

Searching for Gravitational Waves with LIGO: A New Window on The Universe

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Overview

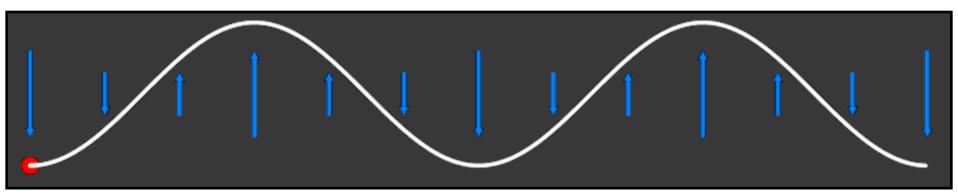
- So far, our knowledge of the universe comes from observing electromagnetic radiation, neutrinos and cosmic rays
- Einstein's theory of General Relativity predicts gravitational waves
- So far there has been no direct detection of gravitational waves
- Their detection would open a new window on the universe
- One of the most promising sources are **binary inspirals**
- What are gravitational waves? What are binary inspirals? How do we search for inspirals and what might we learn when we see them?





Electromagnetic Waves

- From Maxwell's equations in empty space, we can derive wave equations for the Electric and Magnetic fields
- Oscillating charges generate electromagnetic waves



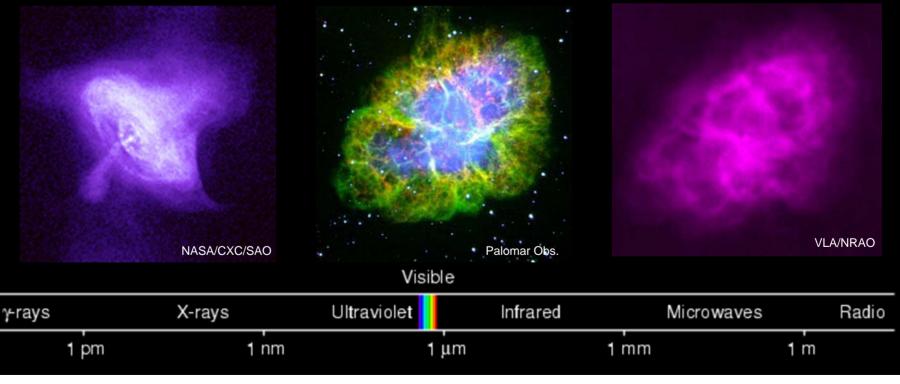
• Different wavelengths make up electromagnetic spectrum





Electromagnetic Astronomy

• Observing electromagnetic waves at different frequencies gives us different views of the universe





- Gravitational waves are not just a different wavelength: they are a different spectrum!
- What will we see when we observe the universe with gravitational waves?





Gravitational Wave Astronomy

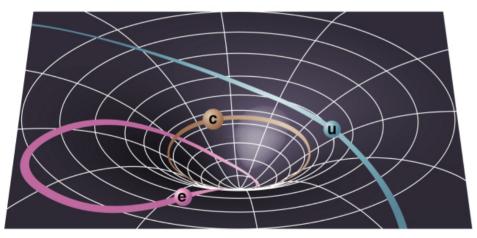
- Gravitational waves interact very weakly with matter
- We will see deep into regions inaccessible to electromagnetic observations
- See far back in to the early universe, beyond the cosmic microwave background
- Detection of gravitational waves would give us astronomy and physics!





General Relativity

• Einstein's theory of general relativity describes gravity as curvature of spacetime



 Gravitational fields are described by Einstein's equation's

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

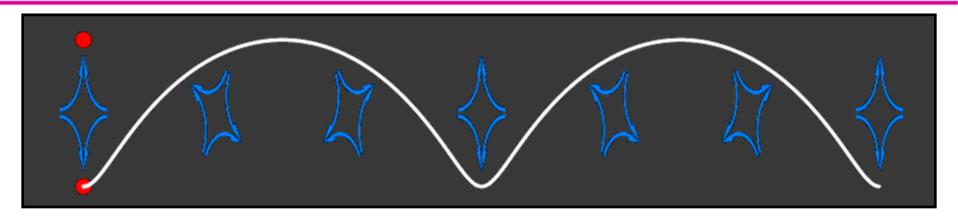
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 Matter tells space how to curve and space tells matter how to move





Gravitational Waves



- Oscillating masses will produce gravitational waves
- But unlike electric charge, mass only has one sign
- Need oscillating quadrupoles: spinning dumbbell shape

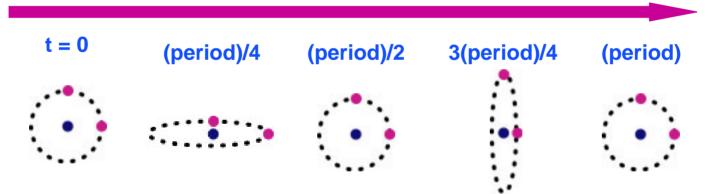




Effect of a Gravitational Wave

• As gravitational waves pass, they change the distance between neighboring bodies

Time



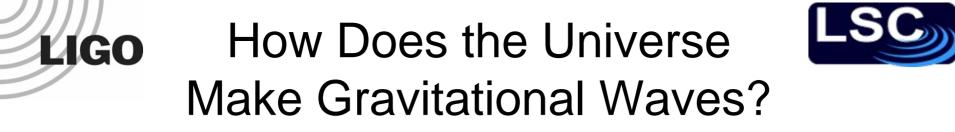
 Strength of a gravitational wave is given by the strain h(t) = change in length / length

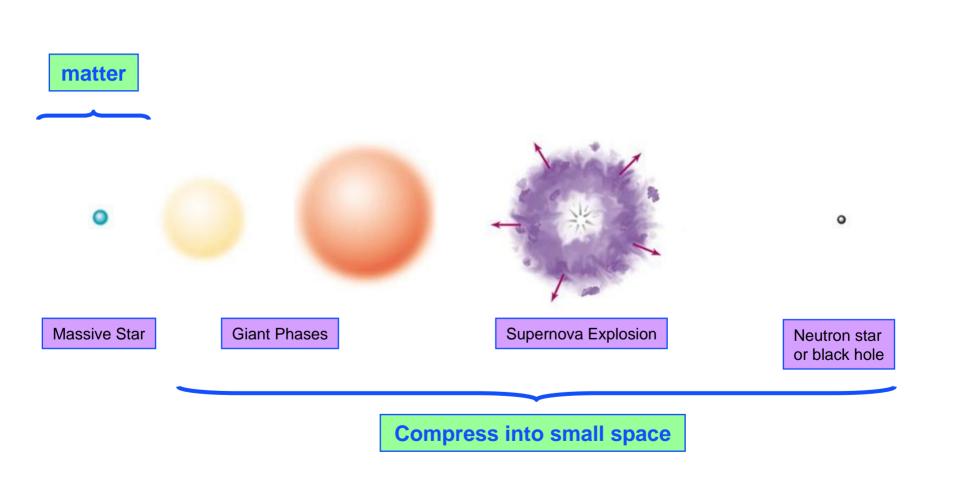
Generation of Gravitational Waves

- Problem: it's hard to make gravitational waves...
- Power radiated

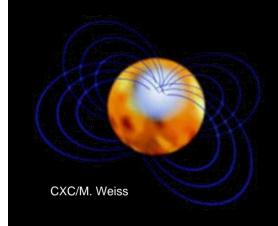
$$P_{\rm EM} \sim c^2 = 10^{17}$$
 $P_{\rm GW} \sim \frac{G}{c^5} = 10^{-53}$

- Need a lot of mass in a small space...
- Need the matter to be moving very fast...

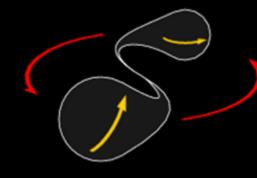




LIGO Sources of Gravitational Waves



Continuous sources: Spinning neutron stars



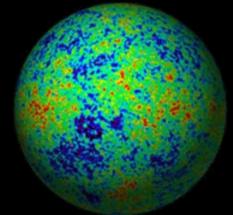
Binary inspirals: "long bursts" of gravitational waves

as stars inspiral

and merge



"Short bursts:" Supernovae, transient sources, ???



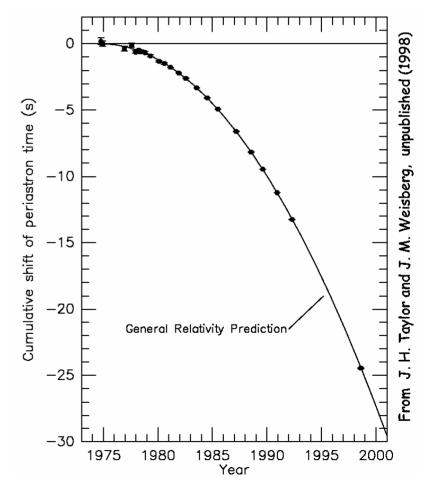
Gravitational wave backgrounds: relic radiation from the big bang





Observation of Inspirals

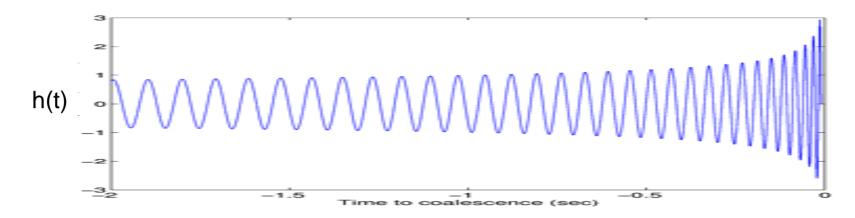
- No direct detection of gravitational waves yet...
- But we have observed binary neutron stars through their radio emissions!



QuickTime[™] and a YUV420 codec decompressor are needed to see this picture.



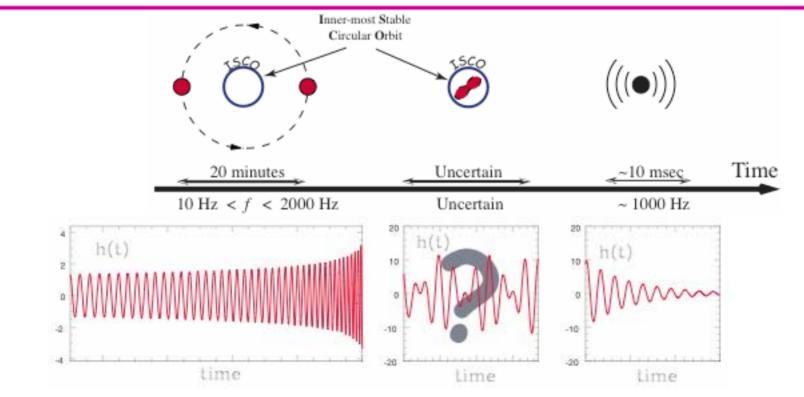
Gravitational Waves from Inspirals



- The frequency of gravitational waves is twice the orbital frequency
- The amplitude increases as the separation decreases
- Putting this all together... the gravitational wave is a chirp



Evolution of Binary System

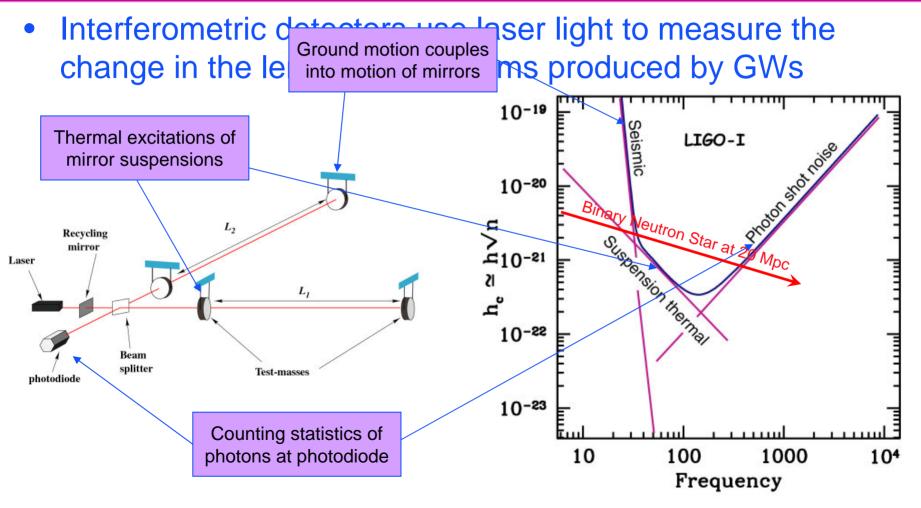


- Gravitational wave strains on earth are h(t) ~ 10⁻²¹
- How do we look for them?



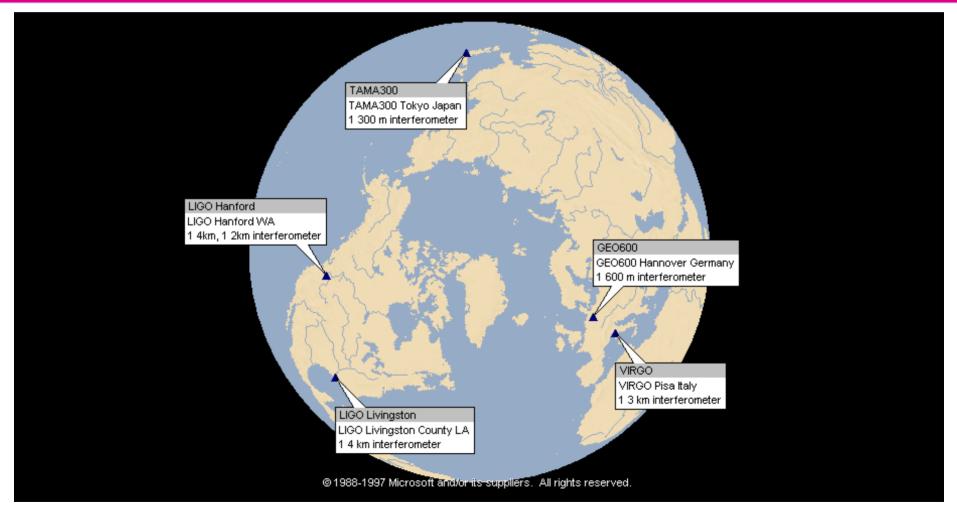


Detection of Gravitational Waves





A World Wide Network







The LIGO Detectors

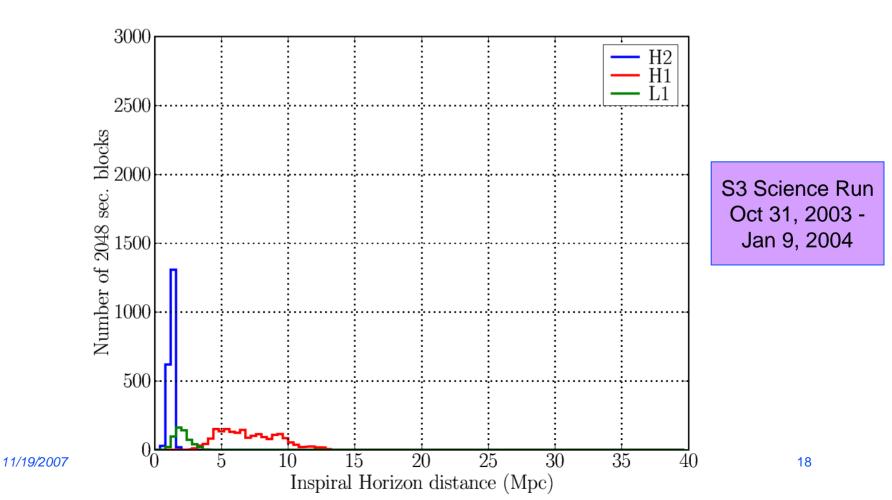






Sensitivity Improvement

Distance to optimally oriented 1.4,1.4 solar mass BNS at SNR = 8

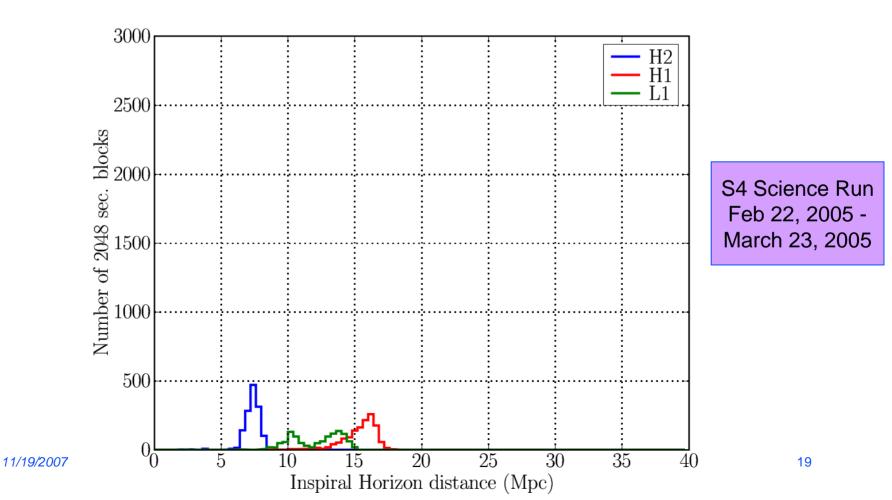






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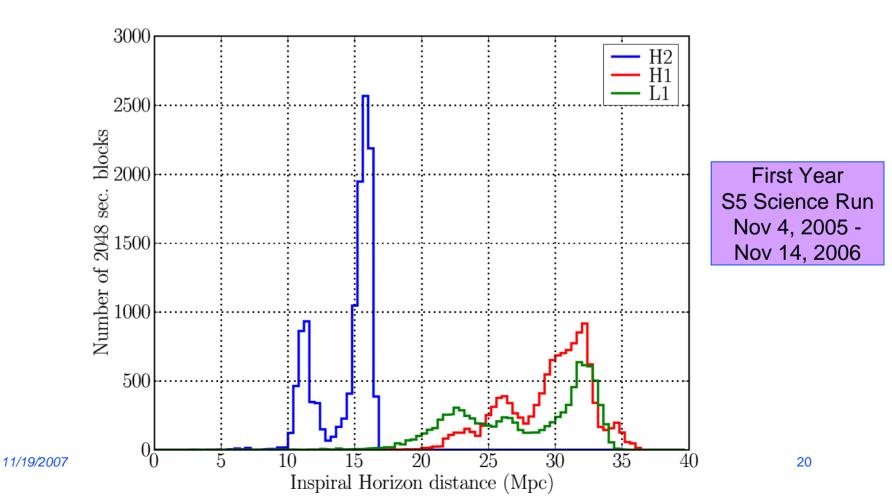






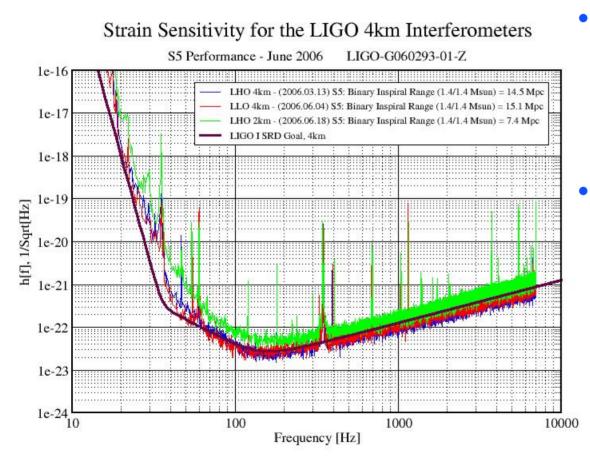
Sensitivity Improvement

Distance to optimally oriented 1.4,1.4 solar mass BNS at SNR = 8





The Fifth Science Run Nov 5, 2005 - Oct 1, 2007



- Recorded one year of
 coincident data from the
 three LIGO detectors at
 design sensitivity
- LIGO is sensitive to binaries consisting of neutron stars and black holes with

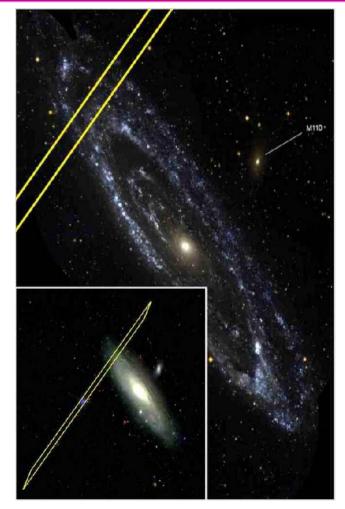
 $M_{\rm total} \lesssim 100 M_{\odot}$



LIGO is already doing astrophysics...



- Gamma Ray Burst 070201
- Short Hard GRB located by five electromagnetic satellites
- SH-GRBs are thought to have inspiral progenitors
- Location error box overlaps the spiral arms of Andromeda (D ~ 770 kpc)
- LIGO Hanford detectors were operating at the time of the GRB

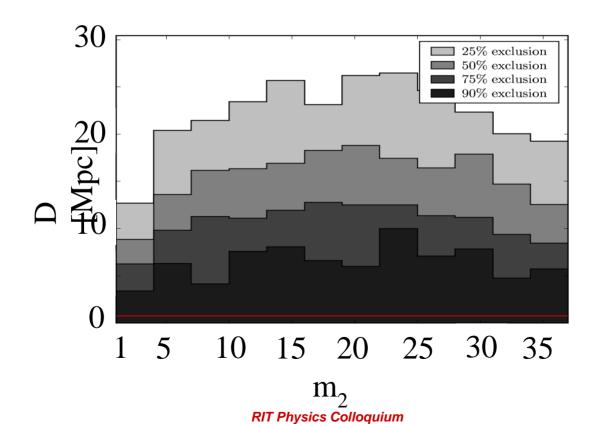






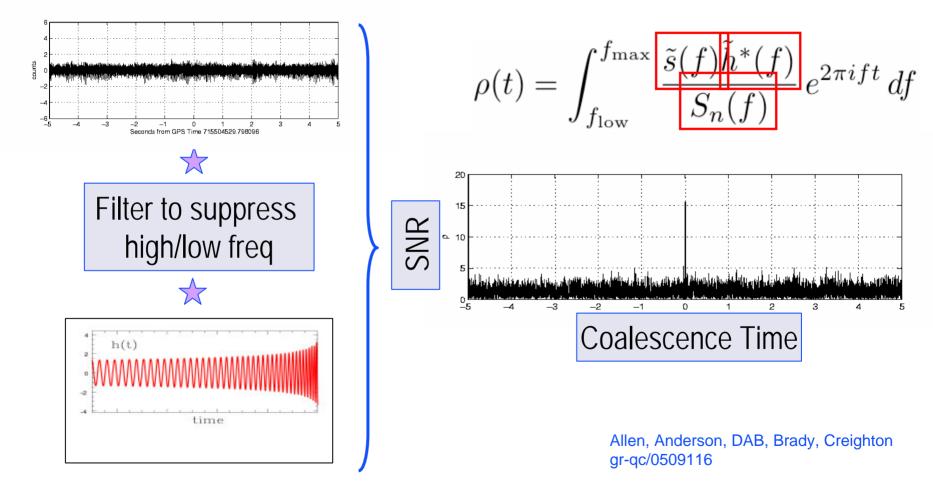
GRB070201

• Inspiral in Andromeda with masses $1.0 < m_1 < 3.0 M_{sun}$ and $1.0 < m_2 < 40 M_{sun}$ excluded at > 99% confidence





Matched Filtering







Mismatch

- What if the template is incorrect?
- Loss in signal to noise ratio is given by the mismatch

$$\begin{aligned} \text{mismatch} &= 1 - \text{match} \\ \text{match} &= \max_{t_0,\phi_0,\mathcal{M},\eta,\dots} \frac{\langle h | h_{\text{true}} \rangle}{\sqrt{\langle h | h \rangle \langle h_{\text{true}} | h_{\text{true}} \rangle}} \\ \\ &\left\langle a | b \right\rangle = \int_{f_{\text{low}}}^{f_{\text{max}}} \frac{\tilde{a}(f) \tilde{b}^*(f)}{S_n(f)} \, df \end{aligned}$$





Mismatch and Event Rate

- Any mismatch between signal and template reduces the distance to which we can detect inspiral signals
- Loss in signal-to-noise ratio is loss in detector range
- Loss in event rate = $(Loss in range)^3$
- Initial LIGO binary neutron star rate ~ 1/3 years
- We must be careful that the mismatch between the signal and our templates does not unacceptably reduce our rate





Current Inspiral Waveforms

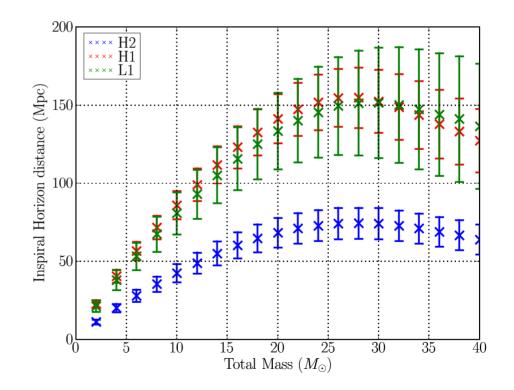
- Current LIGO inspiral searches use "post-Newtonian" waveforms
- These augment a simple "Newtonian" analysis of inspiralling binaries with relativistic corrections

$$\mathcal{F} = \frac{32}{5} \frac{G^4}{c^5} \frac{M^3 \mu}{r^5} \left\{ 1 + \left(-\frac{2927}{336} - \frac{5}{4} \eta \right) \frac{GM}{rc^2} + 4\pi \left(\frac{GM}{rc^2} \right)^{\frac{3}{2}} \right. \\ \left. + \left(\frac{293383}{9072} + \frac{380}{9} \eta \right) \left(\frac{GM}{rc^2} \right)^2 \right. \\ \left. + \left(-\frac{25663}{672} - \frac{125}{8} \eta \right) \left(\frac{GM}{rc^2} \right)^{\frac{5}{2}} + \cdots \right\}$$

Blanchet, Iyer, Will, Wiseman CQG **13** 575 (1996)

LIGO How Good are these Waveforms?

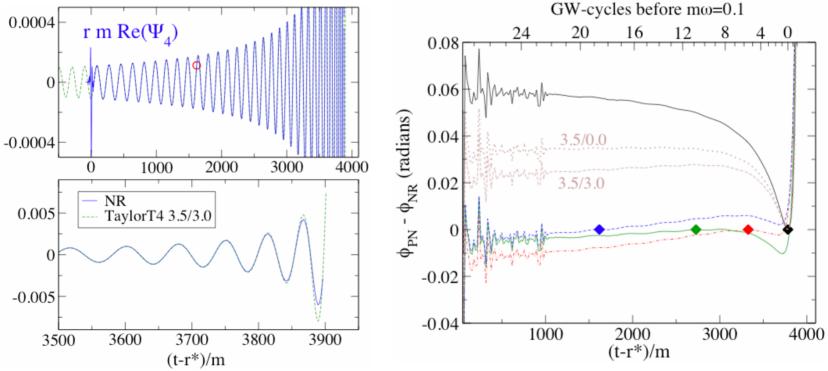
- PN waveforms are great for neutron star binaries where v/c is small while gravitational waves are in the LIGO band
- But the post-Newtonian expansion may fail if v/c is large as in the case of binary black holes in the LIGO band
- Signal strength increases with mass!
- Need numerical relativity...





What can LIGO learn from NR?

- Compare theoretical waveforms with numerical "signals"
- PN looks good for all equal mass inspiral signals

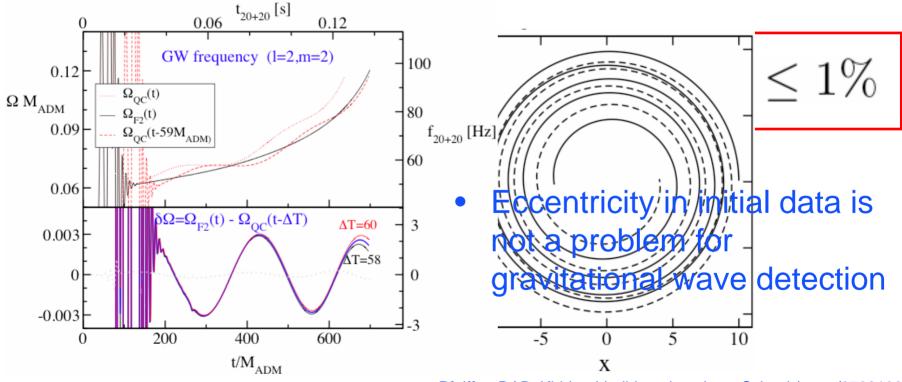


Boyle, DAB, Kidder, Mroue, Pfeiffer, Scheel Cook Teukolsky (arxiv:0710.0158, to appear in PRD)

LIGO

LS What Can NR Learn From LIGO?

• Numerical initial data is not quite inspiralling: no initial radial velocity... not the case for real inspirals!

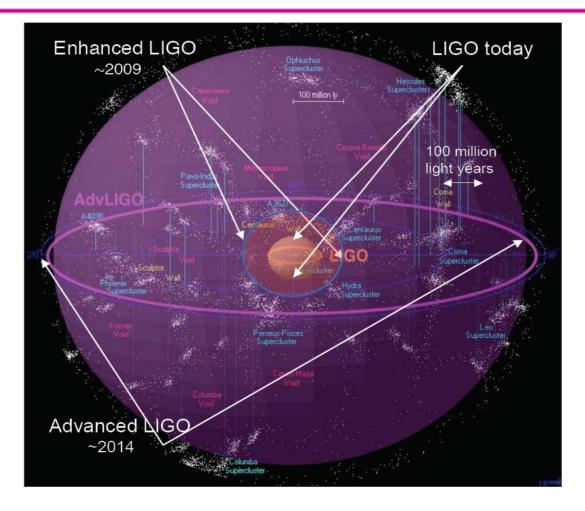


Pfeiffer, DAB, Kidder, Lindblom, Lovelace, Scheel (gr-qc/0702106)





What's next for LIGO?

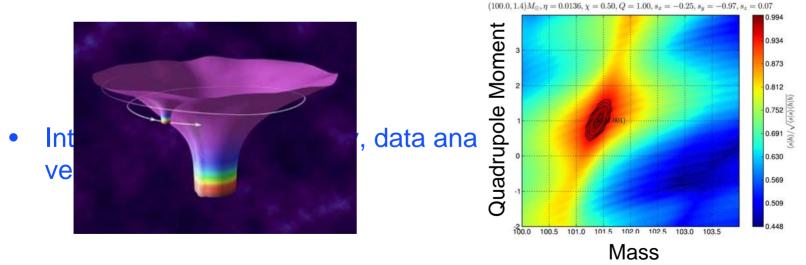




What happens when we see something?



- Goal is to extract as much physics from the gravitational waves as possible!
- Compare **observations** with post-Newtonian and numerical simulations: test GR in the strong field regime...
- With Advanced LIGO detectors, we may be able to map the spacetimes around massive black holes...



DAB, Fang, Gair, Li, Lovelace, Mandel, Thorne (PRL 99 201102)





Conclusion

- The fifth science run is complete and analysis of data is underway
 » We may see something!
- Enhancements to the initial detectors are scheduled for ~ 2009
 - » Factor of ~ 2 increase in sensitivity
- Funding for Advanced LIGO is scheduled to begin in 2008
 - » Factor of ~ 10 increase in sensitivity
- Numerical relativity is making great progress
 - » Interaction between the two communities is very important
- These are exciting time for gravitational-wave astrophysics!