

T1300403 Wide Angle Scatter from ETM
 8-20-12

Displacement noise requirement @ 100 Hz, m/rt Hz	$D_{\text{req}} := 1 \cdot 10^{-21}$
Motion of manifold @ 100 Hz, m/rt Hz	$x_{\text{manifold}} := 8 \cdot 10^{-11}$
motion of ACB @ 100 Hz, m/rtHz	$x_{\text{ACB}} := 1 \cdot 10^{-12}$
motion of ISI optical table @ 100 Hz, m/rtHz	$x_{\text{ISI}} := 3 \cdot 10^{-14}$
Transfer function @ 100 Hz, ITM HR	$TF_{\text{itmhr}} := 1.1 \cdot 10^{-9}$
BRDF of chamber wall, sr ⁻¹	$BRDF_{\text{wall}} := 0.1$
BRDF of oxidized un-polished steel, sr ⁻¹	$BRDF_{\text{oxiunpolish}} := 0.05$
laser wavelength, m	$\lambda := 1.064 \cdot 10^{-6}$
wave number, m ⁻¹	$k := 2 \cdot \frac{\pi}{\lambda} \quad k = 5.905 \times 10^6$
wide angle hemispherical scattering loss fraction from TM wide, ref: T070089	$\alpha_L := 10 \times 10^{-6}$
see T070303 with arm cavity gain = 13000	
arm power, W	$P_a := 8.125 \times 10^5$
input laser power, W	$P_{\text{psl}} := 125$
arm cavity length, m	$L := 4000$

The following data comes from ZEMAX sensor data; see /ALIGO/SLC/ACB ETM power summary.xlsx

SCATTER PATH LENGTH

distance from spool 7A2, m	$L_{7A2} := 7.446$
distance from PCal structure, m	$L_{PCal} := 2.371$
distance from BSC bottom, m	$L_{bscbottom} := 2.248$
distance from BSC front, m	$L_{bscfront} := 1.566$
distance from BSC back, m	$L_{bscbback} := 1.967$
distance from SUS mid, m	$L_{SUS} := 0.172$
distance from ACB PLATE Top ETM, m	$L_{acbptop} := 0.764$
distance from ACB PLATE Bottom ETM, m	$L_{acbpbot} := 0.572$
distance from ACB PLATE 2 ETM, m	$L_{acb2} := 0.716$
distance from ACB PLATE 3 ETM, m	$L_{acb3} := 0.605$
distance from ACB PLATE 4 ETM, m	$L_{acb4} := 0.468$
distance from ACB PLATE 5 ETM, m	$L_{acb5} := 0.475$
distance from ACB PLATE 6 ETM, m	$L_{acb6} := 0.443$
distance from ACB PLATE 7 ETM, m	$L_{acb7} := 0.231$
distance from peak and cabling, m	$L_{cable} := \frac{L_{acb2} + L_{acb6}}{2}$

	$L_{\text{cable}} = 0.58$
distance from ETM to WIDE ANGLE BAF TOP LEDGE ITMX, m	$L_{\text{wabtop}} := 0.901$
distance from ETM to WIDE ANGLE BAF BOTTOM LEDGE ETM m	$L_{\text{wabbot}} := 0.748$
distance from WIDE ANGLE BAF SIDE right, m	$L_{\text{wabsr}} := 0.895$
distance from WIDE ANGLE BAF SIDE left, m	$L_{\text{wabsl}} := 0.788$

SCATTER ANGLE

angle from spool 7A2, rad	$\theta_{7A2} := 0.1$
angle from PCal structure, rad	$\theta_{\text{PCal}} := 0.09$
angle from BSC bottom, rad	$\theta_{\text{bscbottom}} := 1.8$
angle from BSC front, rad	$\theta_{\text{bscfront}} := 1.83$
angle from BSC back, rad	$\theta_{\text{bscback}} := 1.73$
angle from SUS mid, rad	$\theta_{\text{SUS}} := 1.81$
angle from ACB PLATE Top ETM, rad	$\theta_{\text{acbptop}} := 0.99$
angle from ACB PLATE Bottom ETM, rad	$\theta_{\text{acbpbot}} := 0.67$
angle from ACB PLATE 2 ETM, rad	$\theta_{\text{acbp2}} := 0.82$

angle from ACB PLATE 3 ETM, rad $\theta_{acbp3} := 0.605$

angle from ACB PLATE 4 ETM, rad $\theta_{acbp4} := 0.45$

angle from ACB PLATE 5 ETM, rad $\theta_{acbp5} := 0.34$

angle from ACB PLATE 6 ETM, rad $\theta_{acbp6} := 0.31$

angle from ACB PLATE 7 ETM, rad $\theta_{acbp7} := 0.15$

angle from peak and cabling, m $\theta_{cable} := \frac{\theta_{acbp2} + \theta_{acbp6}}{2}$

$\theta_{cable} = 0.565$

angle from ETM to WIDE ANGLE
 BAF TOP LEDGE ITMX, rad $\theta_{wabtop} := 0.71$

angle from ETM to WIDE ANGLE
 BAF BOTTOM LEDGE ETM, rad $\theta_{wabbot} := 0.51$

angle from WIDE ANGLE BAF
 SIDE right, rad $\theta_{wabsr} := 0.54$

angle from WIDE ANGLE BAF
 SIDE left, rad $\theta_{wabsl} := 0.46$

FRACTION of LAMBERTIAN SCATTER FROM COC HITTING SURFACE

fractional power from spool 7A2, W $PF_{7A2} := 0.0122$

fractional power hitting PCal
 structure, W $PF_{PCal} := 0.0278$

fractional power passing through
 hole in ACB, W $PF_{acbhole} := PF_{7A2} + PF_{PCal}$

$$PF_{\text{acbhole}} = 0.04$$

fractional power from BSC bottom, W

$$PF_{\text{bscbottom}} := 0.0311$$

fractional power from BSC front, W

$$PF_{\text{bscfront}} := 0.0544$$

fractional power from BSC back, W

$$PF_{\text{bscbback}} := 0.00444$$

fractional power from SUS mid, W

$$PF_{\text{SUS}} := 0.0456$$

fractional power from ACB PLATE Top
ETM, W

$$PF_{\text{acbptop}} := 0.00444$$

fractional power from ACB PLATE Bottom
ETM, W

$$PF_{\text{acbpbot}} := 0.0278$$

fractional power from ACB PLATE 2
ETM, W

$$PF_{\text{acbp2}} := 0.0689$$

fractional power from ACB PLATE 3
ETM, W

$$PF_{\text{acbp3}} := 0.0211$$

fractional power from ACB PLATE 4
ETM, W

$$PF_{\text{acbp4}} := 0.00889$$

fractional power from ACB PLATE 5
ETM, W

$$PF_{\text{acbp5}} := 0.0578$$

fractional power from ACB PLATE 6
ETM, W

$$PF_{\text{acbp6}} := 0.0633$$

fractional power from ACB PLATE 7
ETM, W

$$PF_{\text{acbp7}} := 0.00778$$

fractional power hitting ACB box, W

$$PF_{\text{acbbox}} := PF_{\text{acbp2}} + PF_{\text{acbp3}} + PF_{\text{acbp4}} + PF_{\text{acbp5}} + PF_{\text{acbp6}}$$

$$PF_{\text{acbbox}} = 0.22$$

fractional power from ETM to WIDE
 ANGLE BAF TOP LEDGE ITMX, W

$$PF_{wabtop} := 0.0722$$

fractional power from ETM to WIDE
 ANGLE BAF BOTTOM LEDGE
 ETM, W

$$PF_{wabbot} := 0.219$$

fractional power from WIDE ANGLE
 BAF SIDE right, W

$$PF_{wabsr} := 0.192$$

fractional power from WIDE ANGLE
 BAF SIDE left, W

$$PF_{wabsl} := 0.0567$$

fractional power hitting ACB plus
 wide angle box, W

$$PF_{acb} := PF_{acbp2} + PF_{acbp3} + PF_{acbp4} + PF_{acbp5} + PF_{acbp6} + PF_{acbp7} + PF_{wabtop} + PF_{wabbot} + PF_{wabsr} + PF_{wabsl}$$

$$PF_{acb} = 0.768$$

INCIDENT POWER

incident power from spool 7A2, W

$$P_{7A2} := P_a \cdot PF_{7A2} \cdot \alpha_L$$

$$P_{7A2} = 0.099$$

incident power hitting PCal structure, W

$$P_{PCal} := P_a \cdot PF_{PCal} \cdot \alpha_L$$

$$P_{PCal} = 0.226$$

incident power from BSC bottom, W

$$P_{bscbottom} := P_a \cdot PF_{bscbottom} \cdot \alpha_L$$

$$P_{bscbottom} = 0.253$$

incident power from BSC front, W

$$P_{bscfront} := P_a \cdot PF_{bscfront} \cdot \alpha_L$$

$$P_{bscfront} = 0.442$$

incident power from BSC back, W

$$P_{bscback} := P_a \cdot PF_{bscback} \cdot \alpha_L$$

$$P_{bscback} = 0.036$$

incident power from SUS mid, W

$$P_{SUS} := P_a \cdot PF_{SUS} \cdot \alpha_L$$

$$P_{SUS} = 0.37$$

incident power from ACB PLATE Top
 ETM, W

$$P_{acbp2} := P_a \cdot PF_{acbp2} \cdot \alpha_L$$

$$P_{acbp2} = 0.036$$

incident power from ACB PLATE Bottom
 ETM, W

$$P_{acbp7} := P_a \cdot PF_{acbp7} \cdot \alpha_L$$

$$P_{acbp7} = 0.226$$

incident power from ACB PLATE 2 ETM, W	$P_{acbp2} := P_a \cdot PF_{acbp2} \cdot \alpha_L$	$P_{acbp2} = 0.56$
incident power from ACB PLATE 3 ETM, W	$P_{acbp3} := P_a \cdot PF_{acbp3} \cdot \alpha_L$	$P_{acbp3} = 0.171$
incident power from ACB PLATE 4 ETM, W	$P_{acbp4} := P_a \cdot PF_{acbp4} \cdot \alpha_L$	$P_{acbp4} = 0.072$
incident power from ACB PLATE 5 ETM, W	$P_{acbp5} := P_a \cdot PF_{acbp5} \cdot \alpha_L$	$P_{acbp5} = 0.47$
incident power from ACB PLATE 6 ETM, W	$P_{acbp6} := P_a \cdot PF_{acbp6} \cdot \alpha_L$	$P_{acbp6} = 0.514$
incident power from ACB PLATE 7 ETM, W	$P_{acbp7} := P_a \cdot PF_{acbp7} \cdot \alpha_L$	$P_{acbp7} = 0.063$
incident power from ETM to WIDE ANGLE BAF TOP LEDGE ITMX, W	$P_{wabtop} := P_a \cdot PF_{wabtop} \cdot \alpha_L$	$P_{wabtop} = 0.587$
incident power from ETM to WIDE ANGLE BAF BOTTOM LEDGE ETM, W	$P_{wabbot} := P_a \cdot PF_{wabbot} \cdot \alpha_L$	$P_{wabbot} = 1.779$
incident power from WIDE ANGLE BAF SIDE right, W	$P_{wabsr} := P_a \cdot PF_{wabsr} \cdot \alpha_L$	$P_{wabsr} = 1.56$
incident power from WIDE ANGLE BAF SIDE left, W	$P_{wabsl} := P_a \cdot PF_{wabsl} \cdot \alpha_L$	$P_{wabsl} = 0.461$

POWER SCATTERED INTO IFO MODE

$$P_{inc} := 1 \quad L_S := 1$$

$$w_{ifo} := 1$$

$$BRDF_s := 1$$

$$\theta_{inc} := 1$$

$$\theta_{s1} := 1$$

$$\theta_{s2} := 1$$

$$\theta := 1$$

$$d\Omega := 1$$

$$P_{sTM} := 1$$

$$A_{TM} := 1$$

Lambertian scatter function for the TM

$$BRDF_L := \alpha_L \cdot \frac{\cos(\theta)}{\pi}$$

differential wide angle scattered light from TM onto adjacent surfaces

$$dP_{sadj} := P_a \cdot BRDF_L \cdot d\Omega$$

total wide angle scattered light from TM onto each adjacent surfaces

$$P_{sadj} := P_a \cdot \alpha_L \cdot \int_{\theta_{s1}}^{\theta_{s2}} \frac{\cos(\theta)}{\pi} d\Omega$$

ZEMAX power fraction

$$PF_s := \int_{\theta_{s1}}^{\theta_{s2}} \frac{\cos(\theta)}{\pi} d\Omega$$

incident power hitting the adjacent surface is

$$P_{\text{inc}} := P_a \cdot \alpha_L \cdot PF_s$$

irradiance of TM by power scattered from adjacent surface, W/m²

$$E_s := P_{\text{inc}} \cdot BRDF_s \cdot \frac{1}{L_s^2}$$

Flanagan-Thorne scattering cross-section

$$\sigma := \lambda^2 \cdot BRDF_L$$

power scattered by TM into IFO mode

$$P_{\text{sifo}} := E_s \cdot \sigma$$

$$P_{\text{sifo}} := P_{\text{inc}} \cdot BRDF_s \cdot \frac{\lambda^2}{L_s^2} \cdot \alpha_L \cdot \frac{\cos(\theta_{\text{inc}})}{\pi}$$

incident power hitting the adjacent surface is

$$P_{\text{inc}} := P_a \cdot \alpha_L \cdot PF_s$$

combining these equations, we get

$$P_{\text{sTMifo}} := P_{\text{inc}} \cdot BRDF_s \cdot \frac{\lambda^2}{L_s^2} \cdot \alpha_L \cdot \frac{\cos(\theta_{\text{inc}})}{\pi}$$

spool 7A2, W

$$P_{7A2\text{ifo}} := \sqrt{4} \cdot P_{7A2} \cdot BRDF_{\text{wall}} \left(\frac{\lambda^2}{L_{7A2}^2} \cdot \alpha_L \cdot \frac{|\cos(\theta_{7A2})|}{\pi} \right)$$

$$P_{7A2\text{ifo}} = 1.282 \times 10^{-21}$$

PCal structure, W

$$P_{\text{PCalifo}} := \sqrt{4} \cdot P_{\text{PCal}} \cdot \left(\frac{\lambda^2}{L_{\text{PCal}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{PCal}})|}{\pi} \right)$$

$$P_{\text{PCalifo}} = 2.884 \times 10^{-20}$$

BSC bottom, W

$$P_{\text{bscbottomifo}} := \sqrt{4} \cdot P_{\text{bscbottom}} \cdot \left(\frac{\lambda^2}{L_{\text{bscbottom}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{bscbottom}})|}{\pi} \right)$$

$$P_{\text{bscbottomifo}} = 8.188 \times 10^{-21}$$

BSC front, W

$$P_{\text{bscfrontifo}} := \sqrt{4} \cdot P_{\text{bscfront}} \cdot \left(\frac{\lambda^2}{L_{\text{bscfront}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{bscfront}})|}{\pi} \right)$$

$$P_{\text{bscfrontifo}} = 3.329 \times 10^{-20}$$

BSC back, W

$$P_{\text{bscbackifo}} := \sqrt{4} \cdot P_{\text{bscback}} \cdot \left(\frac{\lambda^2}{L_{\text{bscback}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{bscback}})|}{\pi} \right)$$

$$P_{\text{bscbackifo}} = 1.065 \times 10^{-21}$$

SUS mid, W

$$P_{\text{SUSifo}} := \sqrt{4} \cdot P_{\text{SUS}} \cdot \left(\frac{\lambda^2}{L_{\text{SUS}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{SUS}})|}{\pi} \right)$$

$$P_{\text{SUSifo}} = 1.069 \times 10^{-18}$$

ACB PLATE TOP ETM, W

$$P_{\text{acbptopifo}} := \sqrt{4} \cdot P_{\text{acbptop}} \cdot \left(\frac{\lambda^2}{L_{\text{acbptop}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbptop}})|}{\pi} \right)$$

$$P_{\text{acbptopifo}} = 1.222 \times 10^{-20}$$

ACB PLATE Bottom ETM, W

$$P_{\text{acbpbotifo}} := \sqrt{4} \cdot P_{\text{acbpbot}} \cdot \left(\frac{\lambda^2}{L_{\text{acbpbot}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbpbot}})|}{\pi} \right)$$

$$P_{\text{acbpbotifo}} = 1.95 \times 10^{-19}$$

ACB PLATE 2 ETM, W

$$P_{\text{acbp2ifo}} := \sqrt{4} \cdot P_{\text{acbp2}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp2}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp2}})|}{\pi} \right)$$

$$P_{\text{acbp2ifo}} = 2.685 \times 10^{-19}$$

ACB PLATE 3 ETM, W

$$P_{\text{acbp3ifo}} := \sqrt{4} \cdot P_{\text{acbp3}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp3}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp3}})|}{\pi} \right)$$

$$P_{\text{acbp3ifo}} = 1.388 \times 10^{-19} \quad L_{\text{acbp3}} = 0.605$$

ACB PLATE 4 ETM, W

$$P_{\text{acbp4ifo}} := \sqrt{4} \cdot P_{\text{acbp4}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp4}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp4}})|}{\pi} \right)$$

$$P_{\text{acbp4ifo}} = 1.07 \times 10^{-19}$$

ACB PLATE 5 ETM, W

$$P_{\text{acbp5ifo}} := \sqrt{4} \cdot P_{\text{acbp5}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp5}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp5}})|}{\pi} \right)$$

$$P_{\text{acbp5ifo}} = 7.071 \times 10^{-19}$$

ACB PLATE 6 ETM, W

$$P_{\text{acbp6ifo}} := \sqrt{4} \cdot P_{\text{acbp6}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp6}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp6}})|}{\pi} \right)$$

$$P_{\text{acbp6ifo}} = 8.994 \times 10^{-19}$$

ACB PLATE 7 ETM, W

$$P_{\text{acbp7ifo}} := \sqrt{4} \cdot P_{\text{acbp7}} \cdot \left(\frac{\lambda^2}{L_{\text{acbp7}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{acbp7}})|}{\pi} \right)$$

$$P_{\text{acbp7ifo}} = 4.221 \times 10^{-19}$$

WIDE ANGLE BAF TOP LEDGE ITMX, W

$$P_{\text{wabtopifo}} := \sqrt{4} \cdot P_{\text{wabtop}} \cdot \left(\frac{\lambda^2}{L_{\text{wabtop}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{wabtop}})|}{\pi} \right)$$

$$P_{\text{wabtopifo}} = 1.975 \times 10^{-19}$$

WIDE ANGLE BAF BOTTOM LEDGE
 ETM, W

$$P_{\text{wabbotifo}} := \sqrt{4} \cdot P_{\text{wabbot}} \cdot \left(\frac{\lambda^2}{L_{\text{wabbot}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{wabbot}})|}{\pi} \right)$$

$$P_{\text{wabbotifo}} = 1 \times 10^{-18}$$

WIDE ANGLE BAF SIDE right W

$$P_{\text{wabsrifo}} := \sqrt{4} \cdot P_{\text{wabsr}} \cdot \left(\frac{\lambda^2}{L_{\text{wabsr}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{wabsr}})|}{\pi} \right)$$

$$P_{\text{wabsrifo}} = 6.019 \times 10^{-19}$$

WIDE ANGLE BAF SIDE left, W

$$P_{\text{wabslifo}} := \sqrt{4} \cdot P_{\text{wabsl}} \cdot \left(\frac{\lambda^2}{L_{\text{wabsl}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \alpha_L \cdot \frac{|\cos(\theta_{\text{wabsl}})|}{\pi} \right)$$

$$P_{\text{wabslifo}} = 2.396 \times 10^{-19}$$

DIFFUSE SCATTERING FROM PEEK AND CABLING

length of cabling, m

$$l_c := 2$$

diameter of cabling, m

$$d_c := 0.006$$

frontal area of cabling, m²

$$A_c := l_c \cdot d_c = 0.012$$

diameter of peek end cap, m

$$d_{\text{pc}} := .025$$

number of peek end caps

$$N_{\text{pc}} := 4$$

total area of scattering surfaces, m²

$$A_{\text{tpc}} := A_c + N_{\text{pc}} \cdot \frac{\pi}{4} \cdot d_{\text{pc}}^2$$

$$A_{\text{tpc}} = 0.014$$

frontal area of ACB, m²

$$A_{\text{acb}} := 0.7$$

Incident Power, W

PEEK AND CABLING, W

$$P_{ipc} := P_a \cdot PF_{acbbox} \cdot \frac{A_{tpc}}{A_{acb}} \cdot \alpha_L = 0.036$$

$$PF_{acbcable} := PF_{acbbox} \cdot \frac{A_{tpc}}{A_{acb}}$$

$$PF_{acbcable} = 4.388 \times 10^{-3}$$

Power Scattered into IFO Mode, W

PEEK AND CABLING, W

$$P_{pcifo} := \sqrt{4} \cdot P_{ipc} \cdot \left(\frac{\lambda^2}{L_{cable}^2} \cdot BRDF_{wall} \cdot \alpha_L \cdot \frac{|\cos(\theta_{cable})|}{\pi} \right)$$

$$P_{pcifo} = 6.463 \times 10^{-20}$$

TOTAL ACB BACK, W

$$P_{wacbbbackifo} := \left(P_{acbp1ifo}^2 + P_{acbp2ifo}^2 + P_{acbp3ifo}^2 + P_{acbp4ifo}^2 + P_{acbp5ifo}^2 \right)^{0.5}$$

$$P_{wacbbbackifo} = 1.278 \times 10^{-18}$$

TOTAL ACB BACK AND BOX, W

$$P_{wacbboxifo} := \left(P_{wacbbbackifo}^2 + P_{wabtopifo}^2 + P_{wabbotifo}^2 + P_{wabsrifo}^2 + P_{wabslifo}^2 \right)^{0.5}$$

$$P_{wacbboxifo} = 1.758 \times 10^{-18}$$

TOTAL BSC Walls, W

$$P_{\text{bscifo}} := \left(P_{\text{bscbottomifo}}^2 + P_{\text{bscfrontifo}}^2 + P_{\text{bscbackifo}}^2 \right)^{0.5}$$

$$P_{\text{bscifo}} = 3.43 \times 10^{-20}$$

DISPLACEMENT NOISE @ 100 Hz, m/rtHz

$$\theta_t := 0 \quad x_s := 1$$

Displacement Noise Requirement @ 100 Hz, m/rt Hz

$$D_{\text{req}} = 1 \times 10^{-21}$$

$$P_{\text{sifo}} := 1$$

Amplitude spectral density of sine phase fluctuations of the injected field

$$S := \sqrt{8 \cdot \pi^2 \cdot \frac{x_s^2}{\lambda^2}}$$

displacement noise according to Flanagan-Thorne

$$DN_{\text{s_thorne}} := \left(\frac{P_{\text{sifo}}}{P_a} \right)^{0.5} \cdot \frac{\lambda}{4 \cdot \pi \cdot L} \cdot S \cdot L$$

displacement noise using Smith_Yamamoto formalism

$$DN_{\text{s_smith}} := TF_{\text{itmhr}} \cdot \left(\frac{P_{\text{sifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot \frac{2 \cdot k \cdot x_s}{\sqrt{2}}$$

where the factor 1/rt2 was added to correct for the slow phase motion that is below the gravity wave band

The two different approaches give results within < 5%

TOTAL ACB BACK AND
 BOX

$$S_{ACB} := \sqrt{8 \cdot \pi^2 \cdot \frac{x_{ACB}^2}{\lambda^2}}$$

$$DN_{wacbboxifo_thorne} := \left(\frac{P_{wacbboxifo}}{P_a} \right)^{0.5} \cdot \frac{\lambda}{4 \cdot \pi \cdot L} \cdot S_{ACB} \cdot L$$

$$DN_{wacbboxifo_thorne} = 1.04 \times 10^{-24}$$

$$DN_{wacbboxifo_smith} := TF_{itmhr} \cdot \left(\frac{P_{wacbboxifo}}{P_{psl}} \right)^{0.5} \cdot x_{ACB} \cdot 2 \cdot \frac{k}{\sqrt{2}}$$

$$DN_{wacbboxifo_smith} = 1.089 \times 10^{-24}$$

$$\frac{DN_{wacbboxifo_smith}}{DN_{wacbboxifo_thorne}} = 1.047$$

SUS

$$DN_{sus} := TF_{itmhr} \cdot \left(\frac{P_{SUSifo}}{P_{psl}} \right)^{0.5} \cdot x_{ISI} \cdot 2 \cdot \frac{k}{\sqrt{2}}$$

$$DN_{sus} = 2.549 \times 10^{-26}$$

TOTAL BSC Walls

$$DN_{bsc} := TF_{itmhr} \cdot \left(\frac{P_{bscifo}}{P_{psl}} \right)^{0.5} \cdot x_{manifold} \cdot 2 \cdot \frac{k}{\sqrt{2}}$$

$$DN_{bsc} = 1.217 \times 10^{-23}$$

spool 7A2

$$DN_{7A2} := TF_{itmhr} \cdot \left(\frac{P_{7A2ifo}}{P_{psl}} \right)^{0.5} \cdot x_{manifold} \cdot 2 \cdot \frac{k}{\sqrt{2}}$$

$$DN_{7A2} = 2.354 \times 10^{-24}$$

PCal structure

$$DN_{PCal} := TF_{itmhr} \cdot \left(\frac{P_{PCalifo}}{P_{psl}} \right)^{0.5} \cdot x_{manifold} \cdot 2 \cdot \frac{k}{\sqrt{2}}$$

$$DN_{PCal} = 1.116 \times 10^{-23}$$

wabsr + PF_{wabsl}

$$+ P_{\text{acbp6ifo}}^2 + P_{\text{acbp7ifo}}^2 + P_{\text{pcifo}}^2)^{0.5}$$

H:\ADLIGO\SLC\wide-angle baffle
ETM\T1300403_ETM_wide-
angle_scatter_AC_ZEMAX.xmcd