



# Electro Optic Modulators and Modulation for Enhanced LIGO and beyond



**"Colliding Black Holes", Werner Berger, AEI, CCT, LSU**

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**for the LIGO Scientific Collaboration**

A visualization of gravitational waves, showing two black holes in the process of colliding. The image features a central point of high energy, with concentric, colorful rings (red, yellow, green, blue) radiating outwards, set against a dark blue background.

Coherent Optical Technologies and Applications (COTA), Boston, MA

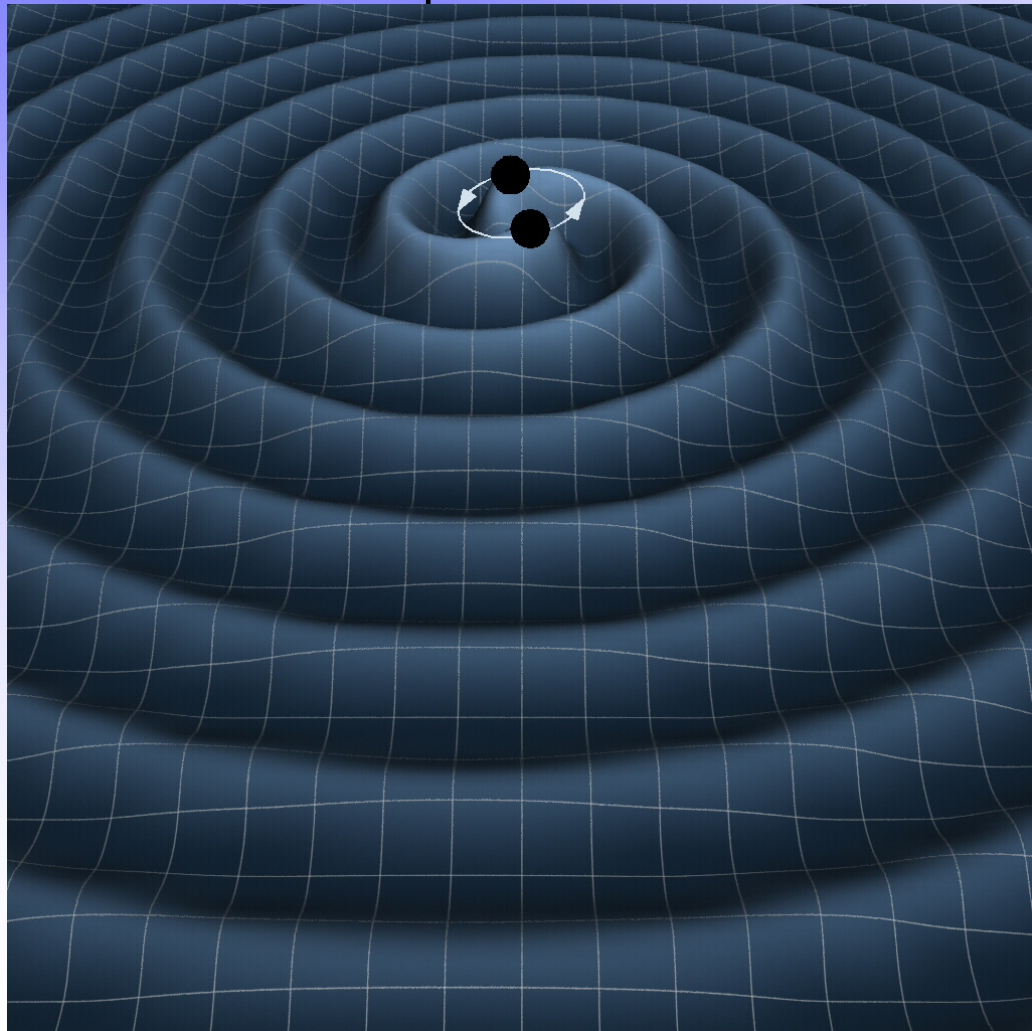


Support: NSF



- Gravitational waves
  - What are they
  - How to measure
- LIGO - the instrument
- Upgrades:
  - Now: Enhanced LIGO
  - Soon: Advanced LIGO
- Phase modulators for LIGO
- Advanced modulation schemes

Predicted by Einstein in 1916, GWs are propagating fluctuations in the curvature of space-time:



- Perturbations of geometry can be expressed as fractional distortion of proper distances:

$$h = \frac{\Delta x}{|x|}$$

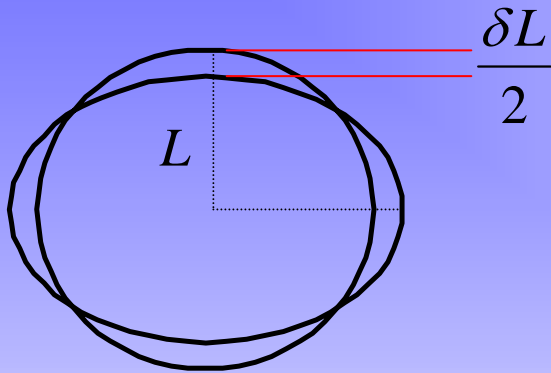
- Calculate emissions from accelerating non-spherical mass distributions:

$$\Rightarrow h_{\mu\nu}(\omega, t) = \frac{2G}{rc^4} \mathbb{T}_{\mu\nu}(\omega, t)$$

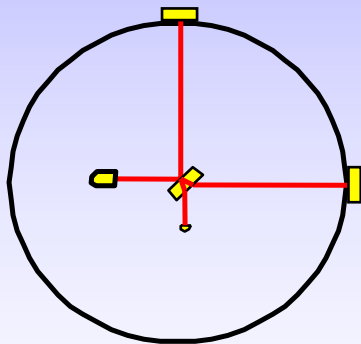
$$\Rightarrow h \approx \frac{4\pi^2 GMR^2 f_{orb}^2}{c^4 r}$$

- Estimated length change for a binary neutron star system (10Mpc / 4000m long arm)

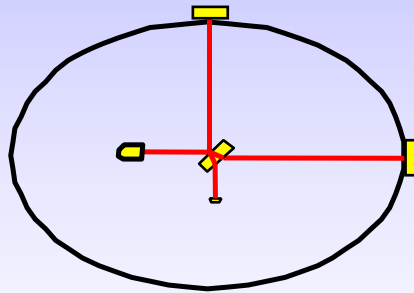
$$\Delta L = h \times L \approx 10^{-21} \times 4,000 m \approx 10^{-18} m$$



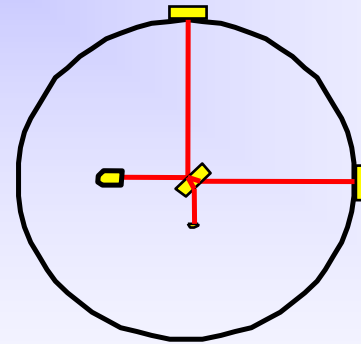
Effect on a ring of free falling masses:  
 Gravitational waves shrink space along one axis perpendicular to the wave direction as they stretch space along another axis perpendicular both to the shrink axis and to the wave direction.



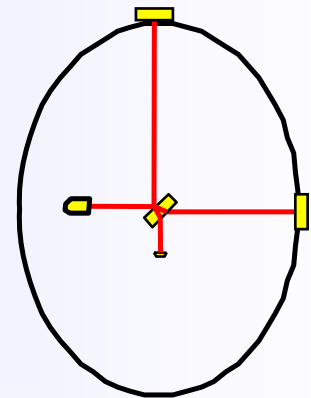
$t = 0$



$t = \frac{\tau}{4}$

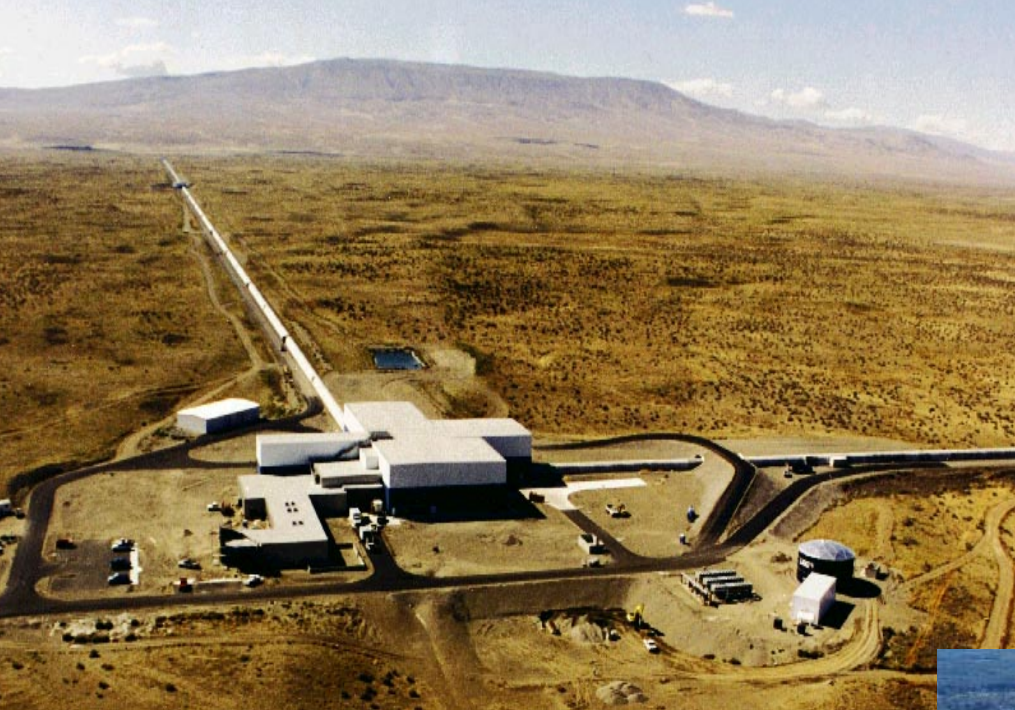


$t = \frac{\tau}{2}$



$t = \frac{3\tau}{4}$

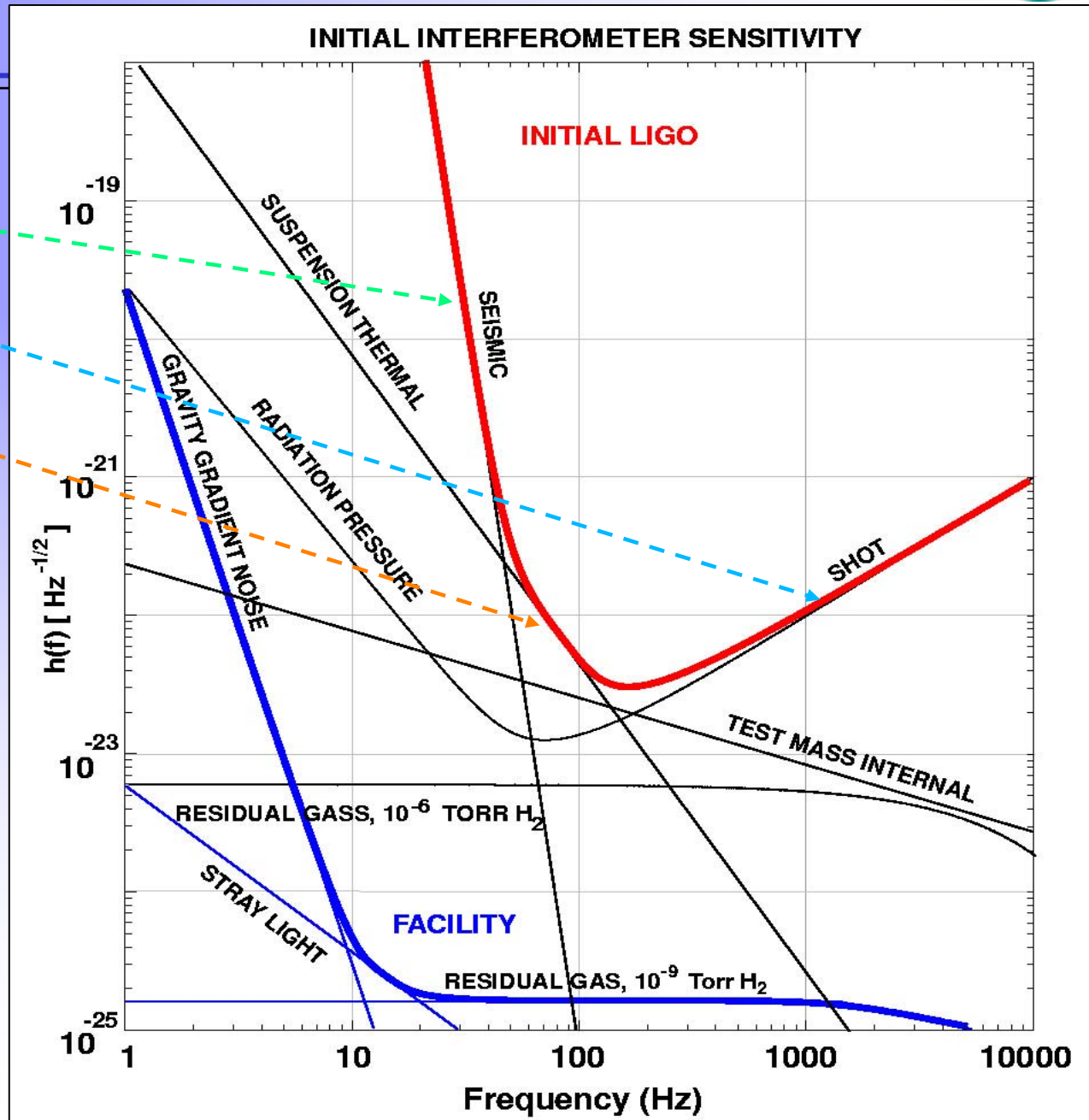




-Adapted from "The Blue Marble: Land Surface, Ocean Color and Sea Ice" at [visit.earth.nasa.gov](http://visit.earth.nasa.gov)  
-NASA Goddard Space Flight Center Image by Reto Stockli (land surface, shallow water, clouds) and technical support: MODIS Land Group; MODIS Science Data Support Team; MODIS Atmosphere Group; USGS Terrestrial Remote Sensing Flagstaff Field Center (Antarctica); Defense Meteorological Satellite Program



- Initial sensitivity limits
  - seismic noise at the lowest frequencies
  - shot noise at high frequencies
  - thermal noise at intermediate frequencies
- Based on conservative extrapolation of prototype technologies (circa ~'97)





View inside Corner Station



Standing at vertex  
beam splitter

Precast concrete enclosure: *bulletproof*

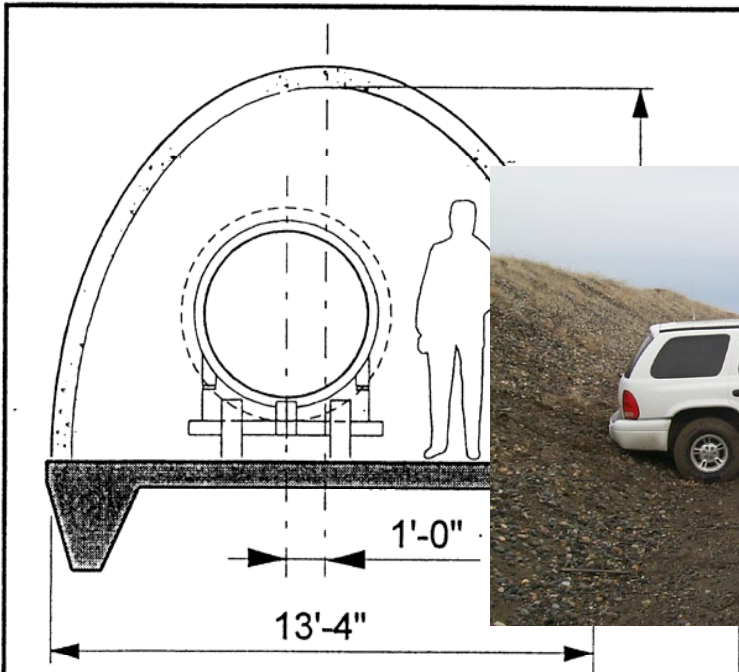


Figure 2.1-1 -- Cross Section of Design Baseline at Hanford

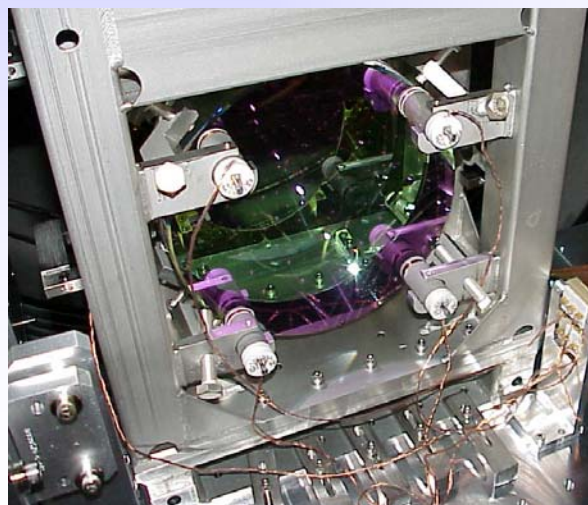


- 304 stainless steel beam; 3 mm stainless steel
- special low-hydrogen steel process
- 65 ft spiral weld sections
- 50 km of weld (NO LEAKS!)
- 20,000 m<sup>3</sup> @ 10<sup>-8</sup> torr; earth's largest high vacuum system

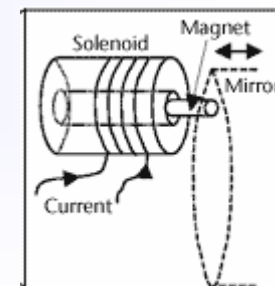


### Pendulum design

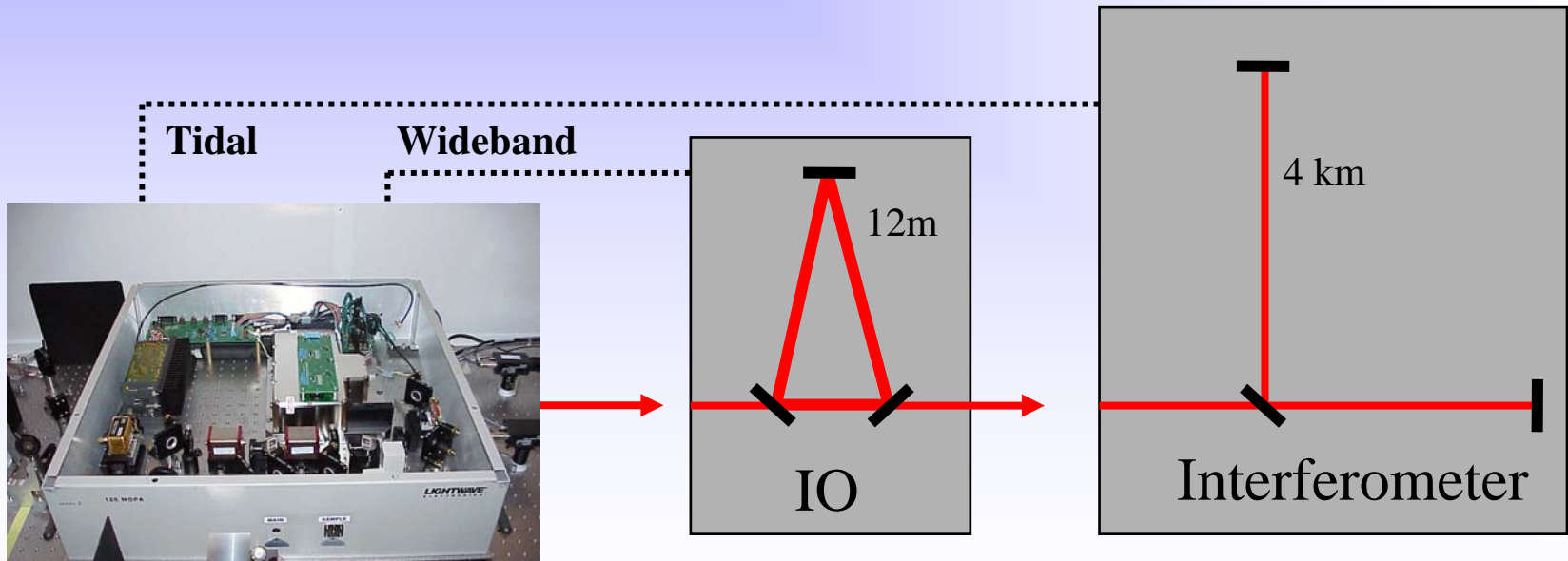
- provide  $10^2$  suppression above 1 Hz
- provide ultraprecise control of optics displacement ( $< 1$  pm)



### OSEM



- Deliver pre-stabilized laser light to the long mode cleaner
  - **Frequency fluctuations**
  - **In-band power fluctuations**
  - **Power fluctuations at 25 MHz**
- Provide actuator inputs for further stabilization
  - **Wideband**  $10^{-4} \text{ Hz} / \sqrt{\text{Hz}}$
  - **Tidal**  $10^{-7} \text{ Hz} / \sqrt{\text{Hz}}$



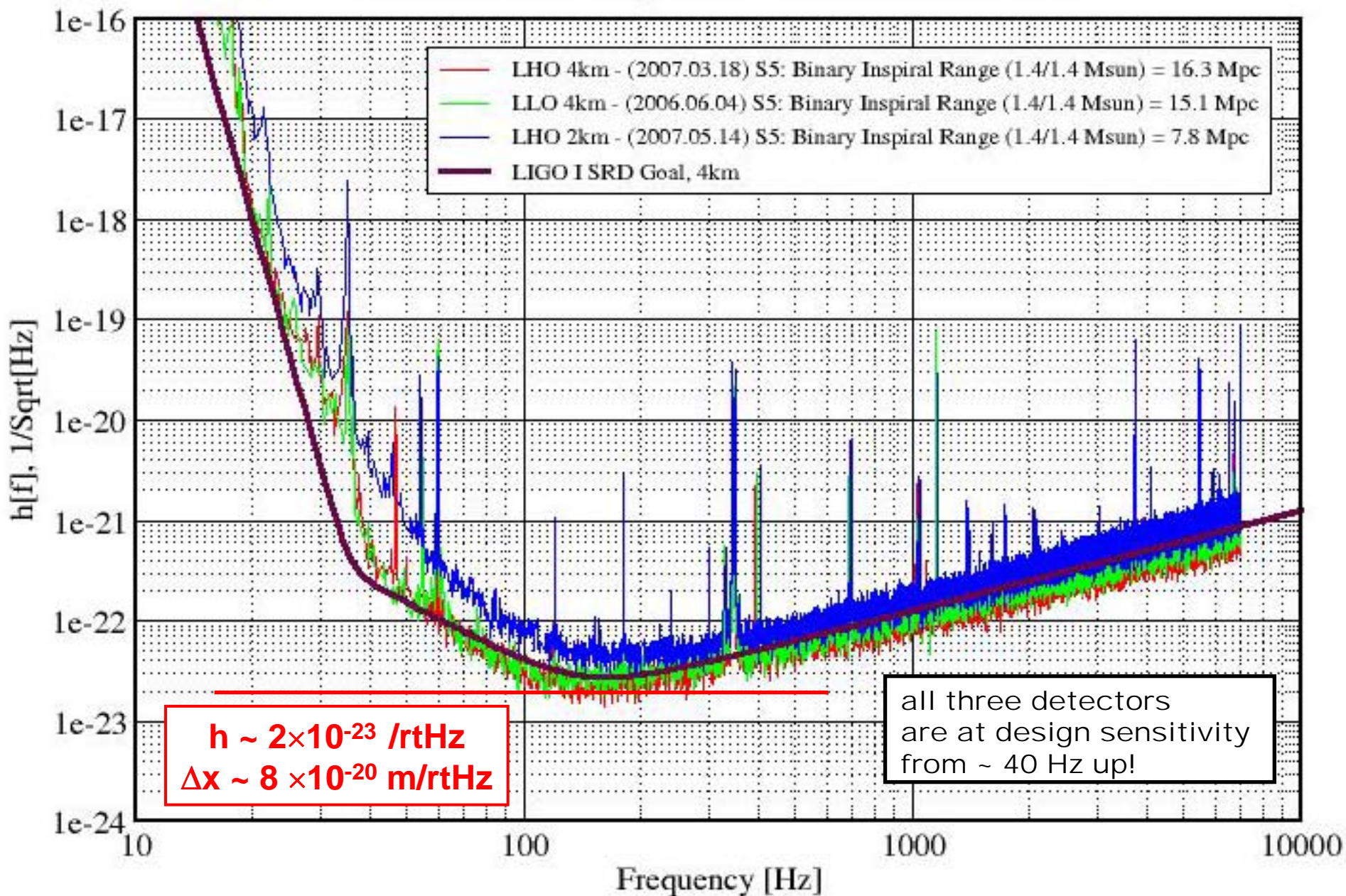
10 W Nd:YAG Laser, joint development with Lightwave Electronics



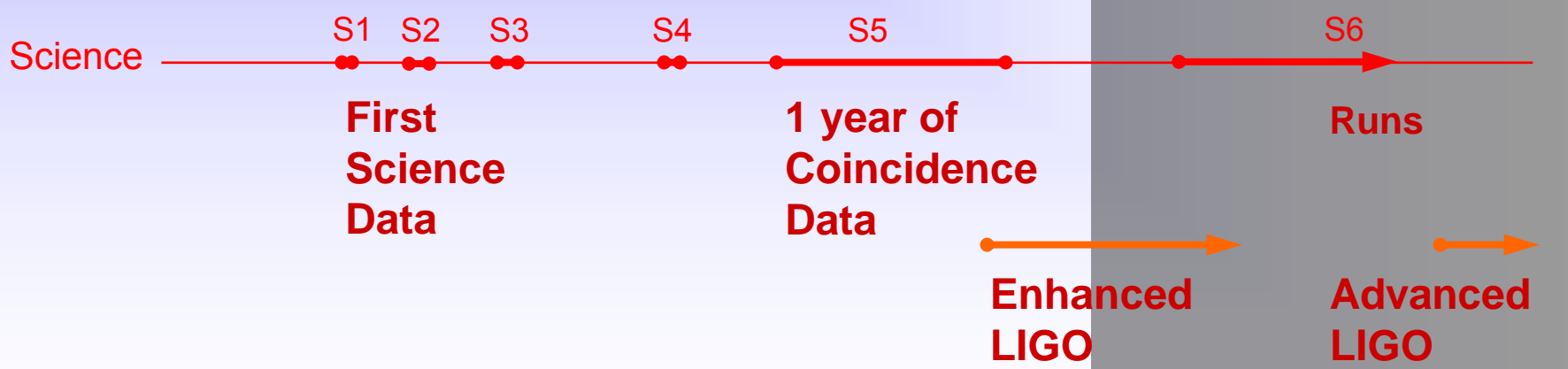
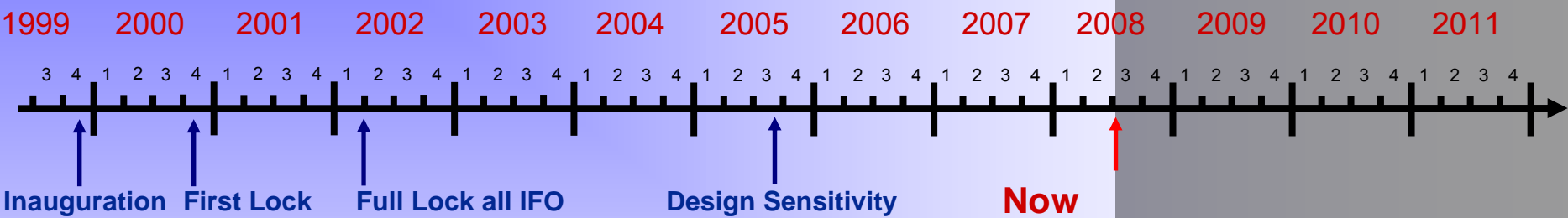
# Strain Sensitivity of the LIGO Interferometers

S5 Performance - May 2007

LIGO-G070366-00-E







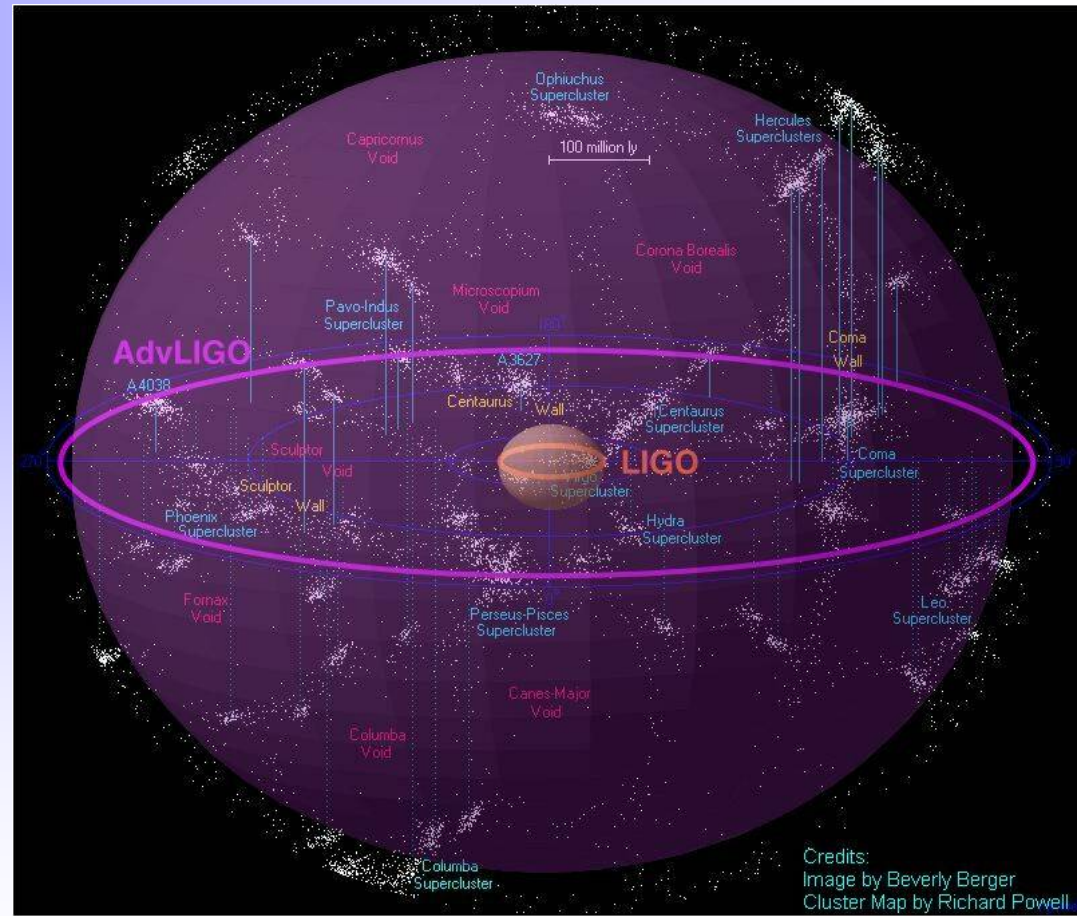
- Factor of  $\sim 2$  improvement in strain sensitivity of the two 4km instruments (nearly order-of-magnitude improvement in rate)
- All upgrades make use of Advanced LIGO technology: retire risk
- Work was started before S5 was finished, installation begun after S5 finished, projected completion date is 02/2009
- Projected date to start S6 is 03/2009

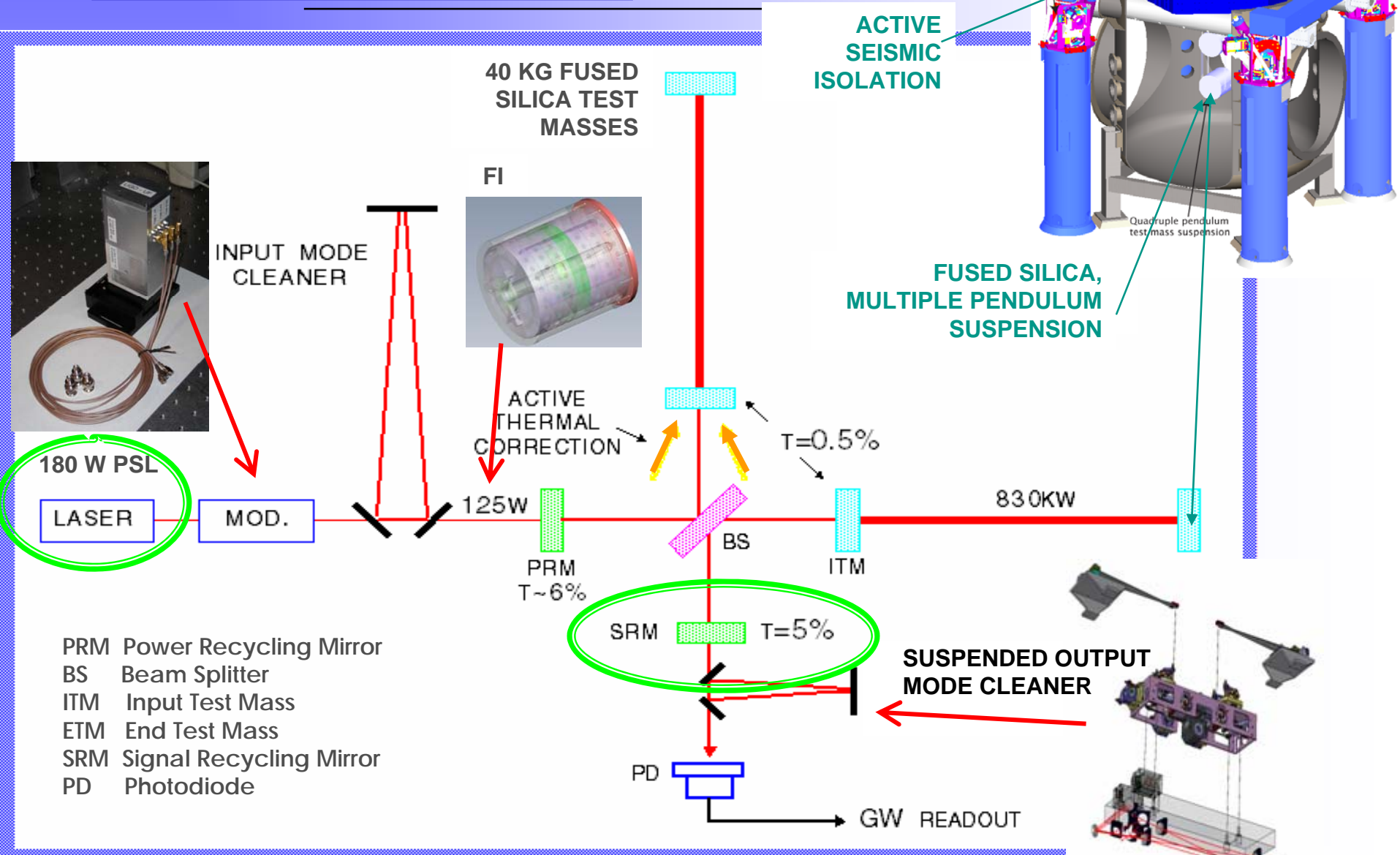
- **35 W Laser**
  - 4x increase in power
  - The “front-end” of the AdL laser
  - Supplied by LZH/AEI as part of Adv. LIGO
- **High Power Input Optics**
  - AdL **electrooptic Modulators (UF)**
  - AdL **Faraday Isolators (UF & IAP, Russia)**
- **AS detection in vacuum**
  - AdL **active seismic** system in HAM6
  - **Output mode cleaner**
  - In-vacuum AdL **photodetectors**
- **DC Readout of GW Strain**
  - AdL readout scheme (**DC** instead of RF)
  - AdL **Output Mode Cleaner** cavity
- **Thermal Compensation**
  - Upgraded power & beam shaping





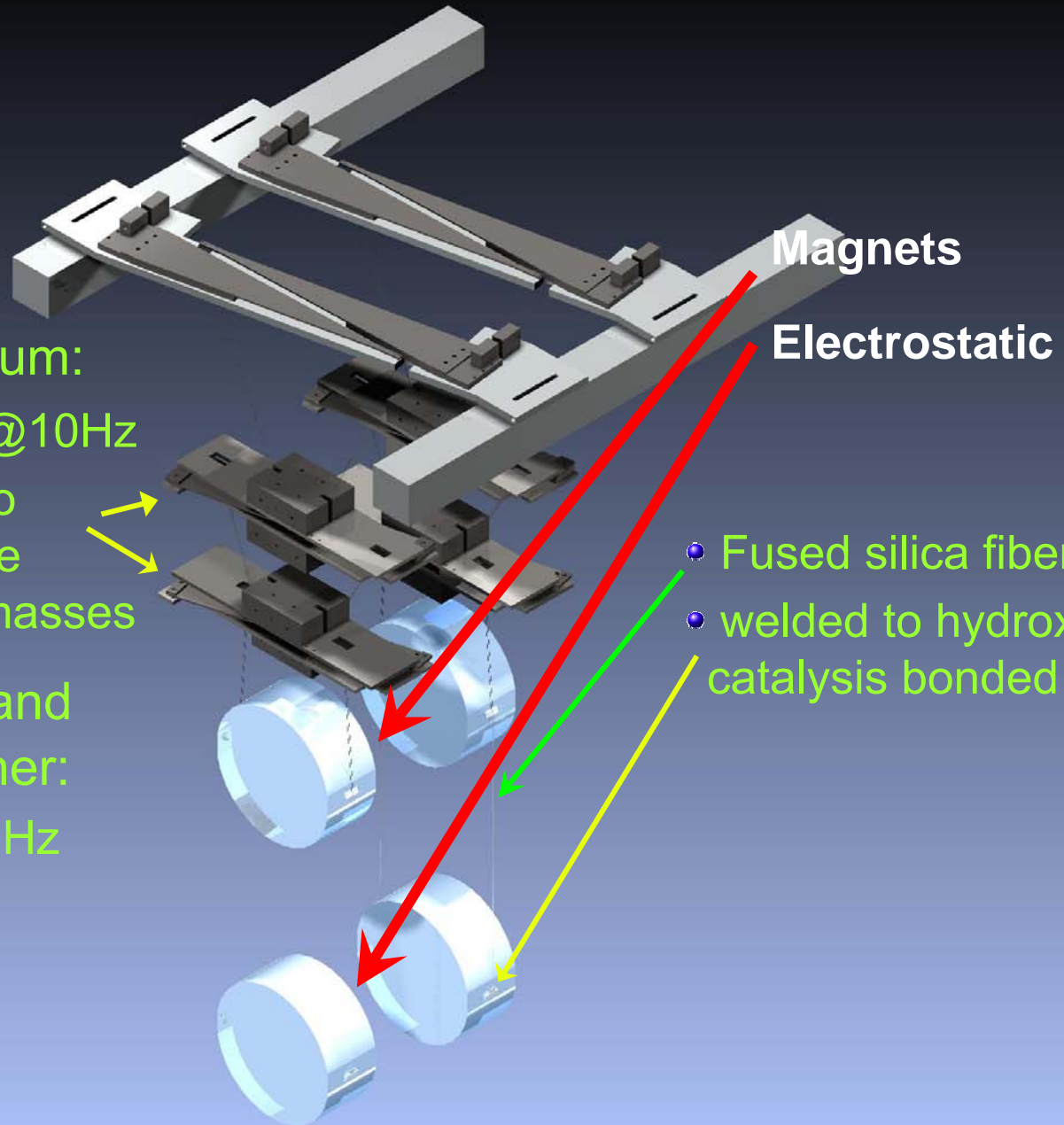
- At current sensitivity, LIGO detectors are rate-limited (NS/NS inspirals)
  - $\sim 0.01$  event per year
- Advanced LIGO will increase sensitivity (hence rate) over initial LIGO
  - range  $r \sim 1/h$
  - Event rate  $\sim r^3$
- Most probable NS/NS event rate in Advanced LIGO is
  - $\sim 40$  per year
- Funding to started in 2008, construction to begin in 2011





- PRM Power Recycling Mirror
- BS Beam Splitter
- ITM Input Test Mass
- ETM End Test Mass
- SRM Signal Recycling Mirror
- PD Photodiode

# Quad Suspensions



- **Quadruple pendulum:**

- $\sim 10^7$  attenuation @10Hz
- Controls applied to upper layers; noise filtered from test masses

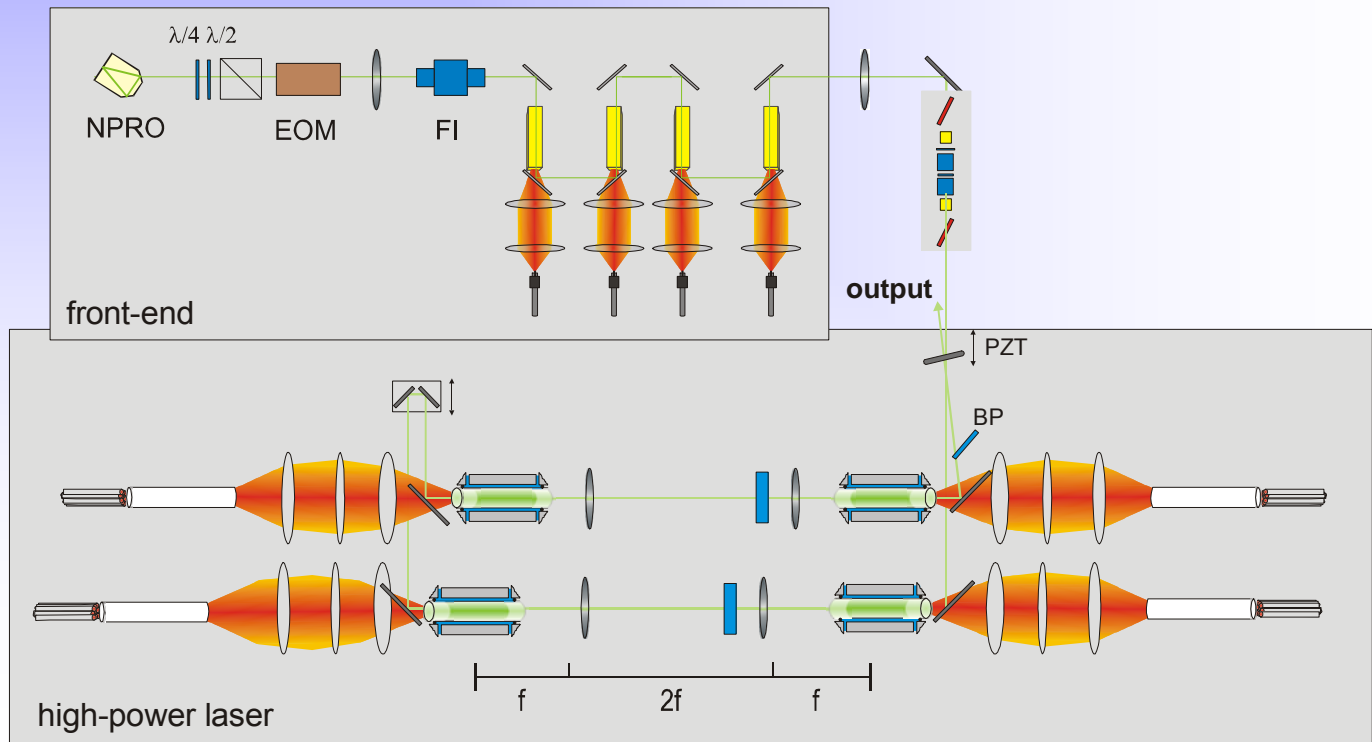
- **Seismic isolation and suspension together:**

- $10^{-19}$  m/rtHz at 10 Hz

- Fused silica fiber
- welded to hydroxy-catalysis bonded 'ears'



- 180 W amplitude and frequency stabilized Nd:YAG laser
- Two stage amplification
  - First stage: MOPA (NPRO + single pass amplifier)
  - Second stage: injection-locked ring cavity
- Developed by Laser Zentrum Hannover (and MPI at Hannover)



- Baseline Review in June 2006, plus follow-on reviews in June 2007 and November 2008...project ready
- R&D is well underway
- Breach vacuum in 2010
- Start commissioning 1st interferometer for Advanced LIGO in 2013

- LIGO is currently being upgraded to eLIGO
- Laser power is increased to 30 W
- Electro-optic modulators (EOMs) are replaced.
  - $\text{LiNbO}_3$  modulators would suffer from severe thermal lensing or might even break
- eLIGO devices (techniques) will be used in AdvLIGO



- eLIGO EOMs

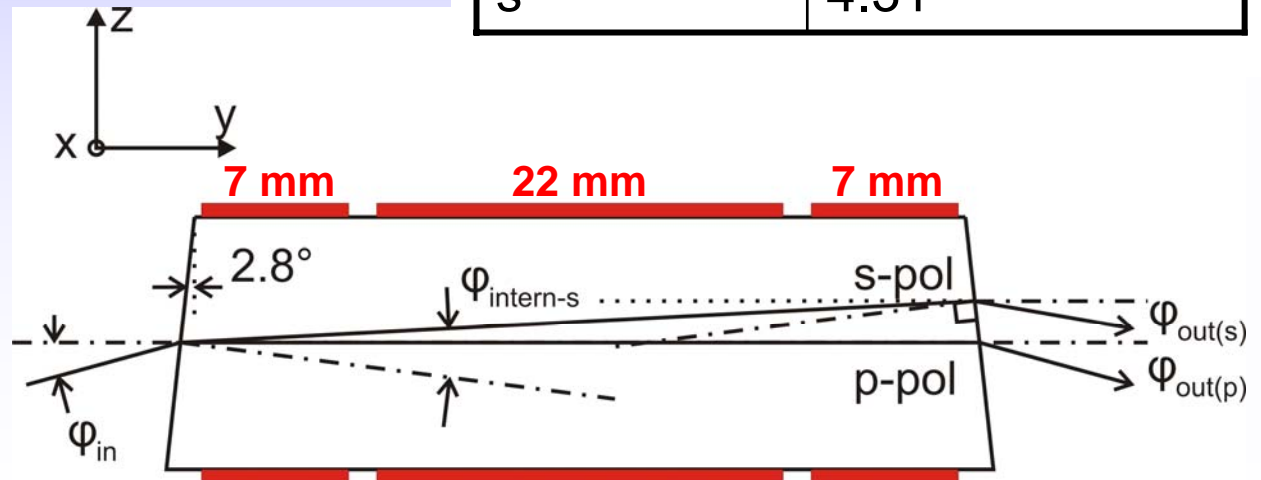
- Lithium niobate ( $\text{LiNbO}_3$ ), used in initial LIGO, not satisfactory
  - Thermal lensing / Damage / Residual absorption
- Choose RTP (rubidium titanyl phosphate -  $\text{RbTiOPO}_4$ ) as EO material
  - RTP has significantly lower absorption and therefore thermal lensing.
- Use custom made housing to separate the crystal housing from the housing for the resonant circuit.  
Advantage: Resonant frequencies can be changed without disturbing the optical alignment.
- Use wedged crystals to reduce spurious amplitude modulation  
Additional advantage: EOM acts as polarizer



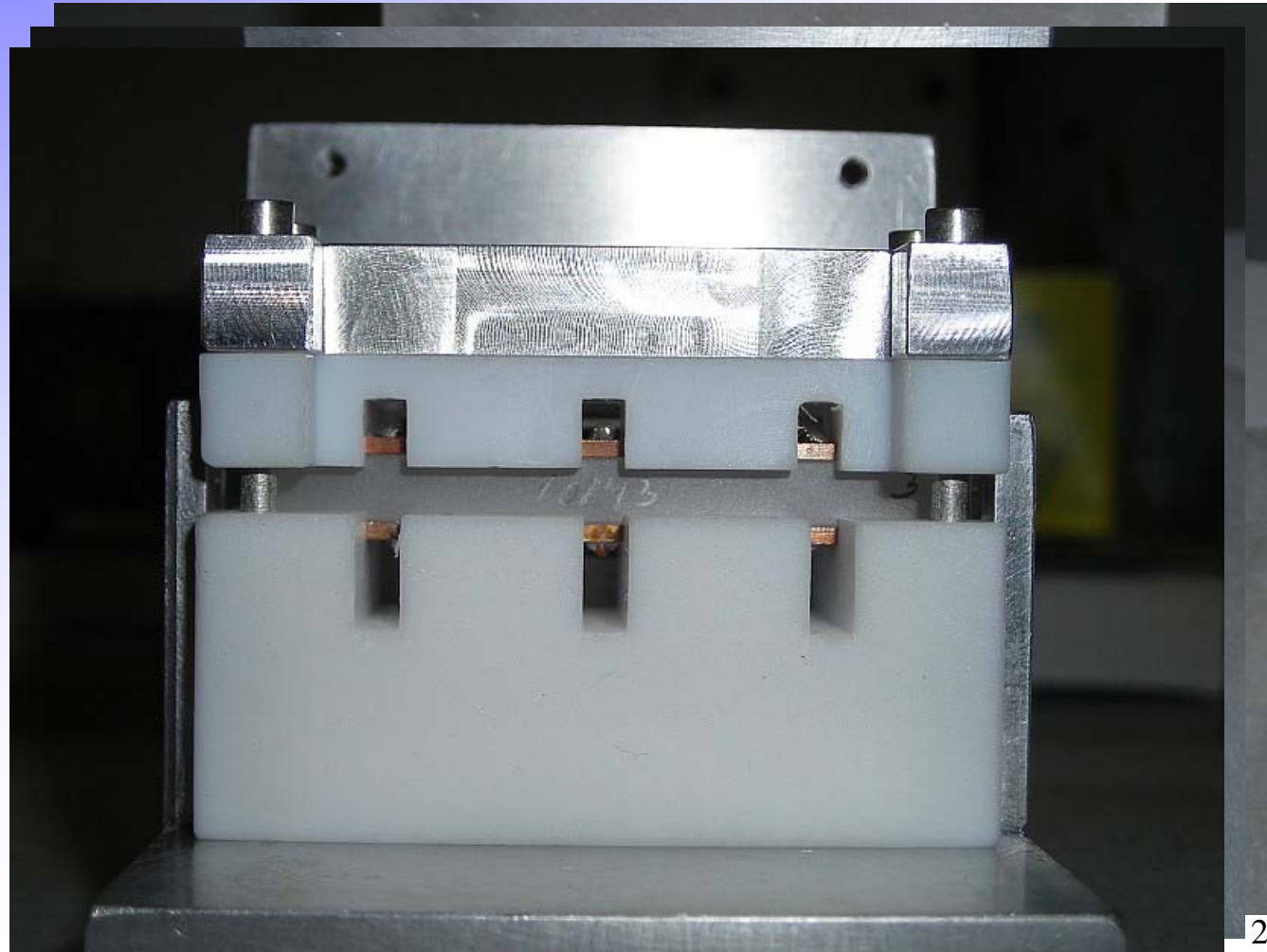
- Wedged crystal separates the polarizations and acts as a polarizer.
  - This avoids cavity effects and reduces amplitude modulation.

- AR coatings (< 0.1%) on crystal faces.

Polarization	Angle [degrees]
p	4.81
s	4.31



- Use one crystal but three separate pairs of electrodes to apply three different modulation frequencies at once.





- Separate the crystal housing from the housing of the electronic circuits to maintain maximum flexibility.

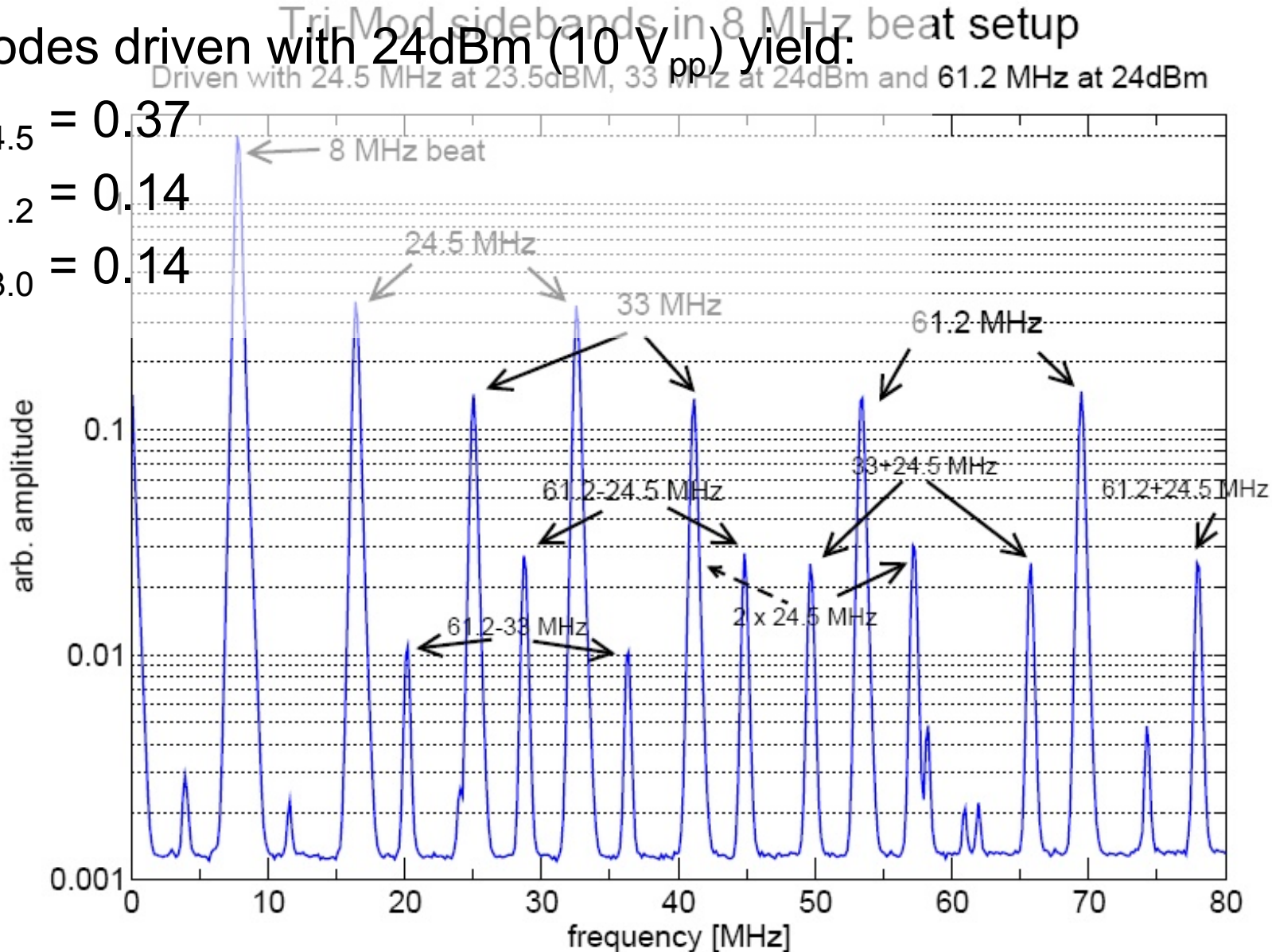


- Electrodes driven with 24dBm (10 V<sub>pp</sub>) yield:

- $m_{24.5} = 0.37$

- $m_{61.2} = 0.14$

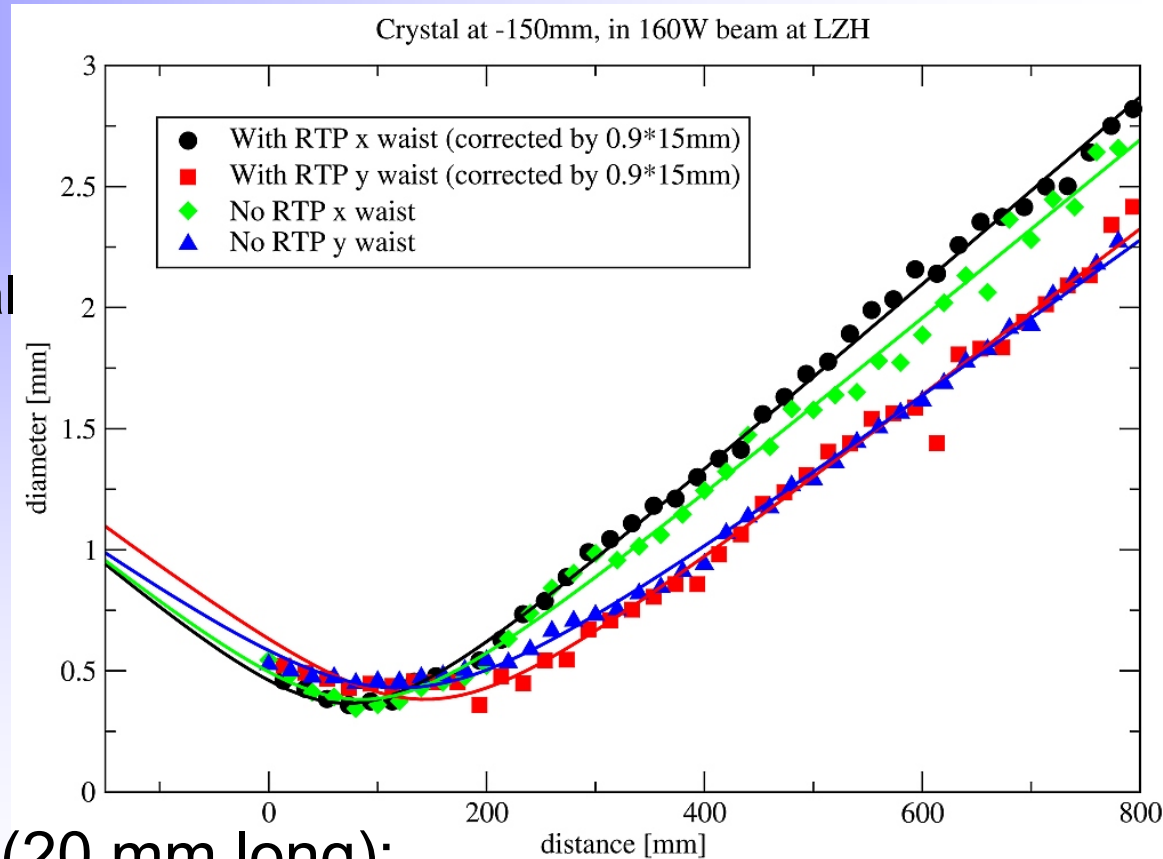
- $m_{33.0} = 0.14$



- The AdvLIGO laser prototype was used to measure the thermal lensing.

- Full Power = 160 W
- Beam Waist = 950  $\mu\text{m}$  diameter at crystal
- 4x4x15 mm RTP crystal

- Thermal lenses:  
 $f_x > 4 \text{ m}$   
 $f_y = \text{much longer}$



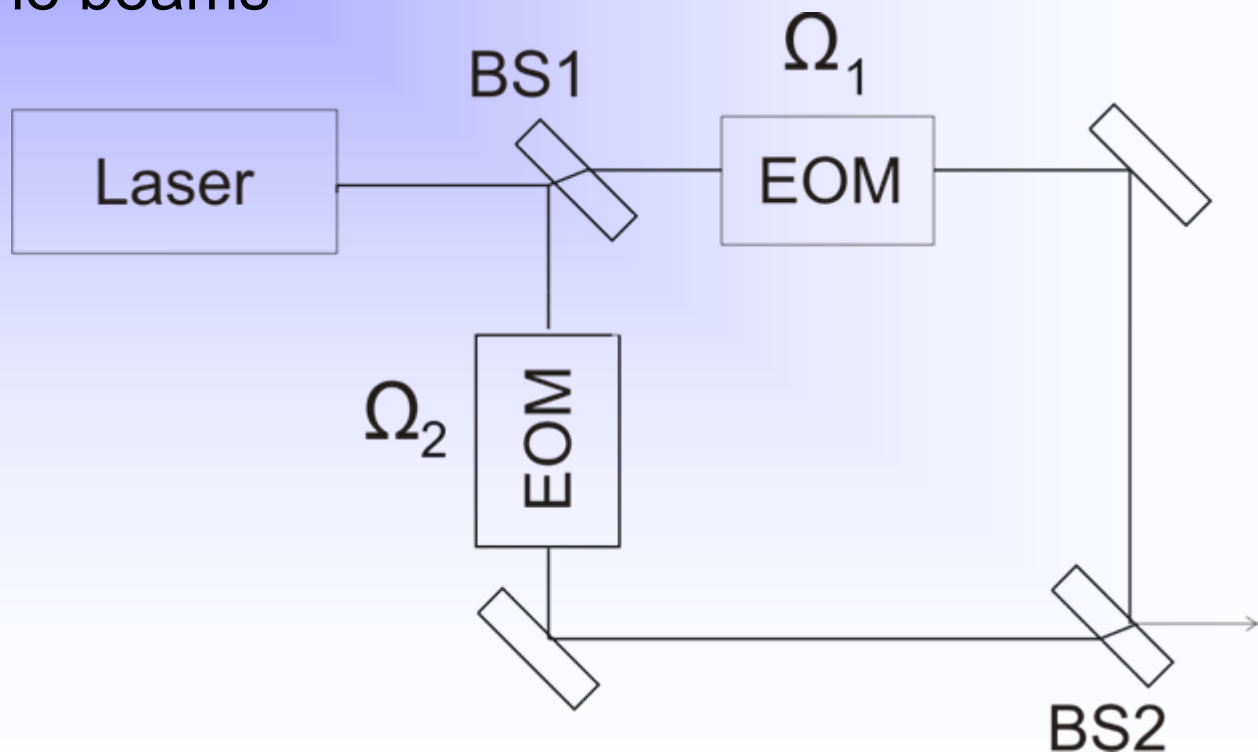
- compare with LiNbO3 (20 mm long):  
 $f_{\text{thermal}} \sim 3.3 \text{ m @ } 10 \text{ W}$



- Wedged geometry suppresses amplitude modulation. (No polarisation rotation possible)
  - Measured AM:  
 $\Delta I/I < 10^{-5}$  at  $\Omega_{mod} = 25.4$  MHz /  $m = 0.17$
- Piezo effects in can lead to standing waves (AOM) and pointing (RF-pointing) at the modulation frequency

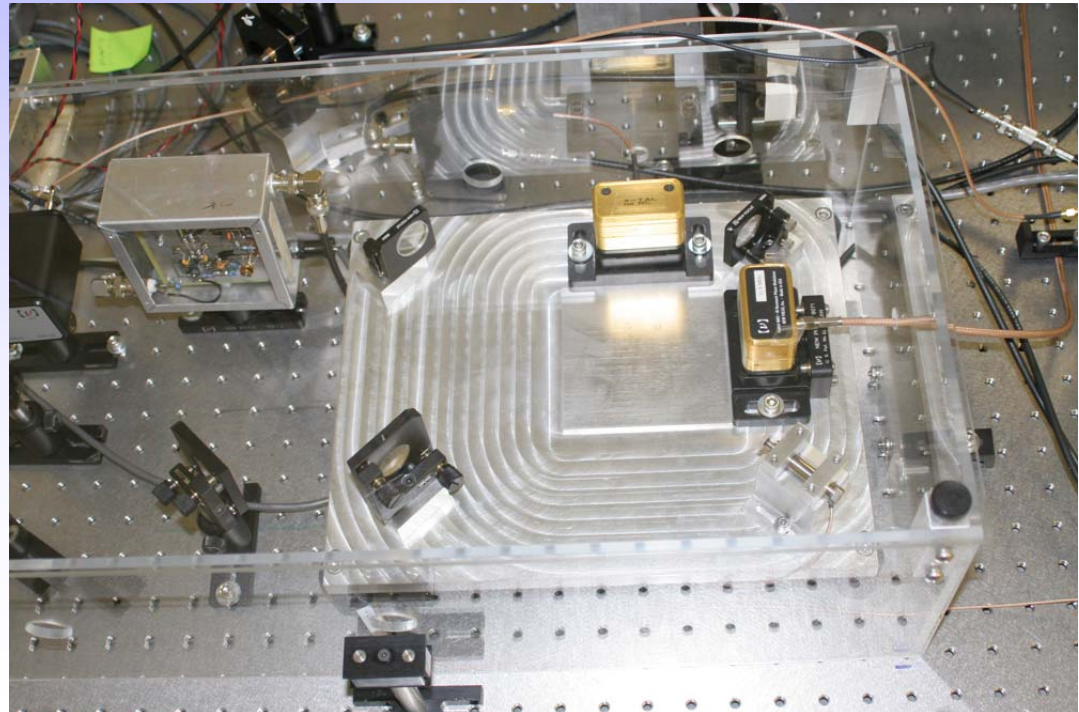
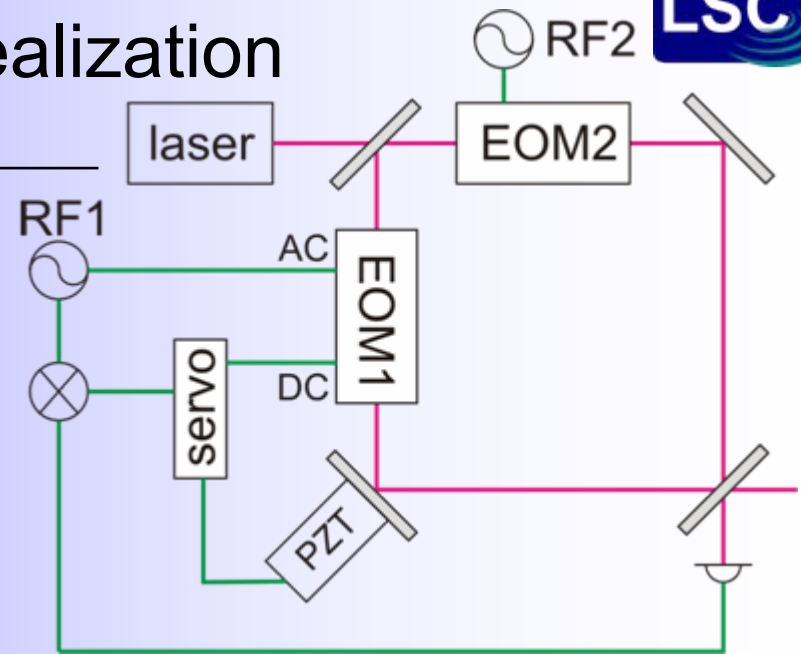
- Not a high power issue, but related to advanced modulation configurations.
- Objective:
  - Solve the sidebands on sidebands problem by using parallel modulation.
  - Currently used in the 40m prototype
- Problems:
  - Sideband power reduced by a factor of 4
  - Additional intensity noise at modulation and mixing (sum/difference) frequencies
  - Excess intensity, frequency and sideband noise is possible depending on the stability of the MZ and the corner frequencies of the MZ stabilization loop.
- Only address the last point for now ..

- Parallel modulation with two modulation frequencies
- Avoid the sideband-on-sideband problem by separating the beams





- Slow length control with big dynamic range with PZT
- Fast phase control with phase correcting EOM
- Stable mechanical “quasi-monolithic” design
- Reduce environmental effects with a Plexiglas enclosure.
- Modulation at 25 MHz and 31.5 MHz
- Current development:  
A stable, high power capable AdvLIGO prototype



## Why use complex modulation?

- Objective:
  - Solve the sidebands on sidebands problem.
  - Reduce the number of modulators to reduce the optical losses
- Idea: Simulate the effect of a MZ without physically separating the beams
- Requirements:
  - Generate AM and PM with arbitrary waveforms at very high sampling frequencies

- General representation for an amplitude- and phase modulated light field:

$$E(t) = \frac{E_0}{2} \exp(i\omega t + f(t)) + c.c.$$

- with

$$f(t) = \phi(t) + i\alpha(t)$$

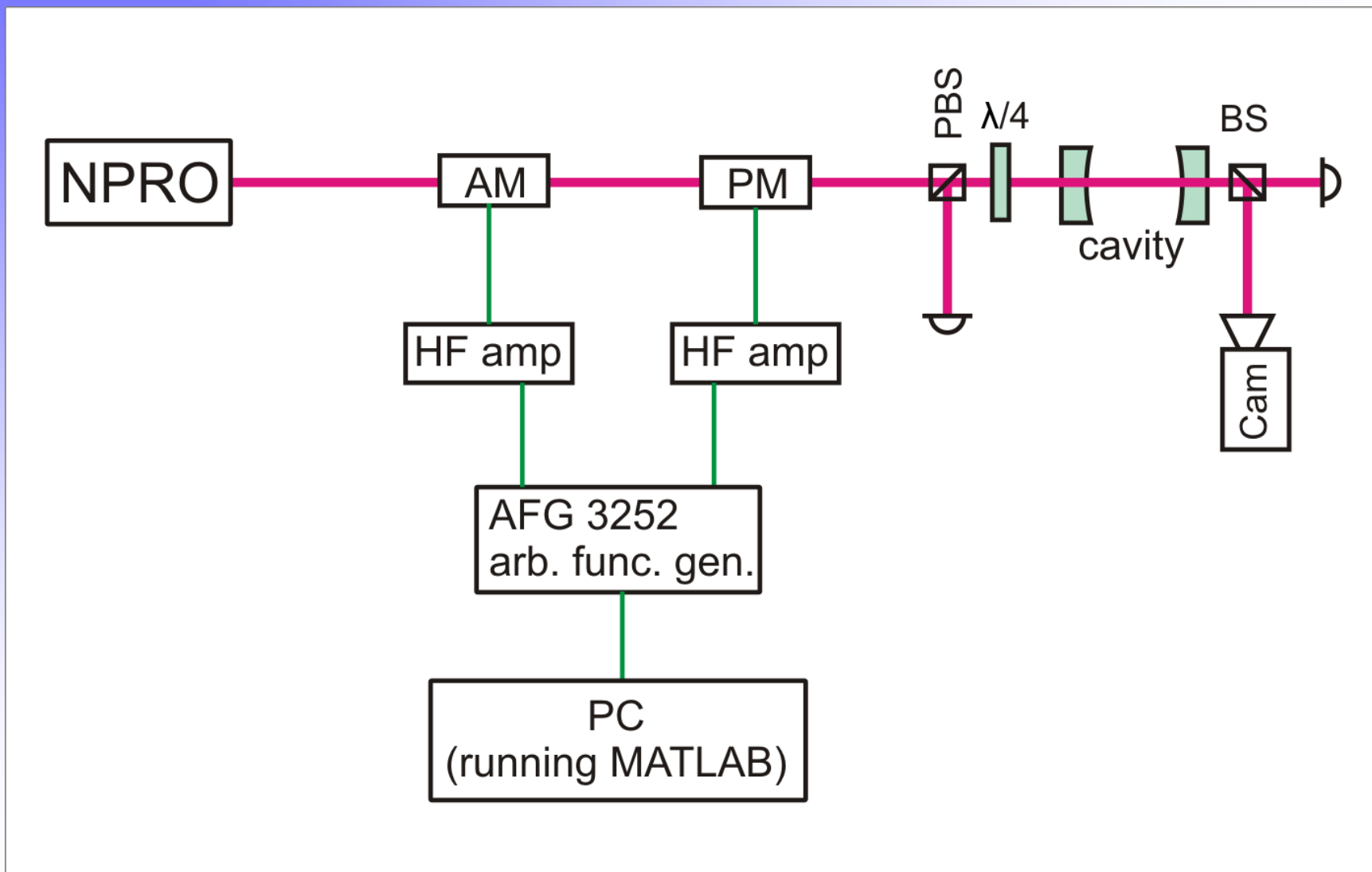
- Question: which modulation is needed to generate a certain light field?

$$E_{new}(t) = E_0(t) \cdot \exp(f(t)) + c.c.$$

- solving (easy without the + c.c.) leads to:

$$\phi(t) = \arg\left(\frac{E_{new}(t)}{E_0(t)}\right) \quad \alpha(t) = \ln\left|\frac{E_{new}(t)}{E_0(t)}\right|$$



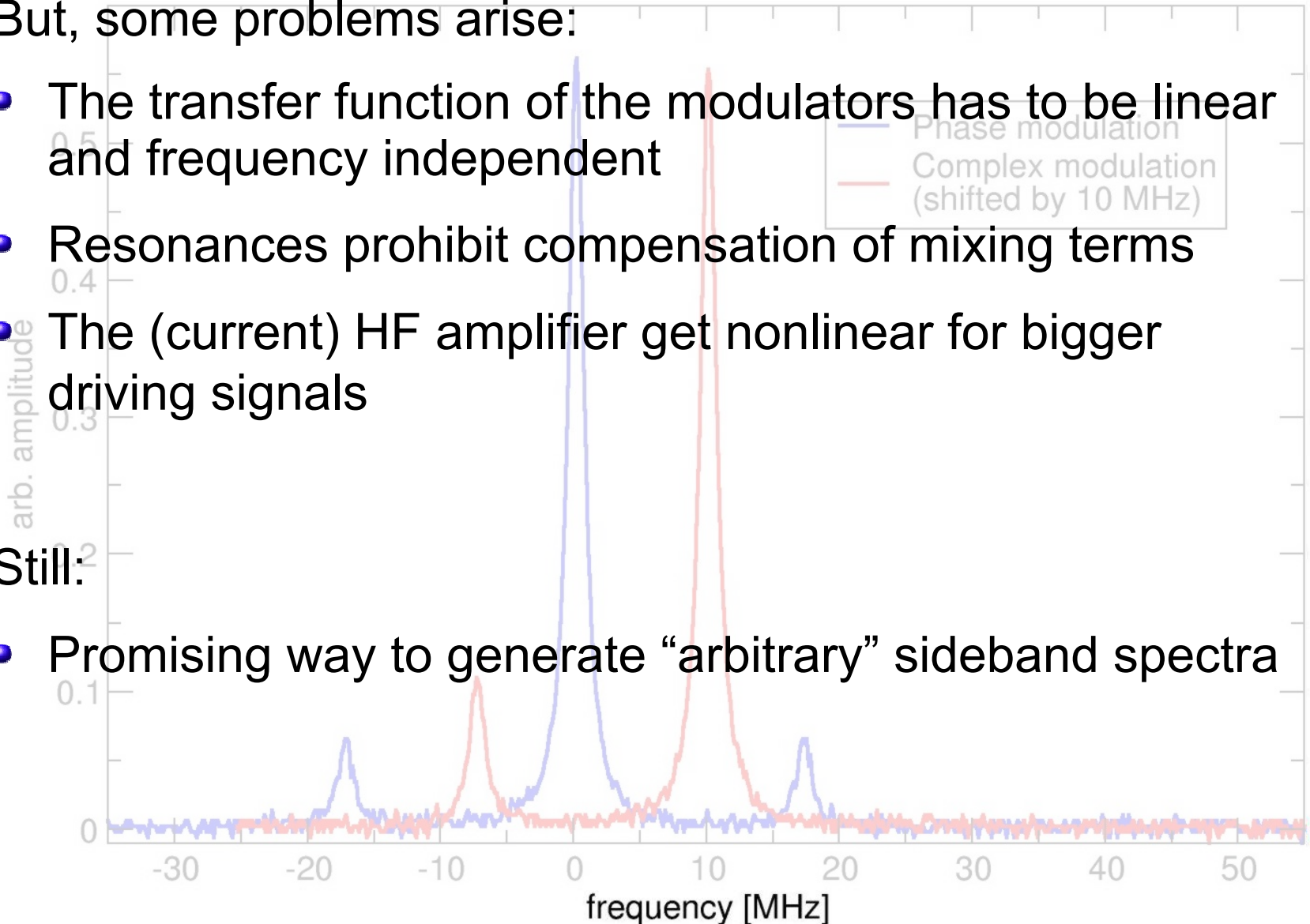


But, some problems arise:

- The transfer function of the modulators has to be linear and frequency independent
- Resonances prohibit compensation of mixing terms
- The (current) HF amplifier get nonlinear for bigger driving signals

Still:

- Promising way to generate “arbitrary” sideband spectra



- **LIGO finished S5 Science run**
- **enhanced LIGO upgrade is happening**
- **advanced LIGO is beginning**
- **modulation challenges are understood/solved**
- **Gravitational wave detection pushes state-of-the art in CW solid state laser technology, optical fabrication and metrology, and control systems**

**Acknowledgments:**



**and the Members of the LIGO Laboratory, members of the LIGO Science Collaboration, National Science Foundation**

**More Information:**

- <http://www.ligo.caltech.edu>; [www.ligo.org](http://www.ligo.org)



**LIGO**

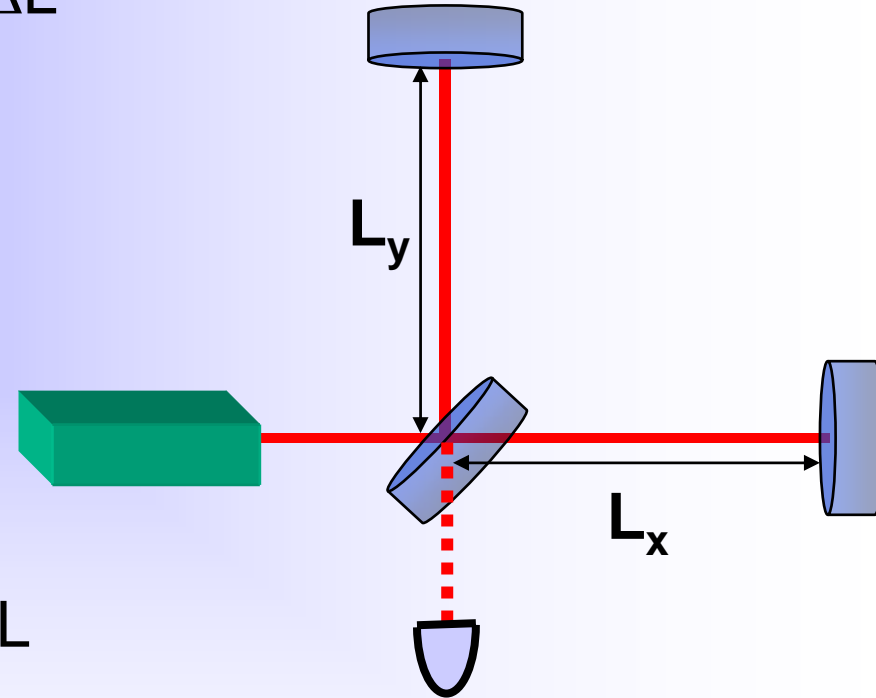
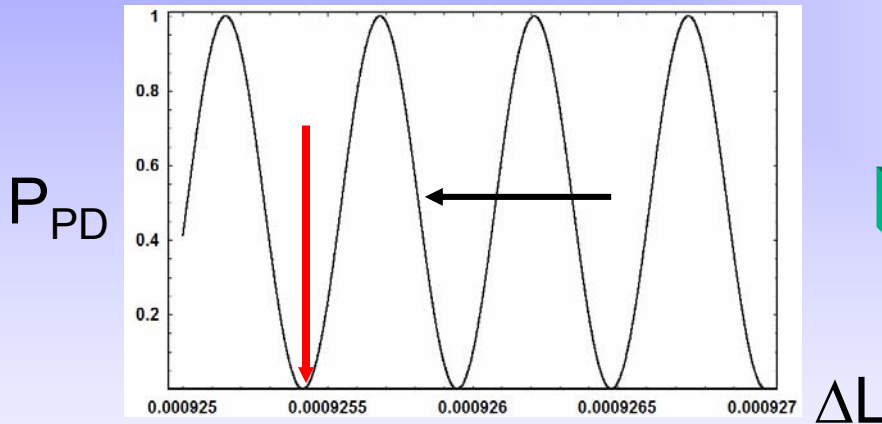
# Supplementary material

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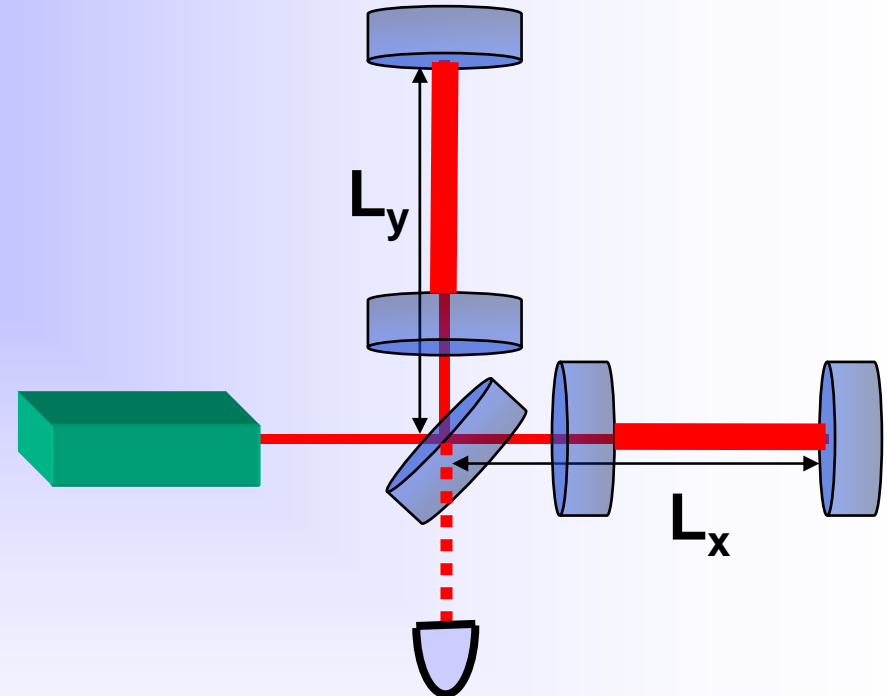
- Simple Michelson
  - Phase:  $\phi = 4\pi (L_x - L_y) / \lambda \sim \Delta L$
  - Power:  $P_{PD} = P_{BS} \sin^2\phi$ 
    - $dP/d\phi \sim P_{BS} \sin \phi \cos \phi$



- Strain:  $h = \Delta L/L$ 
  - Increase sensitivity by using longer arms

$d\phi/dh \sim L$

- Fabry-Perot cavity
  - Increases power in arms
  - Overcoupled cavity gain:  
 $G_{FP} \sim 4 / T_{input}$
  - Enhances storage time of light in cavity
  - Effectively 'lengthens' arms  
 $\sim G_{FP}$



$$d\phi/dh \sim G_{FP} \times L$$

- ‘Recycle’ light coming back from beamsplitter
  - Add a mirror which forms a resonant cavity with the rest of the interferometer

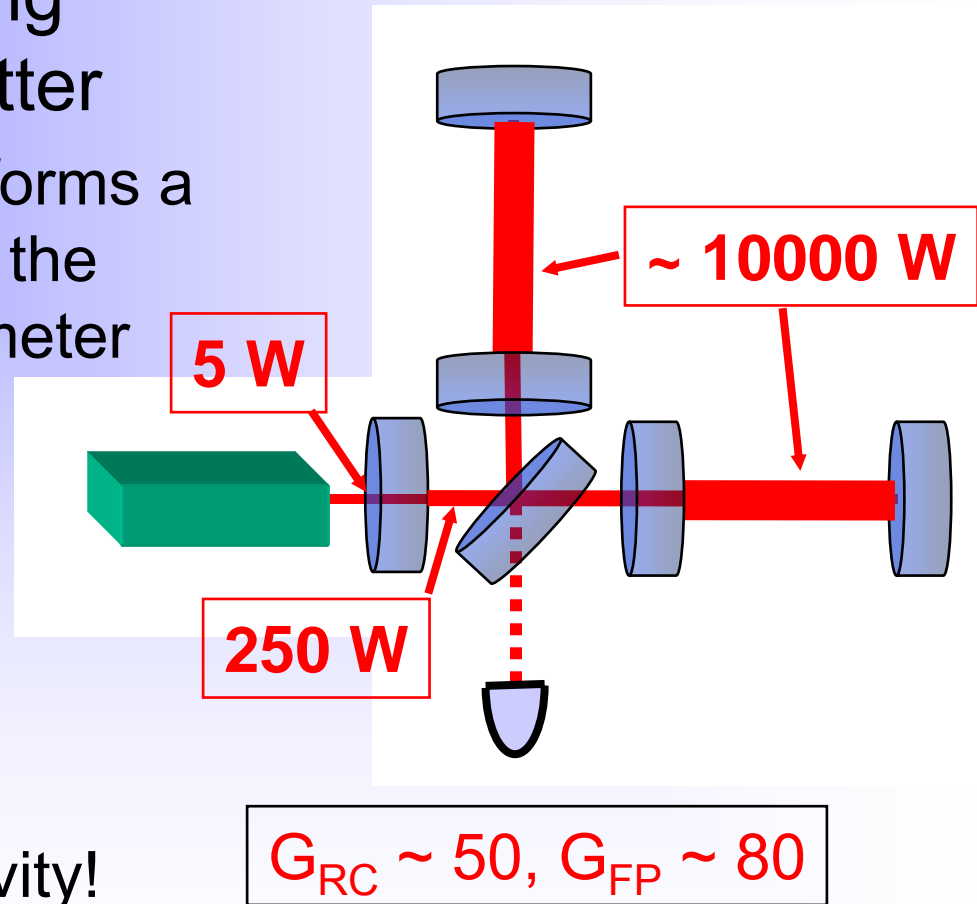
$$P_{BS} = G_{RC} P_{input}$$

+

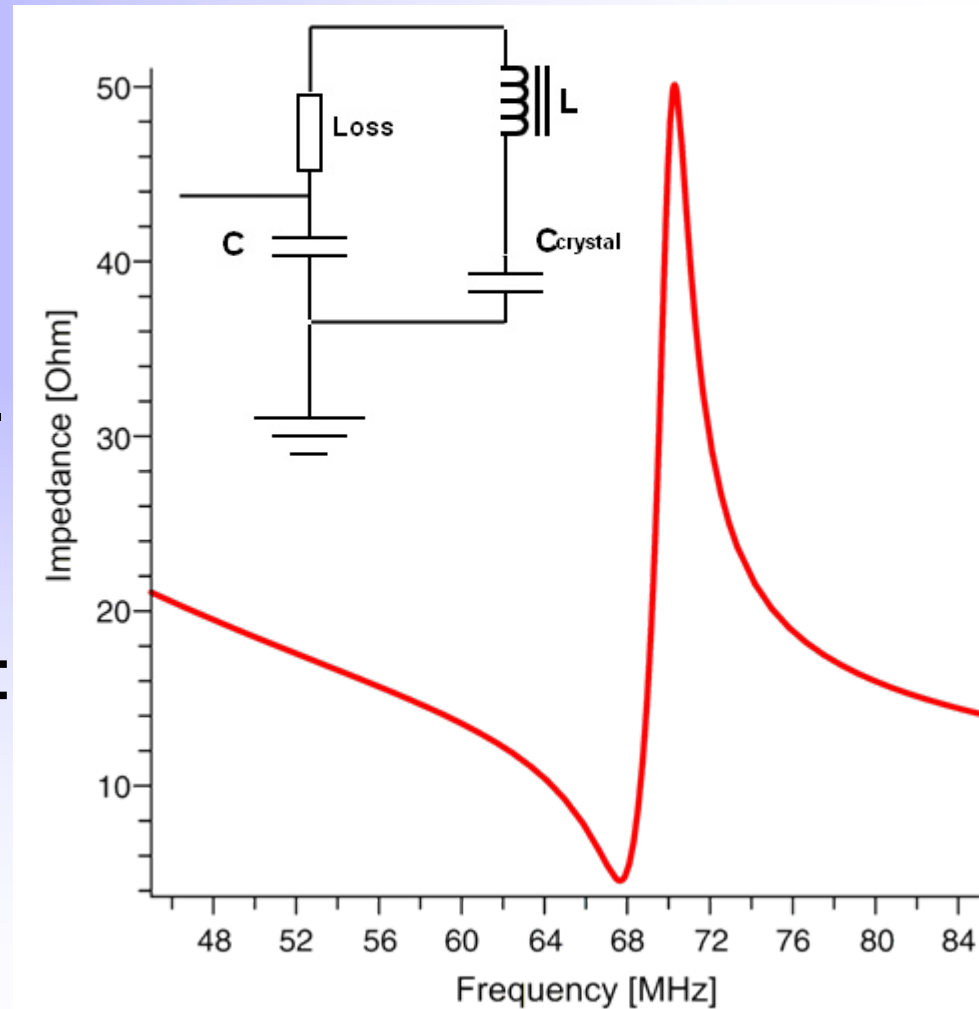
$$d\phi/dh \sim G_{FP} \times L$$

=>

Enhanced Phase Sensitivity!



- Impedance matching circuit in separate housing.
- Resonant circuit with  $50\ \Omega$  input impedance.
- eLIGO version has three resonant circuits:
  - 24.5 / 33.0 / 61.2 MHz

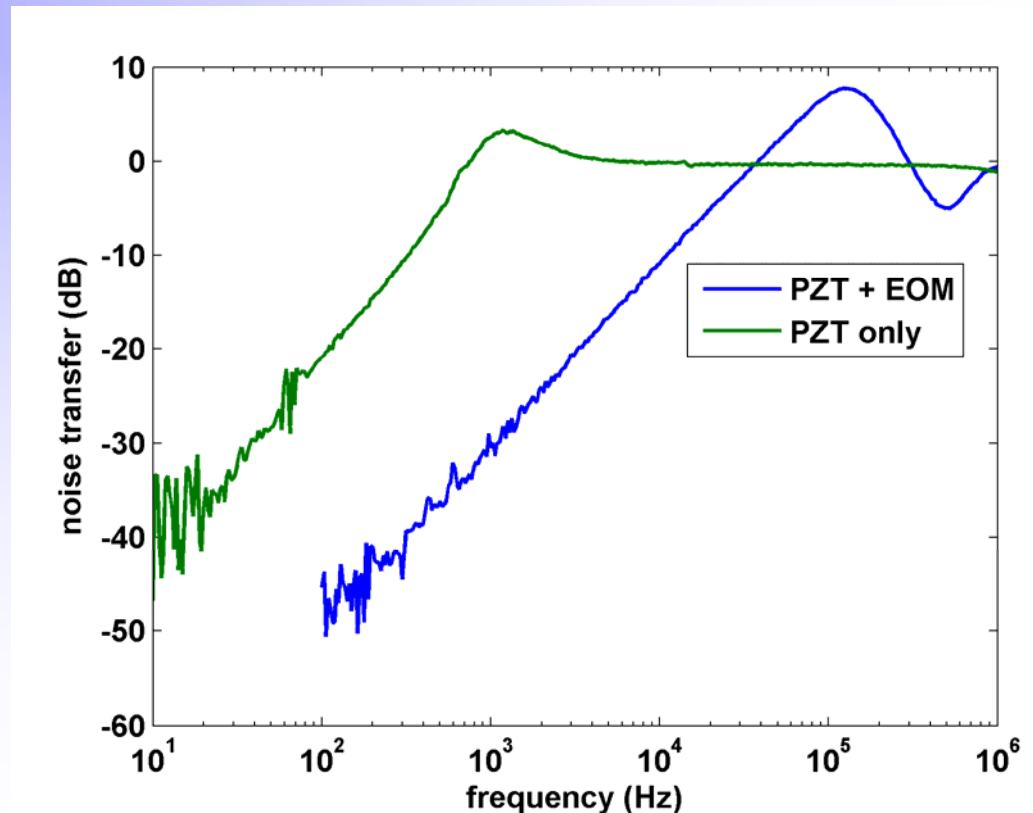
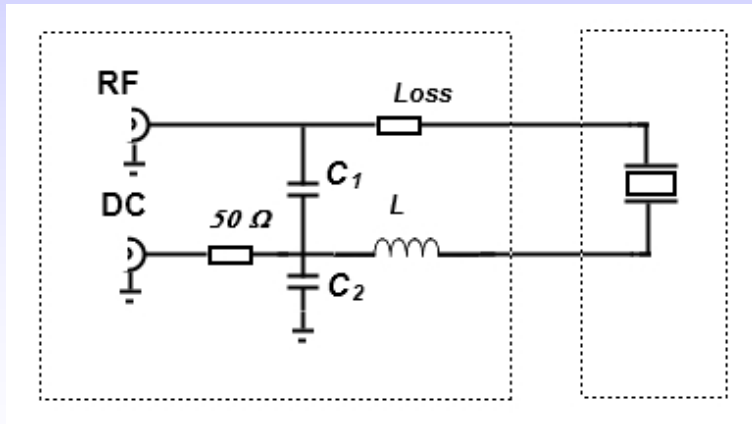




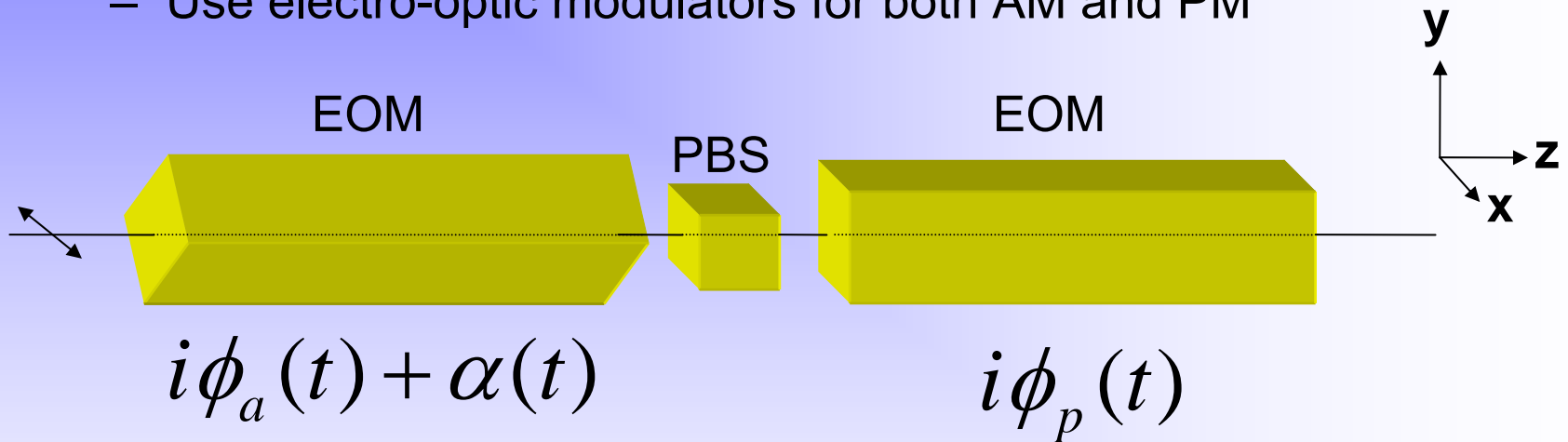
Properties	Units	RTP	RTA	KTP	LiNbO <sub>3</sub>
$dn_x/dT$	10 <sup>-6</sup> /K	-	-	11	5.4
$dn_y/dT$	10 <sup>-6</sup> /K	2.79	5.66	13	5.4
$dn_z/dT$	10 <sup>-6</sup> /K	9.24	11.0	16	37.9
$\kappa_x$	W/Km	3		2	5.6
$\kappa_y$	W/Km	3		3	5.6
$\kappa_z$	W/Km	3		3	5.6
$\alpha$	cm <sup>-1</sup>	< 0.0005	< 0.005	< 0.005	< 0.05
$Q_x$	1/W	-	-	2.2	4.8
$Q_y$	1/W	0.047	0.94	2.2	4.8
$Q_z$	1/W	0.15	1.83	2.7	34

Properties	Units/conditions	RTP	RTA	LiNbO <sub>3</sub>
Damage Threshold	MW/cm <sup>2</sup> ,	>600	400	280
$n_x$	1064nm	1.742	1.811	2.23
$n_y$	1064nm	1.751	1.815	2.23
$n_z$	1064nm	1.820	1.890	2.16
Absorption coeff. $\alpha$	cm <sup>-1</sup> (1064 nm)	< 0.0005	< 0.005	< 0.005
$r_{33}$	pm/V	39.6	40.5	30.8
$r_{23}$	pm/V	17.1	17.5	8.6
$r_{13}$	pm/V	12.5	13.5	8.6
$r_{42}$	pm/V	?	?	28
$r_{51}$	pm/V	?	?	28
$r_{22}$	pm/V			3.4
$n_z^3 r_{33}$	pm/V	239	273	306
Dielectric const., $\epsilon_z$	500 kHz, 22 °C	30	19	
Conductivity, $\sigma_z$	$\Omega^{-1}\text{cm}^{-1}$ , 10 MHz	$\sim 10^{-9}$	$3 \times 10^{-7}$	
Loss Tangent, $d_z$	500 kHz, 22 °C	1.18	-	

- To realize the fast phase correcting without using an additional EOM a slightly modified resonant circuit was used.
  - Simultaneous modulation at resonant frequency
  - DC phase changes up to 1 MHz possible



- Sidebands at several ten MHz require fast phase and amplitude changes.
  - Use electro-optic modulators for both AM and PM

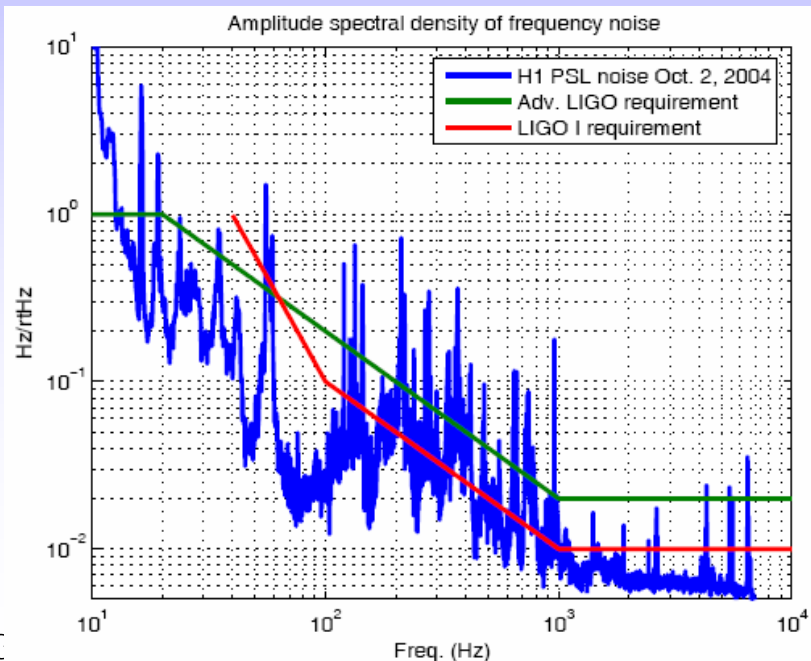
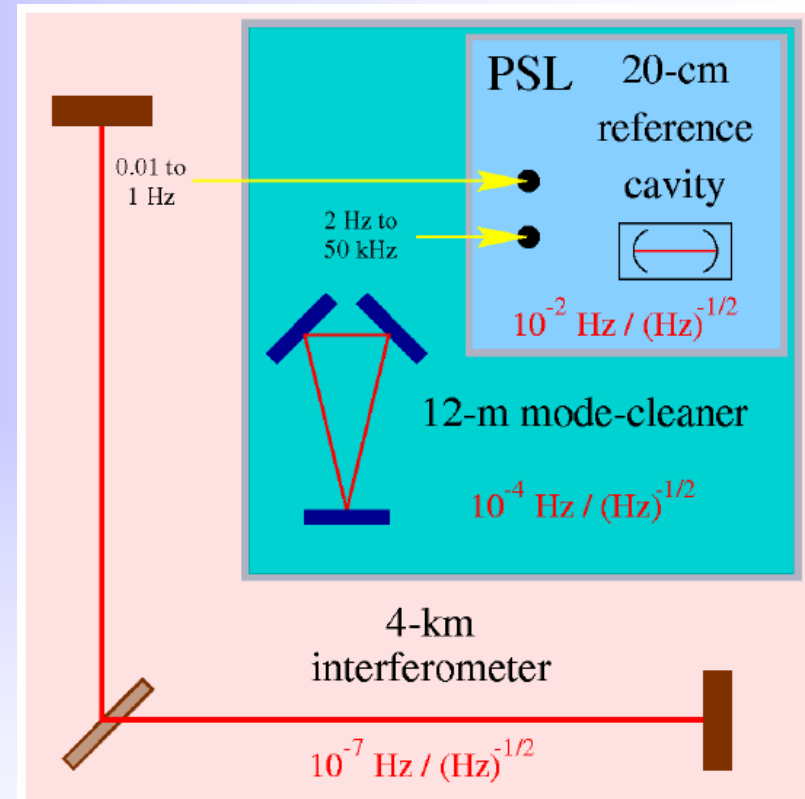


- PM - (OK)
- AM - PM between polarizers (drawback: unwanted phase modulation)
- Creation of complex modulation is possible:

$$f(t) = i\phi_a(t) + i\phi_p(t) + \alpha(t)$$



- Nested control loops
  - Stage 1 – thermally-20 cm long stabilized reference cavity
  - Stage 2 – in vacuum suspended 12 or 15 m long “mode cleaner” cavity
  - Stage 3 – Fabry Perot arm cavities



$$\Delta f/f \sim 3 \times 10^{-22} @ 100 \text{ Hz}$$