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| <b>Alignment sensing control<br/>signals of DRMI</b> |                  |            |
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## 1 Introduction

This document shows the alignment signal matrix for dual-recycling Michelson Interferometer (DRMI) for Advanced LIGO (aLIGO) Livingston corner Michelson commissioning. The calculations are done by the simulation software Finesse. All the scripts can be found MIT CVS `iscmodeling/Finesse/L1/ASC`.

There are several wave front sensors (WFS) available for the corner Michelson commissioning, as listed in Table. 1. There are four sets of WFS; in-vacuum or in-air AS path and in-vacuum or in-air REFL path, and there is a set of DC QPDs in POP path. The path including Gouy phase telescopes are shown in Fig. 1. Each path has WFS<sub>A</sub> and WFS<sub>B</sub> which are 90 ° separated in the accumulated Gouy phase. In the simulation, any fraction of the pick-off optics are taken out, except there is a 50 % pick-off beamsplitter to send the REFL beam to the in-vac or in-air REFL sensors. Table. 2 shows the DC power at each detection port, when the input beam power is 2 W.

The configuration of the corner Michelson interferometer in the simulation is DRMI with carrier fields locked both on PRC and SRC. Note that the DRMI model in the simulation has astigmatisms due to the foldings of PRC and SRC.

## 2 In-vacuum AS path

The Gouy phase telescope design and the beam parameters for in-vacuum (in-vac) AS path are shown in the left panel of Fig. 1 and in [1]. After transmitting SRM, the laser field passes through the tip-tilt M1 ( $R_c = 4.6$  m) and M2 ( $R_c = 1.7$  m), a flat steering beamsplitter M3, and a lens L101 ( $f = 0.334$  m). In the simulation, the two tip-tilt mirrors (M1 and M2)

| Path                   | Mode             | Location |
|------------------------|------------------|----------|
| In-vacuum AS           | Science mode     | HAM6     |
| In-vacuum REFL         | Science mode     | HAM1     |
| In-air AS              | Acquisition mode | ISCT6    |
| In-air REFL            | Acquisition mode | ISCT1    |
| In-vacuum POP (DC QPD) | Science mode     | HAM2     |

Table 1: WFS path list for the corner part of the interferometer. Some of them might not be used for the DRMI commissioning time. Each WFS path has WFS A and WFS B which are  $90^\circ$  separated in the accumulated Gouy phase.

| Path                   | Power             |
|------------------------|-------------------|
| In-vacuum AS           | $3.1 \mu\text{W}$ |
| In-vacuum REFL         | $0.057 \text{ W}$ |
| In-air AS              | $3.1 \mu\text{W}$ |
| In-air REFL            | $0.057 \text{ W}$ |
| In-vacuum POP (DC QPD) | $0.013 \text{ W}$ |

Table 2: DC power at each detection port, in the simulation. No fraction of the pick-off optics are considered, except there is a 50 % pick-off beamsplitter to send the REFL beam to the in-vac or in-air REFL sensors.

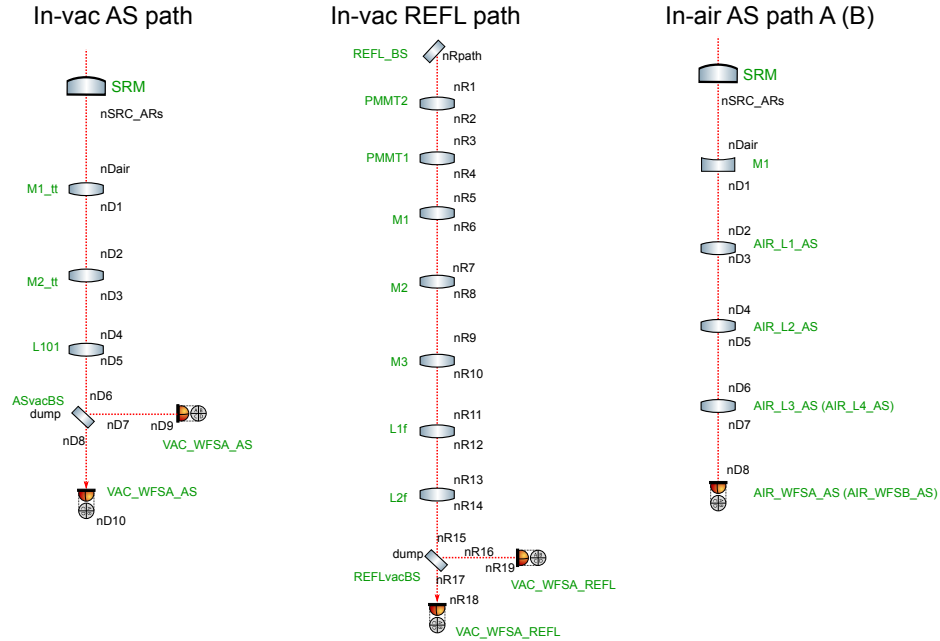


Figure 1: In-vacuum AS, In-vacuum REFL, In-air AS path. Node names used in the simulation are shown as well.

| Label | z [m] | beam radius [mm] (x, y) | Gouy phase from SRM [deg] (x,y) |
|-------|-------|-------------------------|---------------------------------|
| SRM   | 0     | (2.00, 2.12)            | (0, 0)                          |
| WFSA  | 6.46  | (0.32, 0.31)            | (242, 239)                      |
| WFSB  | 6.743 | (0.301, 0.309)          | (328, 331)                      |

Table 3: Beam size and accumulated Gouy phases in in-vac AS path obtained by the simulation.

are approximated as lenses with the focal lengths of the half radius of curvature, and tip-tilt M3 is abbreviated so that we don't take into account any additional astigmatism due to the incident angle of the telescopes, and also the pick-off factors at the WFS path.

The obtained beam parameters are listed in Table. 3, showing a good agreement with the design values in [1].

The calculated ASC matrices in in-vac AS are shown from Table. 4 to Table. 7. They are shown in [W/rad], and any pick-offs at the detection port is taken out, i.e, WFS senses all the power at AS port. In this detection port, because  $f_1$  sideband does not leak to the AS port, signals are obtained only by  $f_2$  demodulation. The strongest ITM and BS signals at in-vac AS port are plotted in Fig. ?? as a function of the accumulated Gouy phase (i.e., the WFS position).

| WFSA, Demod by 36 MHz [W/rad] |           |          |
|-------------------------------|-----------|----------|
|                               | yaw       | pitch    |
| ITMy                          | -0.811    | -0.839   |
| ITMx                          | 0.785     | -0.818   |
| BS                            | -0.760    | 1.13     |
| PRM                           | -0.000935 | 0.000941 |
| PR2                           | 0.00307   | -0.00303 |
| PR3                           | 0.0267    | 0.0263   |
| SRM                           | -0.000759 | 0.000646 |
| SR2                           | -0.00927  | -0.00837 |
| SR3                           | -0.0607   | 0.0548   |

| WFSA, Demod by 45 MHz [W/rad] |          |           |
|-------------------------------|----------|-----------|
|                               | yaw      | pitch     |
| ITMx                          | 2260     | -2140     |
| ITMy                          | -2260    | -2140     |
| BS                            | -2190    | 2980      |
| PRM                           | -0.0301  | 0.0263    |
| PR2                           | 0.151    | -0.132    |
| PR3                           | 1.31     | 1.14      |
| SRM                           | 0.000408 | -0.000403 |
| SR2                           | 0.00307  | 0.00303   |
| SR3                           | 0.0205   | -0.0201   |

Table 4: In-vacuum AS WFSA, demodulated by 36 MHz. Demodulation phases are optimized so that each signal is maximum. Table 5: In-vacuum AS WFSA, demodulated by 45 MHz. Demodulation phases are optimized so that each signal is maximum.

### 3 In-vacuum REFL path

The Gouy phase telescope design and the beam parameters for in-vacuum REFL path are shown in the middle panel of Fig. 1. There are seven telescopes, pre-mode-matching telescope 1 (PMMT1,  $R_c = -6.24$  m), PMMT2 ( $R_c = 12.8$  m), tip-tilt M1 ( $R_c = 1.7$  m), M2 ( $R_c = -0.6$  m), M3 ( $R_c = 1.7$ m), and two lenses, L1f ( $f = 0.333$  m) and L2f ( $f = -0.167$  m). Please

| WFSB, Demod by 36 MHz [W/rad] |          |           |
|-------------------------------|----------|-----------|
|                               | yaw      | pitch     |
| ITMy                          | 0.578    | 0.626     |
| ITMx                          | -0.600   | 0.645     |
| BS                            | 0.554    | -0.860    |
| PRM                           | 0.000972 | -0.000968 |
| PR2                           | -0.00495 | 0.00489   |
| PR3                           | -0.0430  | -0.0426   |
| SRM                           | 0.000631 | -0.000559 |
| SR2                           | 0.00418  | 0.00374   |
| SR3                           | 0.0275   | -0.0245   |

| WFSB, Demod by 45 MHz [W/rad] |         |           |
|-------------------------------|---------|-----------|
|                               | yaw     | pitch     |
| ITMx                          | 2580    | -2270     |
| ITMy                          | -2580   | -2260     |
| BS                            | -2500   | 3160      |
| PRM                           | -0.0366 | 0.0284    |
| PR2                           | 0.191   | -0.148    |
| PR3                           | 1.66    | 1.29      |
| SRM                           | 0.00115 | -0.000831 |
| SR2                           | 0.00864 | 0.00625   |
| SR3                           | 0.0560  | -0.0405   |

Table 6: In-vacuum AS WFSB, demodulated by 36 MHz. Table 7: In-vacuum AS WFSB, demodulated by 45 MHz.

| Label        | z [m] | beam radius [mm] (x, y) | Gouy phase from PRM [deg] (x,y) |
|--------------|-------|-------------------------|---------------------------------|
| Telescope M1 | 0     | (2.01, 2.04)            | (26.1, 24.8)                    |
| WFSA         | 3.26  | (0.330, 0.331 )         | (223, 221)                      |
| WFSB         | 3.63  | (0.378, 0.378 )         | (314, 315)                      |

Table 8: Beam parameters in in-vac REFL path obtained by the simulation.

see [2] for the spacial parameters. Similarly to the in-vac AS path case, all the telescopes are included as lenses in the simulation. The obtained beam size and the accumulated Gouy phase are listed in Table. 8.

The calculated ASC matrices in in-vac REFL are shown from Table. 9 to Table. 12. They are shown in [W/rad], and any pick-offs at the detection port is taken out, i.e, WFS senses all the power at REFL port. In this detection port, PR3 misalignment signals are the strongest of all the signals. The second strongest signals are the ITM and BS signals.

## 4 In-air REFL

There is the in-air REFL path on ISCT1. The detailed parameters are to be determined. The following matrices are example using Kiwamu's solution (C). The estimated  $q$  parameter at the edge of ISCT1 is  $q = 1.13 + 13i$  ( $z = 0$ ). There are two lenses, f0\_airREFL ( $f = 0.6785$  m at  $z = 0.677$  m) and f1\_airREFL ( $f = -0.5727$  m at  $z = 1.0323$  m). The beam waist after these lenses are about  $250 \mu\text{m}$ . The ASC matrices at in-air REFL port are shown in Table. 13 to Table. 16

| WFSA, Demod by 9 MHz [W/rad] |           |          |
|------------------------------|-----------|----------|
|                              | yaw       | pitch    |
| ITM <sub>x</sub>             | 11400     | -11000   |
| ITM <sub>y</sub>             | 11400     | 10900    |
| BS                           | 11300     | -14500   |
| PRM                          | -59.6     | 58.2     |
| PR2                          | 3950      | -3810    |
| PR3                          | 26100     | 26400    |
| SRM                          | -0.000764 | 0.000774 |
| SR2                          | -0.00575  | -0.00583 |
| SR3                          | -0.0377   | 0.0382   |

Table 9: In-vacuum REFL WFSA, demodulated by 9 MHz.

| WFSA, Demod by 45 MHz [W/rad] |        |         |
|-------------------------------|--------|---------|
|                               | yaw    | pitch   |
| ITM <sub>x</sub>              | 11500  | -11000  |
| ITM <sub>y</sub>              | 11400  | 11000   |
| BS                            | 11300  | -14500  |
| PRM                           | -59.6  | 58.2    |
| PR2                           | 3950   | -3810   |
| PR3                           | 26100  | 26400   |
| SRM                           | 0.0638 | -0.0557 |
| SR2                           | 0.480  | 0.419   |
| SR3                           | 3.03   | -2.67   |

Table 10: In-vacuum REFL WFSA, demodulated by 45 MHz.

| WFSB, Demod by 9 MHz [W/rad] |           |          |
|------------------------------|-----------|----------|
|                              | yaw       | pitch    |
| ITM <sub>x</sub>             | 13900     | -12800   |
| ITM <sub>y</sub>             | 13900     | 12800    |
| BS                           | 13400     | -18200   |
| PRM                          | -1280     | 1200     |
| PR2                          | 4210      | -4030    |
| PR3                          | 41700     | 39400    |
| SRM                          | -0.000803 | 0.000790 |
| SR2                          | -0.00604  | -0.00594 |
| SR3                          | -0.0395   | 0.0388   |

Table 11: In-vacuum REFL WFSB, demodulated by 9 MHz.

| WFSB, Demod by 45 MHz [W/rad] |        |         |
|-------------------------------|--------|---------|
|                               | yaw    | pitch   |
| ITM <sub>x</sub>              | 13900  | -12800  |
| ITM <sub>y</sub>              | 13900  | 12800   |
| BS                            | 13400  | -18200  |
| PRM                           | -1280  | 1200    |
| PR2                           | 4210   | -4040   |
| PR3                           | 41700  | 39400   |
| SRM                           | 0.0463 | -0.0402 |
| SR2                           | 0.348  | 0.303   |
| SR3                           | 2.30   | -2.00   |

Table 12: In-vacuum REFL WFSB, demodulated by 45 MHz.

| WFSA, Demod by 9 MHz [W/rad] |          |           |
|------------------------------|----------|-----------|
|                              | yaw      | pitch     |
| ITM <sub>x</sub>             | -16700   | 15300     |
| ITM <sub>y</sub>             | -16700   | -15300    |
| BS                           | -16200   | 21300     |
| PRM                          | 540      | -500      |
| PR2                          | -5270    | 4970      |
| PR3                          | -46000   | -43500    |
| SRM                          | 0.000957 | -0.000936 |
| SR2                          | 0.00720  | 0.00704   |
| SR3                          | 0.04702  | -0.0460   |

Table 13: In-air REFL WFSA, demodulated by 9 MHz.

| WFSA, Demod by 45 MHz [W/rad] |         |        |
|-------------------------------|---------|--------|
|                               | yaw     | pitch  |
| ITM <sub>x</sub>              | -16700  | 15300  |
| ITM <sub>y</sub>              | -16700  | -15300 |
| BS                            | -16200  | 21300  |
| PRM                           | 540     | -500   |
| PR2                           | -5270   | 4970   |
| PR3                           | -46100  | -43500 |
| SRM                           | -0.0767 | 0.0655 |
| SR2                           | -0.577  | -0.493 |
| SR3                           | -3.77   | 3.22   |

Table 14: In-air REFL WFSA, demodulated by 45 MHz.

| WFSA, Demod by 9 MHz [W/rad] |          |           |
|------------------------------|----------|-----------|
|                              | yaw      | pitch     |
| ITMx                         | -7830    | 7400      |
| ITMy                         | -7820    | -7410     |
| BS                           | -7590    | 10300     |
| PRM                          | 1160     | -1120     |
| PR2                          | -2470    | 2410      |
| PR3                          | -21600   | -21100    |
| SRM                          | 0.000572 | -0.000581 |
| SR2                          | 0.00430  | 0.00437   |
| SR3                          | 0.0281   | -0.0286   |

Table 15: In-air REFL WFSB, demodulated by 9 MHz.

| WFSA, Demod by 45 MHz [W/rad] |         |        |
|-------------------------------|---------|--------|
|                               | yaw     | pitch  |
| ITMx                          | -7840   | 7420   |
| ITMy                          | -7820   | -7410  |
| BS                            | -7590   | 10300  |
| PRM                           | 1170    | -1120  |
| PR2                           | -2470   | 2410   |
| PR3                           | -21600  | -21100 |
| SRM                           | -0.0200 | 0.0176 |
| SR2                           | -0.150  | -0.133 |
| SR3                           | -0.983  | 0.867  |

Table 16: In-air REFL WFSB, demodulated by 45 MHz.

## 5 In-air AS

There will be in-air AS path on ISCT6. The two solutions of the beam parameters are summarized in [1]. Here, we used the first solution for the ASC matrix calculation, and its setup is shown in the right panel of Fig. 1. The beam transmits a curved mirror M1 (common as in-vacuum AS path), then two lenses AIR\_L1\_AS ( $f = 1.146\text{m}$ ), AIR\_L2\_AS ( $f = 0.556\text{m}$ ). Then there is a lens AIR\_L3\_AS ( $f = -0.0556\text{m}$ ) before in-air AS WFSA, and AIR\_L4\_AS ( $f = -0.111\text{m}$ ) before in-air WFSB.

Table. 17 and Table. 20 are the sensing matrix at in-air AS QPDs.

| WFSA, Demod by 36 MHz [W/rad] |           |          |
|-------------------------------|-----------|----------|
|                               | yaw       | pitch    |
| ITMy                          | -0.257    | -0.291   |
| ITMx                          | 0.248     | -0.283   |
| BS                            | -0.213    | 0.356    |
| PRM                           | -0.00109  | 0.00108  |
| PR2                           | 0.00538   | -0.00536 |
| PR3                           | 0.0468    | 0.046717 |
| SRM                           | -0.000940 | 0.000868 |
| SR2                           | -0.00831  | -0.00778 |
| SR3                           | -0.0545   | 0.051122 |

Table 17: In-air AS WFSA, demodulated by 36 MHz.

| WFSA, Demod by 45MHz [W/rad] |           |          |
|------------------------------|-----------|----------|
|                              | yaw       | pitch    |
| ITMy                         | 838       | 585      |
| ITMx                         | -838      | 586      |
| BS                           | 813       | -817     |
| PRM                          | 0.01524   | -0.0101  |
| PR2                          | -0.0865   | -0.0607  |
| PR3                          | -0.756    | 0.531    |
| SRM                          | -0.000710 | 0.000452 |
| SR2                          | -0.00534  | -0.00340 |
| SR3                          | -0.0343   | 0.0218   |

Table 18: In-air AS WFSA, demodulated by 45 MHz.

| WFSB, Demod by 36 MHz [W/rad] |           |           |
|-------------------------------|-----------|-----------|
|                               | yaw       | pitch     |
| ITMy                          | 0.949     | 0.956     |
| ITMx                          | -0.951    | 0.958     |
| BS                            | 0.907     | -1.31     |
| PRM                           | 0.000791  | -0.000829 |
| PR2                           | -0.00265  | 0.00280   |
| PR3                           | -0.0230   | -0.0242   |
| SRM                           | -6.25e-05 | 7.11e-05  |
| SR2                           | 0.00411   | 0.00416   |
| SR3                           | 0.0268    | -0.0271   |

Table 19: In-air AS WFSB, demodulated by 36 MHz.

| WFSB, Demod by 45MHz [W/rad] |         |           |
|------------------------------|---------|-----------|
|                              | yaw     | pitch     |
| ITMy                         | -3460   | -2990     |
| ITMx                         | 3470    | -2990     |
| BS                           | -3360   | 4170      |
| PRM                          | -0.0470 | 0.0366    |
| PR2                          | 0.239   | -0.186    |
| PR3                          | 2.08    | 1.61      |
| SRM                          | 0.00113 | -0.000837 |
| SR2                          | 0.00848 | 0.00630   |
| SR3                          | 0.0554  | -0.0412   |

Table 20: In-air AS WFSB, demodulated by 45 MHz.

## 6 POP DC QPD signal

There is a DC QPD in the POP path to monitor the beam pointing inside PRC [2]. After transmitting PR2, there are two lenses, POPL1 ( $f = 0.333$  m) and POPL2 ( $f = -0.556$  m). The ASC matrices at POP QPDs are shown in Table. 21 and 22. The POP signals will be used for the pointing control of the PRC and the signals will be fed back to the beam pointing actuators before PRM. Both POP1 and POP2 are most sensitive to PR3.

| QPD1 [W/rad] |                        |                        |
|--------------|------------------------|------------------------|
|              | yaw                    | pitch                  |
| ITMy         | -4770                  | -4180                  |
| ITMx         | -4770                  | 4190                   |
| BS           | -4630                  | 5820                   |
| PRM          | 378                    | -349                   |
| PR2          | -1510                  | 1360                   |
| PR3          | -13200                 | -11900                 |
| SRM          | $-7.44 \times 10^{-6}$ | $6.44 \times 10^{-6}$  |
| SR2          | $-5.60 \times 10^{-5}$ | $-4.85 \times 10^{-5}$ |
| SR3          | -0.000366              | 0.000317               |

Table 21: POP DC QPD1 signal.

| QPD2 [W/rad] |                        |                        |
|--------------|------------------------|------------------------|
|              | yaw                    | pitch                  |
| ITMy         | 5870                   | 5230                   |
| ITMx         | 5870                   | -5240                  |
| BS           | 5700                   | -7290                  |
| PRM          | -211                   | 179                    |
| PR2          | 1850                   | -1700                  |
| PR3          | 16200                  | 14900                  |
| SRM          | $-1.89 \times 10^{-6}$ | $1.15 \times 10^{-6}$  |
| SR2          | $-1.42 \times 10^{-5}$ | $-8.63 \times 10^{-6}$ |
| SR3          | $-9.29 \times 10^{-5}$ | $5.65 \times 10^{-5}$  |

Table 22: POP DC QPD2 signal.

## 7 Next steps

Our next step is to create the model in Optickle and to double check the calculation. Also, the signals of the beam pointing towards PRM should be calculated.

For the full interferometer, the strategy for the SRC alignment control should be considered. In our signal extraction scheme, the SRC misalignment signal is difficult to be extracted.



## References

- [1] LIGO-T1200410-v2, Lisa Barsotti
- [2] LIGO-T1000247-v3, Sam Waldman
- [3] Internal note by Kiwamu Izumi