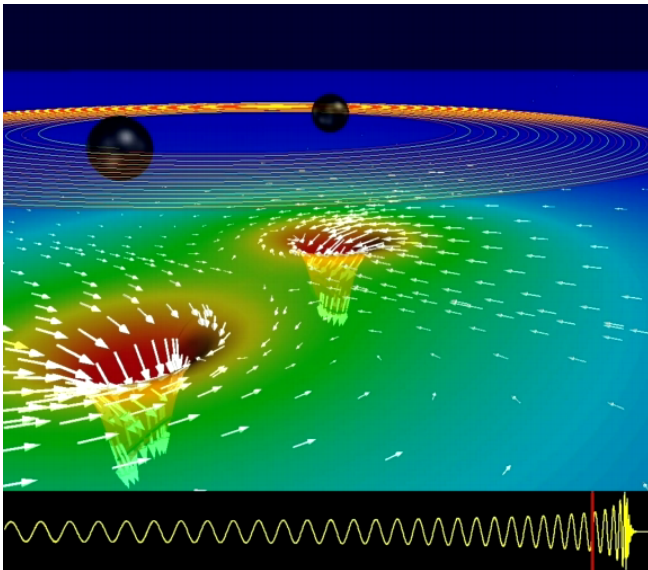
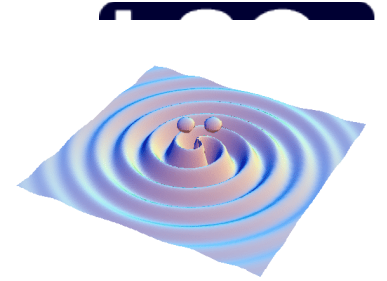


Improve amplitude sensitivity by a factor of 10x, and...
 ⇒ Number of sources goes up 1000x!

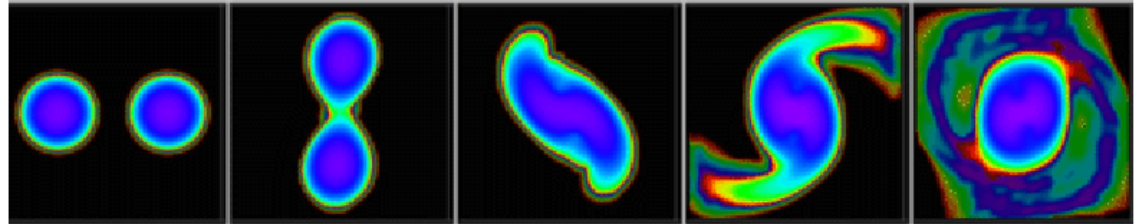


LIGO

GWs from coalescing compact binaries (NS/NS, BH/BH, NS/BH)

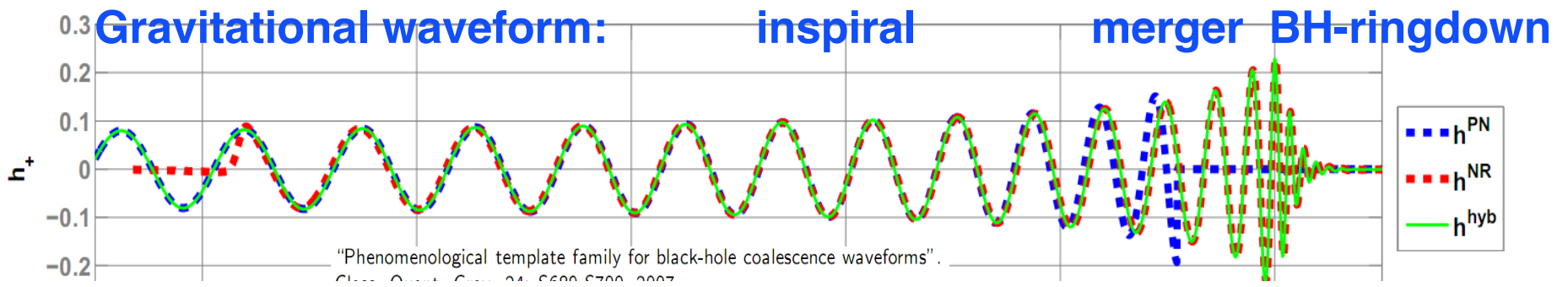


- Neutron star – neutron star (Centrella et al.)



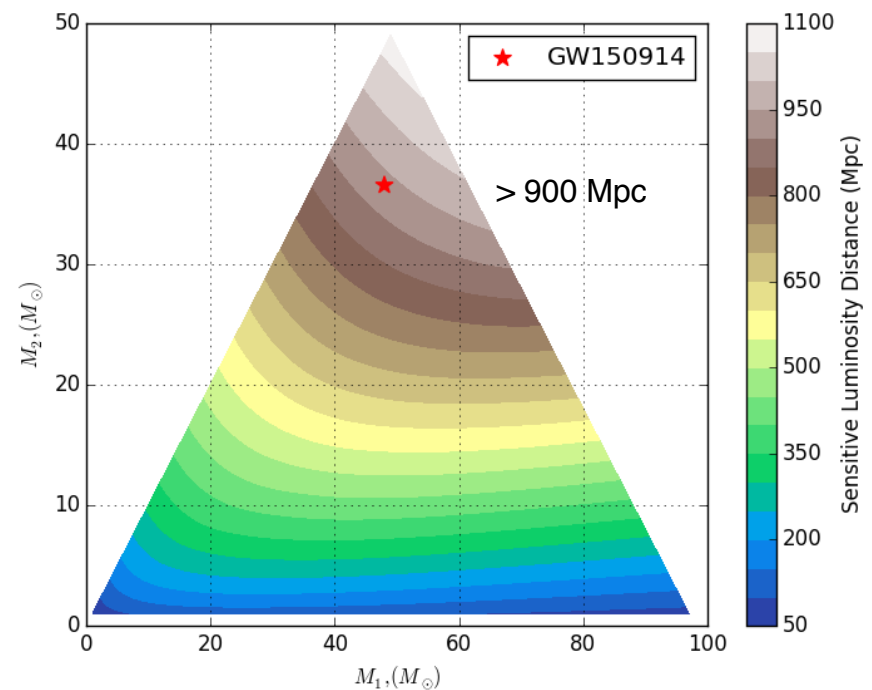
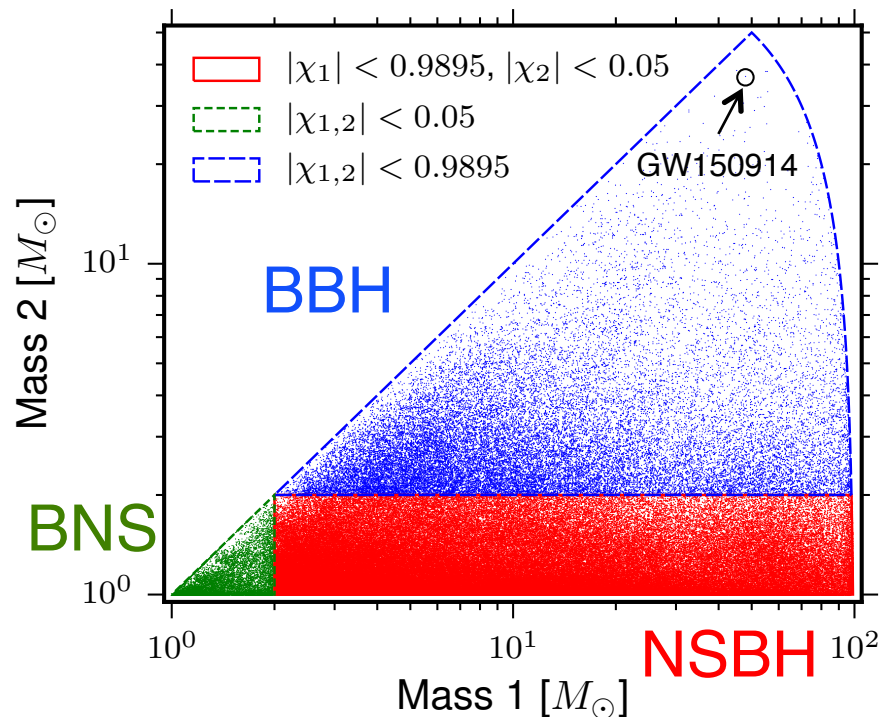
Tidal disruption of neutron star

A unique and powerful laboratory to study strong-field, highly dynamical gravity and the structure of nuclear matter in the most extreme conditions



Waveform carries lots of information about binary masses, orbit, merger

Template-based searches

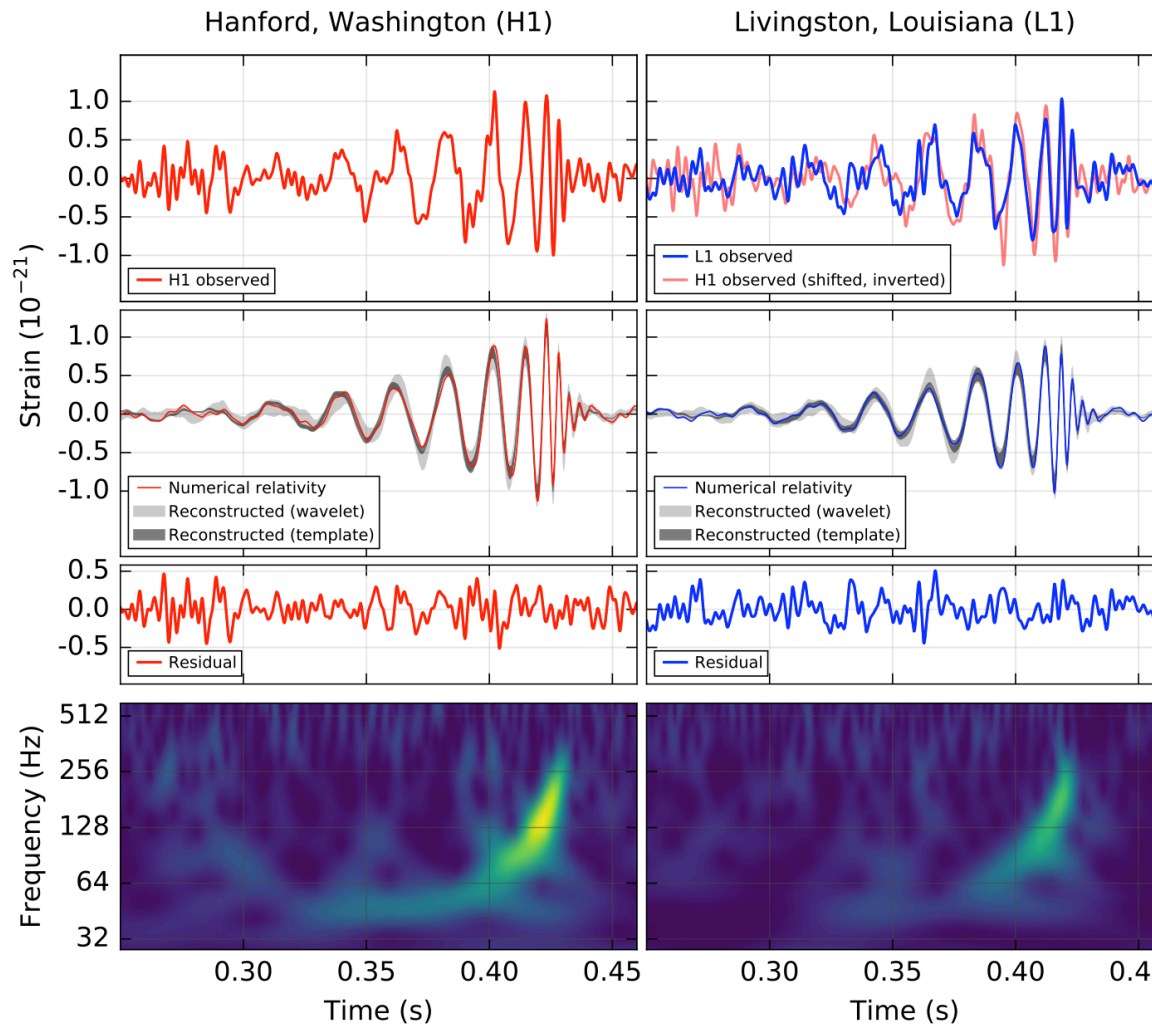


Masses and (aligned) spins
 Templates spaced for $< 3\%$
 loss of SNR: 250K templates.

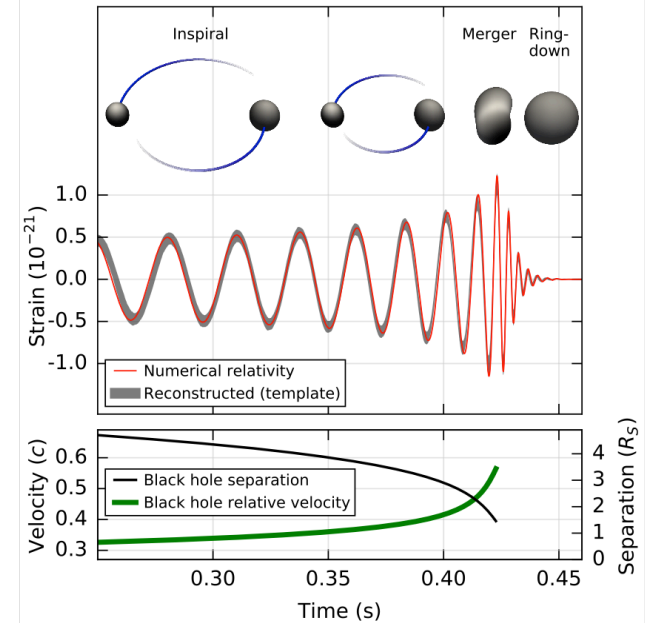
Sensitive distance in Mpc

GW150914

Phys. Rev. Lett. 116, 061102 – Published 11 February 2016
<https://dcc.ligo.org/LIGO-P150914/public/main>



Whitened and band-passed [40-300] Hz



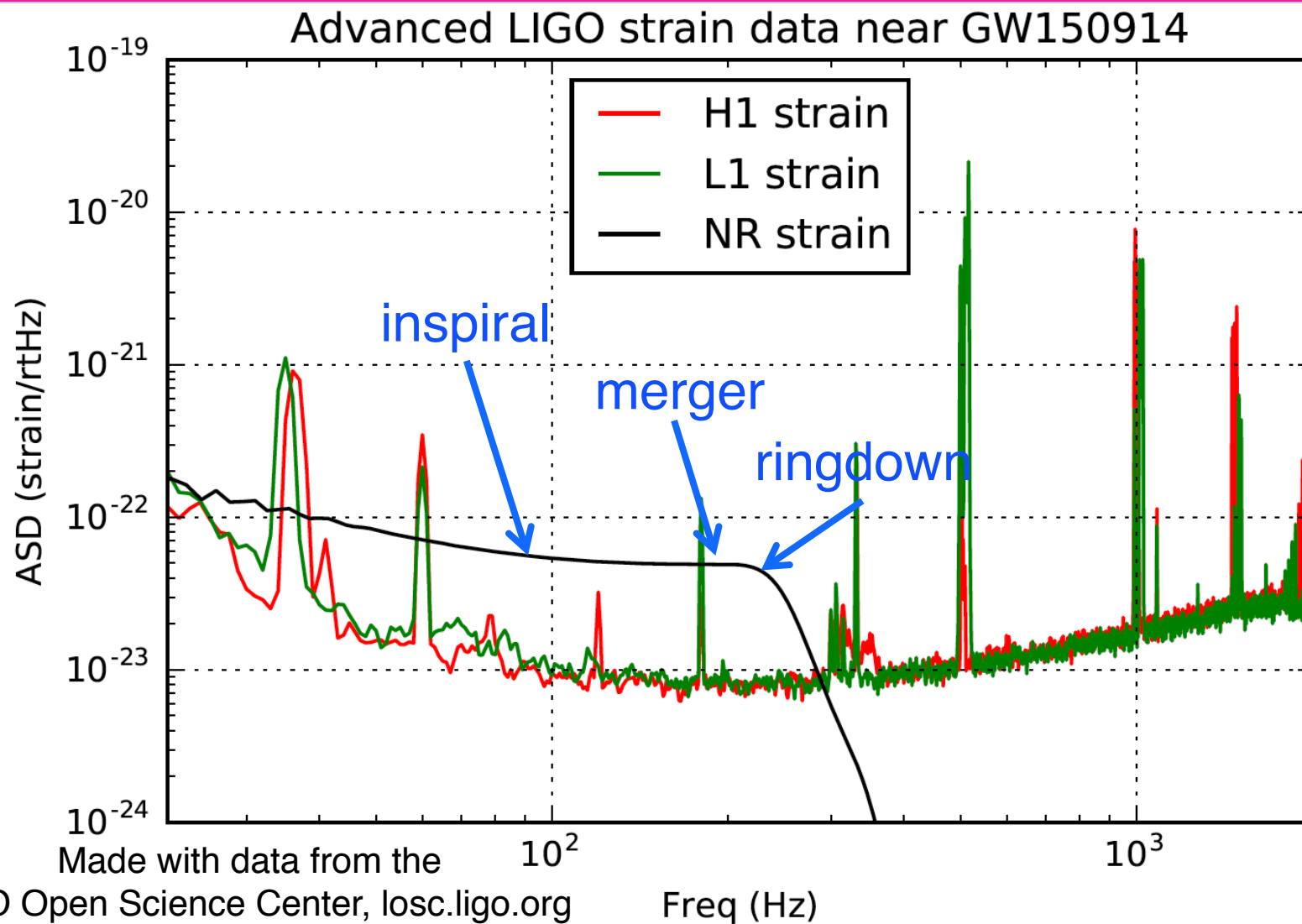
Reconstructed
(no whitening)

Audio:

- filtered data
- freq-shifted data
- reconstructed & shifted

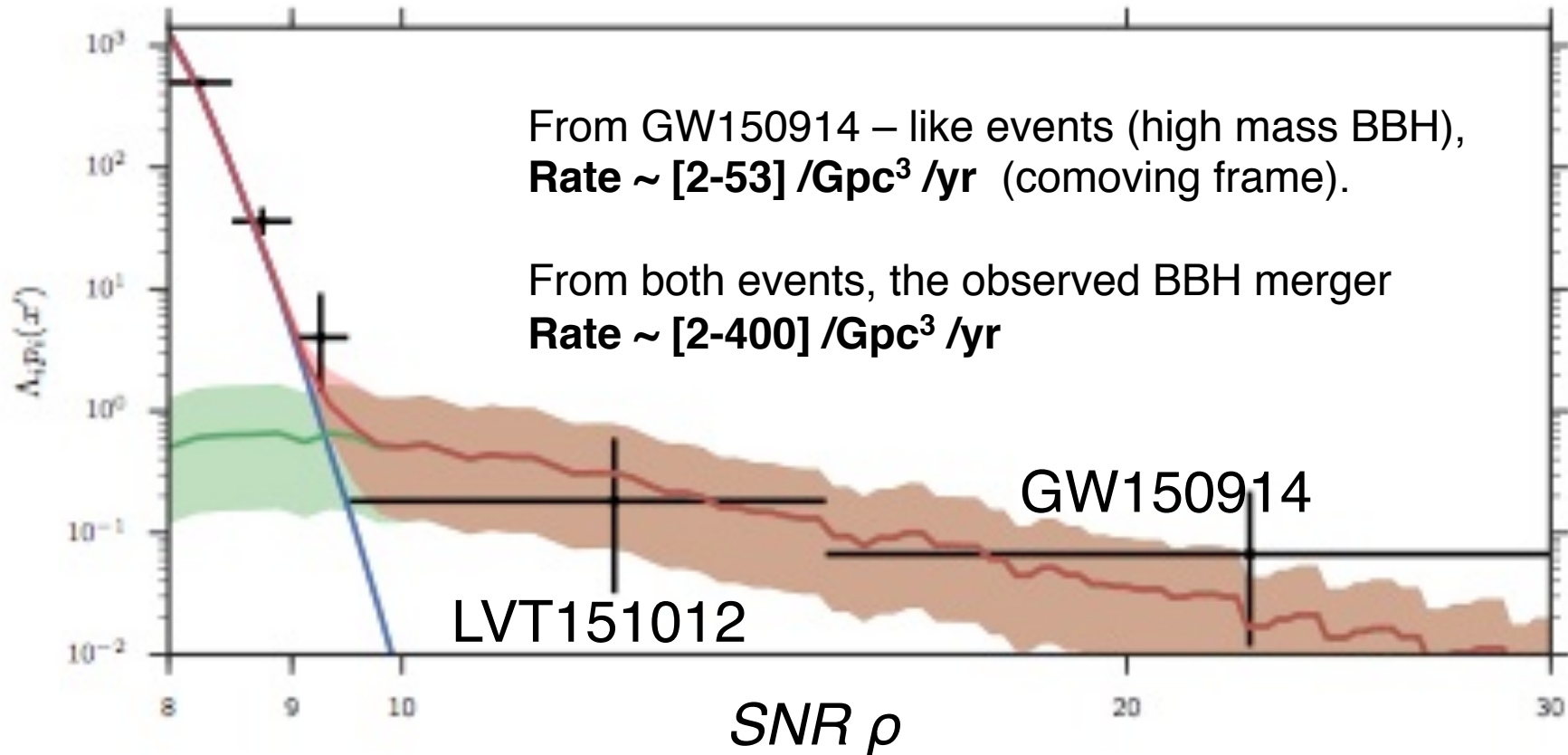


GW150914 in the frequency domain



Observed BBH merger rate

<https://dcc.ligo.org/LIGO-P1500217/public/main>

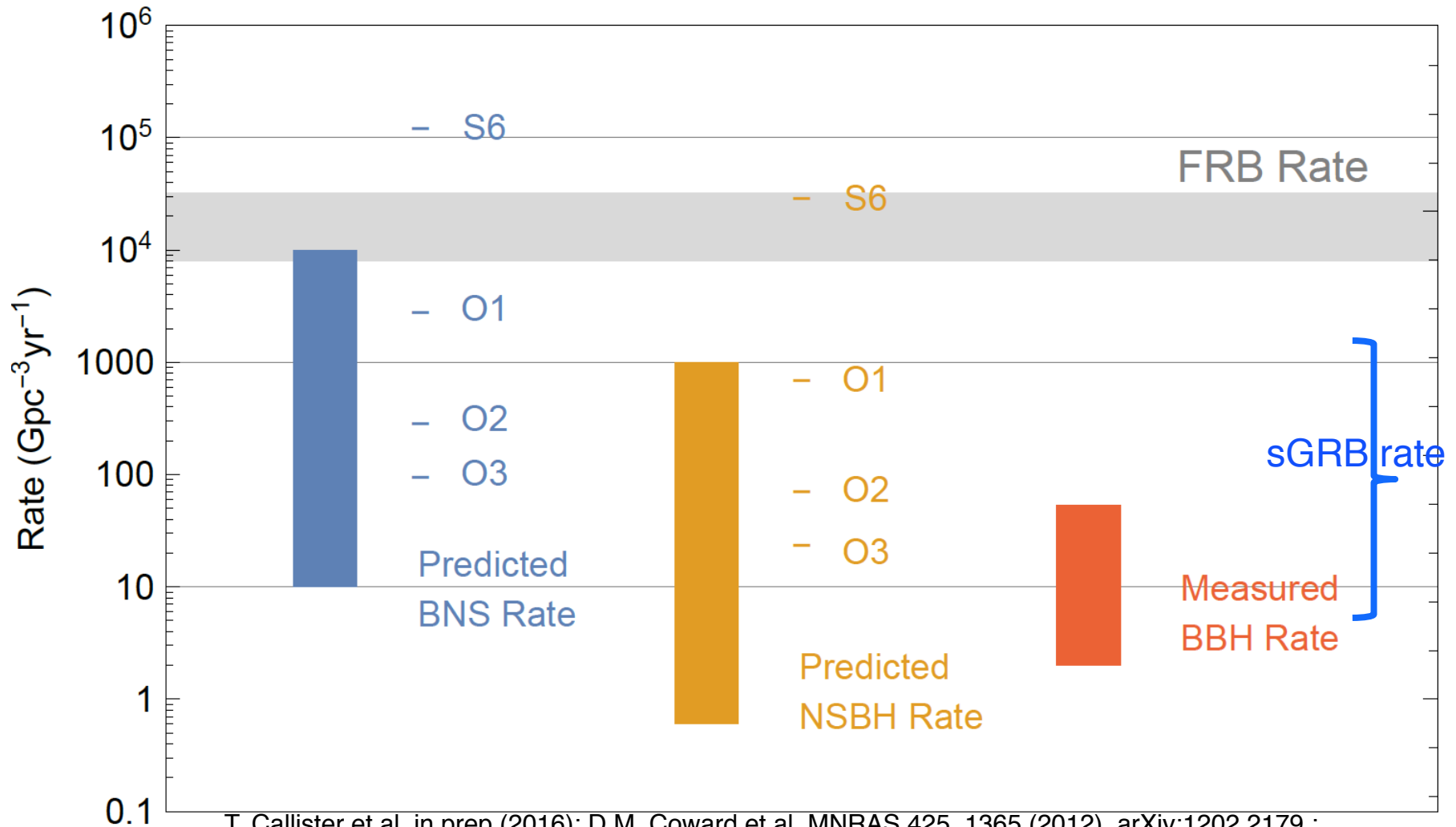


Same ballpark as population synthesis models, CCSN rate, etc

iLIGO+eLIGO BBH rate upper limit: $\sim < 420 \text{ Gpc}^{-3} \text{ yr}^{-1}$



Expected (and measured!) compact binary merger rates

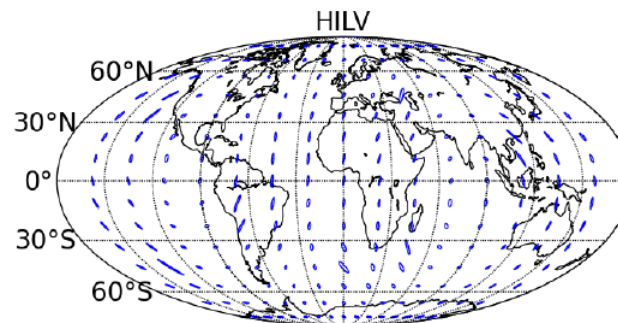
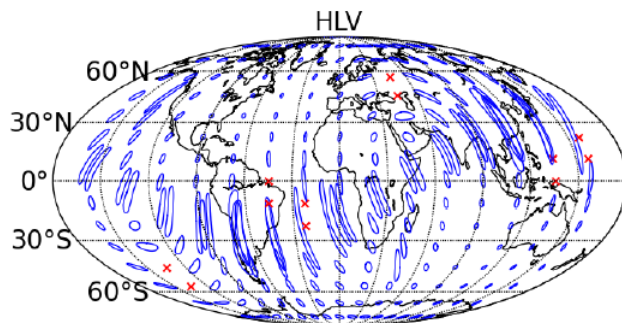


T. Callister et al, in prep (2016); D.M. Coward et al, MNRAS 425, 1365 (2012), arXiv:1202.2179 ;
B. Abbott et al, Living Rev. Relativity, 19, 1 (2016) arXiv:1304.0670.

Expected ranges of binary neutron star merger rates and detections

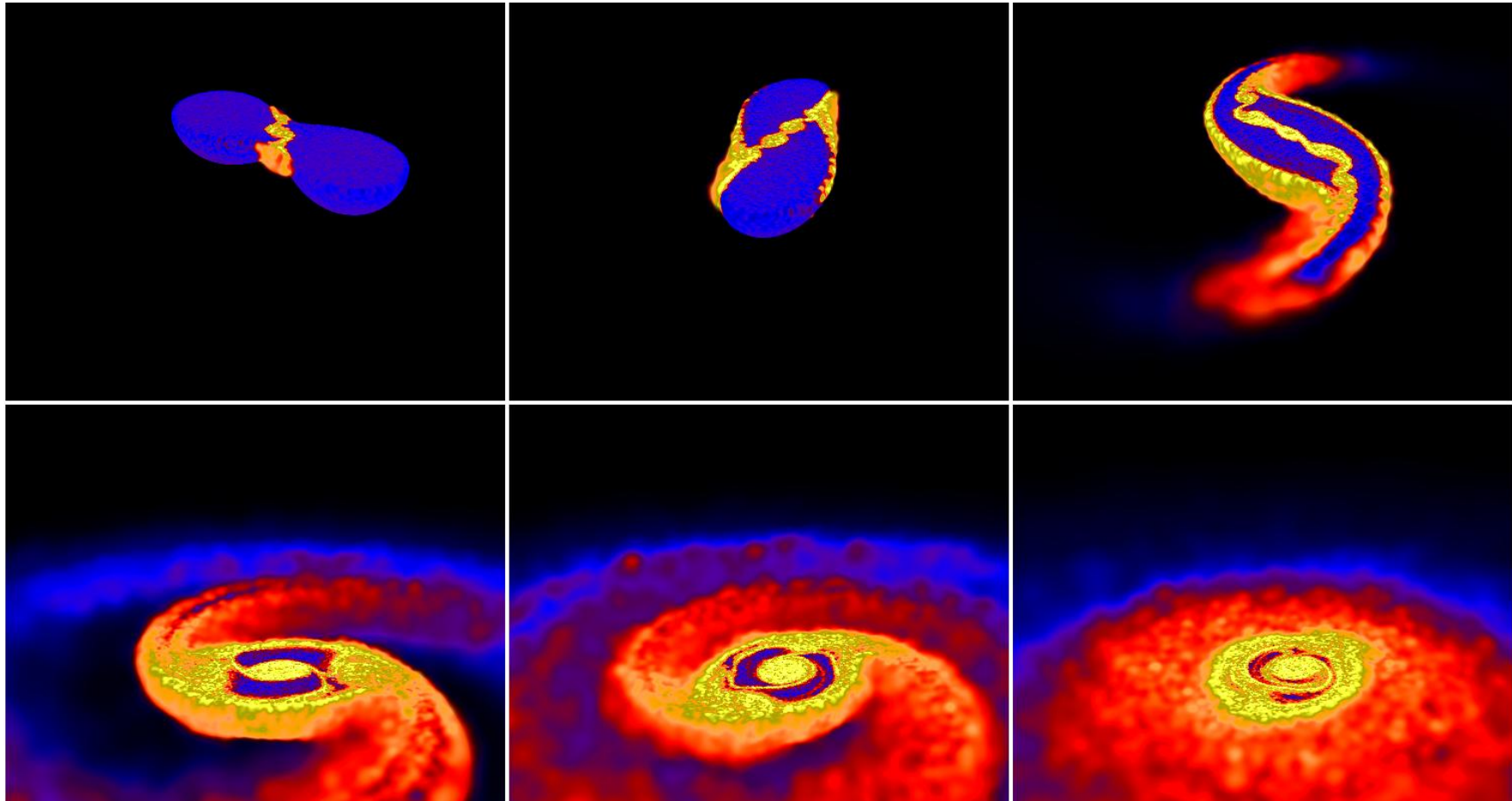
- “It’s tough to make predictions, especially about the future” (Yogi Berra)
- Estimated BNS rate: $[10^1 - 10^4] \text{ Gpc}^{-3}\text{yr}^{-1}$

Epoch	Estimated Run Duration	BNS Range (Mpc)		Number of BNS Detections
		LIGO	Virgo	
2015	3 months	40 – 80	–	0.0004 – 3
2016–17	6 months	80 – 120	20 – 60	0.006 – 20
2017–18	9 months	120 – 170	60 – 85	0.04 – 100
2019+	(per year)	200	65 – 130	0.2 – 200
2022+ (India)	(per year)	200	130	0.4 – 400

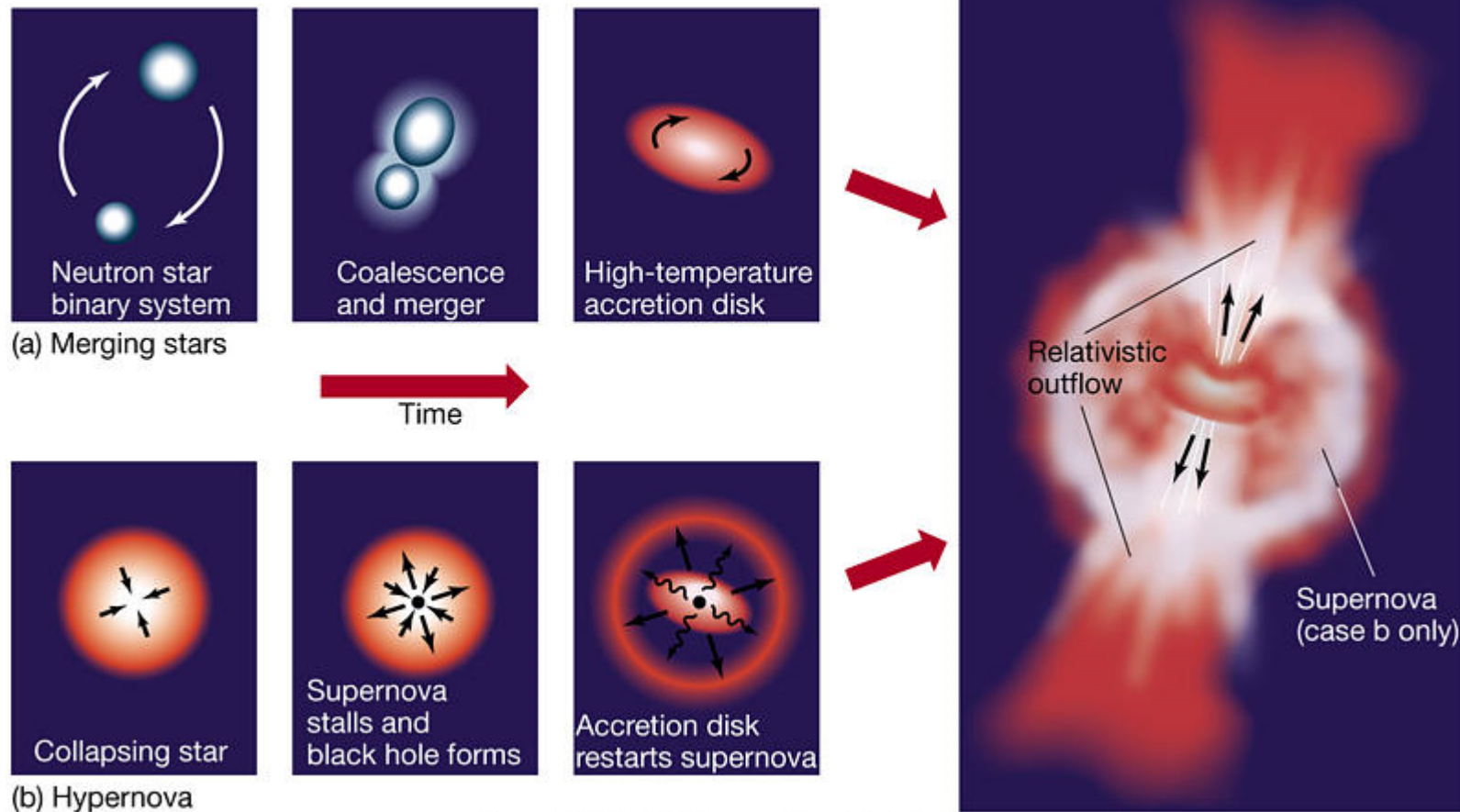


LIGO and Virgo Collaborations,
 “Prospects for Observing and Localizing
 Gravitational-Wave Transients with Advanced
 LIGO and Advanced Virgo”
Living Rev. Relativity, 19, 1 (2016)

Binary neutron star mergers are a unique laboratory for nuclear (astro)-physics

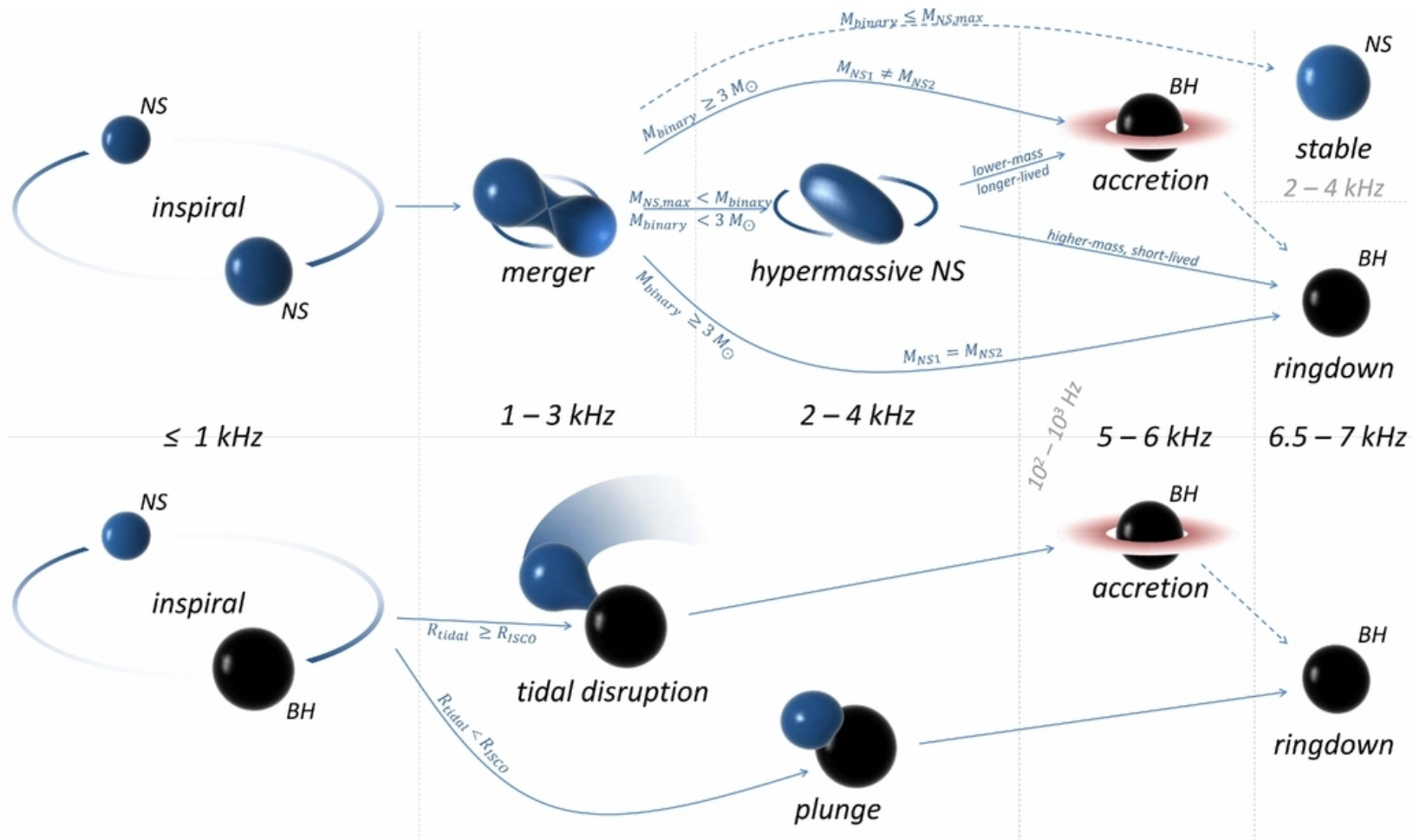


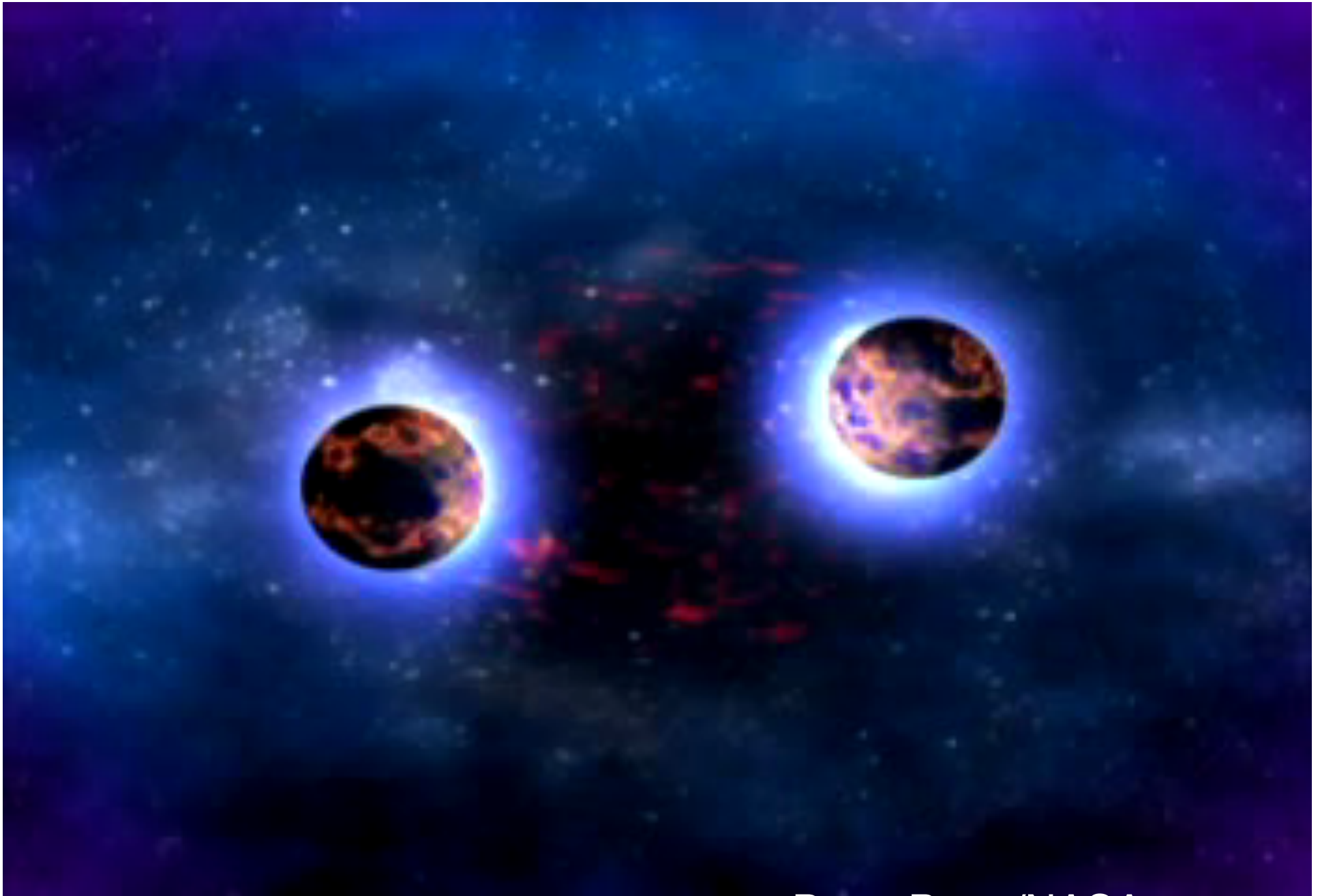
Short-hard and Long-soft GRBs



BNS and NSBH mergers

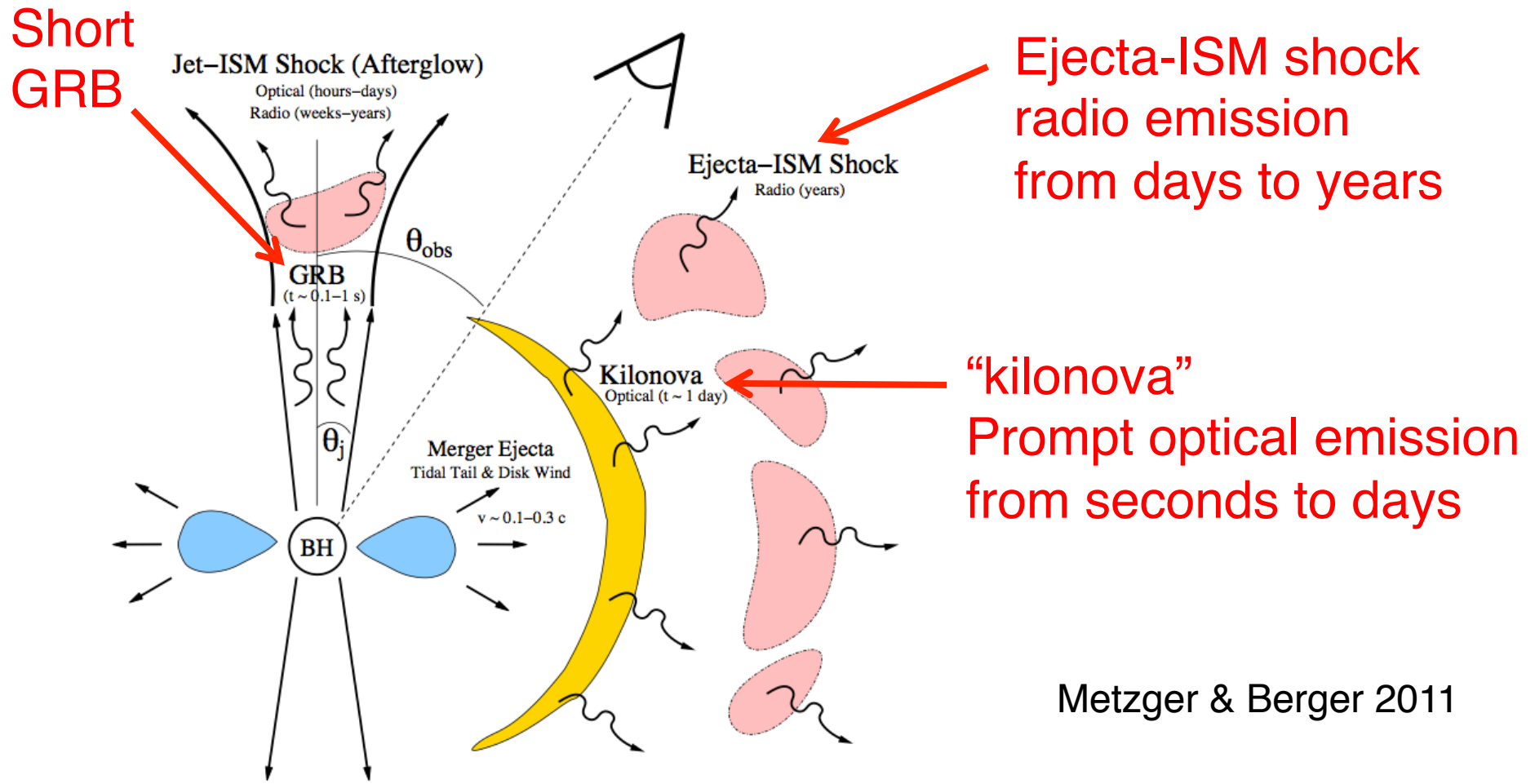
Figure 1 from I Bartos et al 2013 Class. Quantum Grav. 30 123001





Dana Berry/NASA

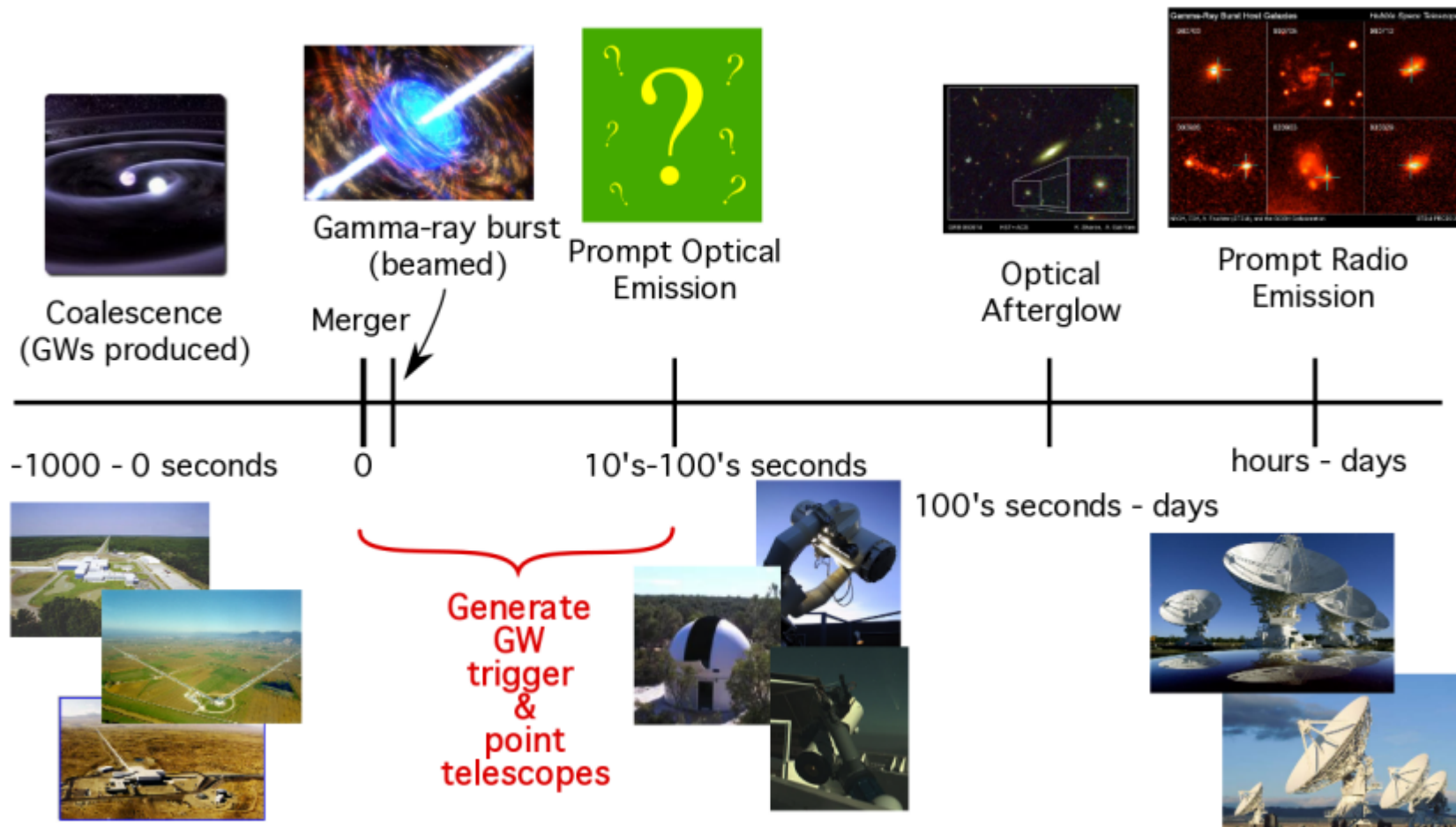
Electromagnetic radiation from sGRB progenitors



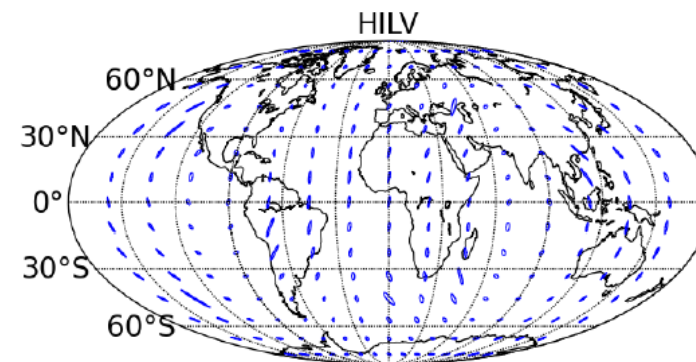
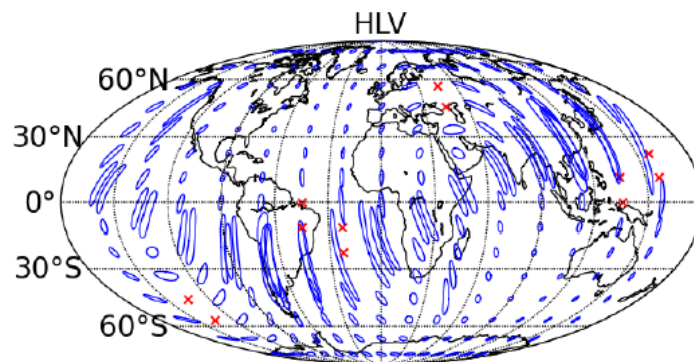
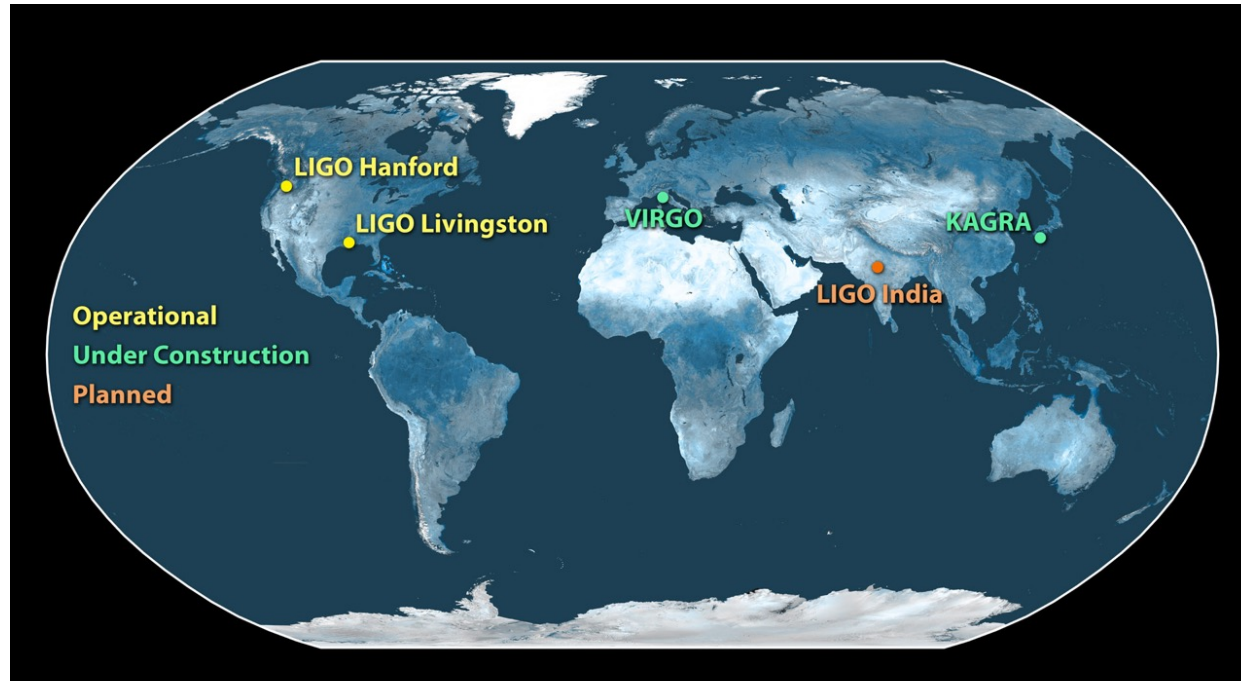
Metzger & Berger 2011

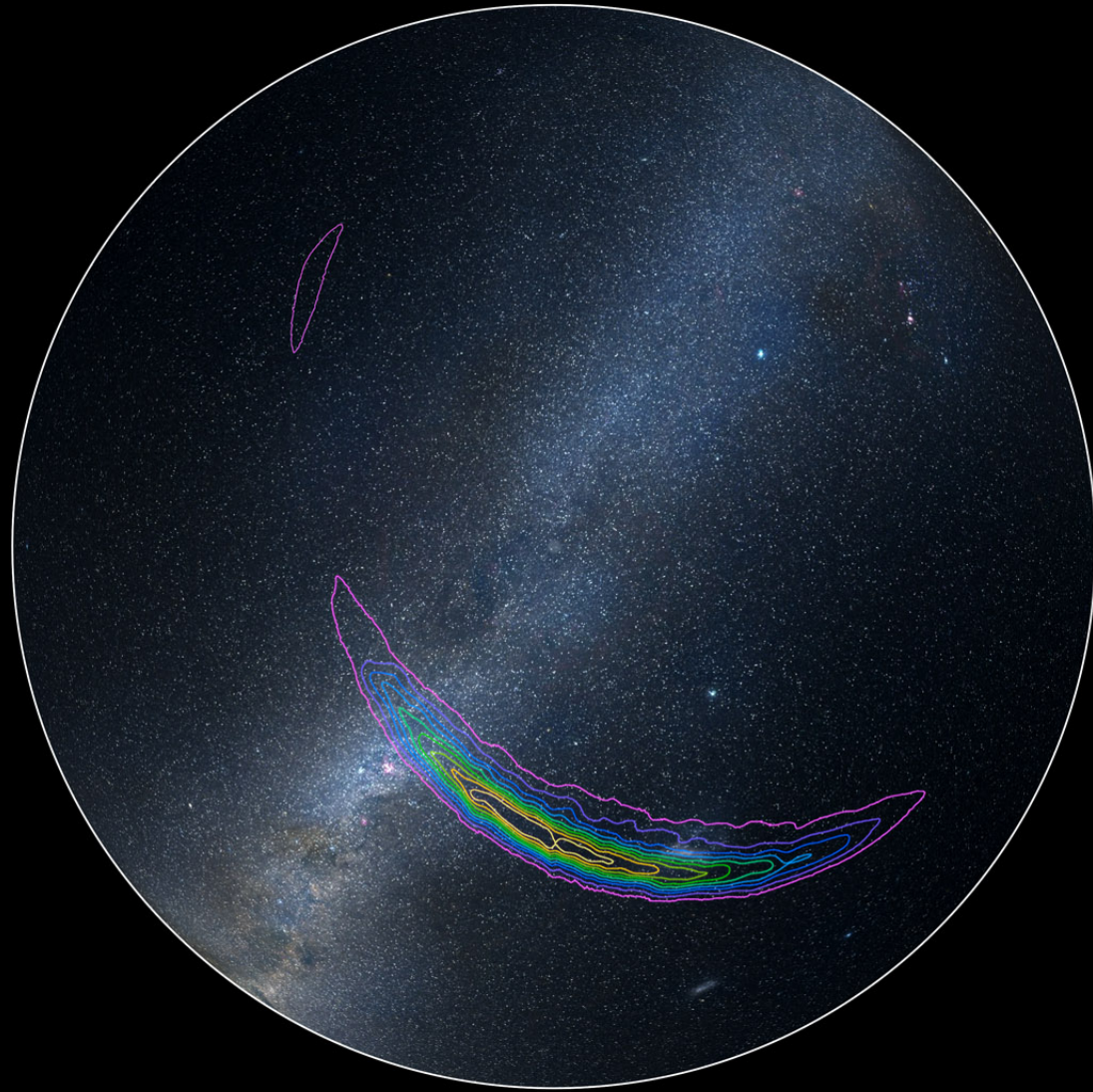
Low-latency identification of transients for rapid ($< \sim 100\text{s}$) followup

EM counterparts to GW sources (if any) are short-lived and faint

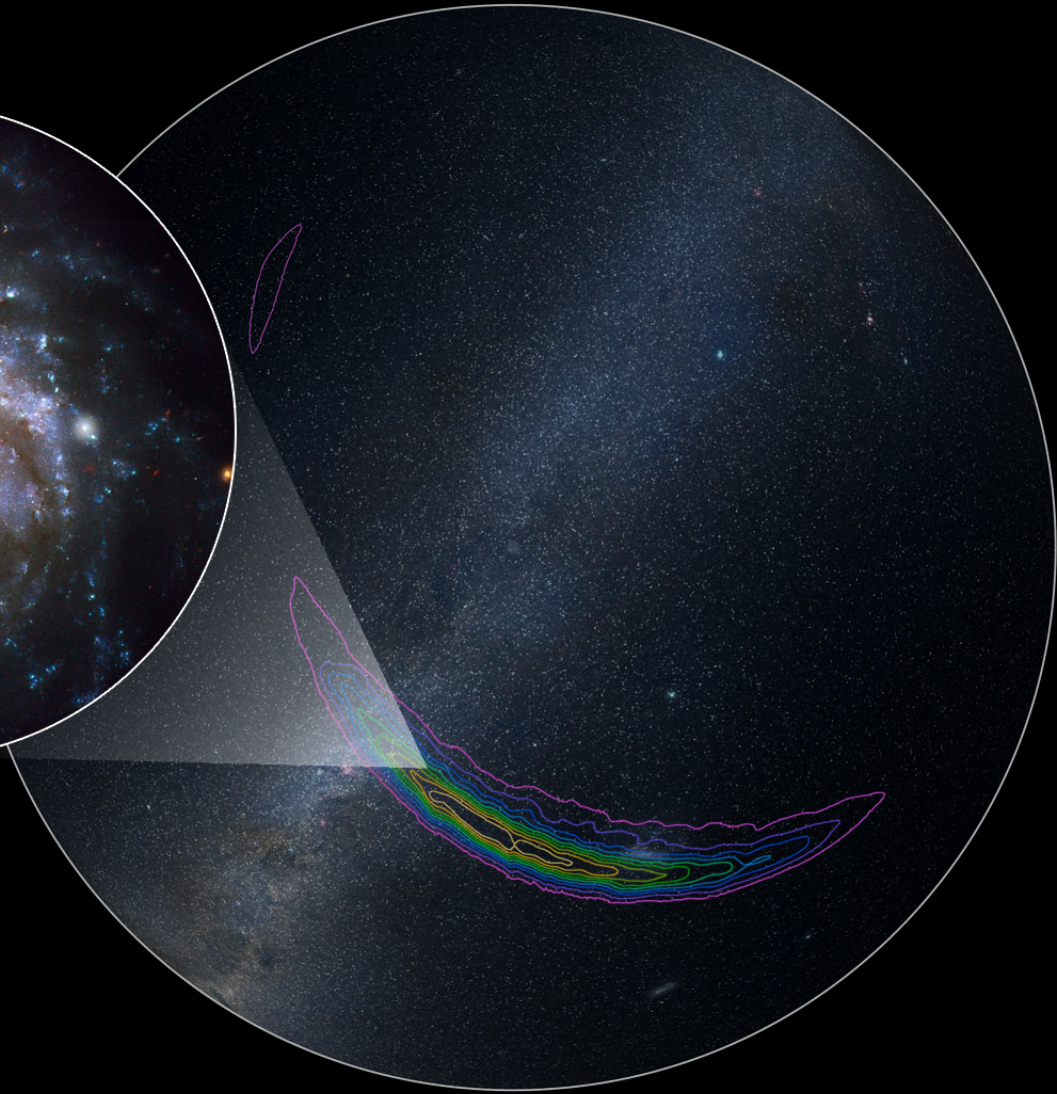


sky localization with the GW detector network

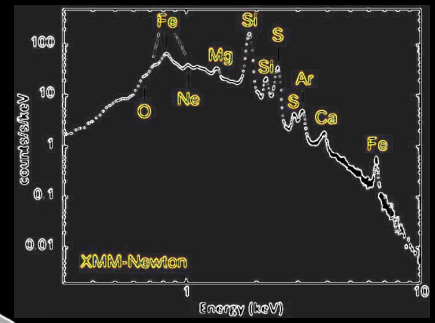
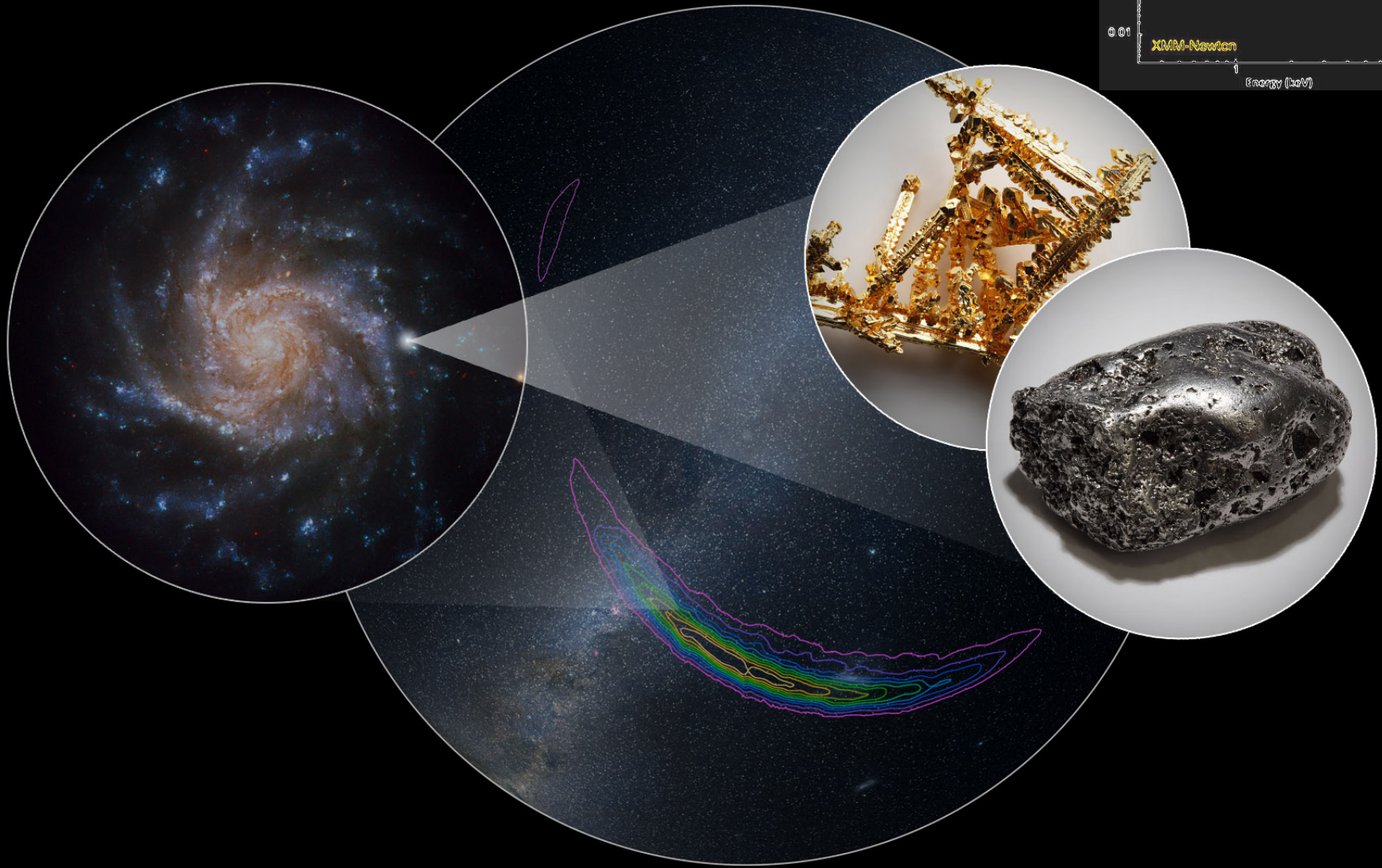




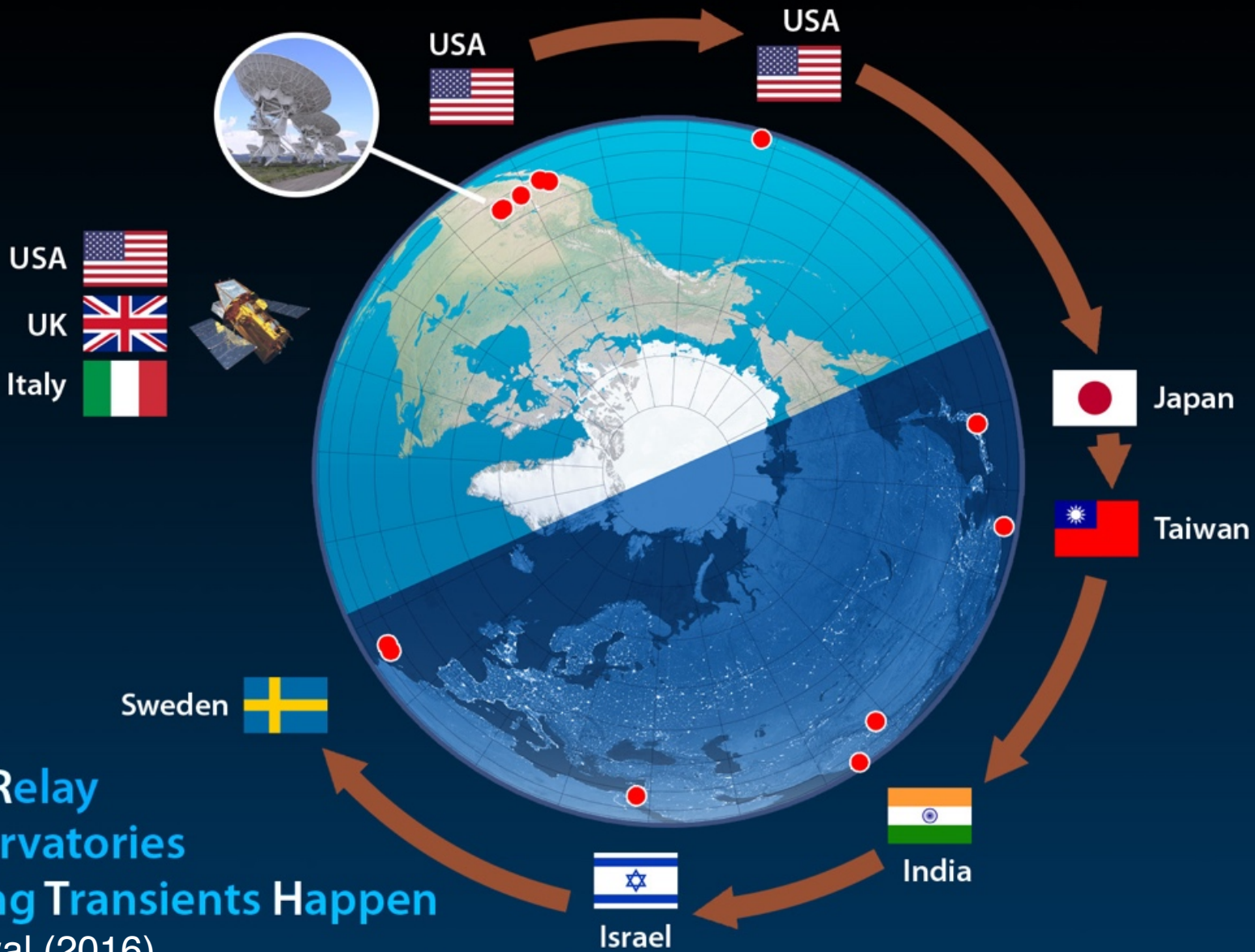
Kasliwal (2016)



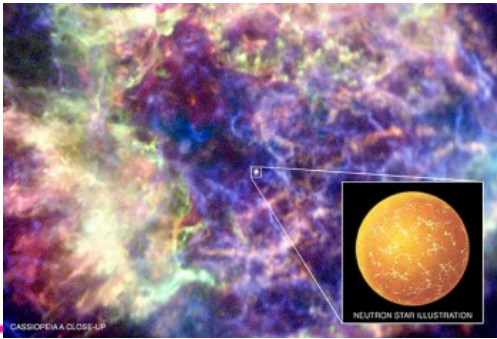
Kasliwal (2016)



Kasliwal (2016)

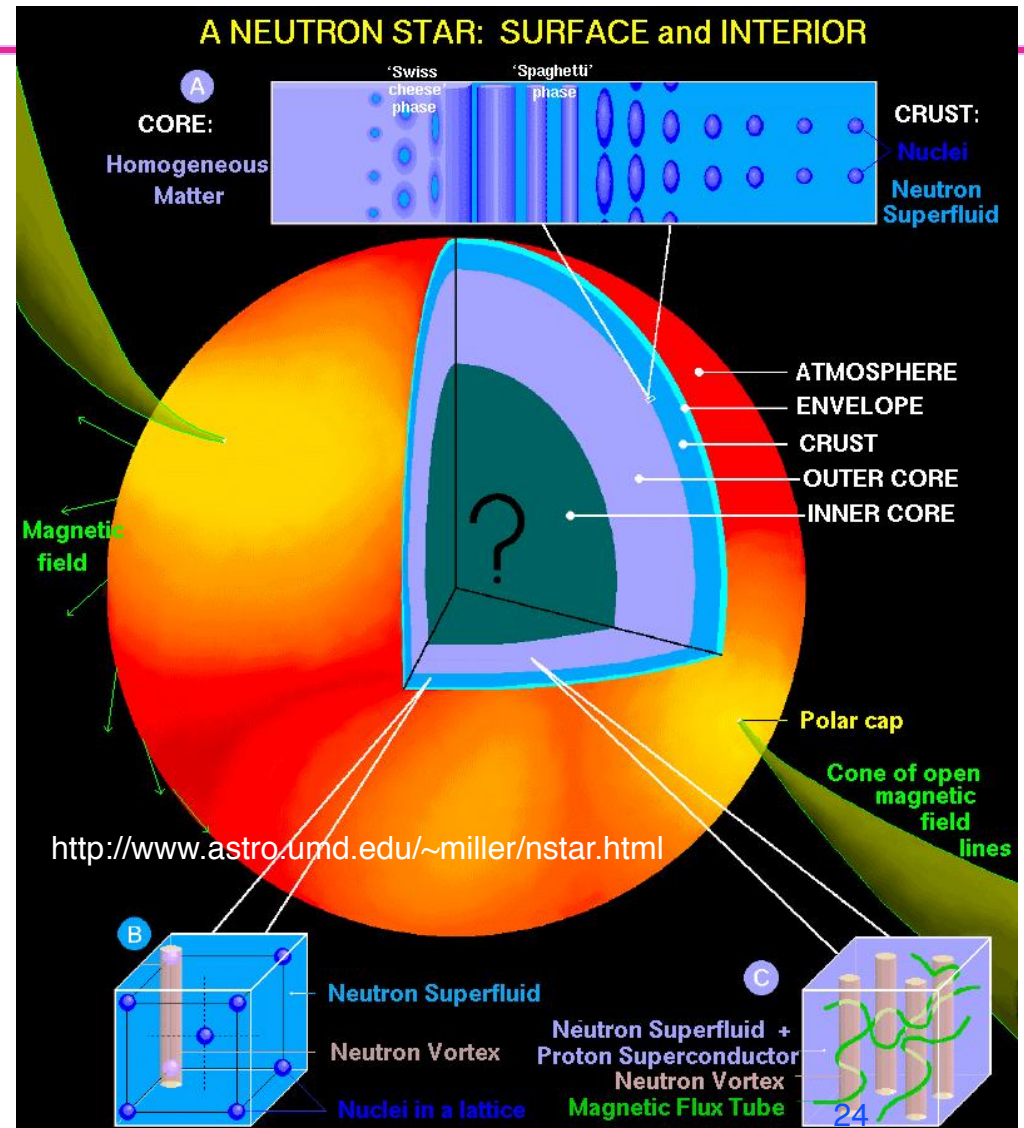
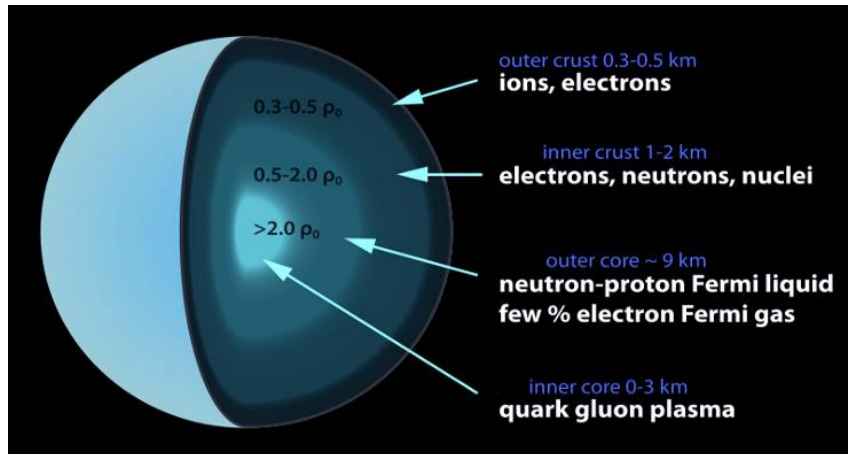


**Global Relay
of Observatories
Watching Transients Happen**
Kasliwal (2016)



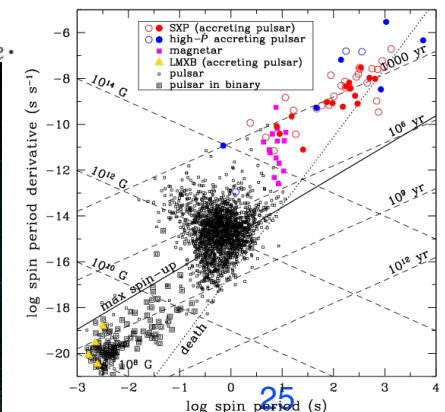
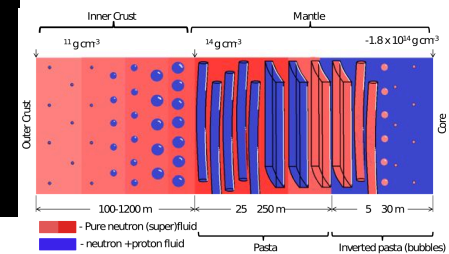
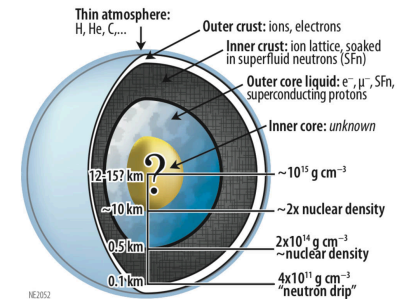
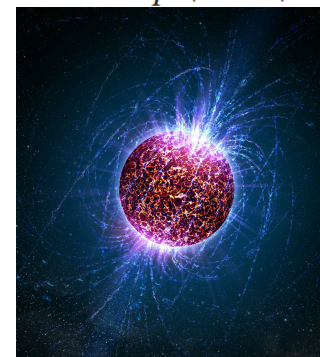
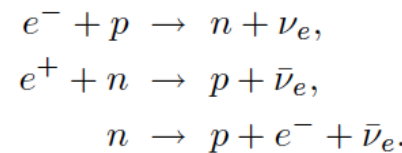
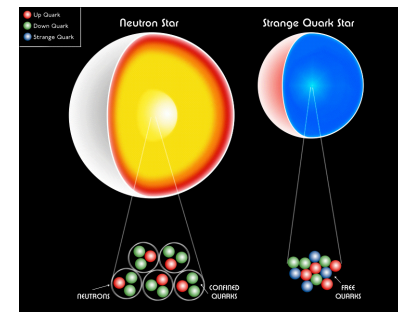
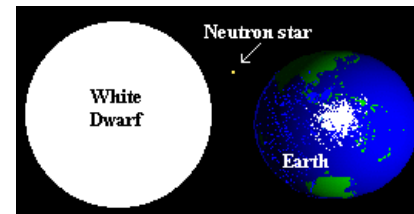
Neutron stars

- Remnants of core collapse supernovae
- A unique laboratory for fundamental physics
- Strong, Weak, EM, gravity – all under the most extreme conditions
- Structure can be revealed through binary mergers



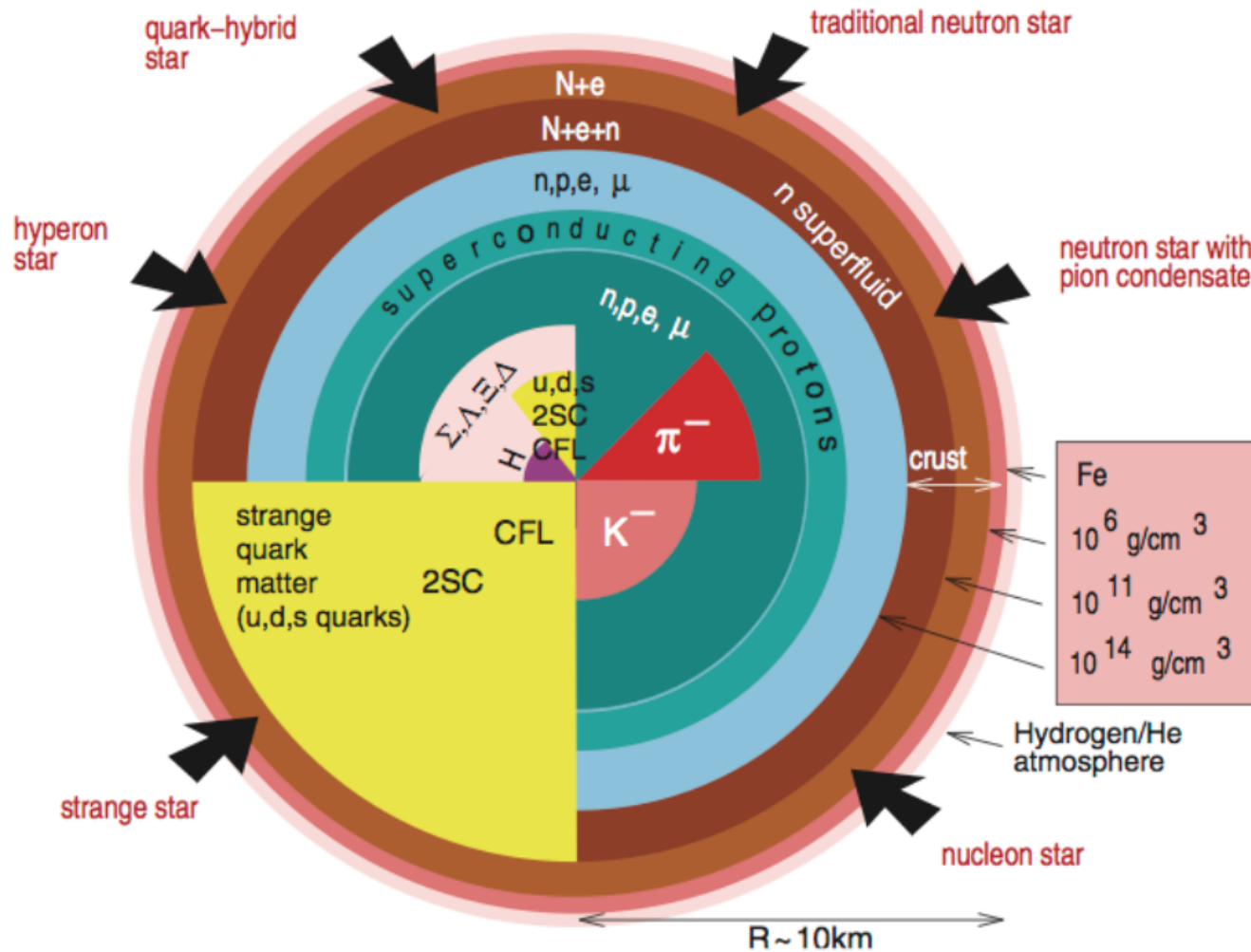
All four fundamental forces under the most extreme conditions

- Gravity:** Compact stars have gravitational fields $GM/c^2R \sim O(1)$, strong tidal effects, strong curvature, highly relativistic
- Strong interaction at $> 2x$ nuclear density in core**
 - » Hard repulsive core of nucleon-nucleon interaction plays crucial role
 - » Potential transition to hyperonic matter, strange quark matter, QGP
 - » Complex ionic crystal lattice structure in crust: “nuclear pasta”
- Weak interaction under extreme conditions with neutrino trapping -> beta equilibrium**
- EM:** Superfluid core supporting extreme magnetic fields (perhaps $> 10^{15}$ Gauss at surface), flux tube pinning in core

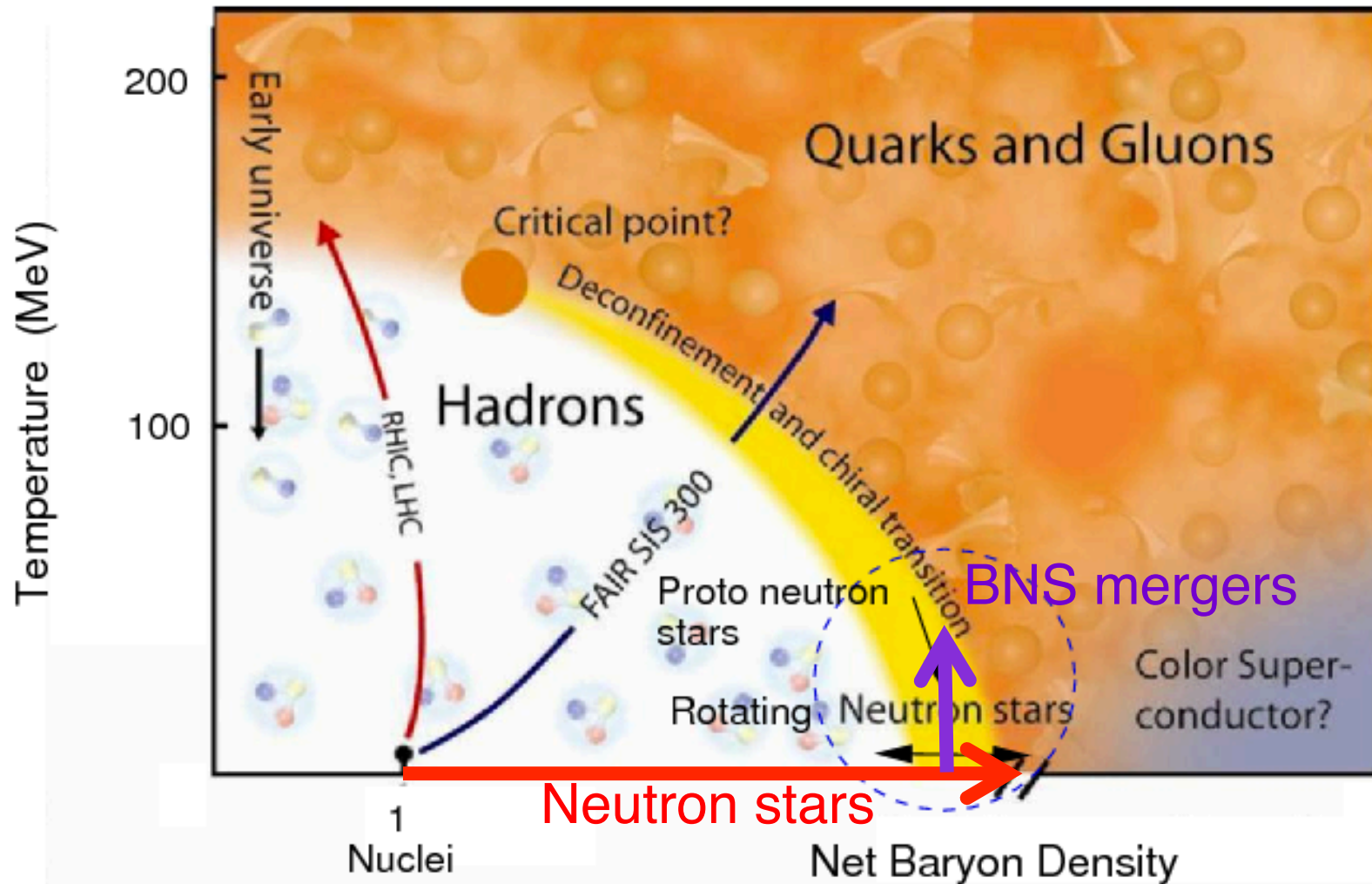


Neutron Star Equation of State

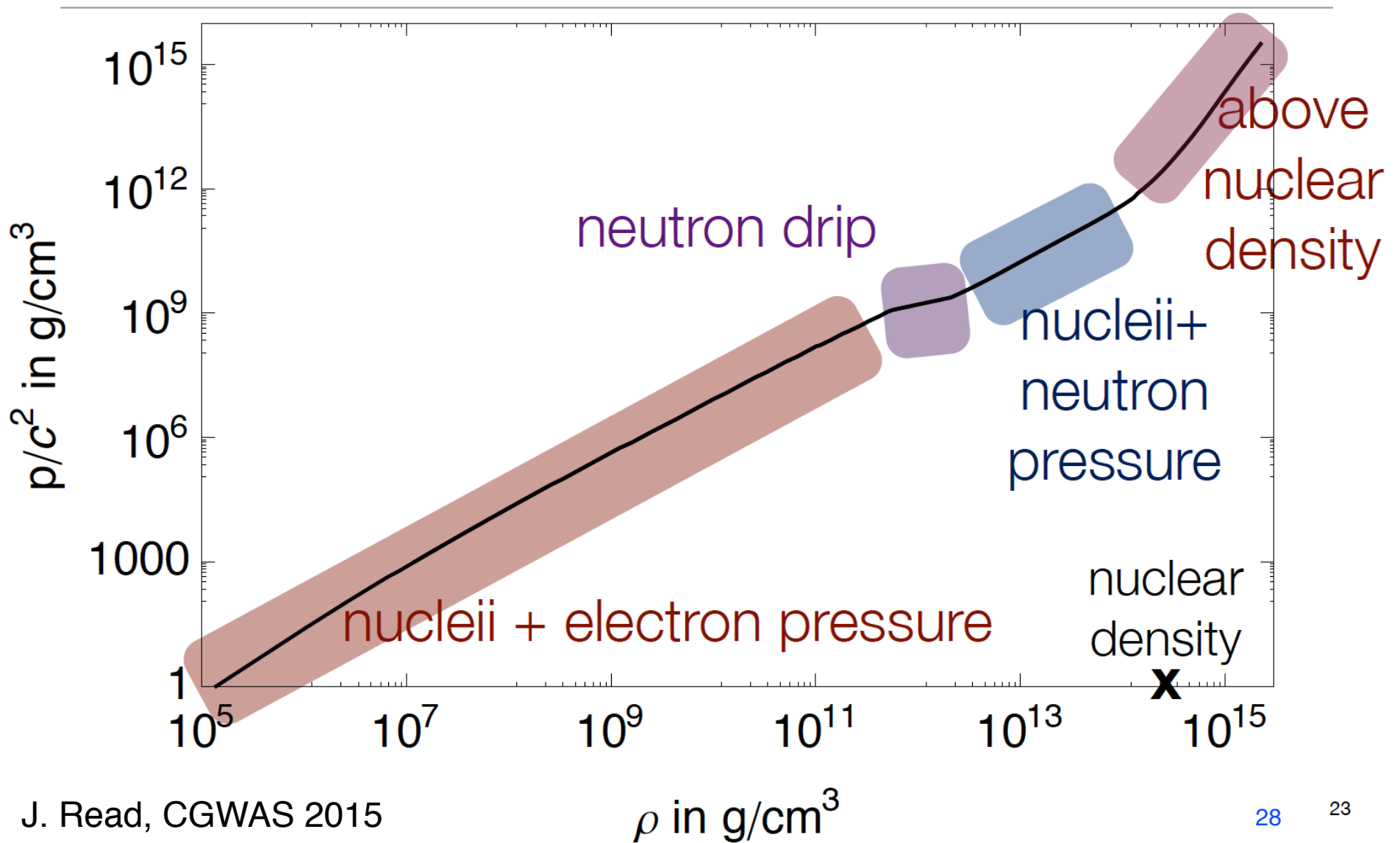
- Simplification: $T=0$, pure neutron & proton gas. Appropriate (?) for interior of cold neutron stars.



Phase diagram of ground state



Cold equation of state: pressure vs density



Neutron Star Equation of State

- $T=0$, pure neutron & proton gas. $f = \epsilon$

$$\epsilon(n_n, n_p) = \frac{3}{5} \frac{p_{F,n}^2}{2m_n} \frac{n_n}{n} + \frac{3}{5} \frac{p_{F,p}^2}{2m_p} \frac{n_p}{n} \quad p_F = (3\pi^2 \hbar^3)^{1/3} n^{1/3}$$

$$P = n^2 \frac{\partial \epsilon}{\partial n} \propto n^{5/3}$$

$$\Gamma = \left. \frac{d \ln P}{d \ln \rho} \right|_s = \frac{5}{3}$$

$$P = K \rho^\Gamma$$

“polytrope”

$\Gamma = 5/3$ corresponds to a non-relativistic gas.

A relativistic gas has $\Gamma = 4/3$, which is unstable to collapse.

Note that (unlike ideal gas law $P = nkT$)

the result is independent of temperature.

In general, $pv^n = \text{const}$ is polytropic, with $\Gamma = 1 + 1/n$; here,

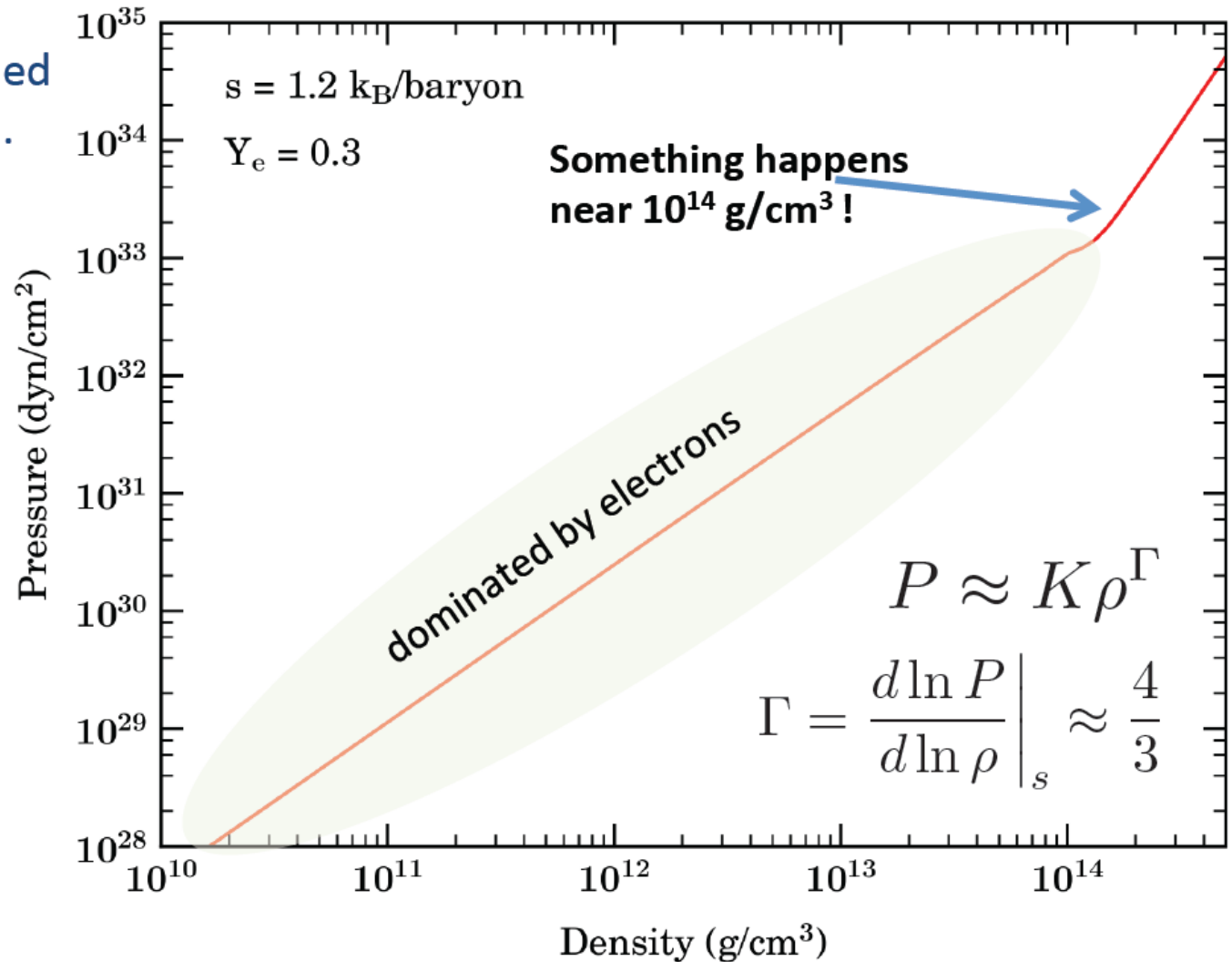
$n = \text{polytropic index (NOT } n = \rho/m_N)$

Neutron Star Equation of State

Nuclear Statistical Equilibrium ($\rho > 10^7 \text{ g/cm}^3$, $T > 0.5 \text{ MeV}$)

-> $P = P(\rho, T, Y_e)$

Composition determined
by Saha-type equation.



Neutron Star Equation of State

Nuclear Physics:

$$R_{\text{nuc}} = A^{1/3} r_0$$

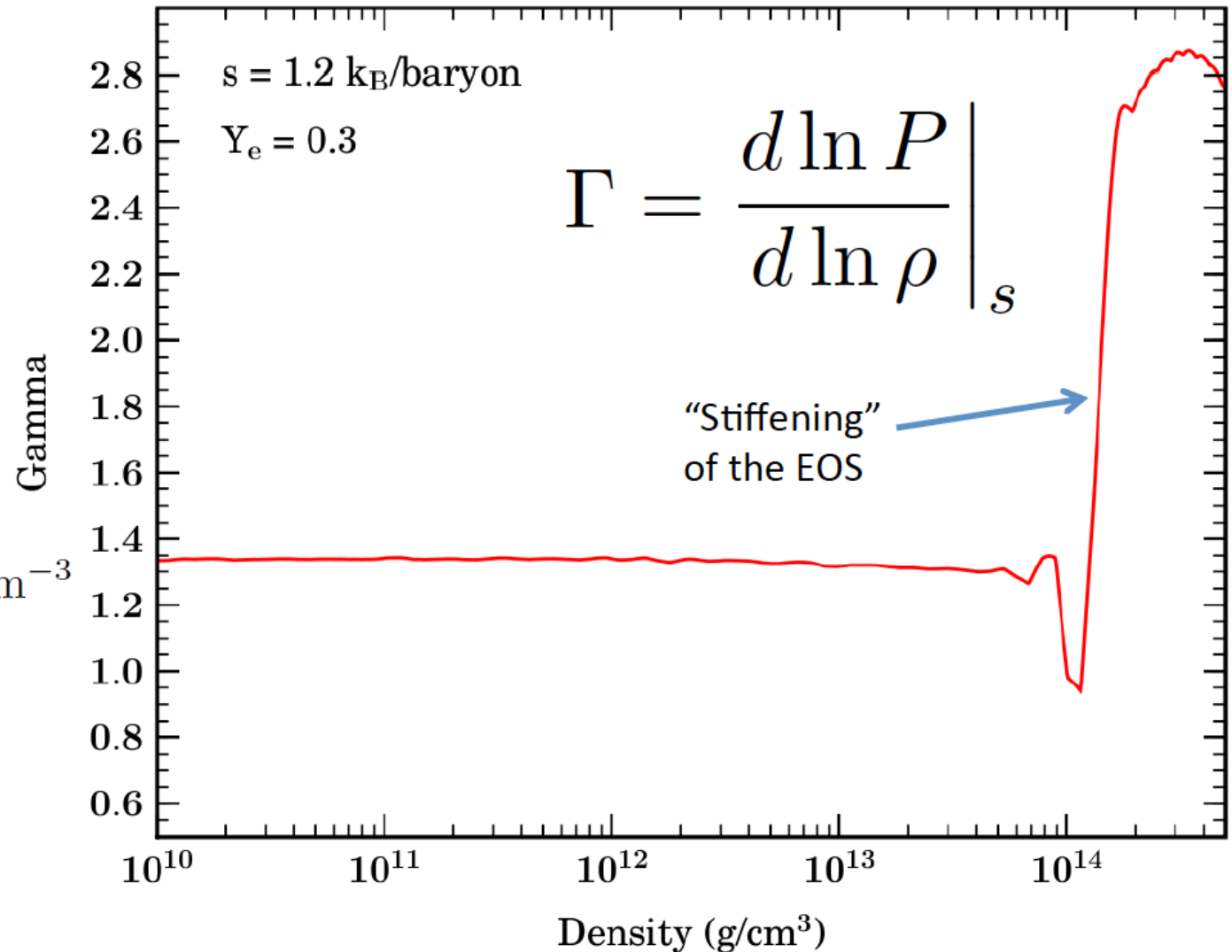
$$r_0 = 1.25 \text{ fm}$$

Nuclear Density:

$$\bar{\rho}_{\text{nuc}} = \frac{A m_b}{\frac{4}{3}\pi R_{\text{nuc}}^3}$$

$$\rho_{\text{nuc}} \sim 2.7 \times 10^{14} \text{ g cm}^{-3}$$

$$n_{\text{nuc}} \sim 0.16 \text{ fm}^{-3}$$



Neutron Star Equation of State

Nuclear Physics:

$$R_{\text{nuc}} = A^{1/3} r_0$$

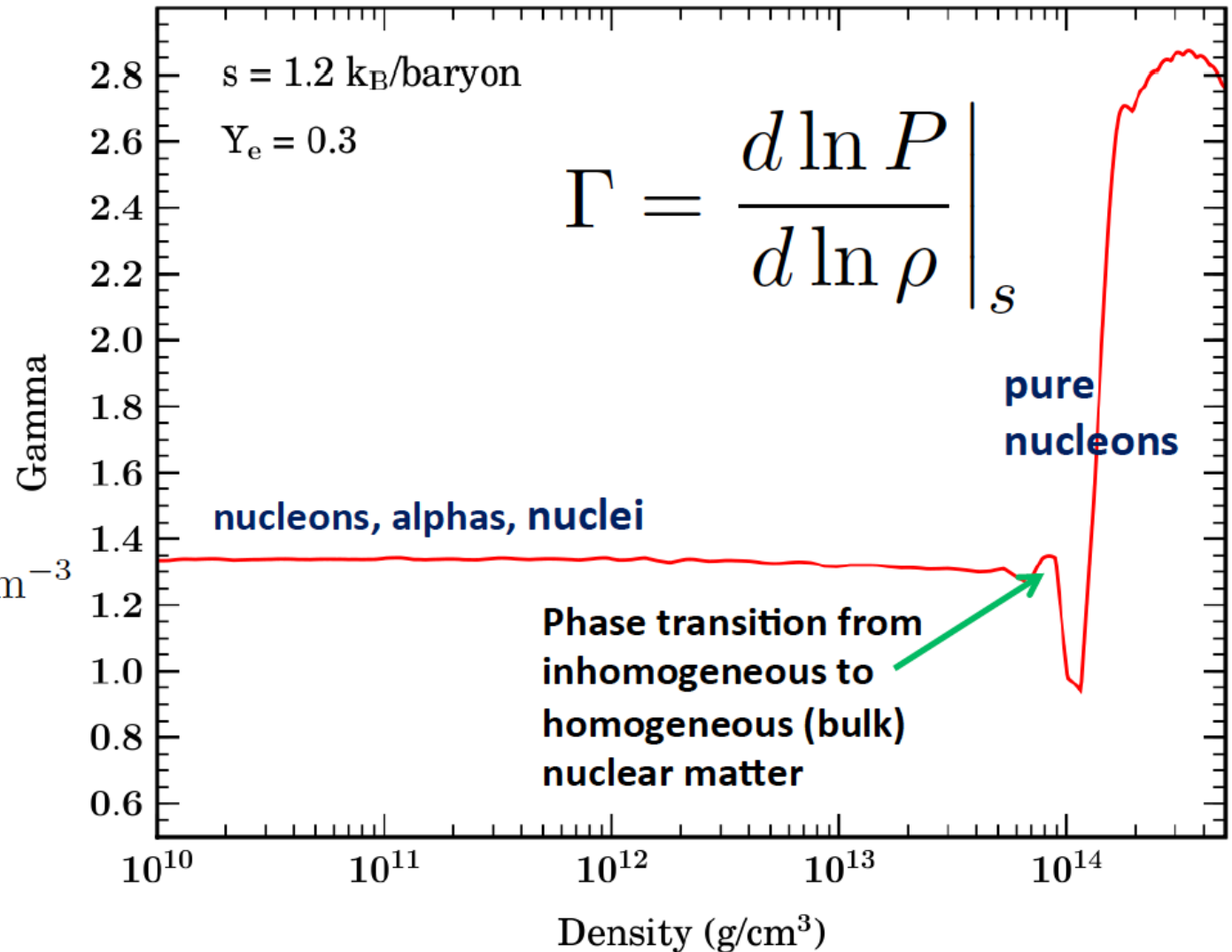
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Nuclear Density:

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$$\rho_{\text{nuc}} \sim 2.7 \times 10^{14} \text{ g cm}^{-3}$$

$$n_{\text{nuc}} \sim 0.16 \text{ fm}^{-3}$$



What is causing the stiffening of the nuclear EOS?

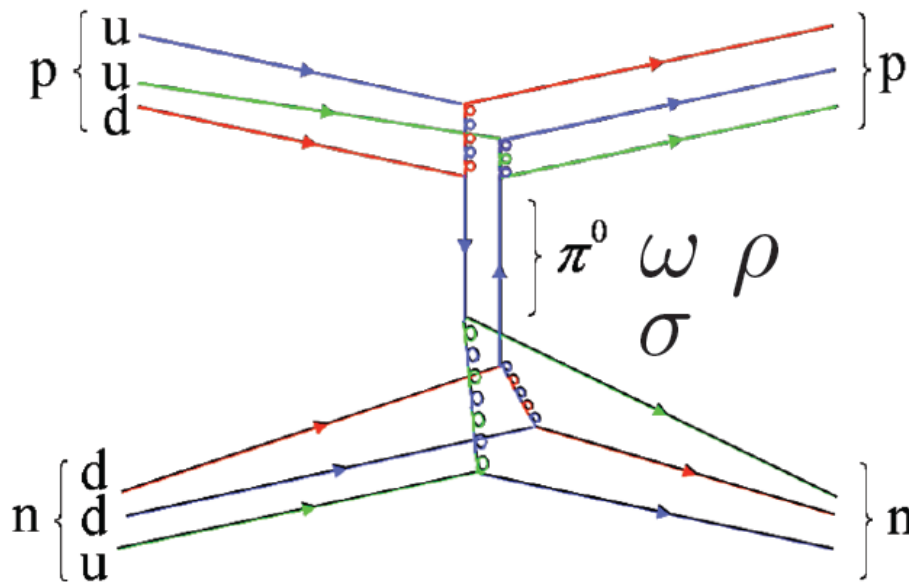
C. Ott, 2012

Nuclear Equation of State

- $T=0$, **interacting** pure neutron & proton gas.

$$\epsilon(n_n, n_p) = \frac{3}{5} \frac{p_{F,n}^2}{2m_n} \frac{n_n}{n} + \frac{3}{5} \frac{p_{F,p}^2}{2m_p} \frac{n_p}{n} + \frac{V_{np}(n_n, n_p)}{n}$$

nucleon-nucleon (NN) potential energy density



- Nuclear force is NN many-body interaction = “effective” strong force interaction.
- Mediated by mesons:
 π ($s=0$), σ ($s=0$), ω ($s=1$), ρ ($s=1$)
- Dependent on separation and spin orientation. **Scalar, vector, and tensor** components.
Vector component is repulsive.

Nucleon-Nucleon Interaction

Example: Bethe & Johnson 74

2-pion exchange attractive; omega-exchange repulsive

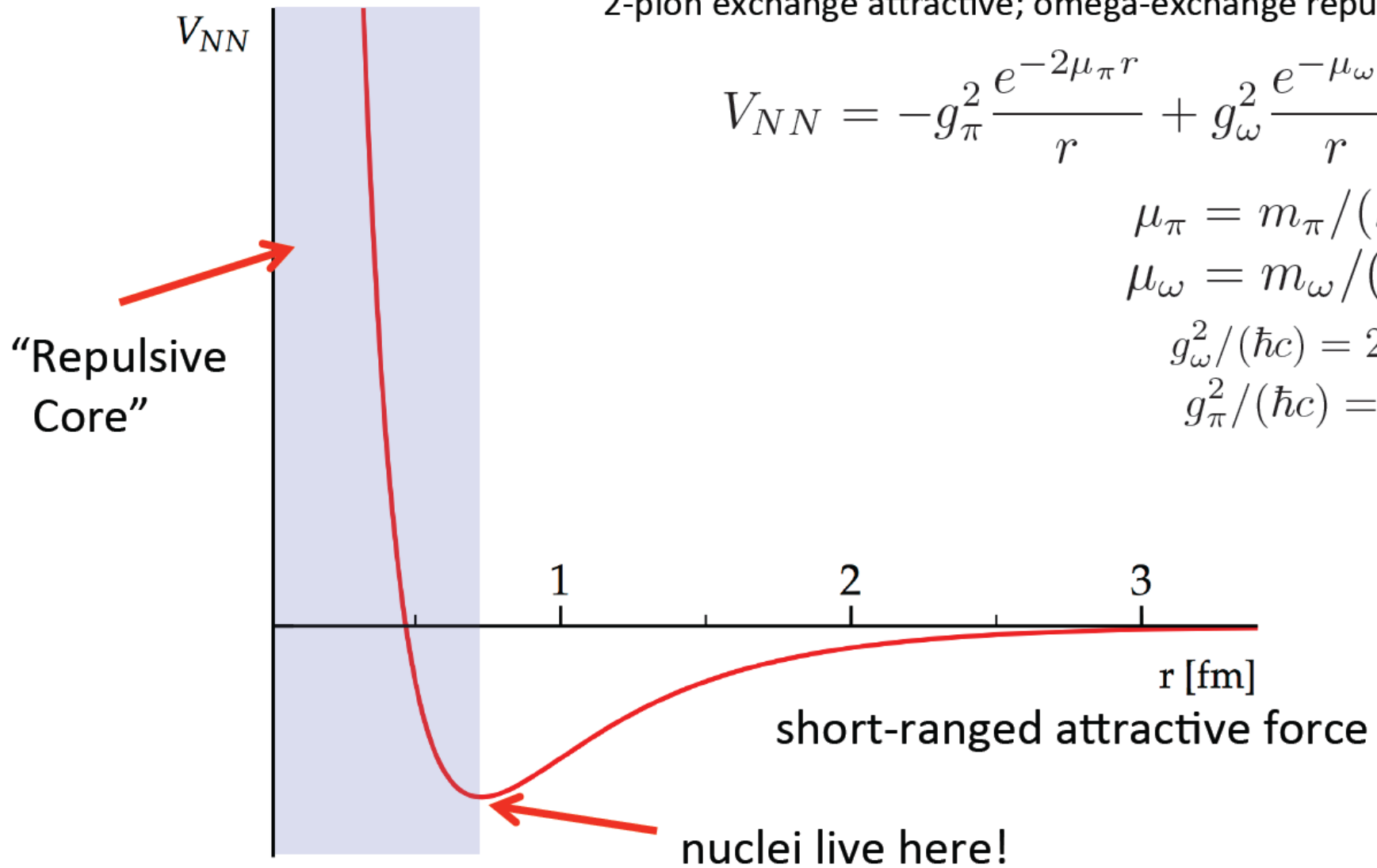
$$V_{NN} = -g_{\pi}^2 \frac{e^{-2\mu_{\pi}r}}{r} + g_{\omega}^2 \frac{e^{-\mu_{\omega}r}}{r}$$

$$\mu_{\pi} = m_{\pi}/(\hbar c)$$

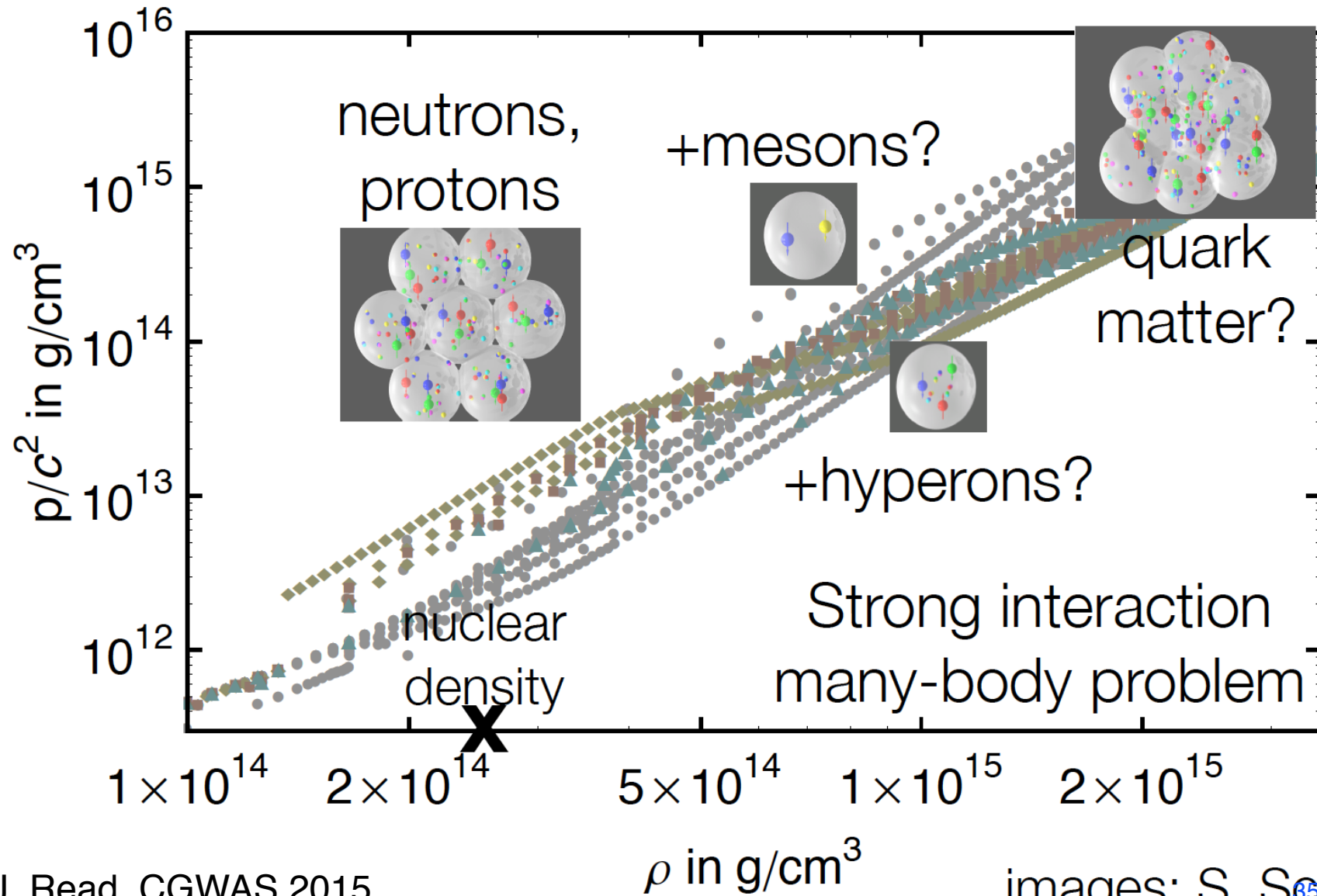
$$\mu_{\omega} = m_{\omega}/(\hbar c)$$

$$g_{\omega}^2/(\hbar c) = 29.6$$

$$g_{\pi}^2/(\hbar c) = 10$$



What happens above nuclear density? Inside neutrons: quarks



Neutron Star Structure

Newtonian: $\frac{dP}{dr} = -\frac{GM\rho}{r^2}$ $\frac{dM}{dr} = 4\pi r^2 \rho$ (no maximum mass!)

GR: Tolman-Oppenheimer-Volkov (TOV) eqns

$$\frac{dP}{dr} = -G(\rho(1 + \epsilon/c^2) + P/c^2) \frac{M + 4\pi r^3 p/c^2}{r(r - 2GM/c^2)}$$

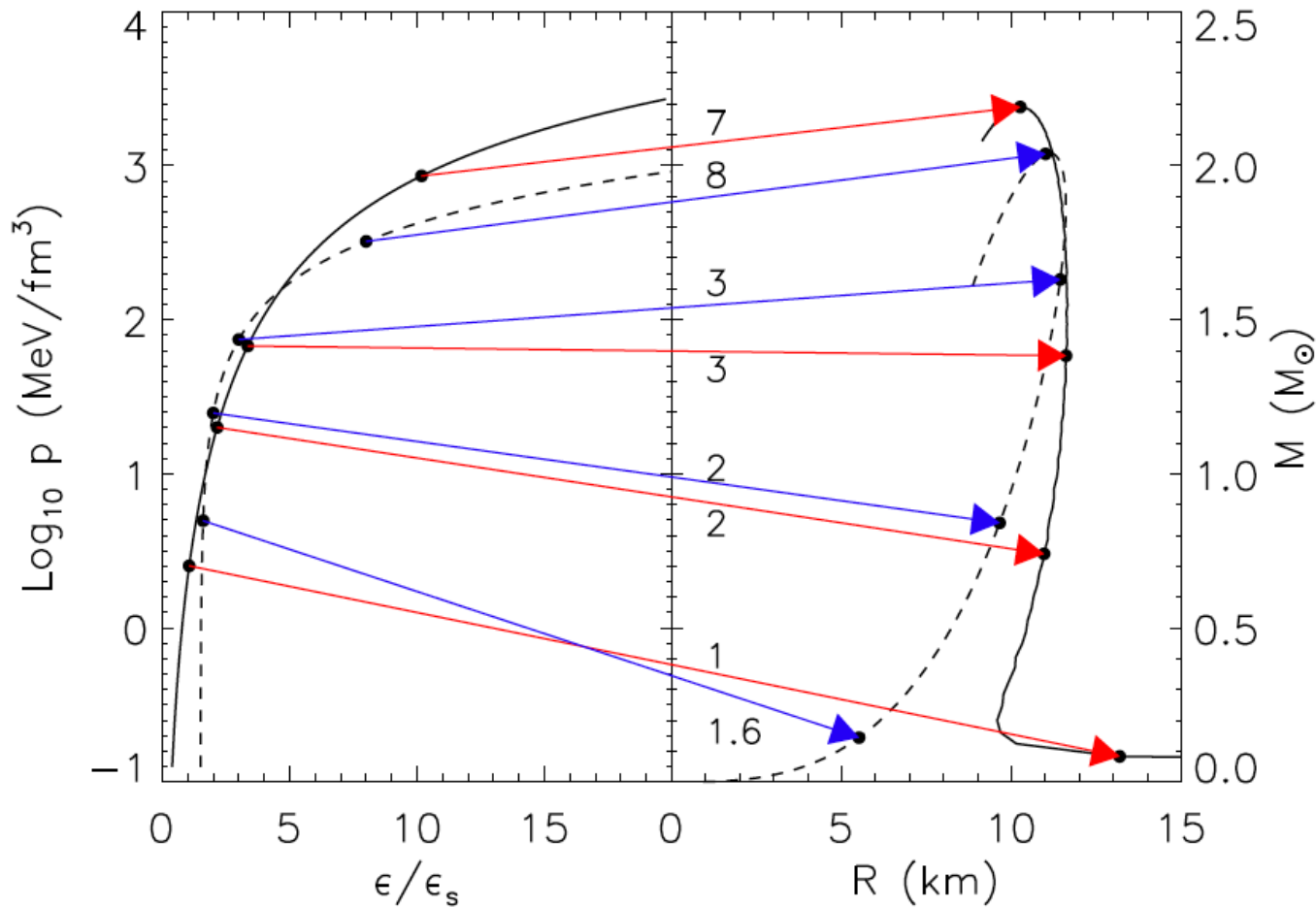
$$\frac{dM_g}{dr} = 4\pi r^2 \rho(1 + \epsilon/c^2) \quad \text{gravitational mass}$$

$$\frac{dM_b}{dr} = \frac{4\pi r^2}{\sqrt{1 - \frac{2GM}{rc^2}}} \rho \quad \text{baryonic mass}$$

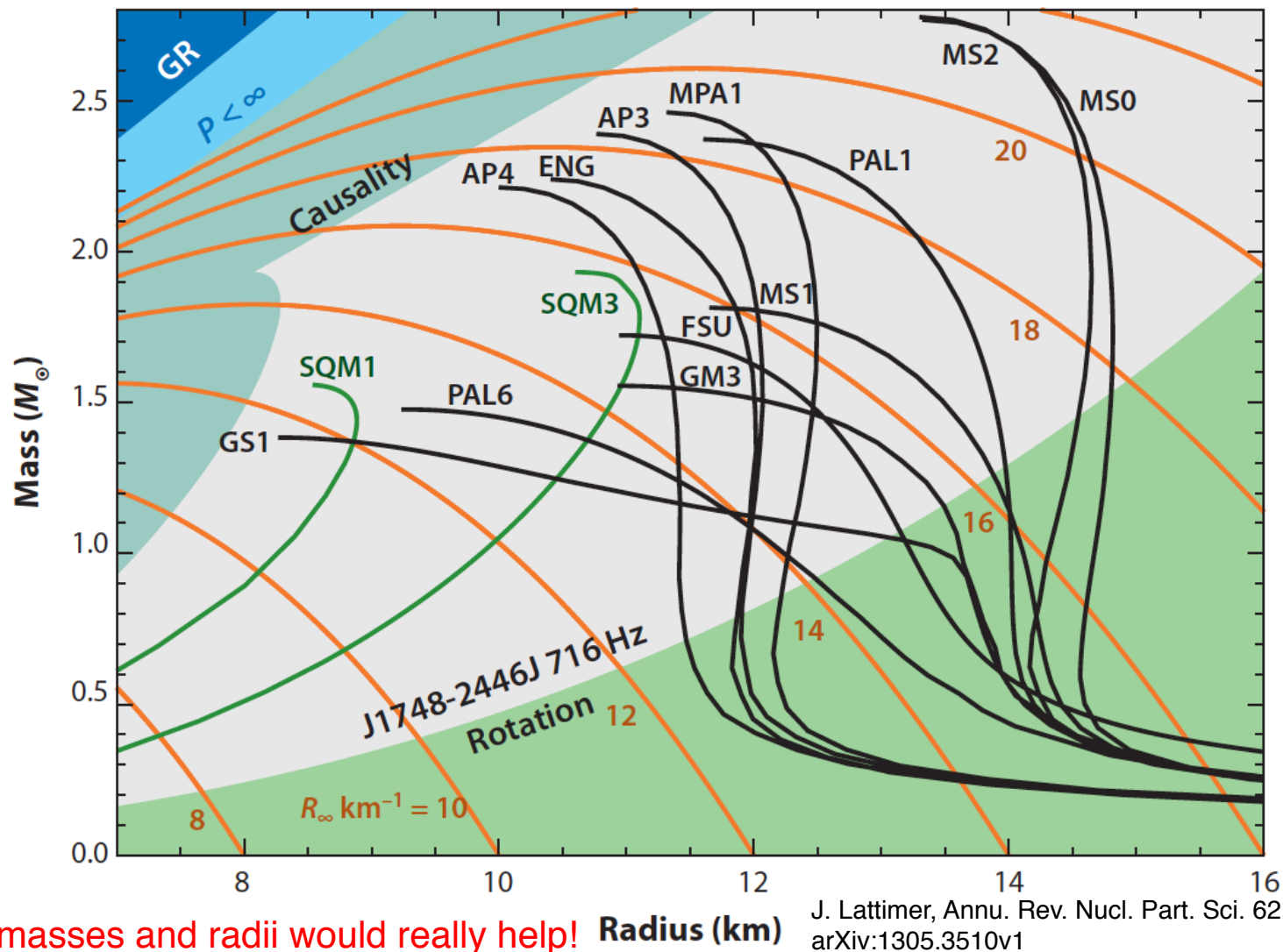
Radius is circumferential radius!

- Solve by ODE integration from $r=0$, invert $P(\rho)$ at each step to obtain ρ .

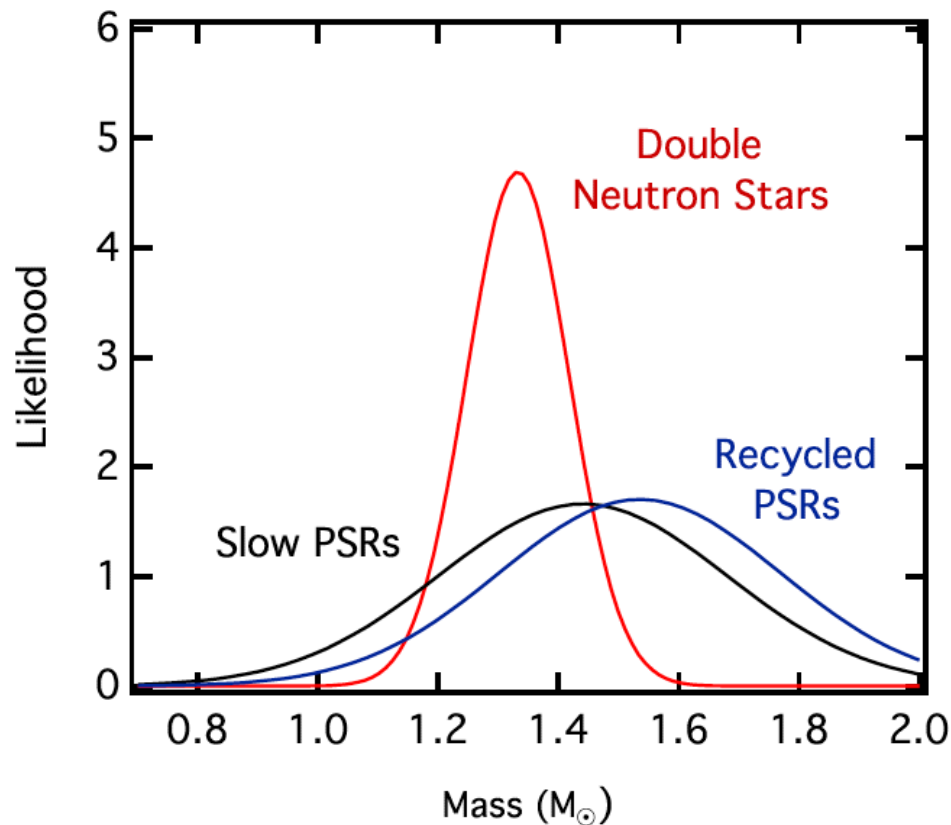
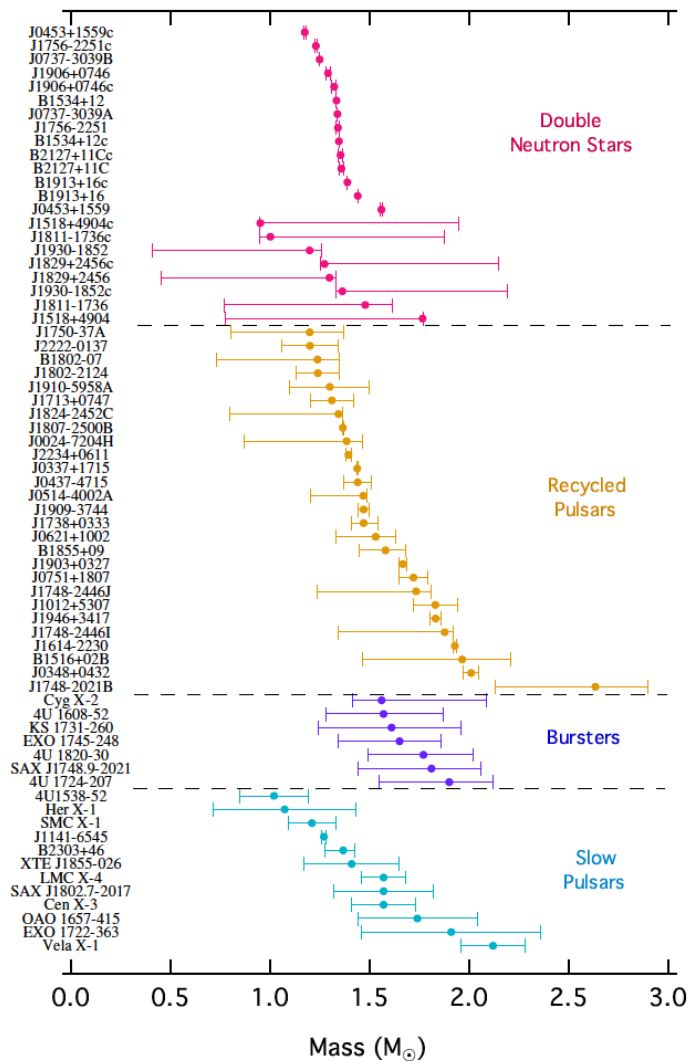
Building neutron star mass-radius relation with TOV and NEOS



EOS and Neutron star structure

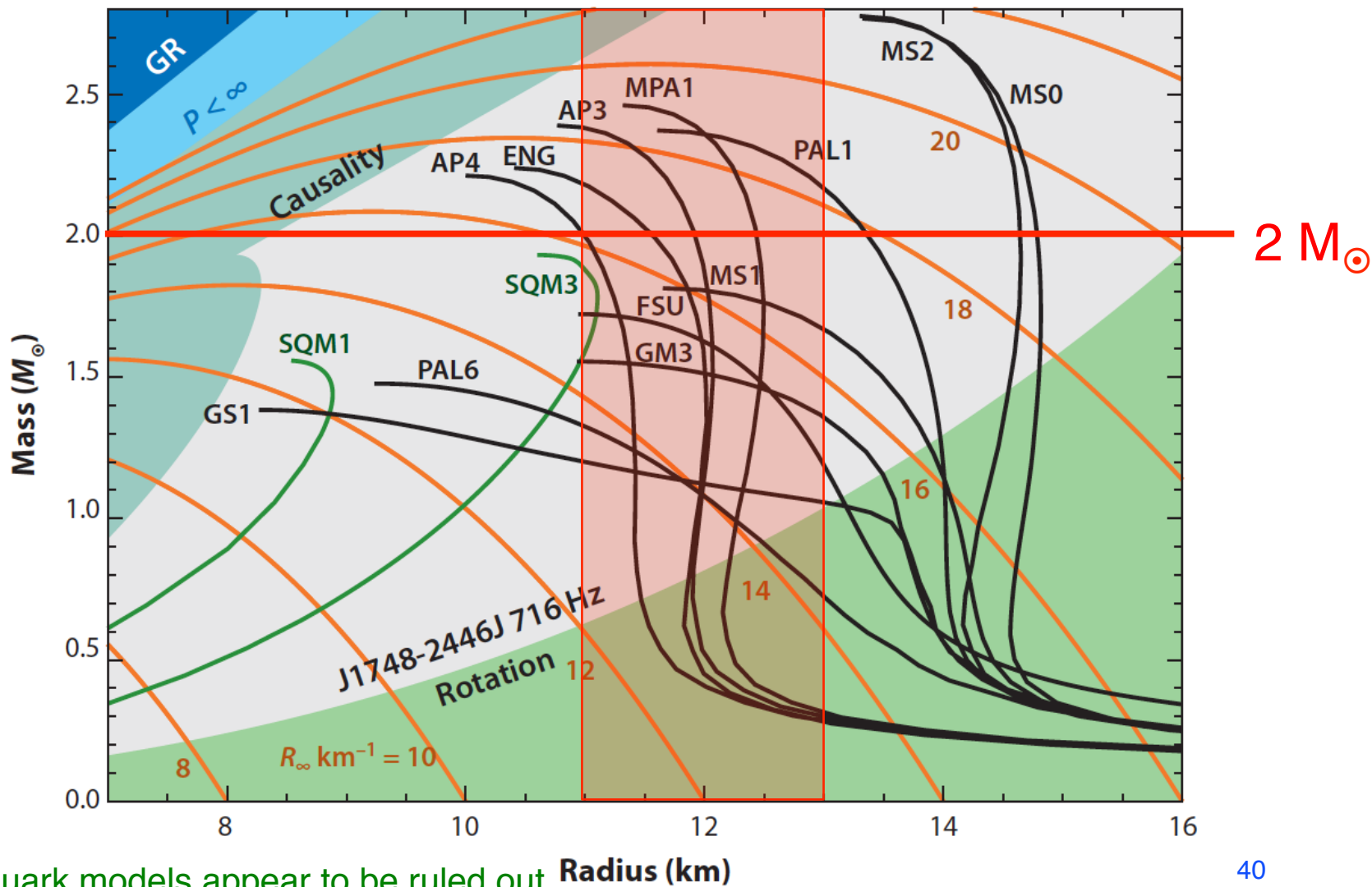


Neutron star masses



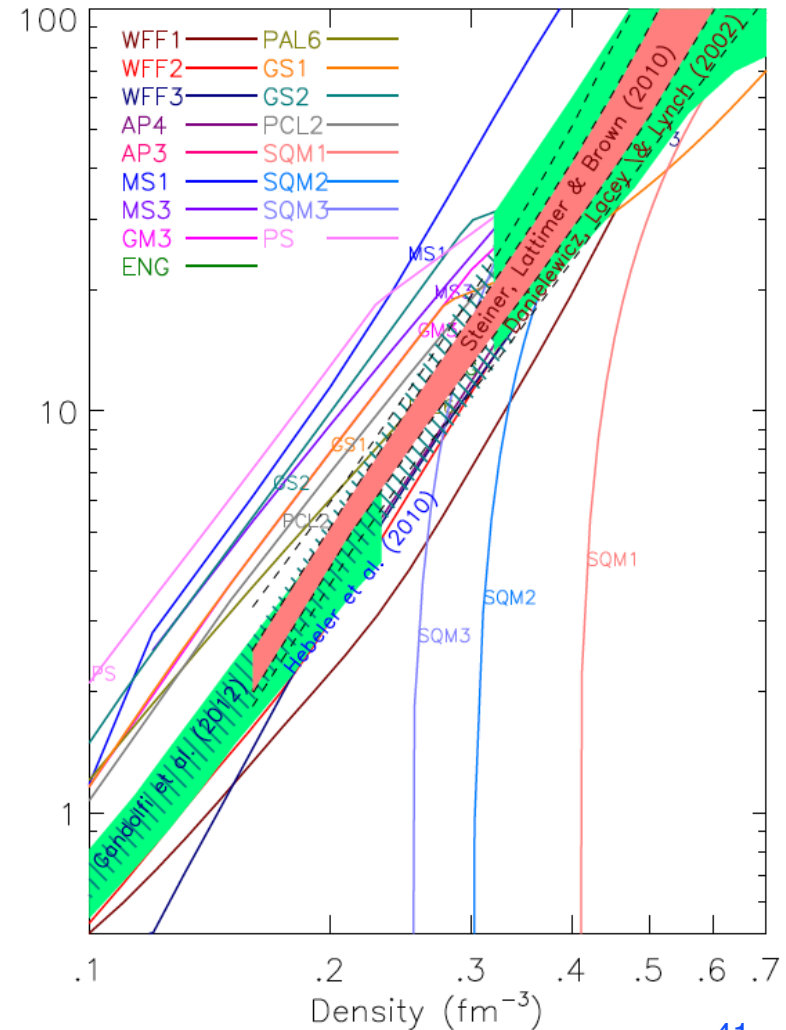
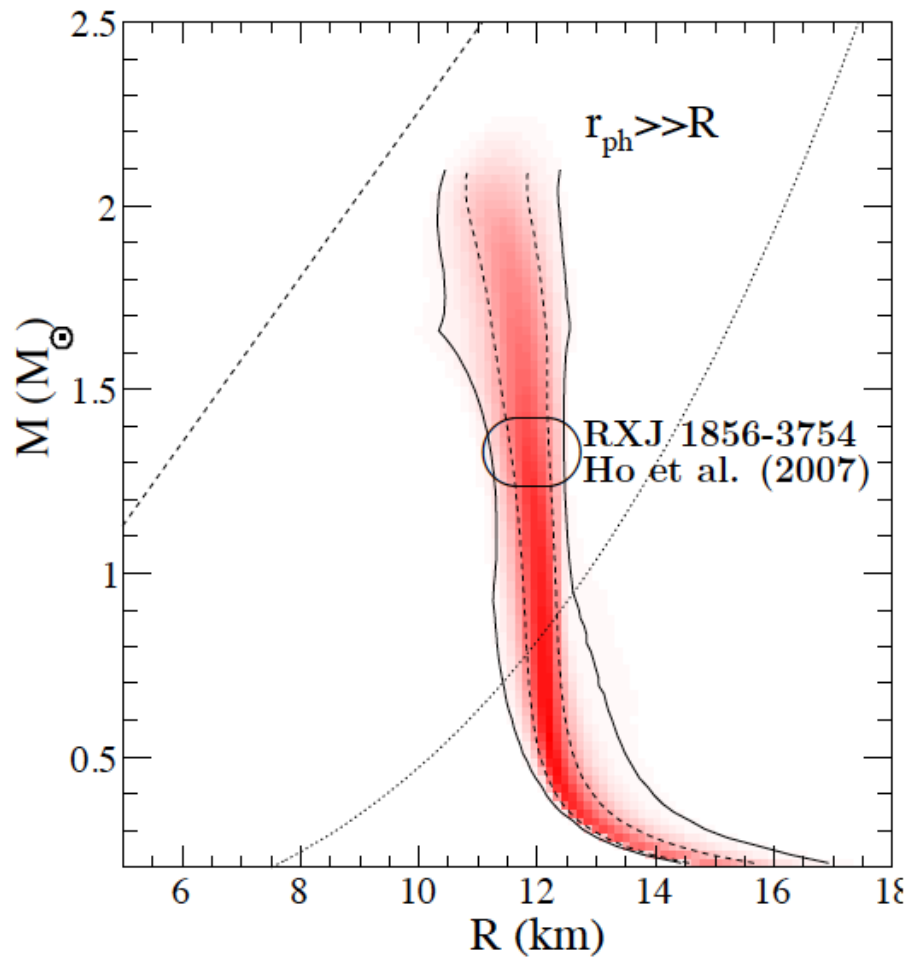
Feryal Ozel, Paulo Freire, <http://arxiv.org/abs/1603.02698v1>

Mass and radius constraints

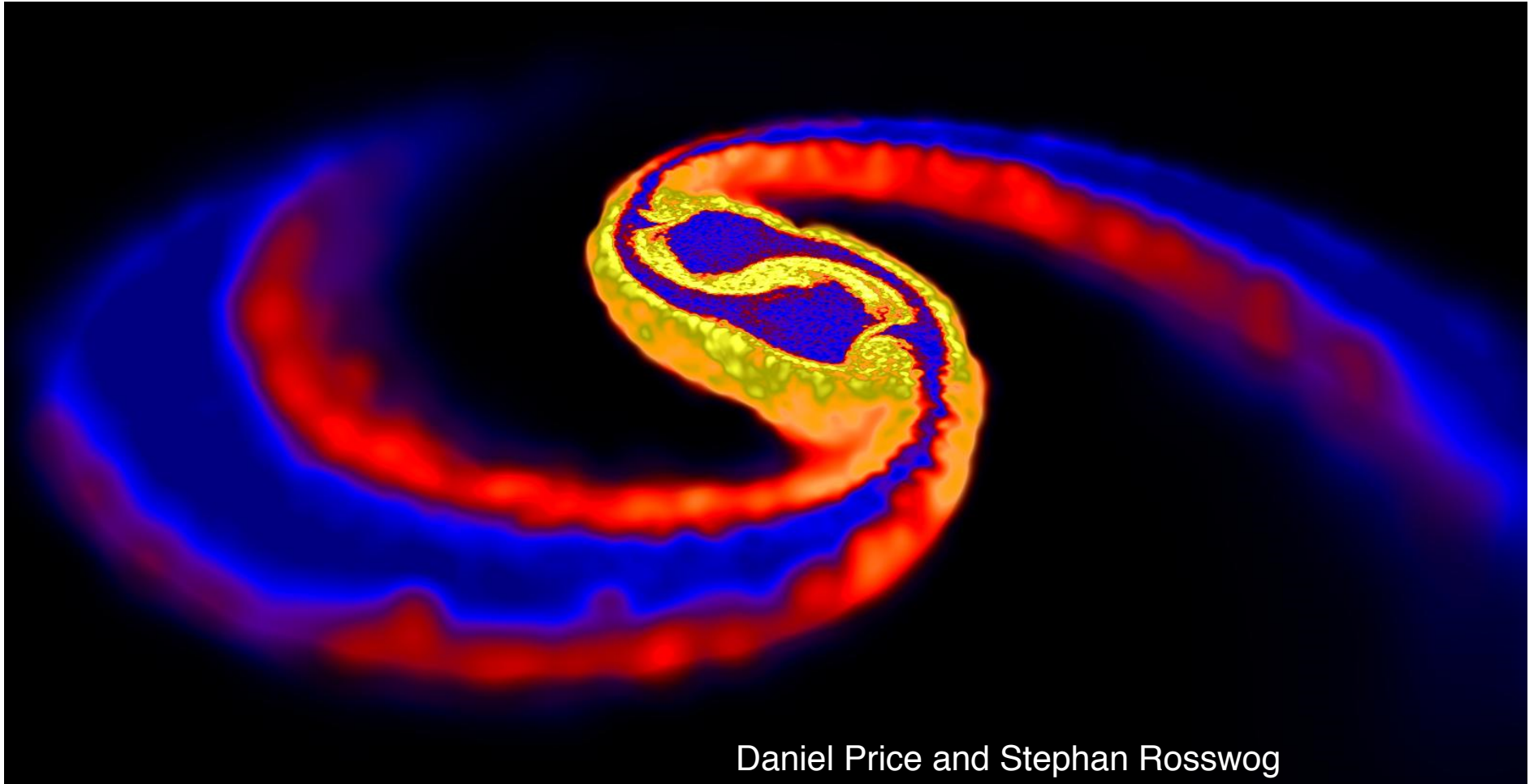


Strange quark models appear to be ruled out...

Astrophysical constraints on masses and radii of NSs

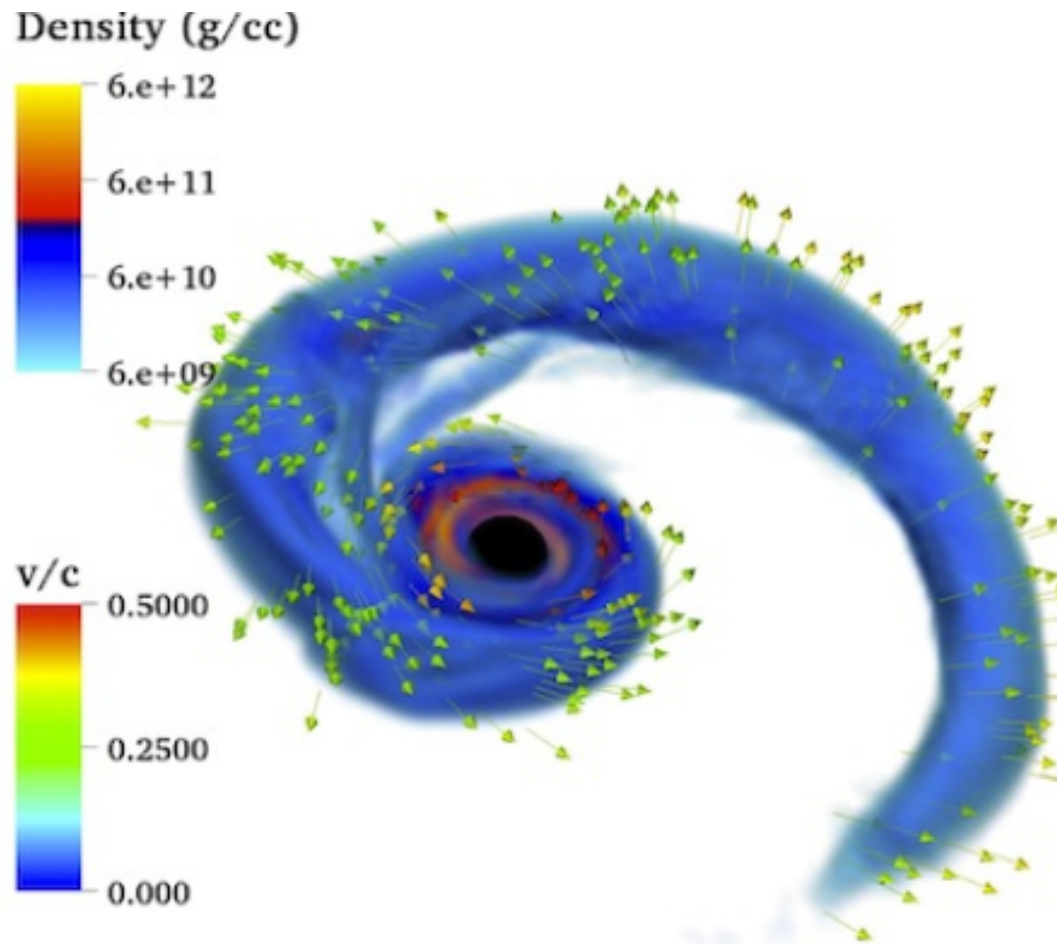


Binary neutron star mergers



Daniel Price and Stephan Rosswog

Matter distribution during the disruption of the neutron star



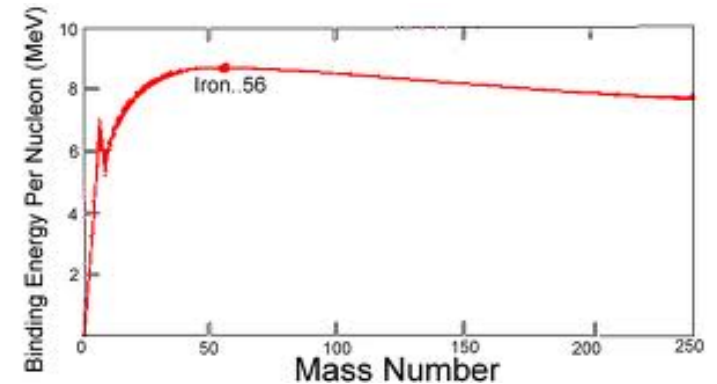
About half of the remnant material is unbound, while a relatively low mass hot disk forms.



The origin of the elements – astrophysical nucleosynthesis

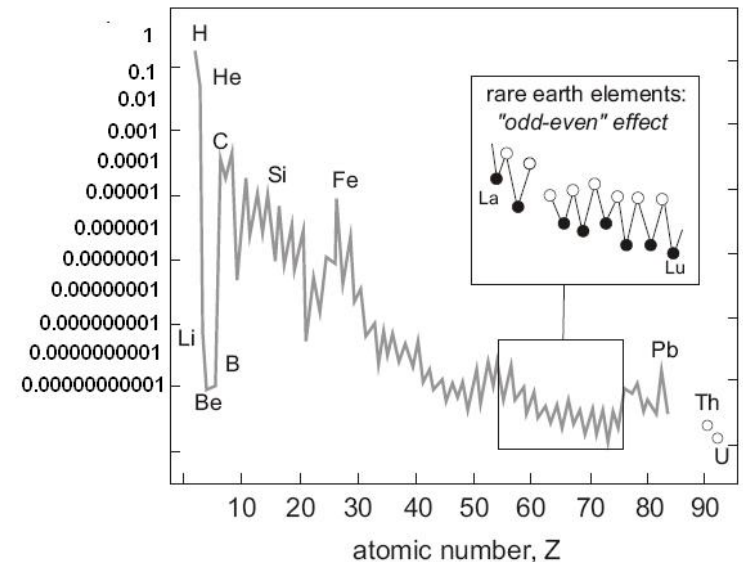


- Lightest elements (H, He, Li) forged in Big Bang
- Heavier elements (C, O, N, ... Fe) forged in the core of massive stars, distributed to ISM by core-collapse supernovae (star-death)
- Elements beyond Fe (like Cu, Au, Pb, Pt, U...) are forged during the SN (“r-process”)
- but many/most of them might come from binary neutron star mergers (second-death)

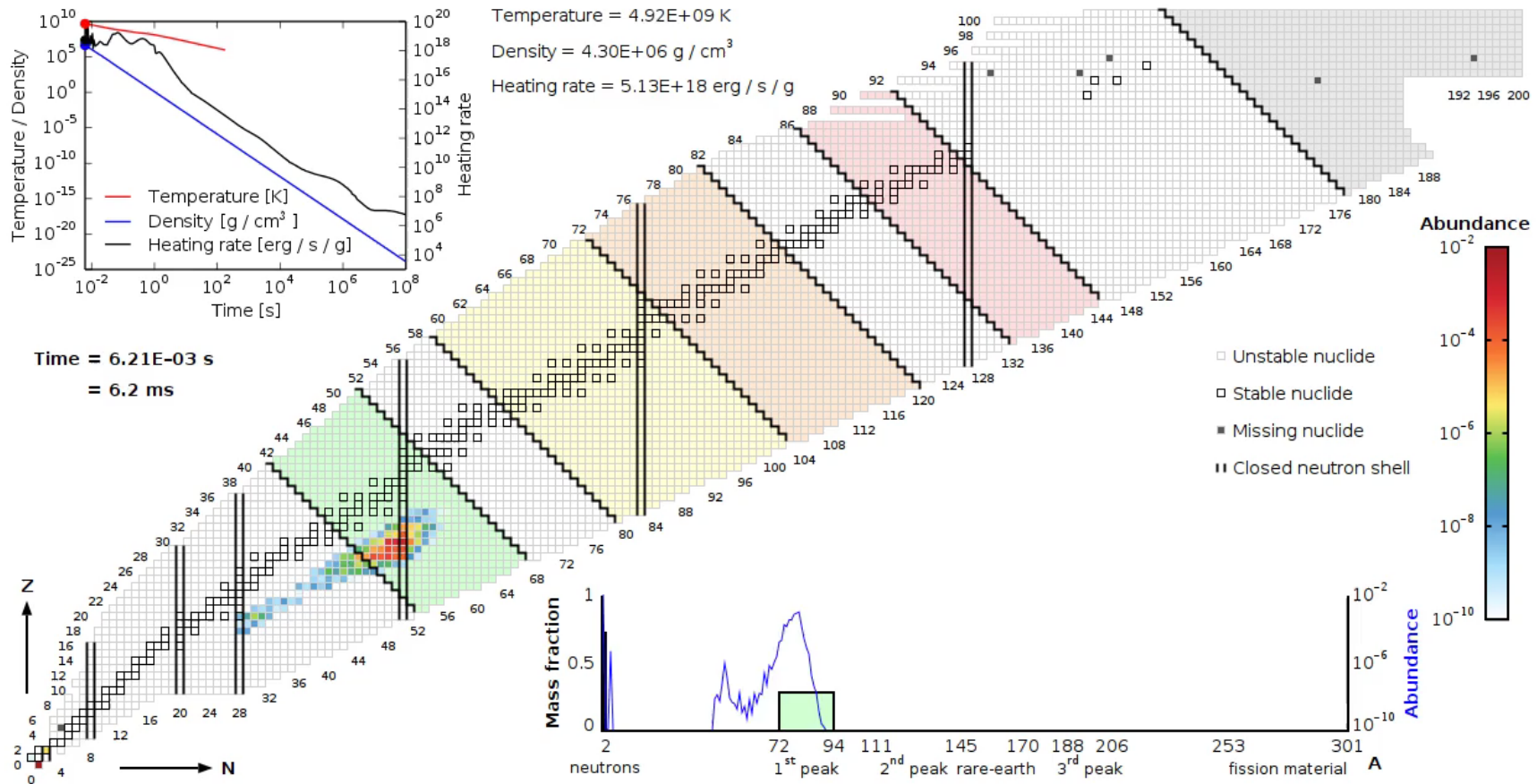


COSMIC ABUNDANCES of the elements

H B																	He B																
Li C	Be C															B C	C S L	N S L	O S L	F L	Ne S L												
Na L	Mg L															Al S L	Si S L	P L	S S L	Cl L	Ar L												
K L	Ca L	Sc L	Ti S L	V S L	Cr L	Mn L	Fe S L	Co S	Ni S	Cu L	Zn L	Ga S	Ge S	As L	Se S	Br S	Kr S																
Rb S	Sr L	Y L	Zr L	Nb L	Mo L	Tc L	Ru S L	Rh S	Pd S L	Ag S L	Cd S L	In S L	Sn S L	Sb S	Te S	I S	Xe S																
Cs S	Ba L																	Hf S L	Ta S L	W S L	Re S	Os S	Ir S	Pt S	Au S	Hg S L	Tl S L	Pb S	Bi S	Po S	At S	Rn S	
Fr S	Ra S																																
		La L	Ce L	Pr S L	Nd S L	Pm S L	Sm S L	Eu S	Gd S	Tb S	Dy S	Ho S	Er S	Tm S	Yb L	Lu S																	
		Ac S	Th S	Pa S	U S	Np S	Pu S	Am M	Cm M	Bk M	Cf M	Es M	Fm M	Md M	No M	Lr M																	

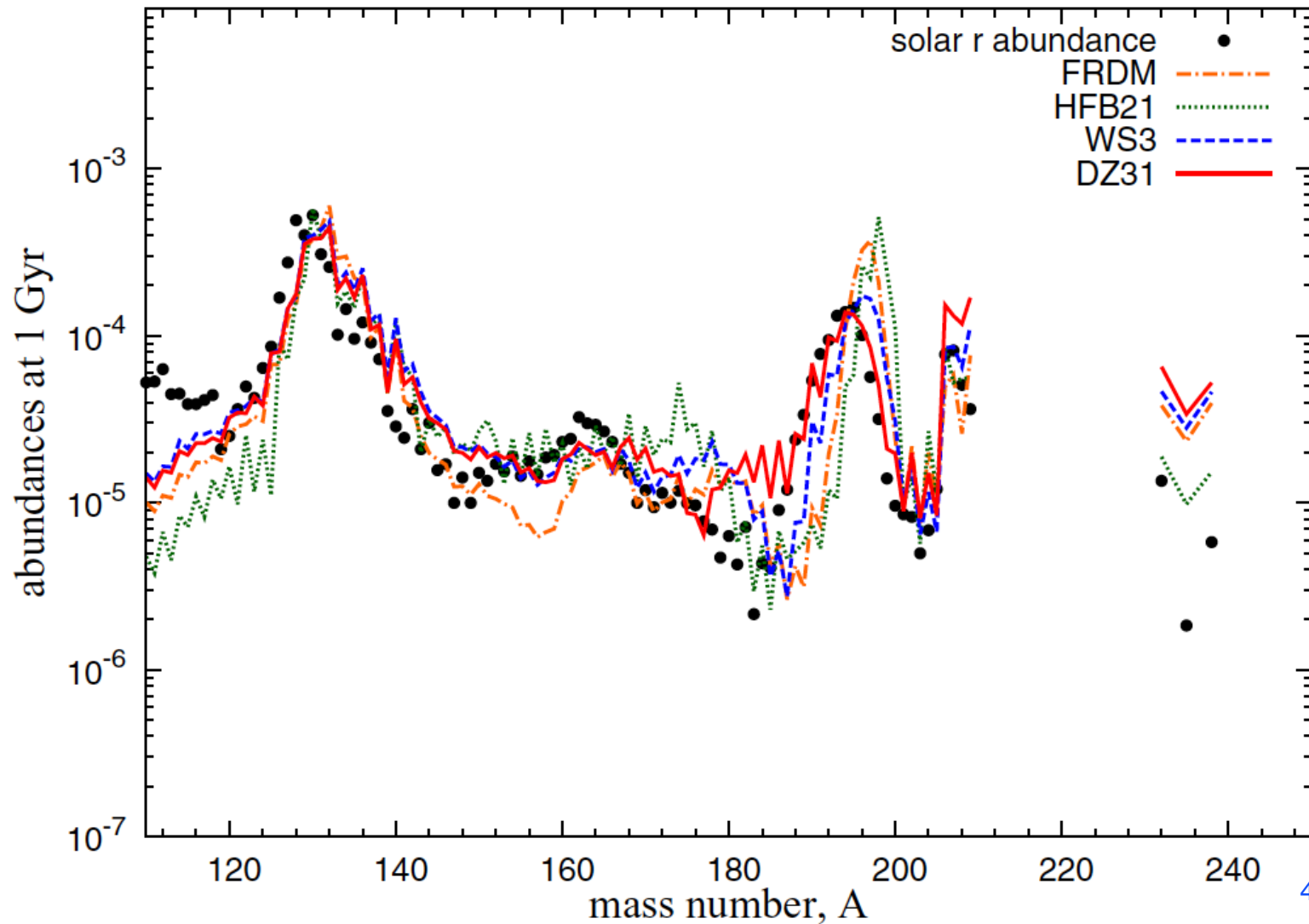


Nucleosynthesis in binary neutron star collisions

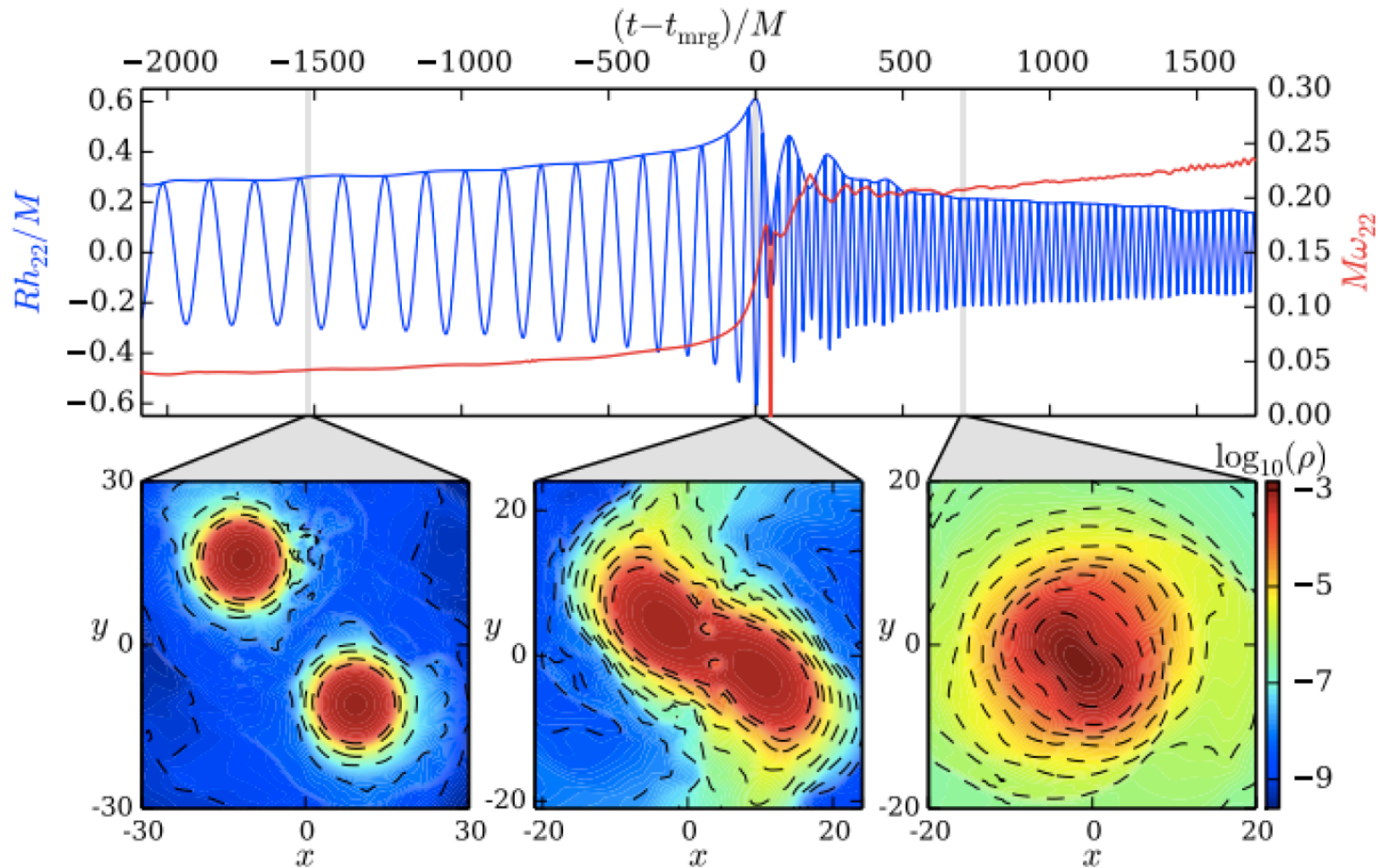


C. Ott; http://www.lippuner.ca/files/nucleosynthesis_000_med.mp4

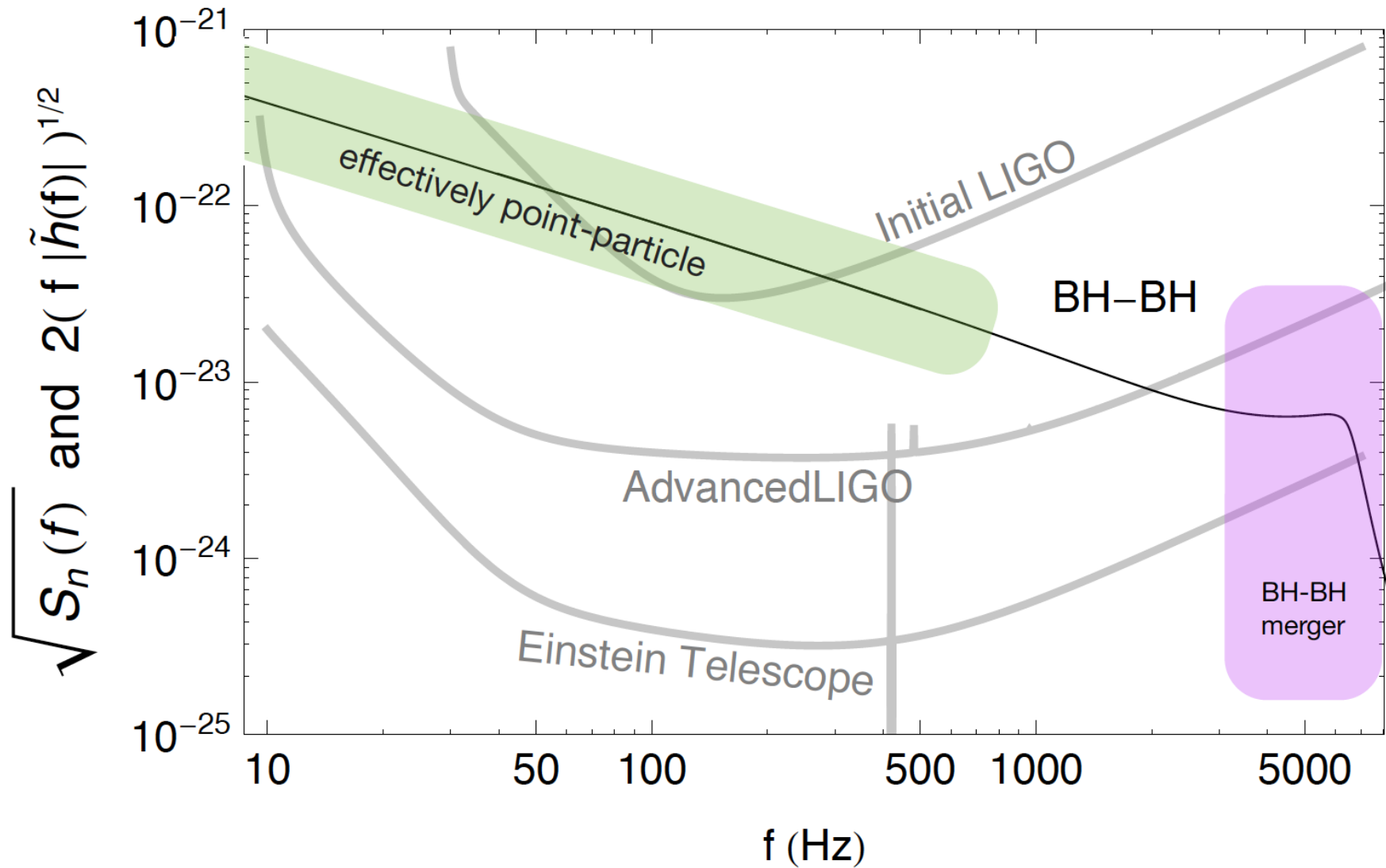
Nuclear abundances from detailed simulations on BNS mergers



GWs from BNS mergers

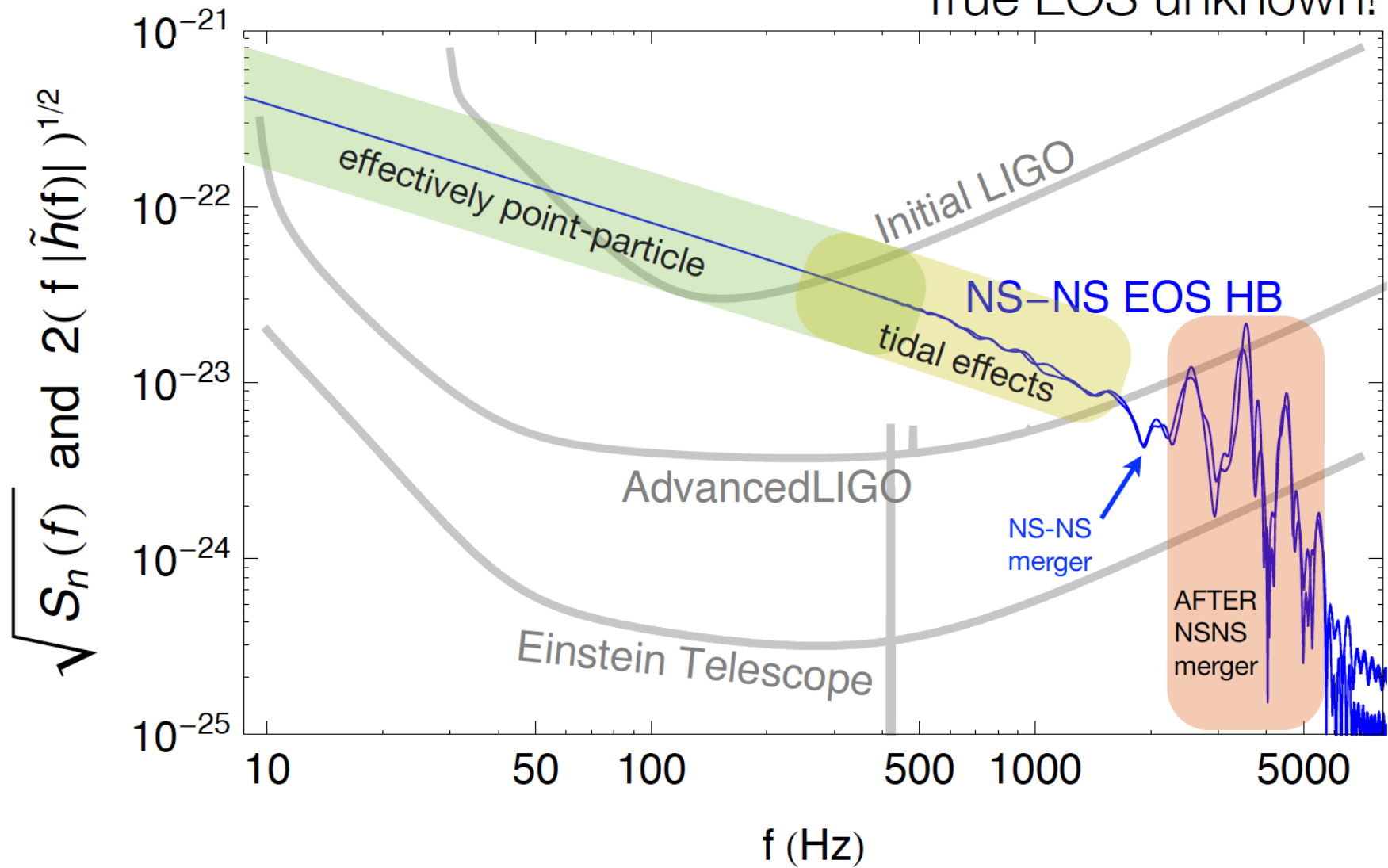


Spectrum of BBH inspiral, scale to 1.35-1.35, 45 Mpc



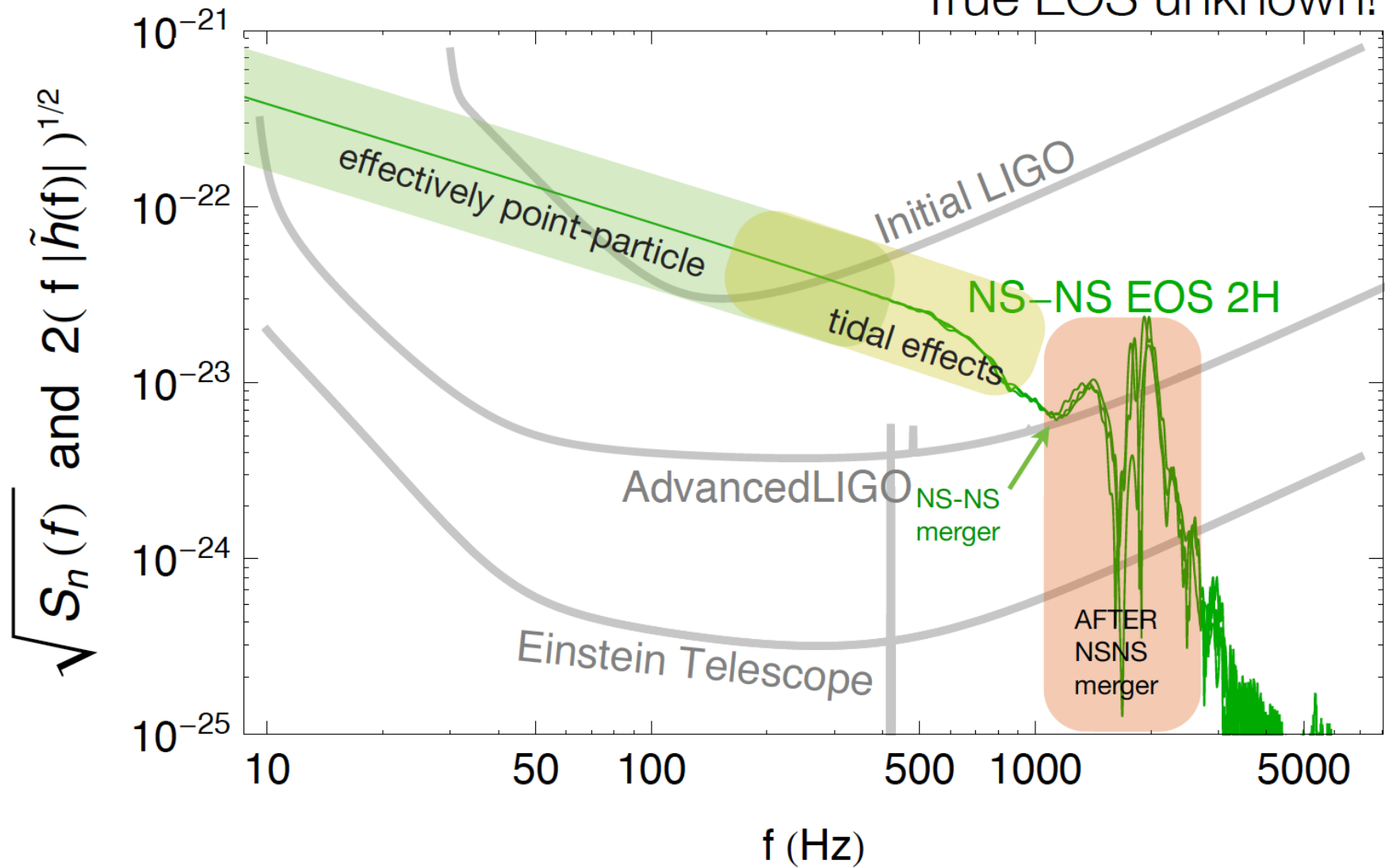
Spectrum of NS-NS inspiral, 1.35-1.35, 45 Mpc

True EOS unknown!

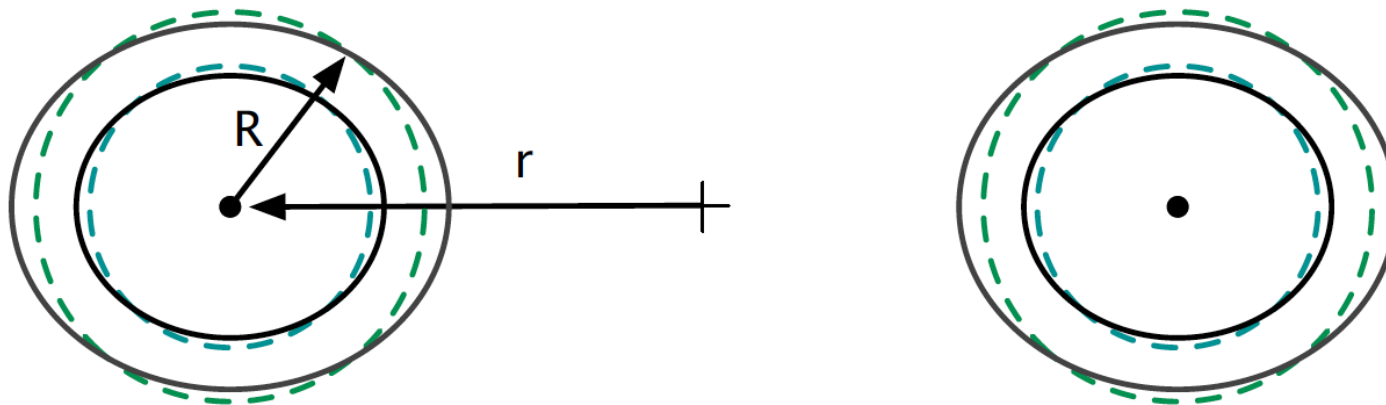


Spectrum of NS-NS inspiral, 1.35-1.35, 45 Mpc

True EOS unknown!



Consider two extended bodies in orbit or free-fall:

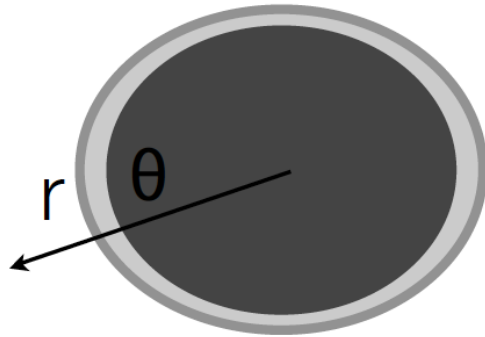


Residual gravitational effect is **tide**.

Amount of deformation depends on size and matter properties.

Deformation induces change in gravitational potential.

Tides and the Quadrupole moment Q



mass M radius R
Love number k
deformed by mass m
distance a away

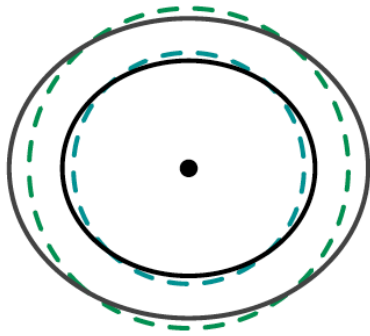
$$Q = \frac{2}{3} k R^5 \left(\frac{m}{d^3} \right)$$

gives the gravitational potential
around a deformed body

$$U = -\frac{M}{r} - \frac{3}{2} \frac{Q(\cos^2 \theta - 1)}{r^3}$$

This tells us about things like satellite movement, tidal locking (“back-reaction” on bulges), and **orbital dynamics in binary systems**

Calculate in GR:



Perturb a spherically symmetric neutron star
impose quadrupole angular dependence
look at scaling with distance from star r

([0711.2420](#), [0906.1366](#), [0906.0096](#))

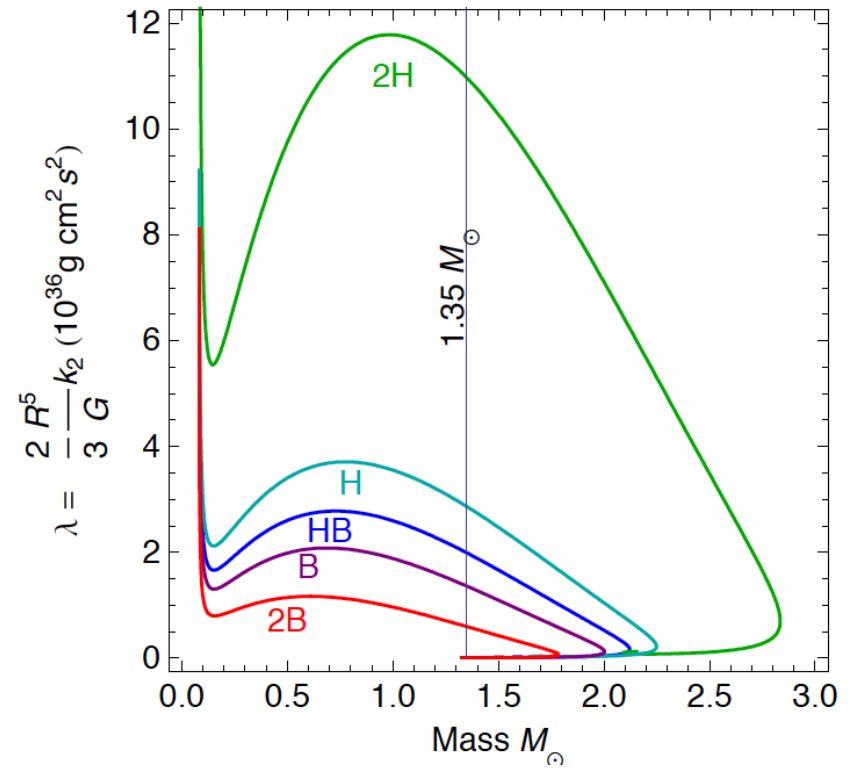
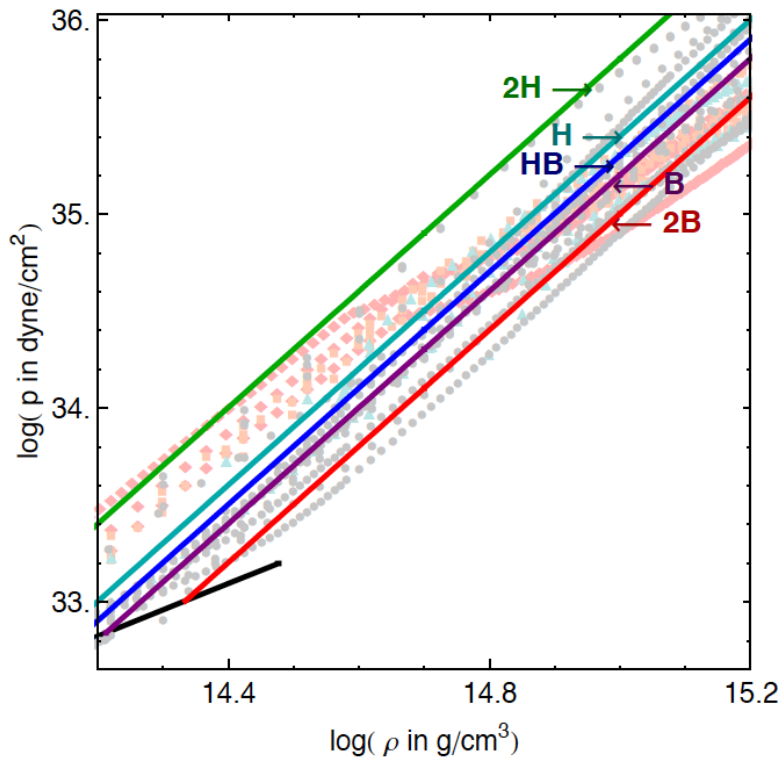
$$\lambda = \frac{Q}{\mathcal{E}} = \frac{\text{size of quadrupole deformation}}{\text{strength of external tidal field}} \quad \begin{array}{l} (\sim r^{-3}) \\ (\sim r^2) \end{array}$$

Love number k_2

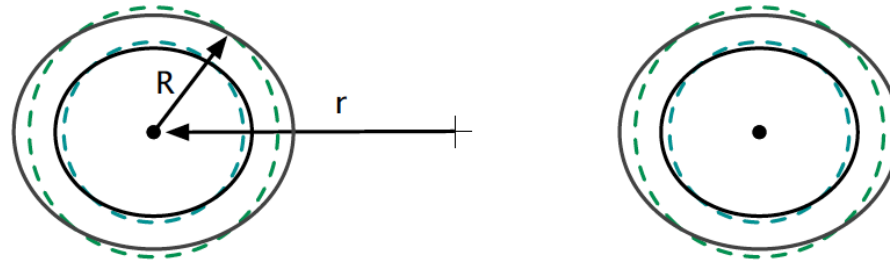
Radius R

$$\lambda = \frac{2}{3} k_2 R^5 \quad (G = c = 1)$$

Equation of state determines λ for each M



Effect of tides on orbit:

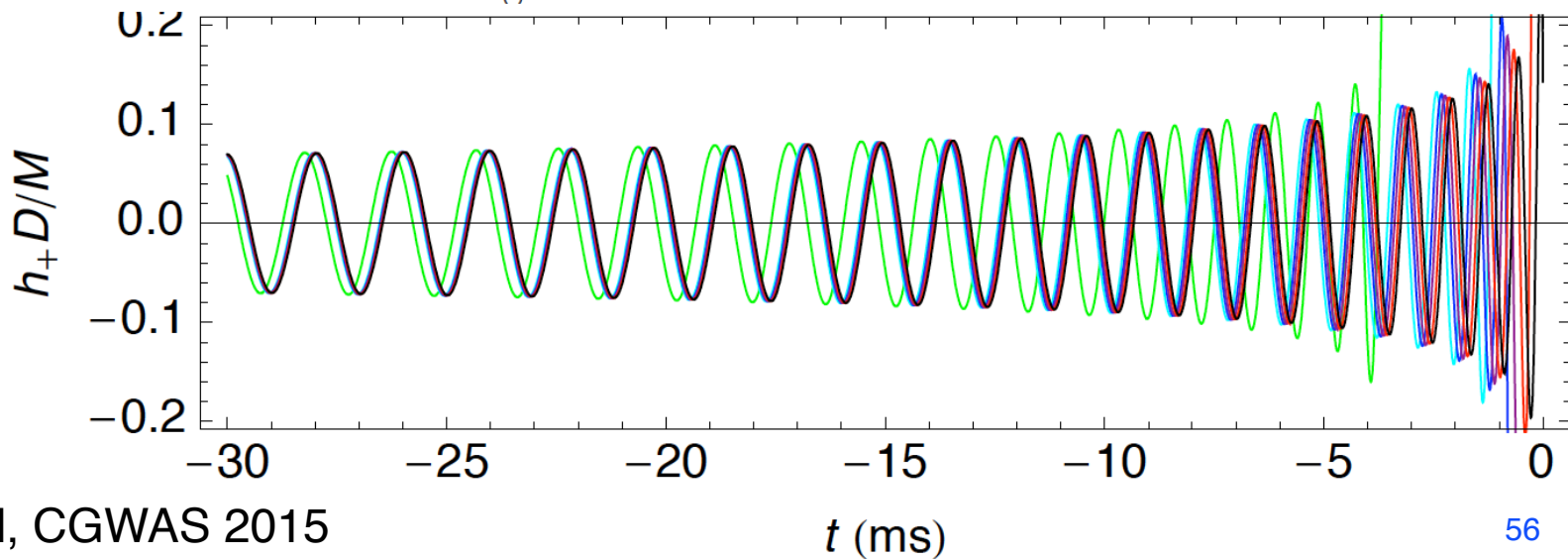
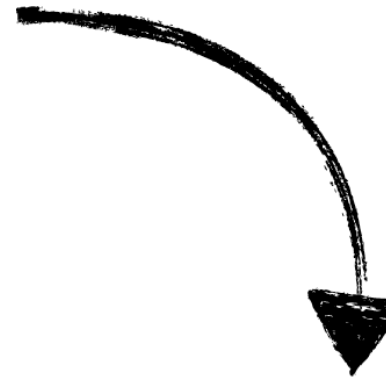
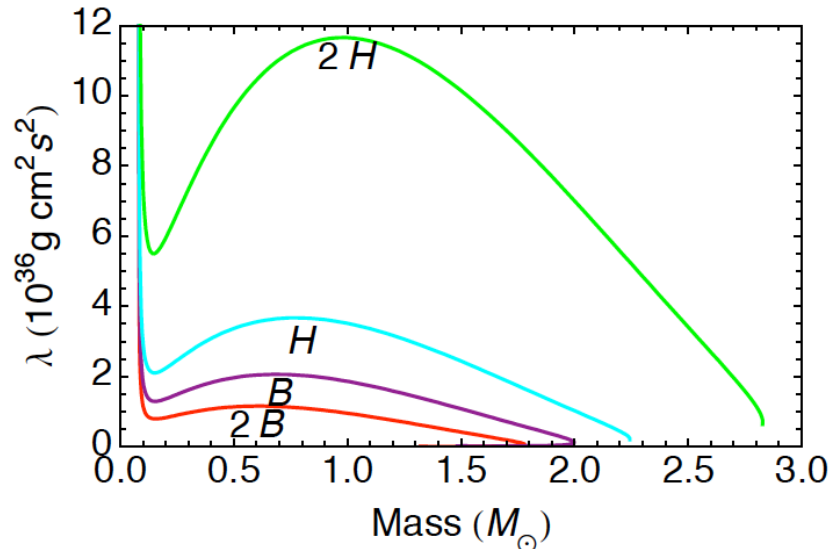


some energy into tides as stars come closer together
a bit of extra GW luminosity from rotating quadrupoles

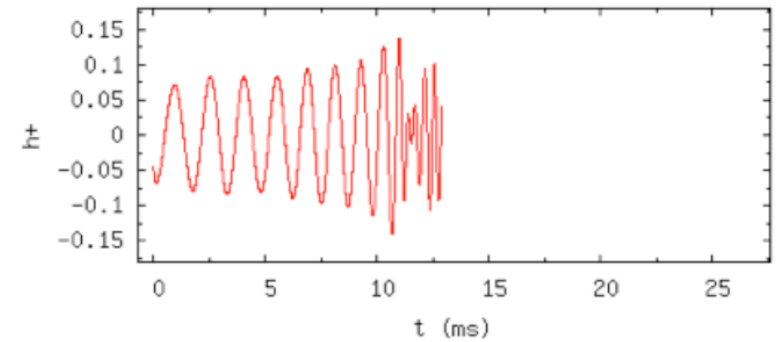
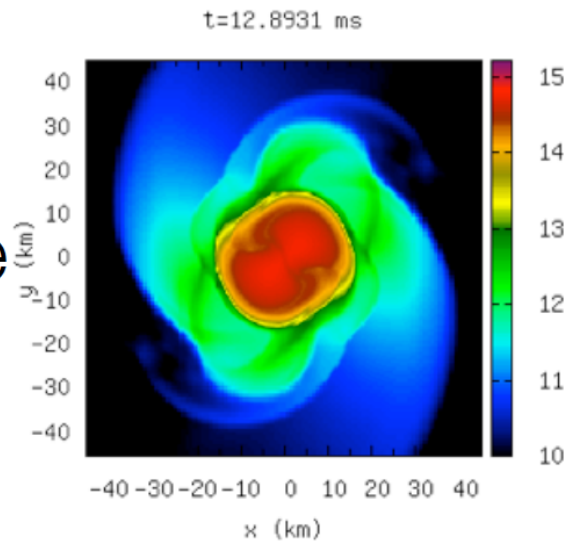


stars merge earlier

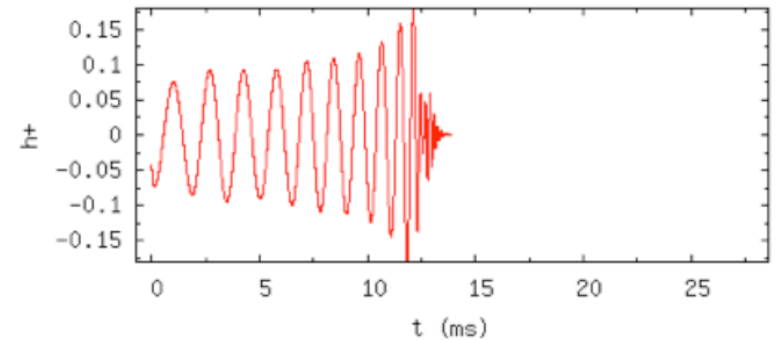
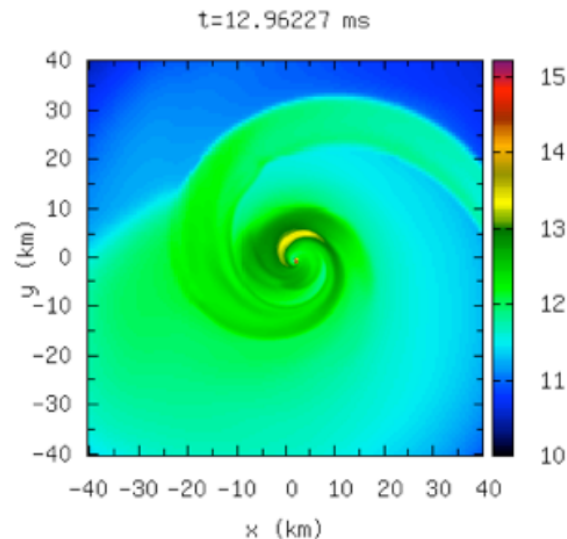
Tidal effect on PN waveforms



Large stars,
Hypermassive
Remnant

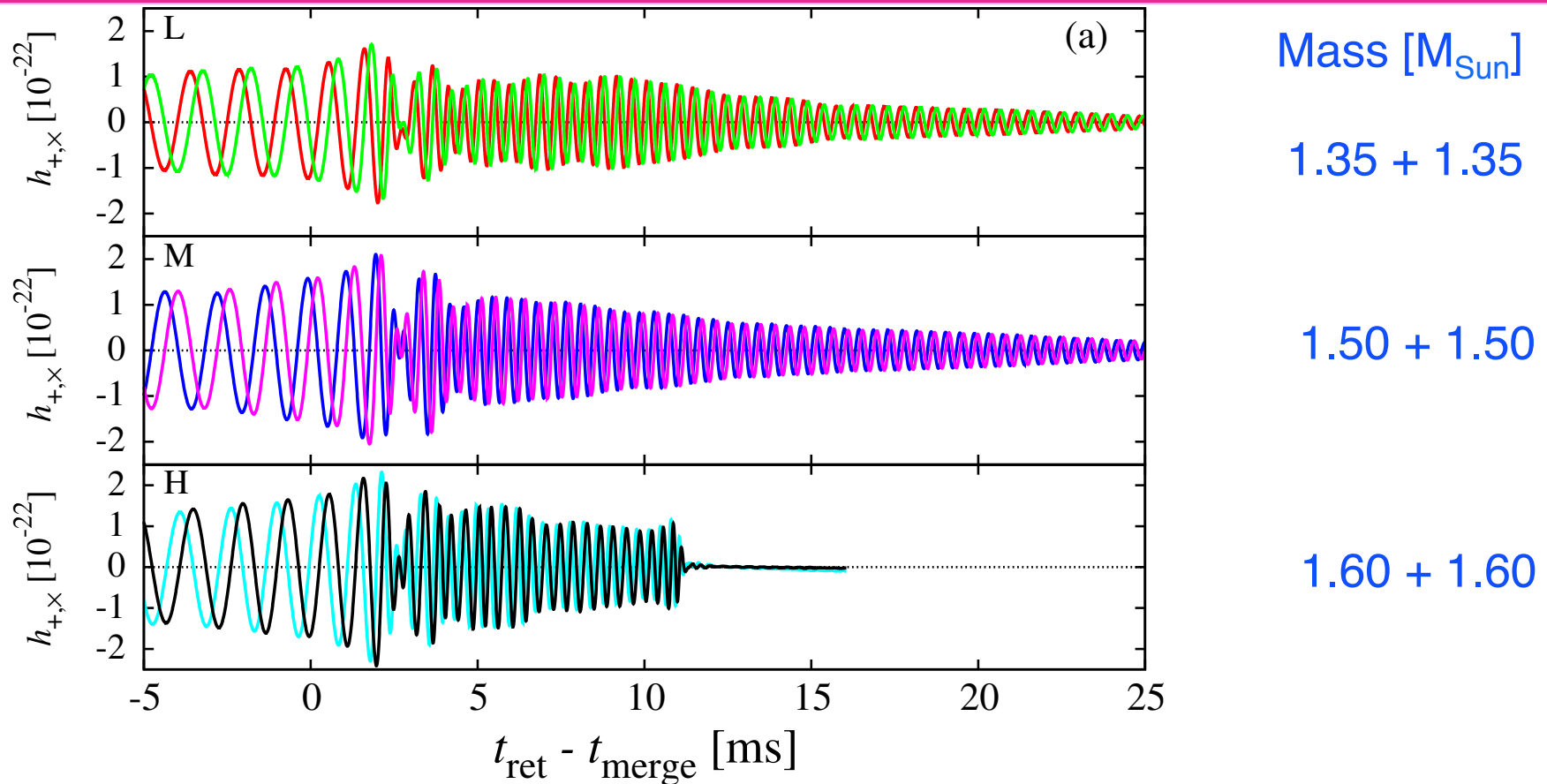


Compact
stars,
Prompt
Collapse



Simulations & animations by K Hotokezaka

Nuclear Astrophysics: NS-NS Mergers



Sekiguchi+ 11: First full GR NS-NS simulation with realistic microphysics, finite-temperature nuclear EOS of H. Shen+ '98, '11

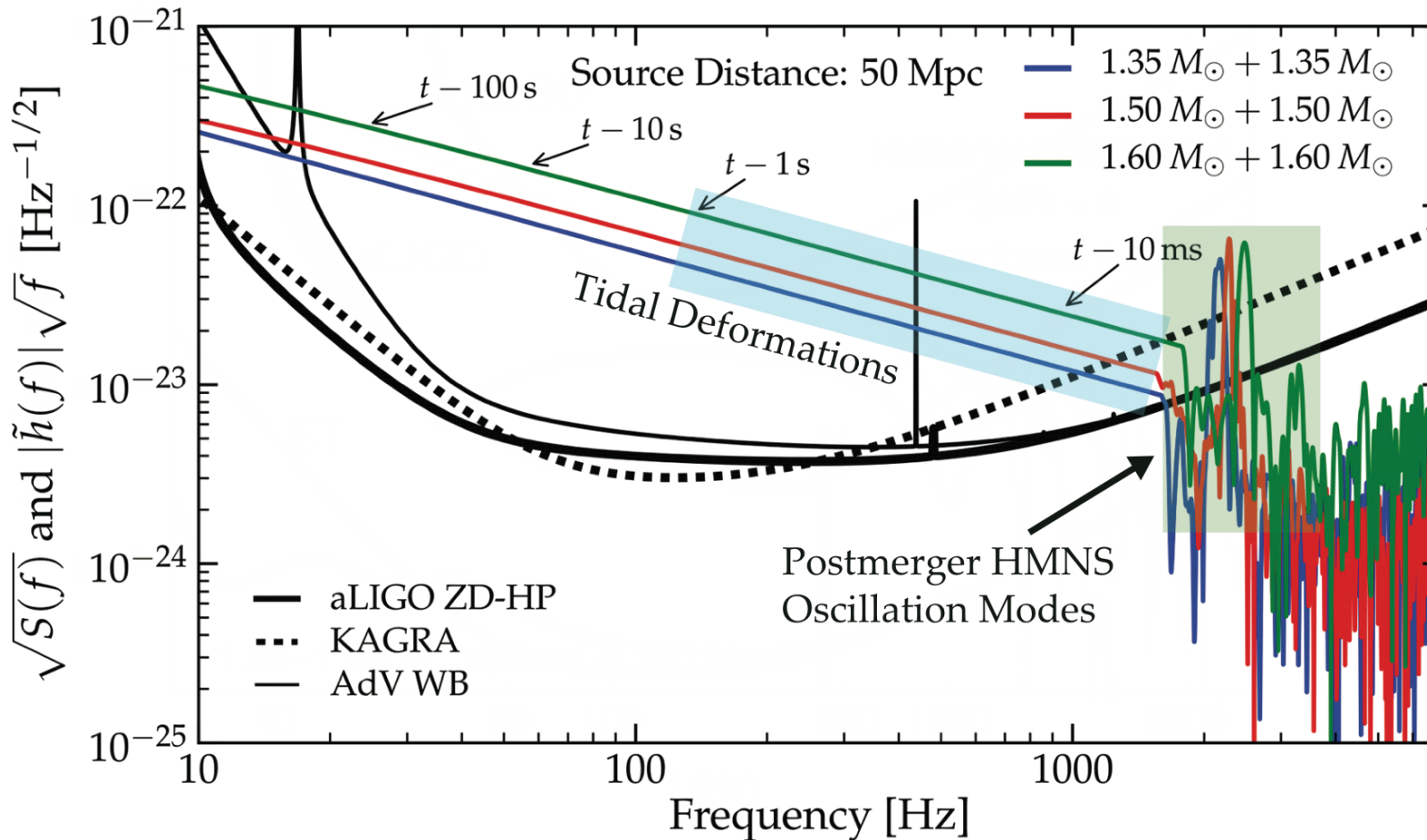


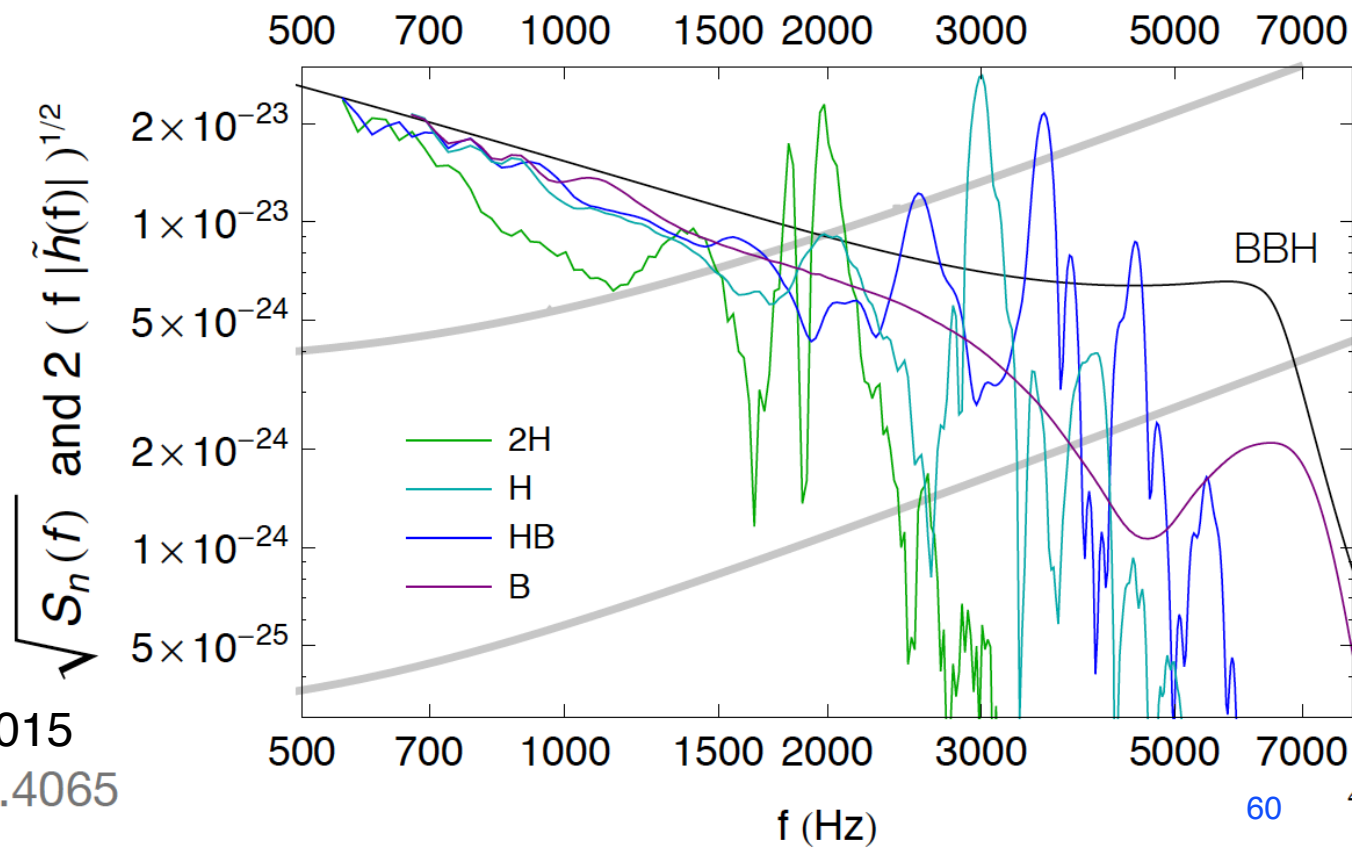
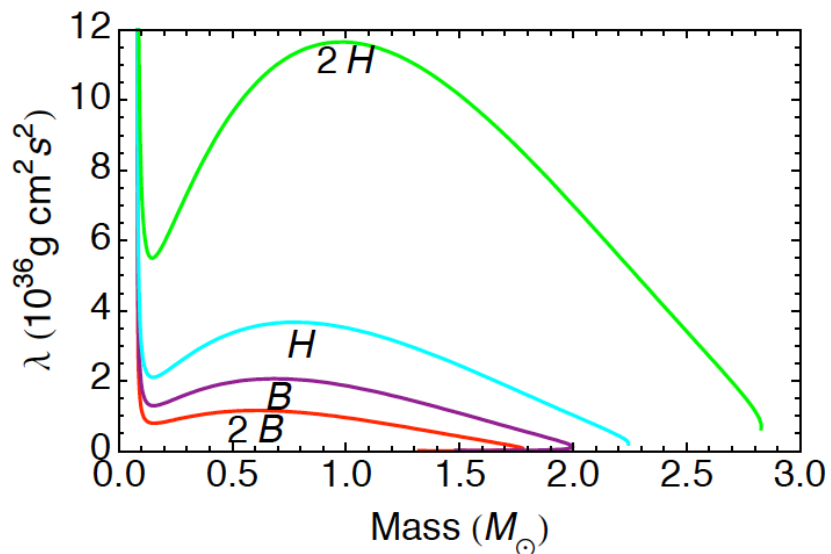
LIGO

Effects of tidal disruption of neutron stars near merger



Credit: Daniel Price and Stephan Rosswog

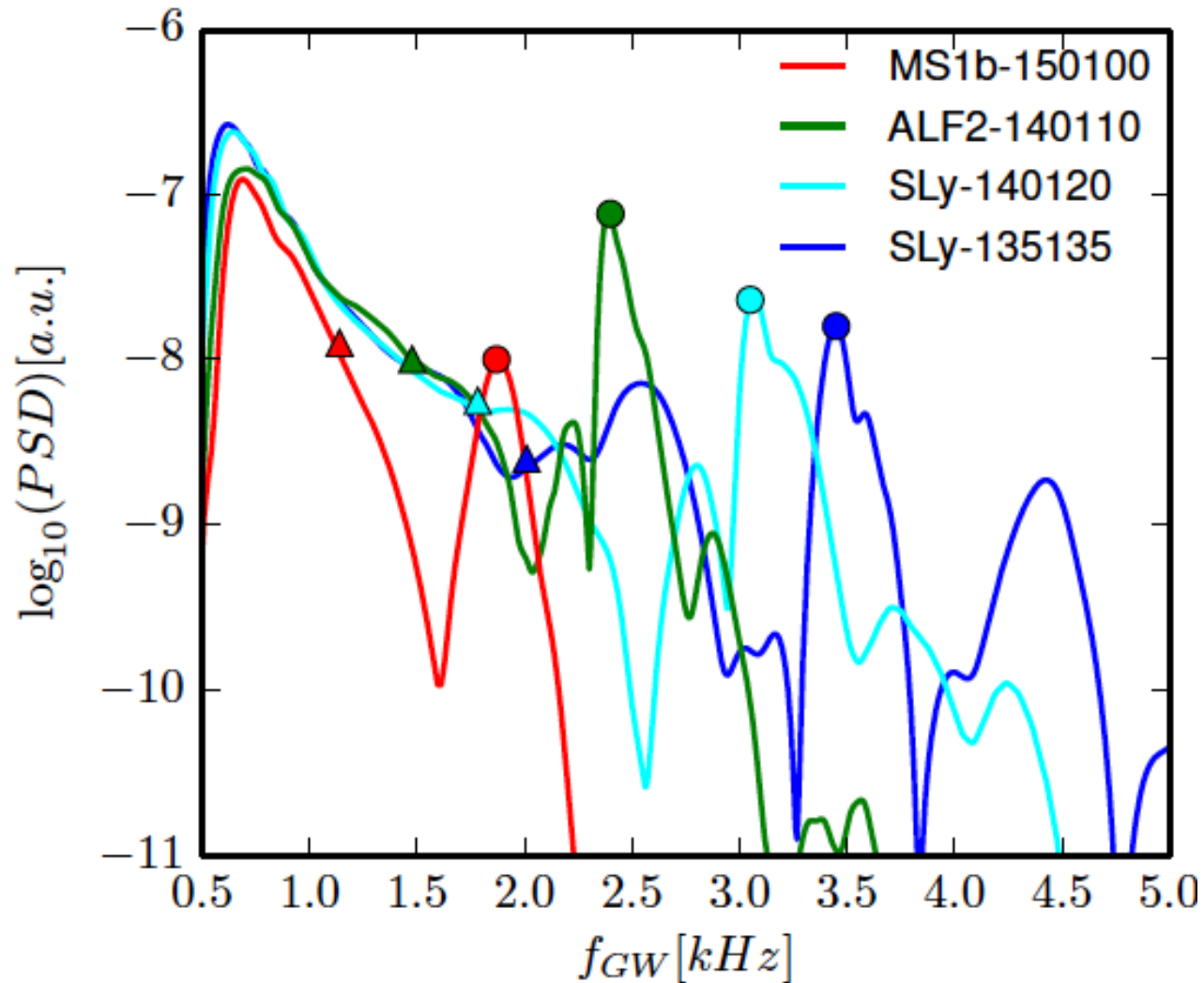




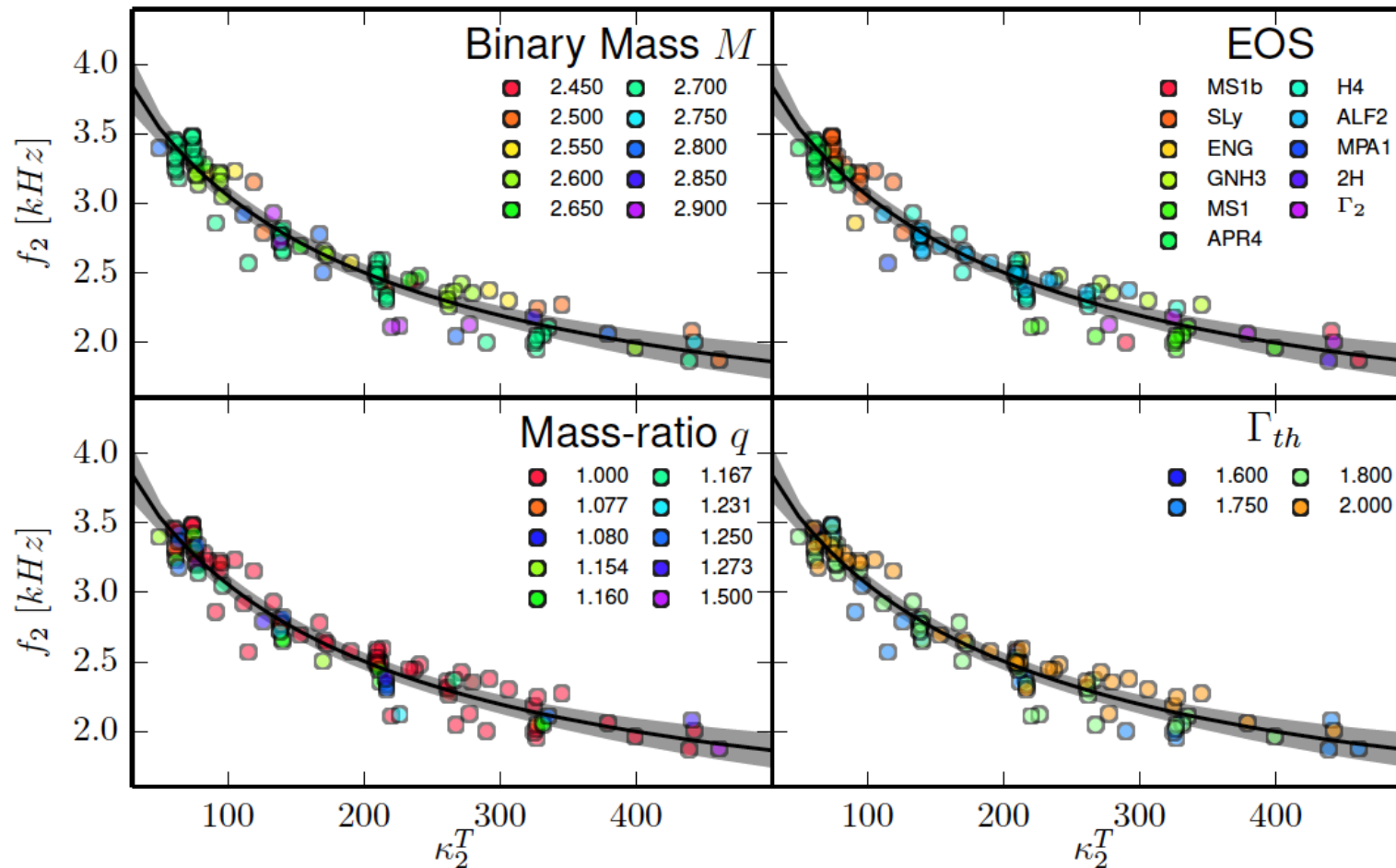
J. Read, CGWAS 2015

• arxiv.org/abs/1306.4065

Frequency of peak of final hyper-massive NS resonance



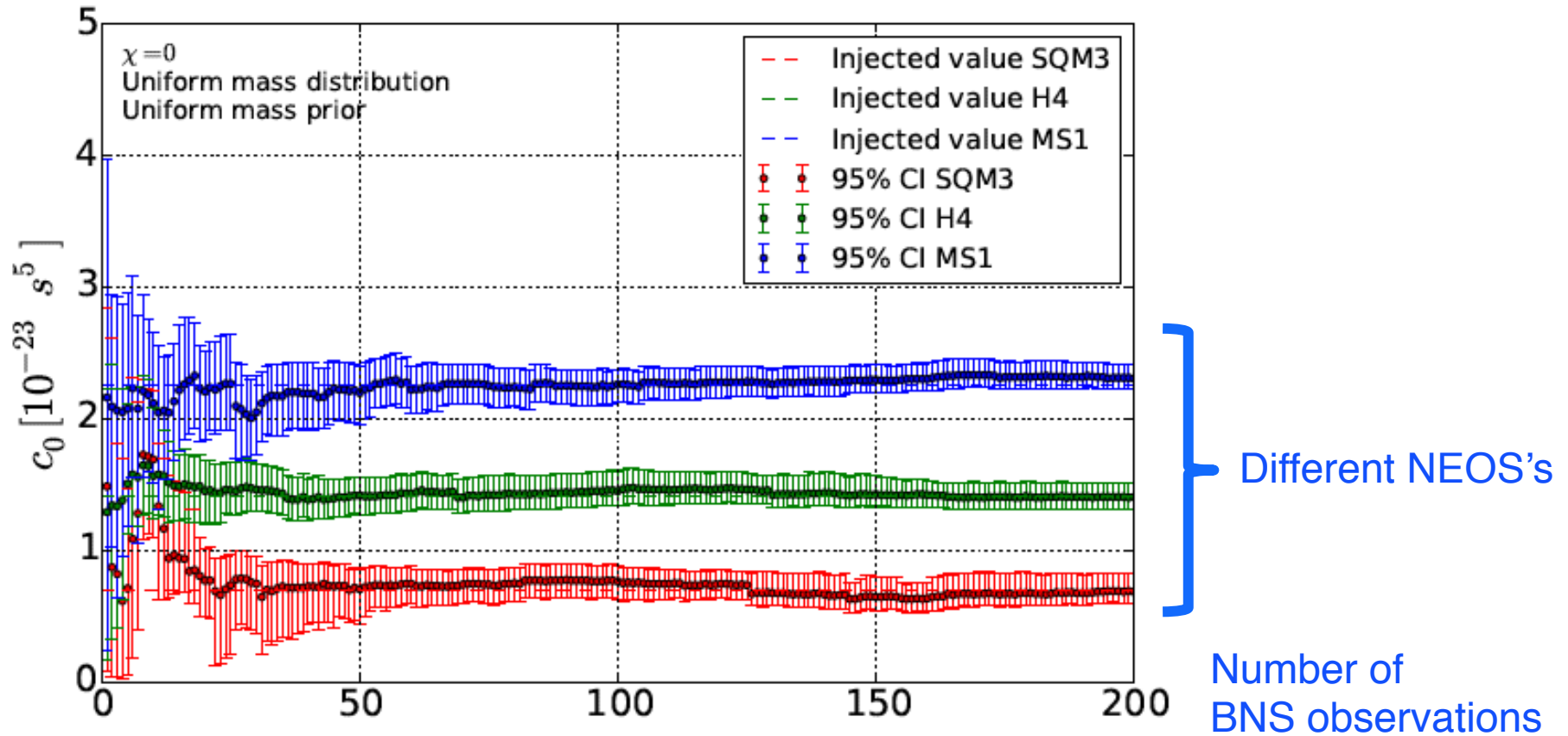
Universality of peak frequency



$$\kappa_2^T = 2 \left(\frac{q^4}{(1+q)^5} \frac{k_2^A}{C_A^5} + \frac{q}{(1+q)^5} \frac{k_2^B}{C_B^5} \right)$$

S Bernuzzi, T Dietrich, A Nagar,
 Phys Rev Lett 115, 091101 (2015) arxiv.org:1504.01764

Many observations required to constrain NEOS

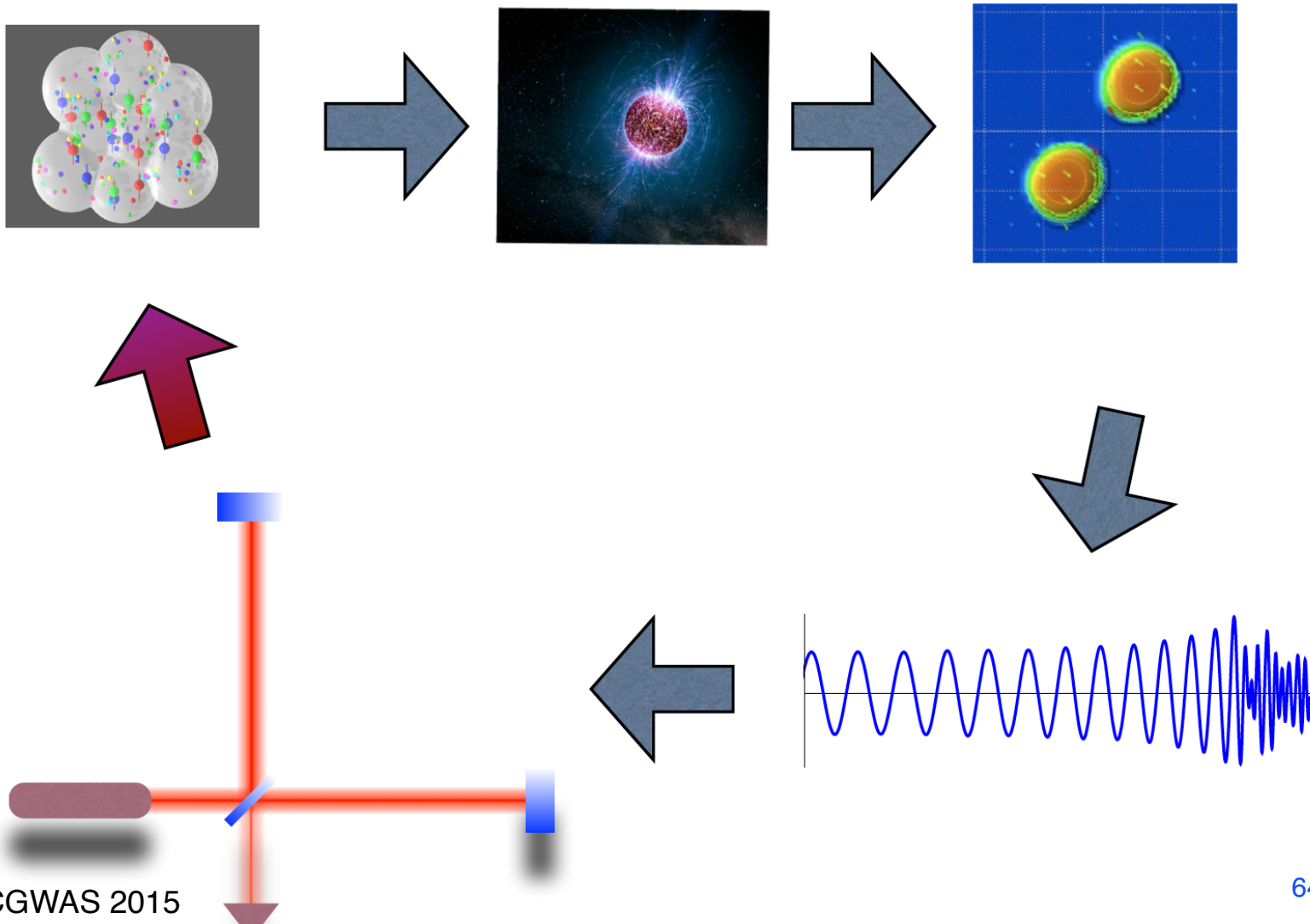


$$Q_{ij} = -\lambda(\text{EOS}; m) \mathcal{E}_{ij}$$

$$\lambda(m) = (2/3)k_2(m)R^5(m)$$

M. Agathos et al (LVC), Phys. Rev. D 92, 023012 (2015),
 arXiv:1503.05405v1

Constraining the NEOS using GWs from BNS





THANK YOU!

Questions?