

Compact object merger rates

Predictions

Constraints

(including short GRBs)

work in progress!

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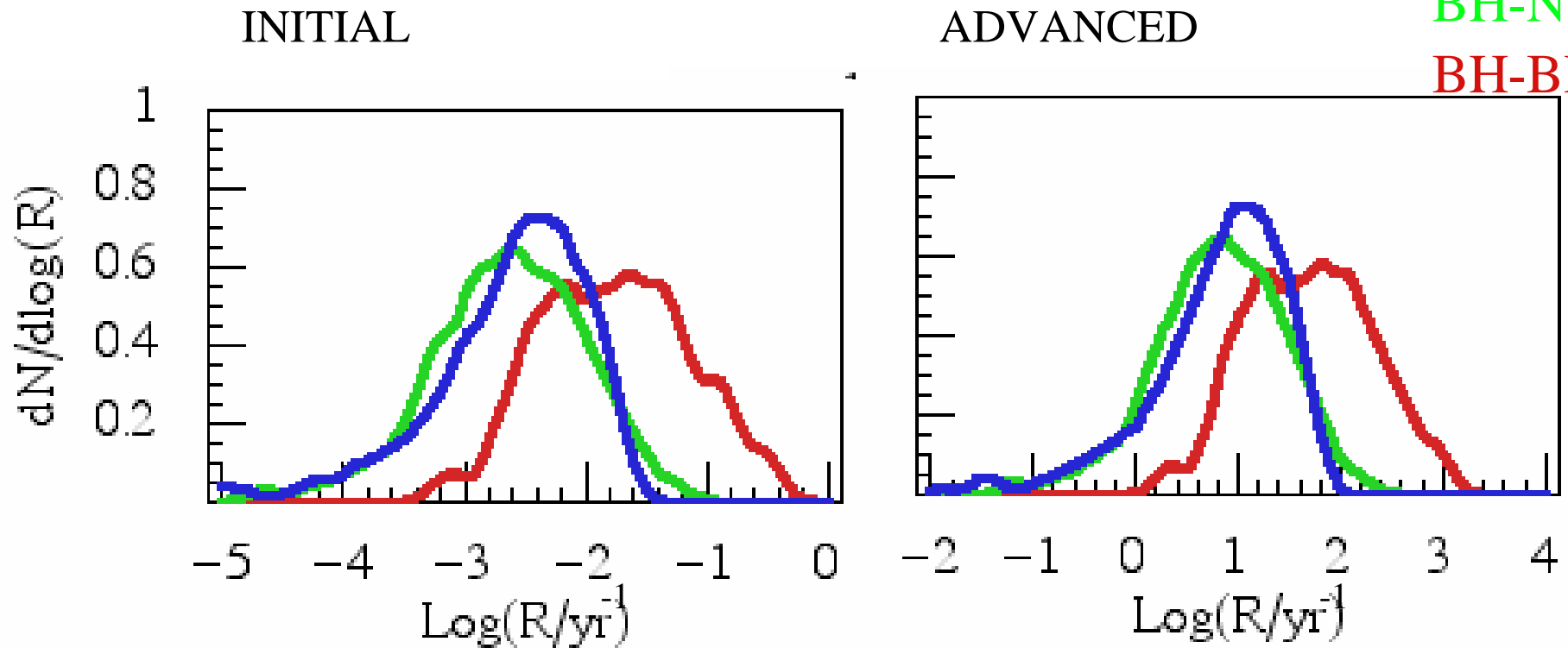
LSC, March 21, 2006

LIGO-G060157-00-Z

Results (2005)

- LIGO rates:

Key:
NS-NS
BH-NS
BH-BH



Details (2005) [H]

- LIGO rates:

+ spiral density

$$\rho_{gal} = 0.01 / \text{Mpc}^3$$

+ euclidean universe (no cosmology)

+ LIGO single-IFO range

$$d_{init} = 14 \text{Mpc} (M_c / 1.2 M_O)^{5/6}$$

$$d_{adv} = 191 \text{Mpc} (M_c / 1.2 M_O)^{5/6}$$

+ Chirp mass distrib (estimate):

$$\langle M_c^{15/6} \rangle = 111 M_O^{15/6} \text{ BH-BH (i.e. } M_{\text{BH}} < 10)$$

$$= 5.8 M_O^{15/6} \text{ BH-NS}$$

$$= 2 M_O^{15/6} \text{ NS-NS (i.e. } M_{\text{NS}} > 1.4)$$

$$R_{init} = 0.7 \times 10^2 R_{MW} \langle (M_c / M_O)^{15/6} \rangle$$

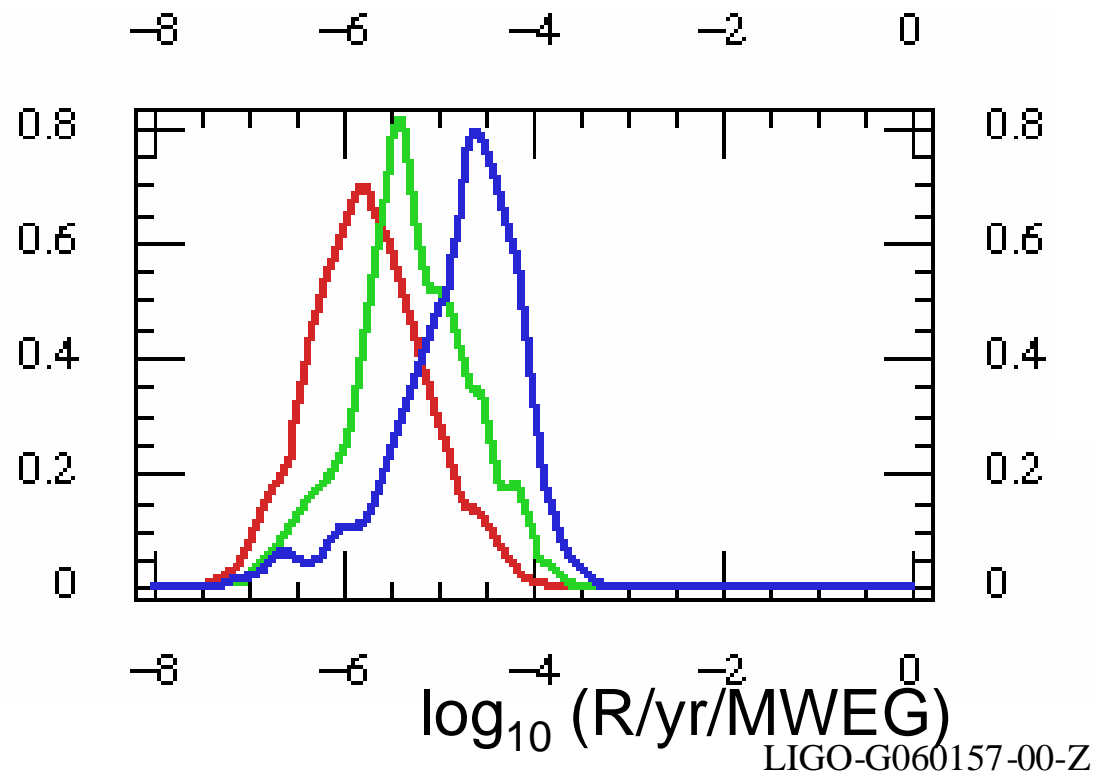
$$R_{adv} = 2 \times 10^5 R_{MW} \langle (M_c / M_O)^{15/6} \rangle$$

Method (2005)

- **Based on Milky Way** (well understood: history, population, ...)

___ + **density of spirals** $\rho_{gal} = 0.01 / \text{Mpc}^3$

- Rates/MW (now):



Key:

NS-NS

BH-NS

BH-BH

Uncertainties

Monte carlo over plausible
astrophysical assumptions

Method (2005)

- Other contributions?:

- Prompt mergers ($\ll 1400$ Myr \sim universe age)

PSR name	P_s (ms)	P_b (hr)	e	τ_{life} (Myr)
B1913+16	59.03	7.752	0.617	365
B1534+12	37.90	10.1	0.274	2700
J0737-3039A	22.70	2.45	0.088	185
J1756-2251	28.46	7.67	0.181	2.0

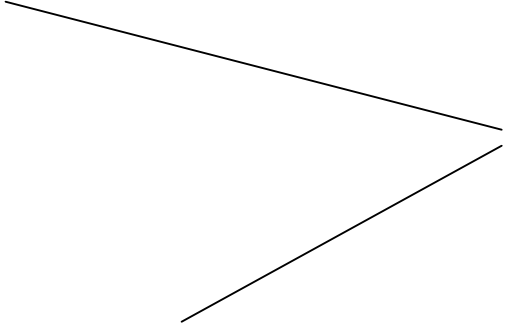
[C. Kim](#) (talk 2005)
[ROS et al](#) (2005)

- Spirals dominate local SFR / blue light

Reason why N_G used
(in inspiral analysis interpretation)

Key assumptions (2005)

- Steady star formation
- Prompt mergers dominate
- Spiral-like birth conditions (IMF)



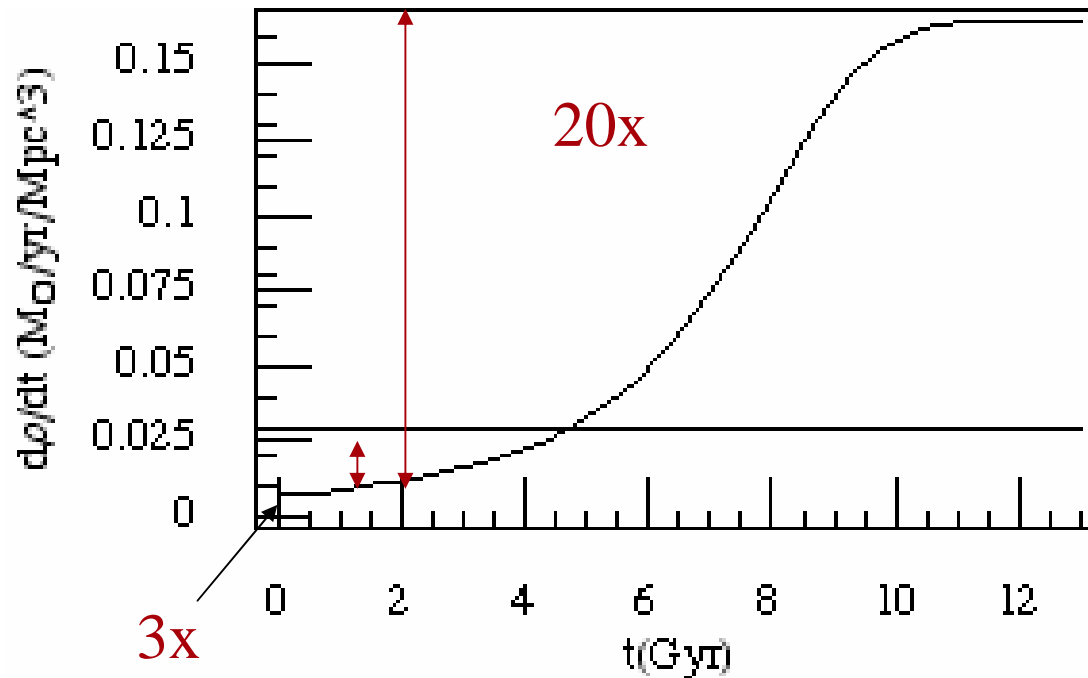
Extrapolation
Universe **all** like
Milky Way

Refinements

Star formation history:

- Previous estimate: $\rho_{gal} = 0.01 / \text{Mpc}^3$ $SFR_{mw} = 3 M_{\odot} \text{yr}^{-1}$

- Observed history:



- Estimate 3x too high (locally)

- Past $\sim 20x$ present

...are mergers

“prompt enough?”

Refinements

Delay time distribution :

- Delay time = merger time - birth time

Sample distribution

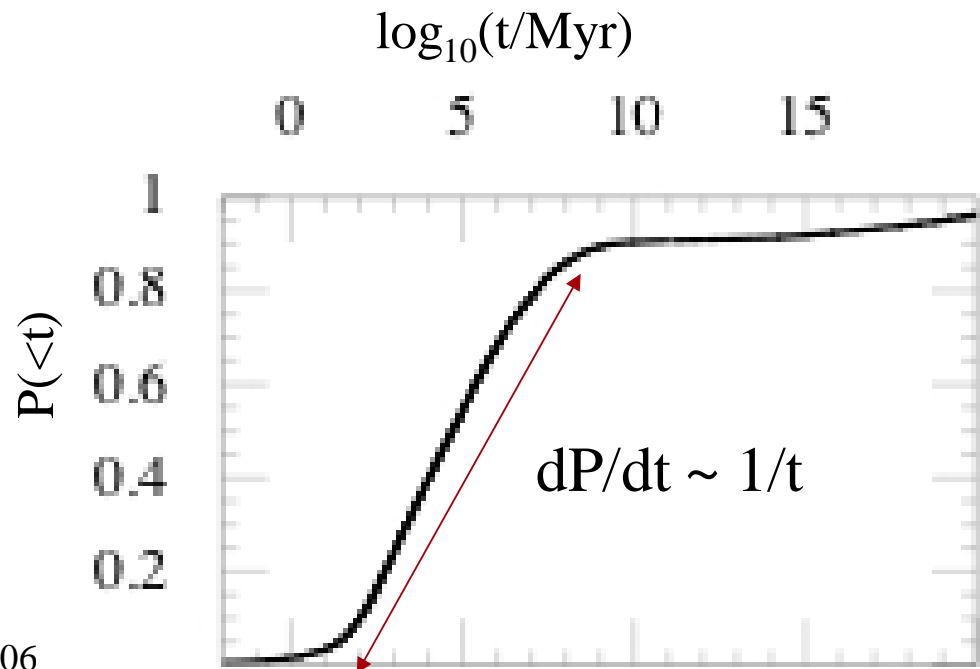
(model-dependent)

+ **1/t** works well

[long times]

... over a **specific range**

+ some prompt/instant



Refinements

Delay time distribution :

- Delay time = merger time - birth time

Sample distribution

(model-dependent)

+ **1/t** works well

[long times]

... over a **specific range**

+ some prompt/instant

Recent vs ancient contribution?

$$d\text{Rate} \sim (d\rho/dt) dt/t$$

$$\frac{d\text{Rate}(1\text{Gyr})}{d\text{Rate}(10\text{Gyr})} \sim \frac{\dot{\rho}(1\text{Gyr})}{\dot{\rho}(10\text{Gyr})} 10 \sim 1$$

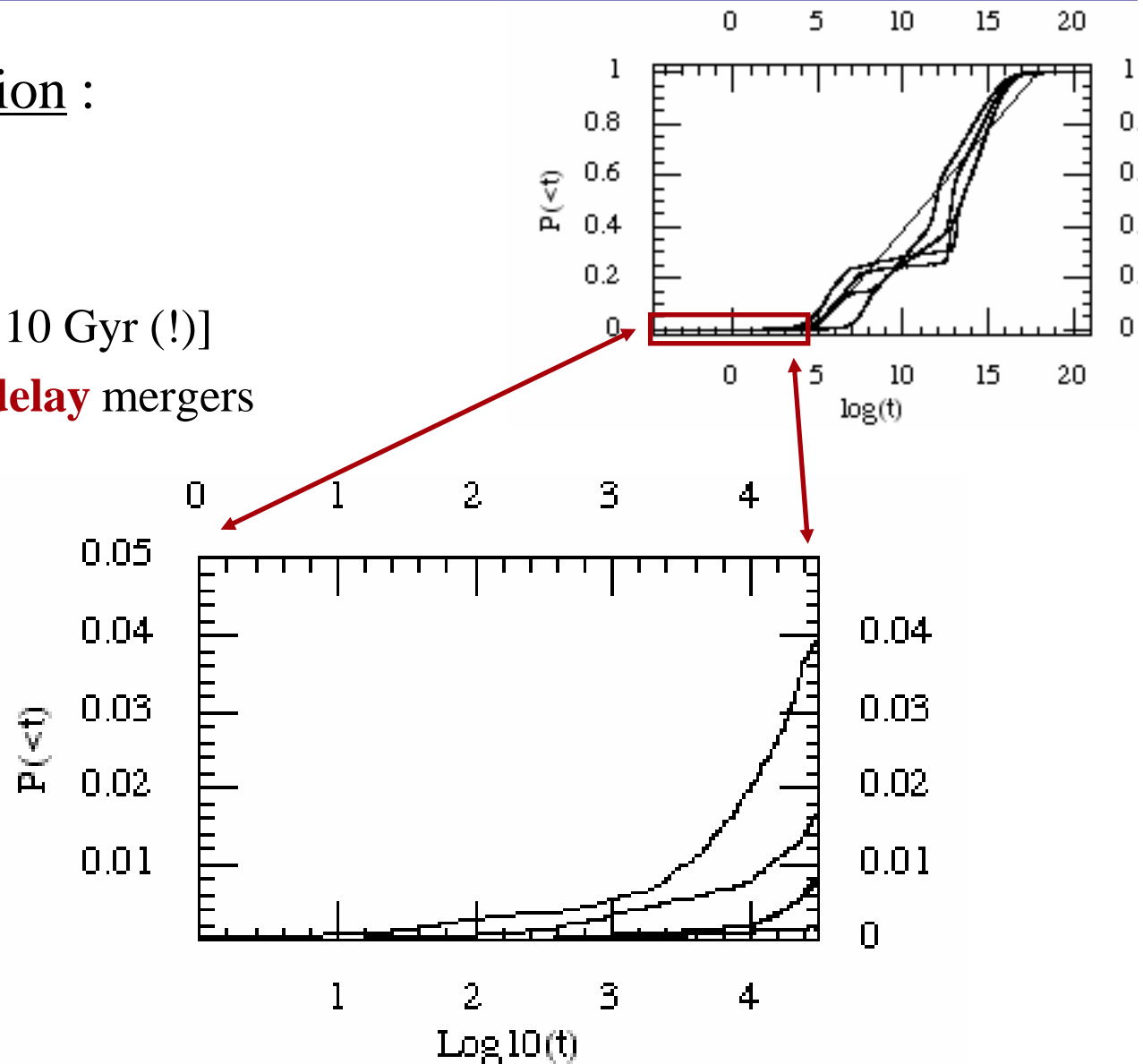
ancient star formation important...

What's changed? [H]

Delay time distribution :

.....**except**

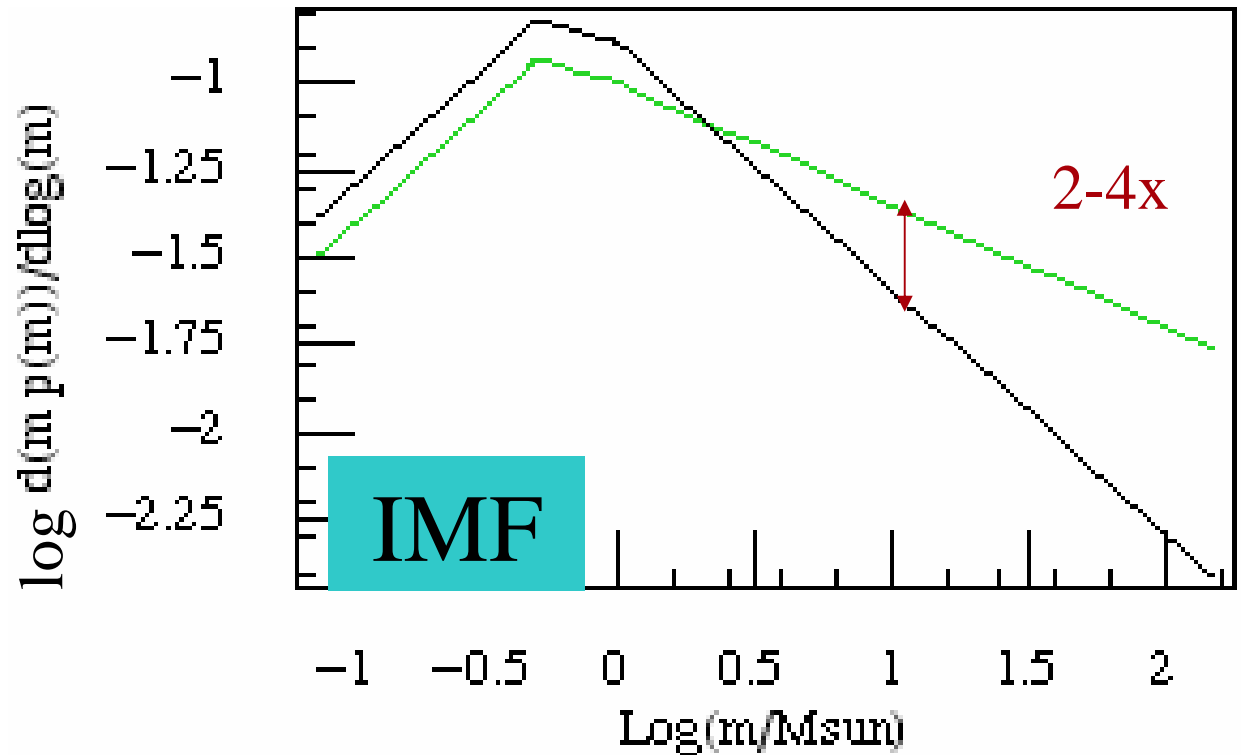
- BH-BH :
 - **1/t fails:** [$t_{\min} \sim 10$ Gyr (!)]
 - \sim requires **long-delay** mergers



Refinements

Heterogeneity

- Spirals
 - Young
 - Hard to make high M stars
- Ellipticals
 - Old
 - Easier to make high M stars



Ellipticals: **at least 2-4x** more high-mass progenitors

What's changed? [H] (*)

Heterogeneity: Details

- Elliptical/spiral census (now, evolving)
Census info
Panter et al 2004, [Read & Trentham 2005](#)
Fukugita, Hogan, Peebles [1998](#), 2004
[Bundy et al 2004](#) [low-z]
- Elliptical conditions (=old stars)
[Smith et al 2005](#),
[De Lucia et al 2006](#)
- Star formation histories
[Heavens 2004](#), s [De Lucia et al 2006](#)

Ingredient: Galaxy heterogeneity I [H]

Heterogeneity details: Census

Census info

Fukugita, Hogan, Peebles [1998](#), 2004

$$\Omega_{\text{spheroid stars}} = \left(0.00180^{+0.00121}_{-0.00085} \right) h^{-1},$$

$$\Omega_{\text{disk stars}} = \left(0.00060^{+0.00030}_{-0.00024} \right) h^{-1},$$

$$\Omega_{\text{stars in Irr}} = \left(0.000048^{+0.00033}_{-0.00026} \right) h^{-1},$$

Census info

[Read & Trentham 2005](#)

	Ω_b	Ω_*
E	0.00064	0.00064
S0	0.00073	0.00068
Sa+Sab	0.00036	0.00032
Sb+Sbc	0.00056	0.00040
Sc+Scd	0.00072	0.00047
Sd+Sdm+Sm	0.00037	0.00021
Irr+dIrr	0.00013	0.00007
dE	0.00002	0.00002
total	0.0035	0.0028

What's changed? [H](*)

Heterogeneity + SFR : Model A:

Key features:

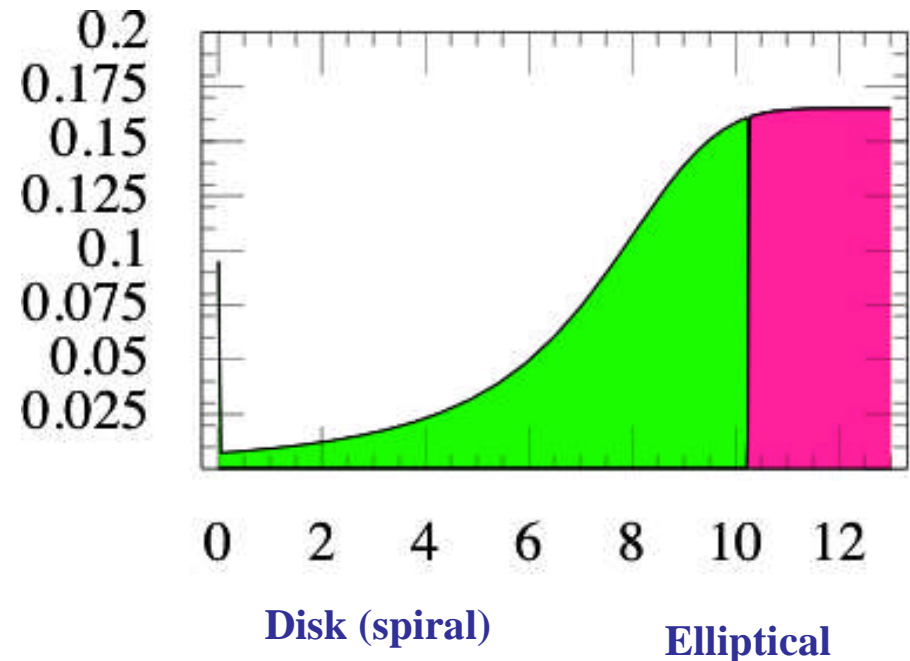
- More formation long ago
- Recently ($z < 2$) ~ ok;

early = ??

- Ellipticals all old

...but

lots of early spirals



Refinements

Summary (usually)

- Steady star formation
 - **Wrong**....early dominates
- Prompt mergers dominate
 - **Wrong**...long delays dominate
- Spiral-like birth conditions (IMF)
 - **Wrong**...ellipticals dominate

Scorecard: old vs young

IMF : up x 3

SFR : up x 10

Delay: down x 10

Net : up x ~ 3

Revised results?

Merger rates (/volume) versus redshift:

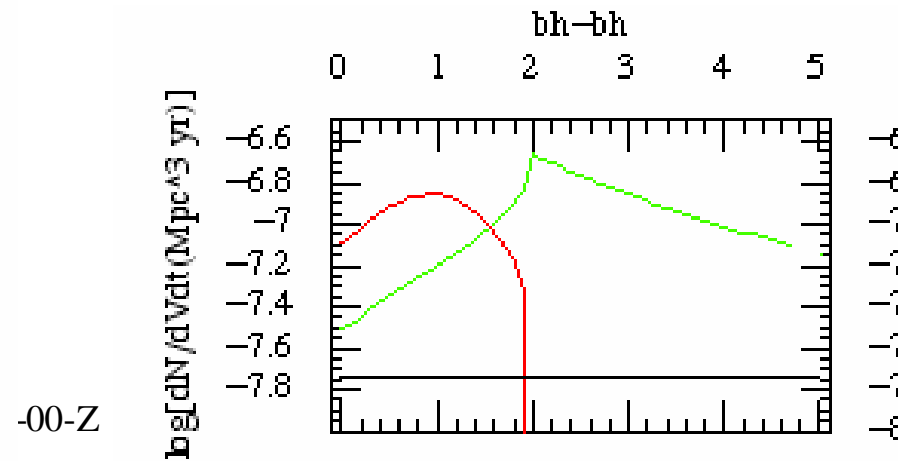
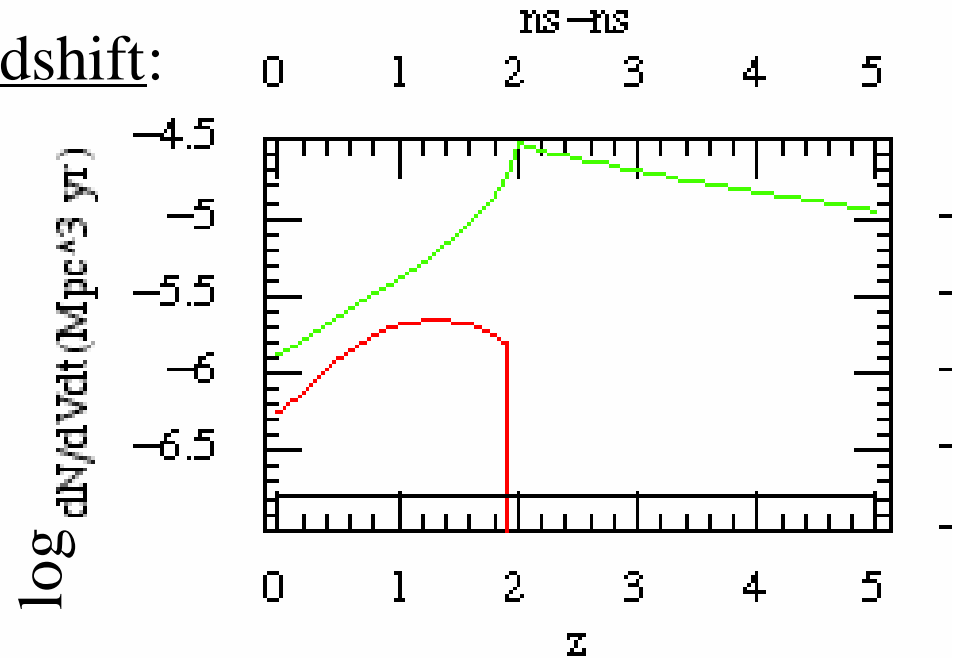
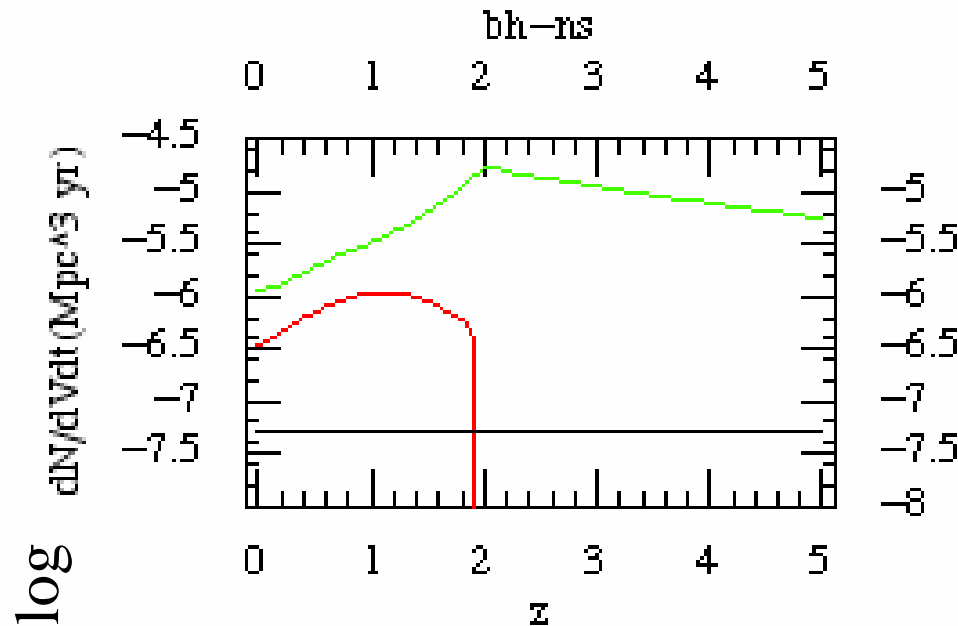
...sample result

Key

'Reference'

Spirals

Ellipticals

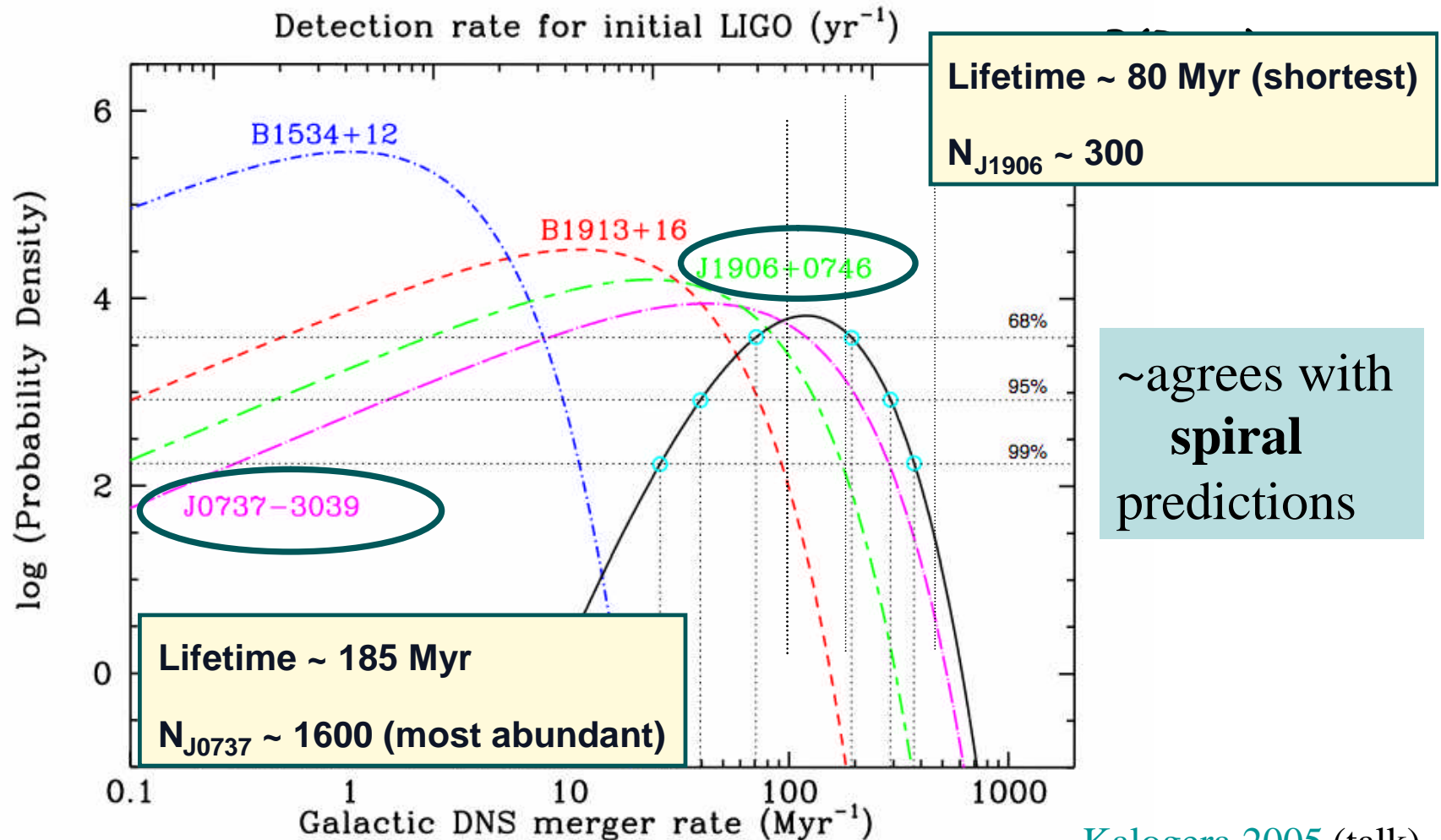


Matching observations? [H]

- Relative galaxy populations/histories (check)
- Milky way
 - Overall pulsar-like sources [check, mod beaming]
 - Overall active binaries [selection effects unknown?]
 - Distribution of NS-NS?
 - Merger rates [w/ tuning, mod beaming]
 - Ratio young:old [check]
 - Distribution of WD-NS ? [w/ tuning]
- Local universe
 - Supernova rates [**spiral-dominated**] [check]
- Distant universe
 - Short GRBs [~check; broad range]

Observations: MW NS-NS [H]

- Observed (MW) NS-NS population -> MW merger rate



Observations: MW NS-NS [H]

- **Observed (MW) population -> merger rate**

Method =

SELECTION EFFECTS (understood)

+ POPULATION MODEL

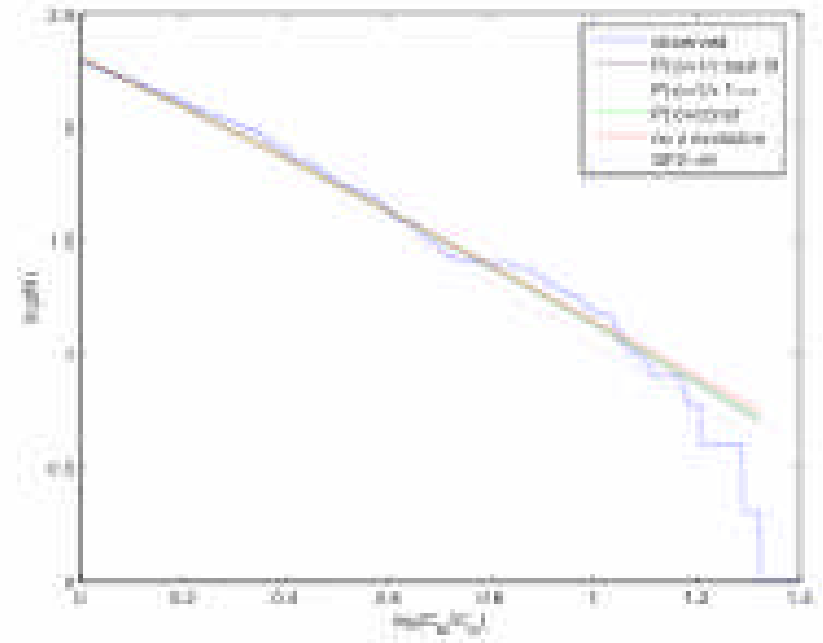
...including

- **Luminosity** function [allow for *faint unseen* sources]
...understood from **single** pulsars
- **Beaming correction**

Observations: Short GRBs

Review

- Many seen (gamma-ray)
[detection rate 1/(2-3 months)]
... many **missed** (too faint)
- Afterglows & associations
 - **Variety**, includes **OLD**
 - Offsets (!)
 - Weak afterglows [low-density]
...not SN
 - Beaming?



Merger model
(BH-NS, NS-NS)
consistent

Observations: Short GRBs [H]

Details: Known systems

Short GRB	Host galaxy	Redshift	Energy
050509b	Very old (E)	0.22 (~900 Mpc)	4.5×10^{48}
050709	Young (Sb/Sc)	0.16 (~660 Mpc)	6.9×10^{49}
050724	Old (E)	0.26 (~1 Gpc)	4×10^{50}
050813	Very old (cluster)	1.8 / 0.72[?]	
051221	young	0.547	9×10^{50}

[E. Berger](#) (review article)

Gehrels (KITP talk) [\[link\]](#)

Nakar (LIGO talk) [\[link\]](#)

...suggests rate $\sim 1/(2 \text{ month})(\text{Gpc})^3$

Observations: Short GRBs [H]

Details: Opening angles

...still **very sketchy/tentative** measurements

- Jet opening angles

$$\theta \sim 10\text{-}20^\circ$$

...**suggests** rate ~ 50 x higher
 $\sim 50 / (\text{Gpc})^3/\text{year}$

QuickTime™ and a
TIFF (LZW) decompressor
are needed to see this picture.

Observations: Short GRBs

- ‘Experimental’ rates:
 - Conservative : (~what is **seen**)
 $R_{\text{GRB,low}} \sim 3 \times 10^{-8} / \text{Mpc}^3 / \text{yr}$
= ~ expected [spirals alone]
 - Optimistic?: (correct for **faint** and **off-axis**)
 $R_{\text{GRB,high}} \sim R_{\text{GRB,low}} (L_{\text{cut}} / L_{\text{min}}) f_b$
 $\sim R_{\text{GRB,low}} (\sim 100) \times (\sim 3)$
 $\sim 1 \times 10^{-5} / \text{Mpc}^3 / \text{yr}$

would be **almost** visible by initial LIGO
...runs into problems (run out of SN)

Applying experimental constraints I:

$N(<P)$ [H]

- Matching:

SFR history

+ (homogeneous)

+ **delay time distribution**

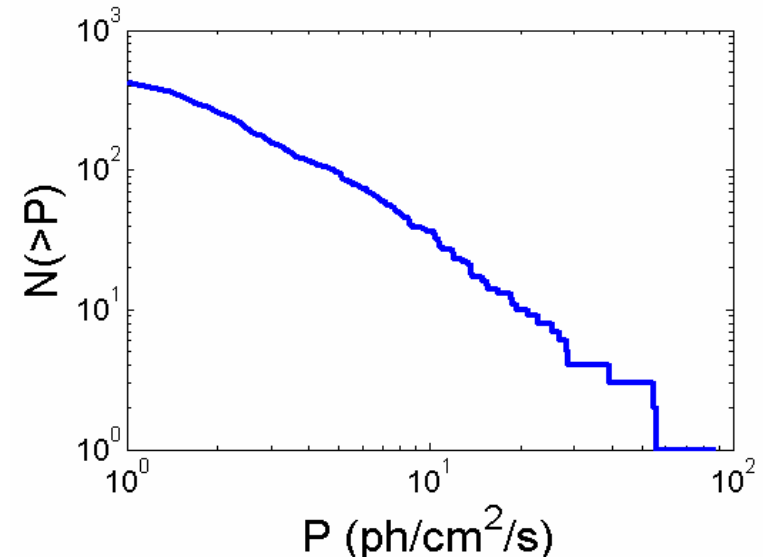
(try a few)

+ **intrinsic LF**

(try a few)

= **guess**

FIT TO OBSERVED



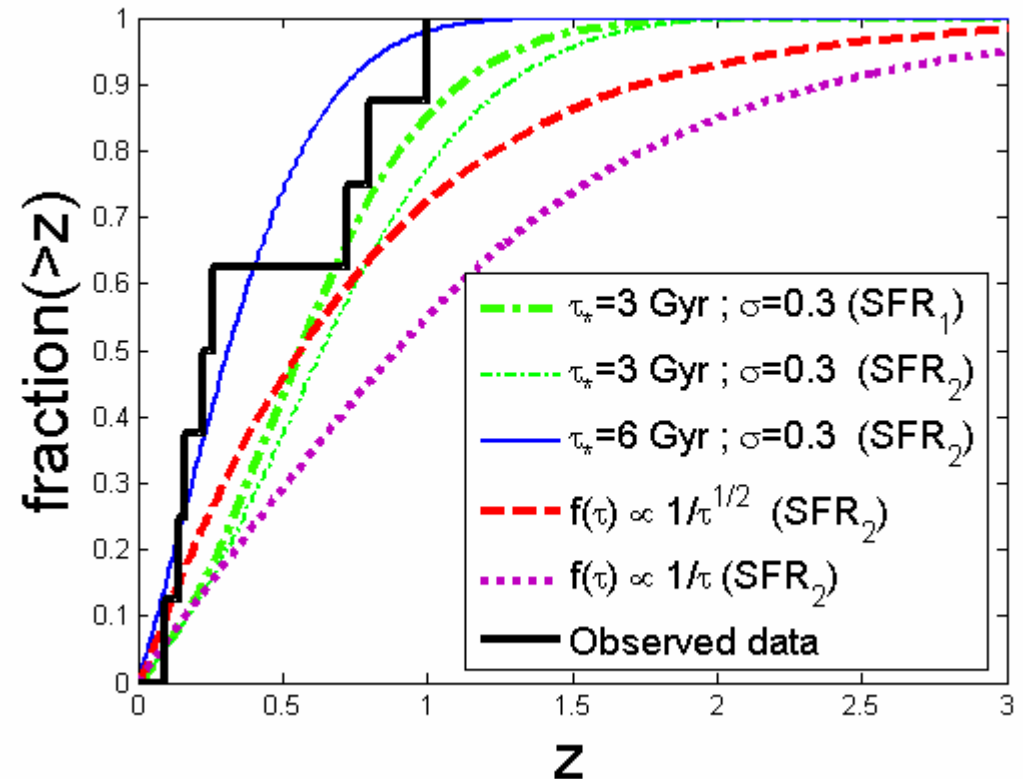
Guetta and Piran 2005/6
Ando 2004

LIGO-G060157-00-Z

Results:
rate $\sim O(0.1-10 / \text{Gpc}^3/\text{yr})$
[depends on model]

Applying experimental constraints III: N(<P) + observed 'z'

- Method:
 - Previous
 - + match z distrib
 - + limit faint end
[Tanvir et al 2005]
- Odd claims:
 - 1/t excluded (!?)
[what is tmin?]
 - 6 Gyr lifetime preferred?



Results

- (i) No beaming: 10/Gpc³/yr
- (ii) Beaming, faint: 10⁵/Gpc³/yr
(~x30) (~ 3x10³)

Nakar et al 2005