

Hartmann Sensor for advanced gravitational wave interferometers

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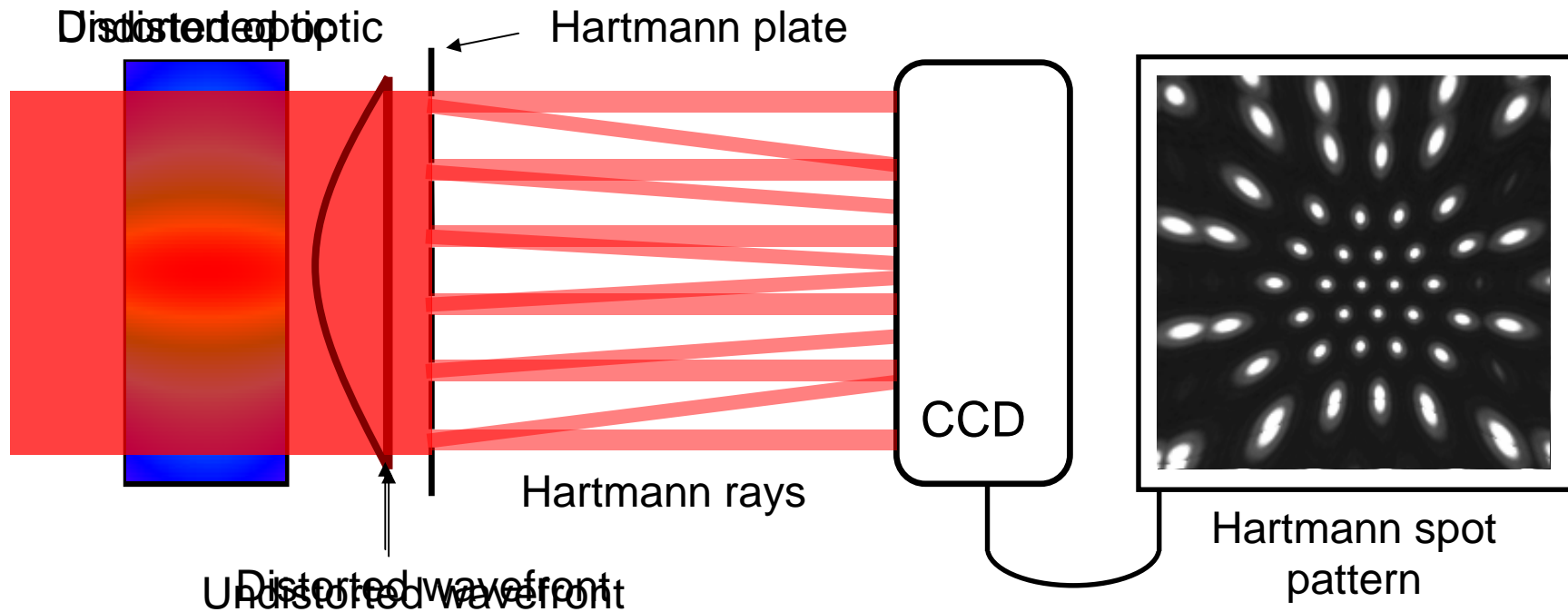
Outline of Talk

- Hartmann wavefront sensor
- Experimental validation
- Tomographic capabilities

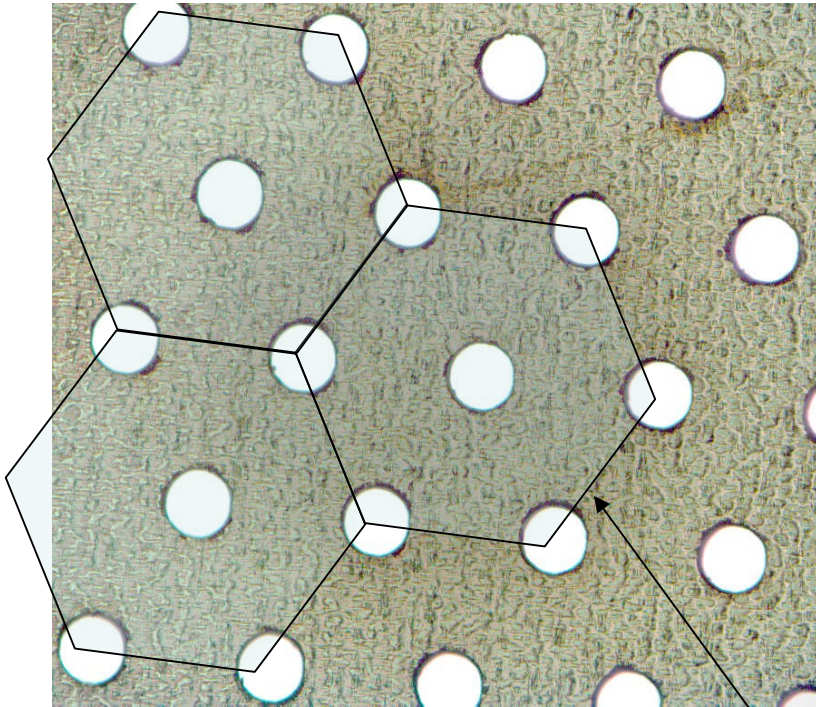
Objectives

- Develop versatile, robust wavefront sensor
- Distortion must ultimately be corrected to $\lambda/100$
- Sensor needs to have sensitivity $\ll \lambda/100$
- Sensor should not interfere with input mirrors or GWI laser beam.
- Sensor suitable for wavefront servo

Hartmann Wavefront Sensor: How It Works



Optimized Hartmann Plate



Hexagonal cells added to highlight arrangement

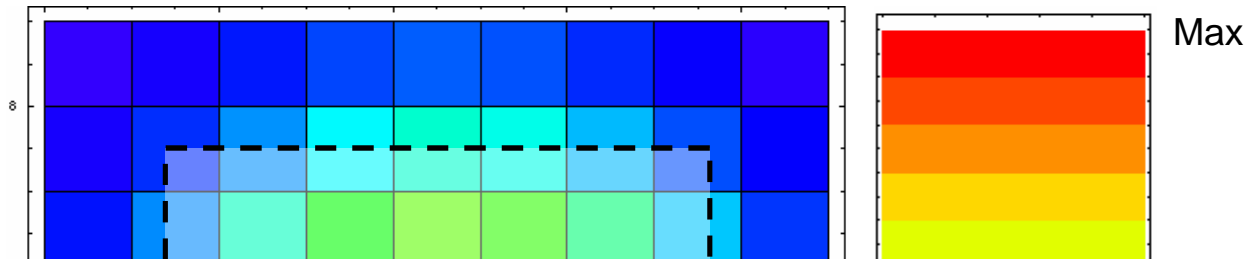
- Optimized for distortion in advanced GWIs
 - Spatial resolution
 - Sensitivity

| | |
|-----------------|-------------|
| Hole size | 150 μ m |
| Hole spacing | 430 μ m |
| Distance to CCD | 10mm |

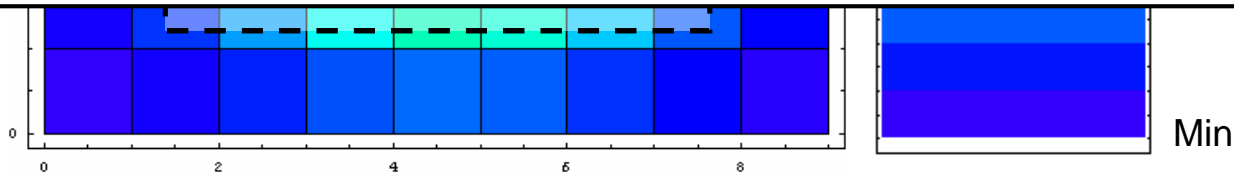


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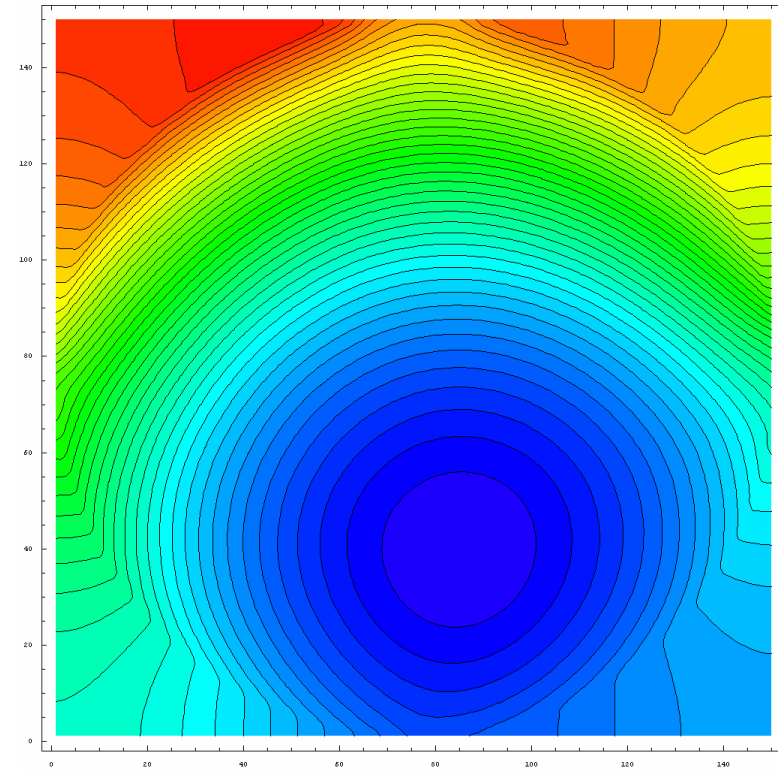
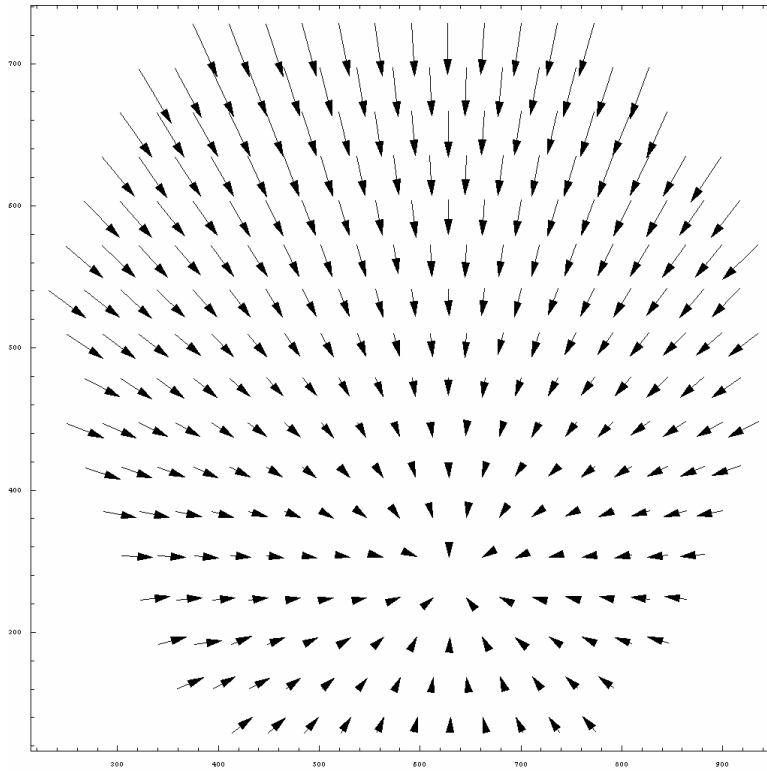
Centroiding Single Hartmann Spot to Sub-Pixel Accuracy



- Fractional centroiding algorithm allows positioning of centroid to approximately (pixel size) / (number of grayscale levels)
- Dynamic Range of Camera \cong 11.5 bits.
- Pixel Size = $12\mu\text{m}$
- Theoretical Accuracy of centroid \cong 4nm

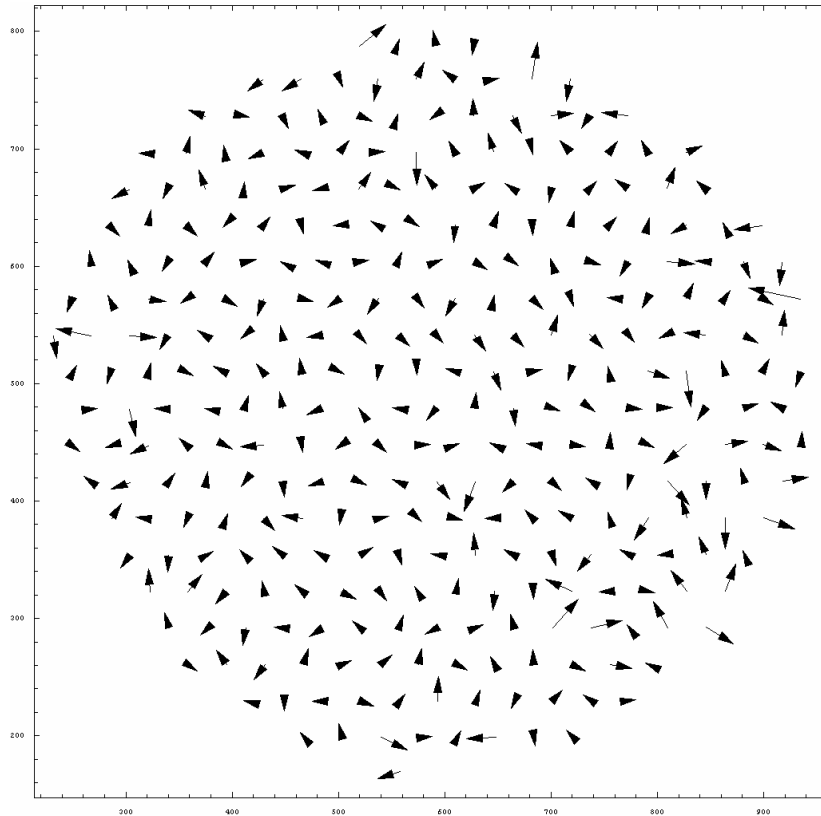


Hartmann Wavefront Sensor: How It Works

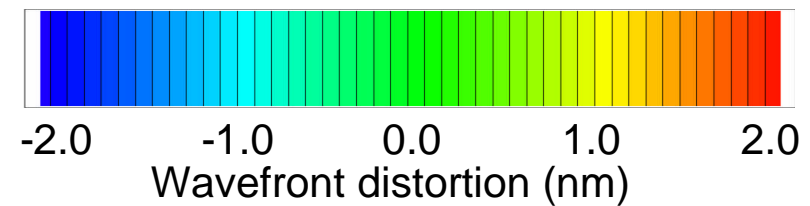
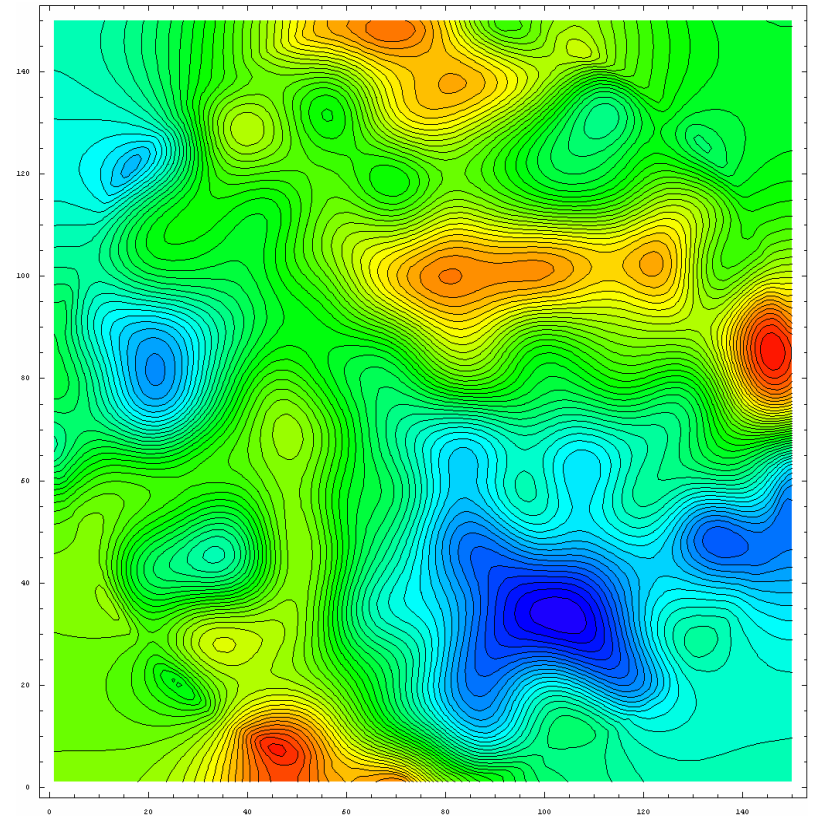


- Spot displacement proportional to ***gradient*** of wavefront
- We can locate spots $\pm 20\text{nm}$

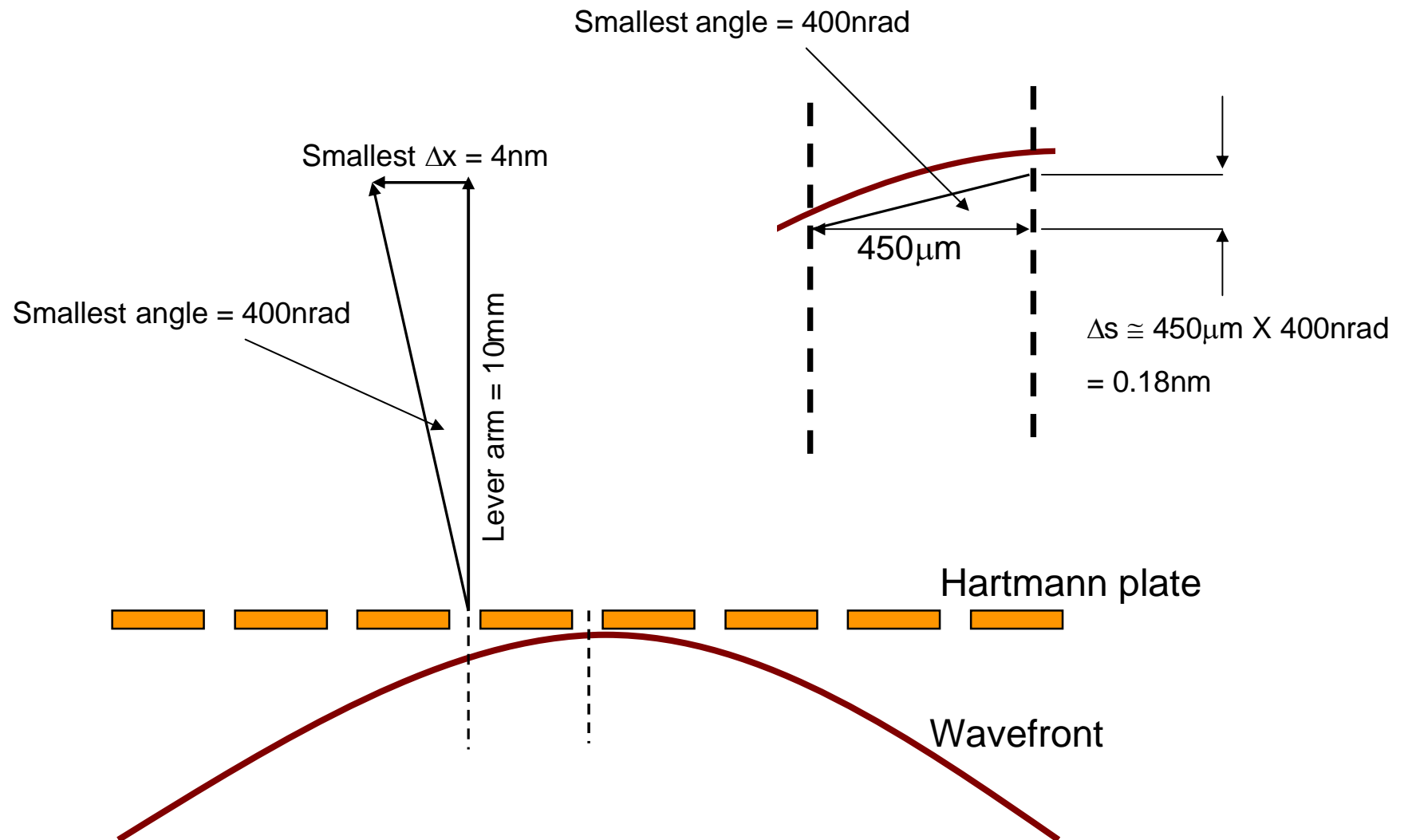
Sensor Has Very Low Noise



RMS noise = $\lambda/1100$



Sensor accuracy



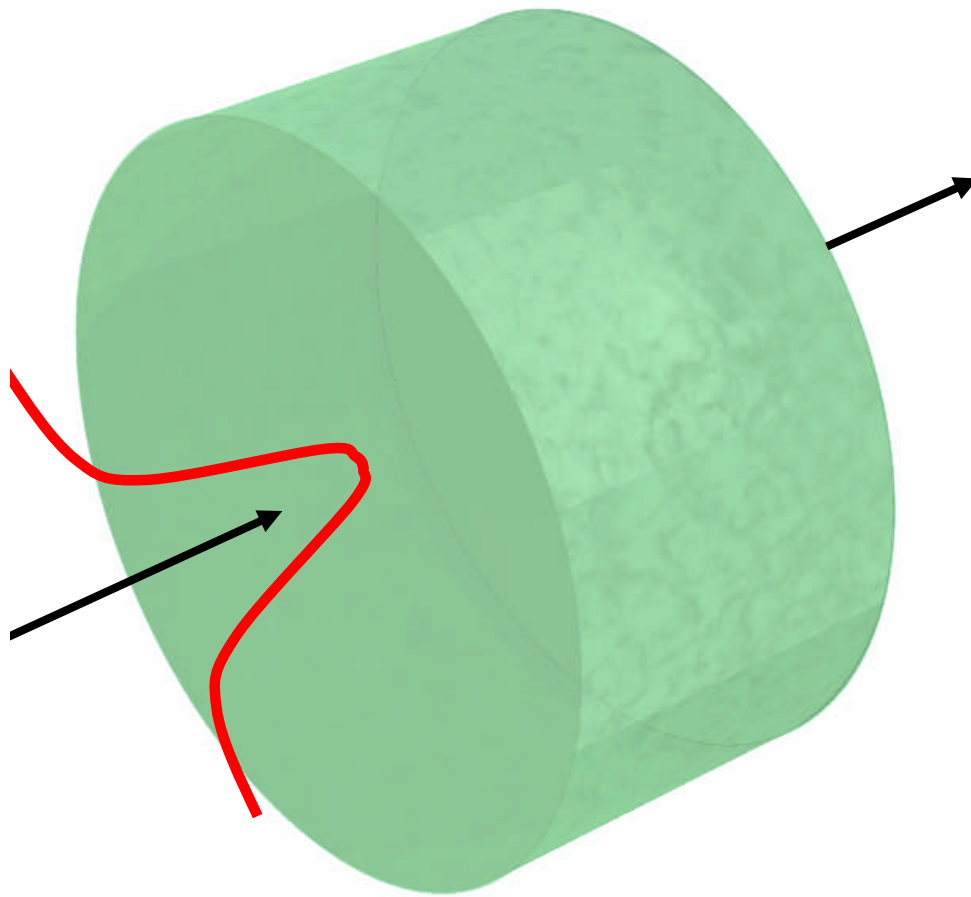
Hartmann Sensor

- Very low noise, because each pixel is separate against a dark surround, due to the optimization of hole size, separation and lever arm
- Superior to other sensors (eg Shack Hartmann, Interferometers etc)
- Suitable for wavefront correcting servo system

Hartmann Sensor

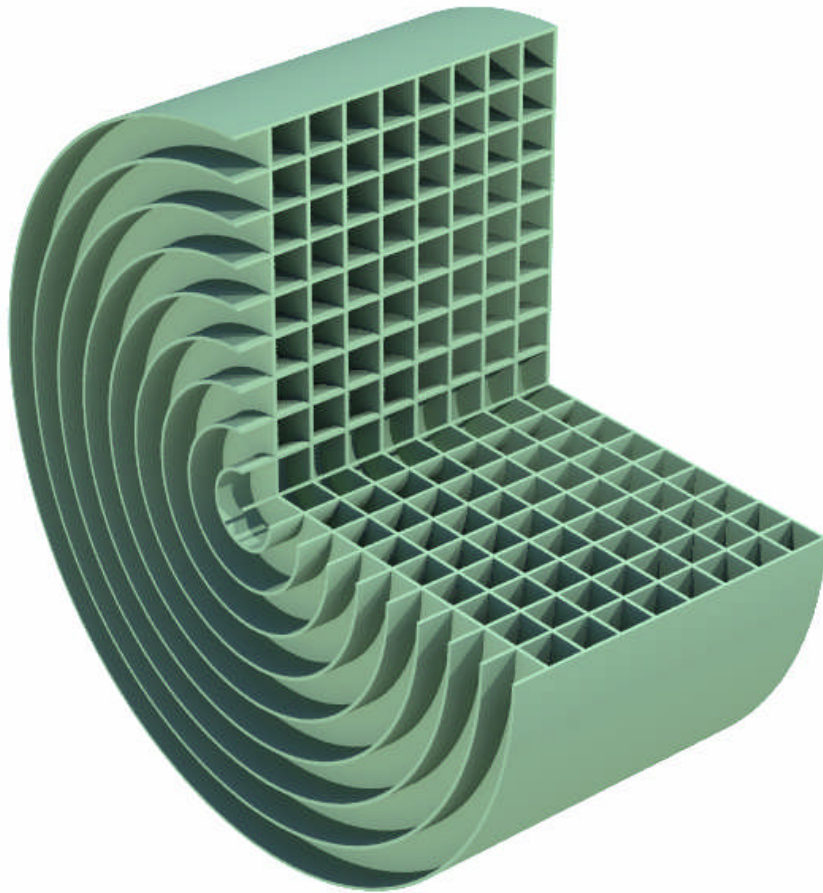
- On axis
- Off axis
- Tomography
(more than one off axis view)

Single View Optical Tomography Works for Cylindrical Symmetry



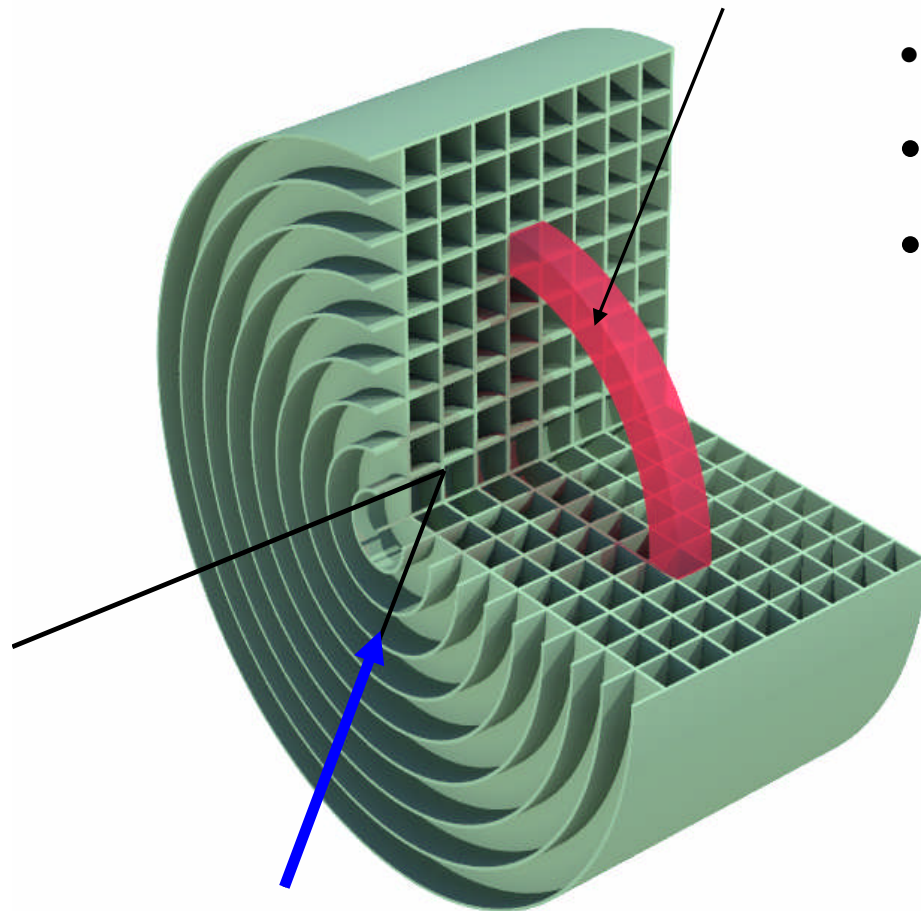
- E.g. Distortion induced by absorption of Gaussian beam heating an isolated optic

Representation of Refractive Index Distribution in Distorted Optic



- Divide into annular volume elements (voxels)
- Cylindrical symmetry assumed

Wavefront Distortion Analyzed with Radon Transforms



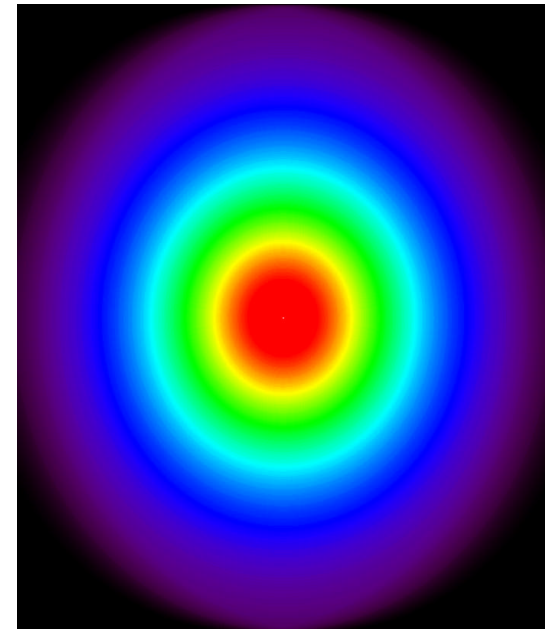
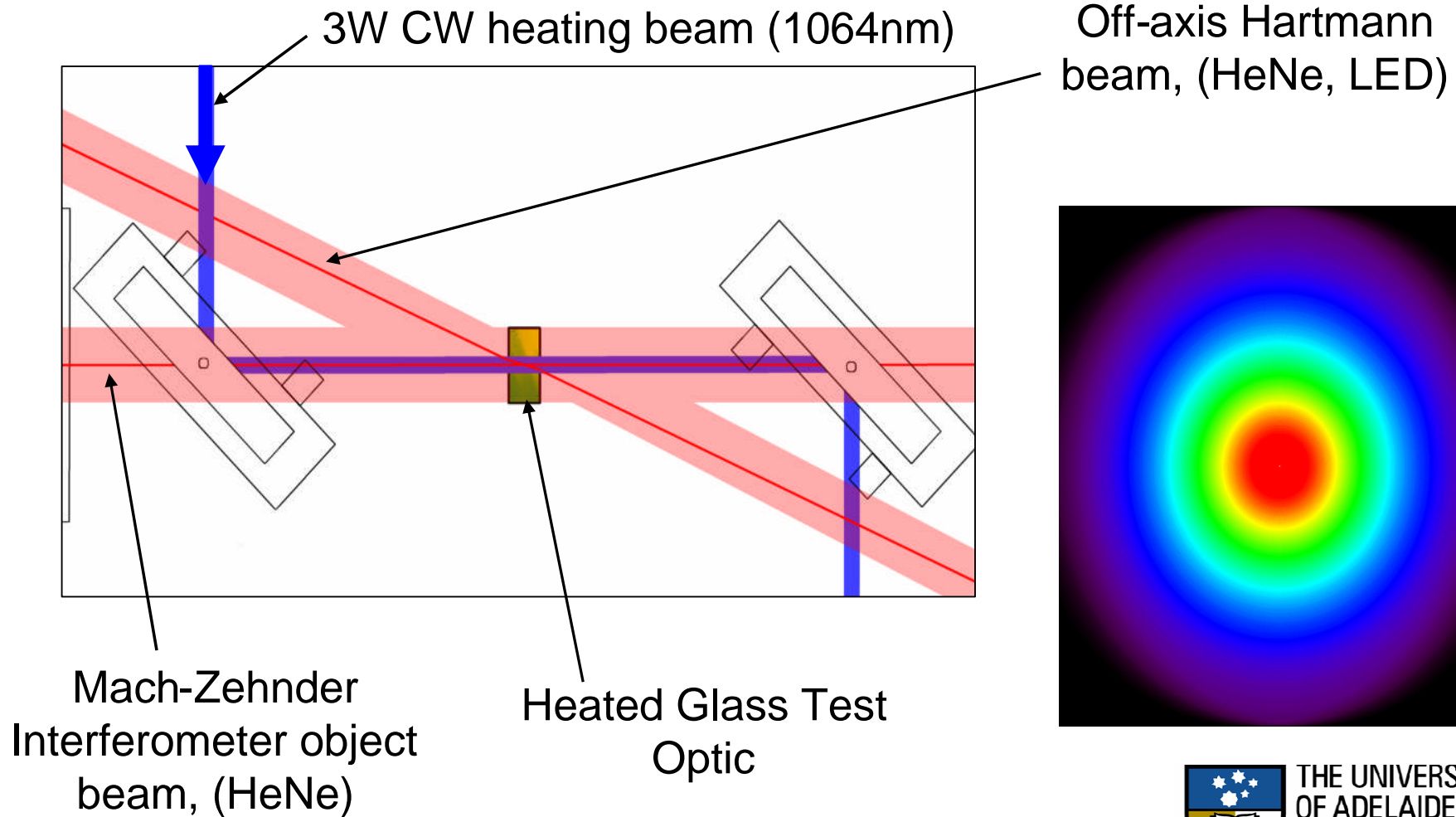
- Voxel_{I,J} has uniform refractive index
- Radon Transform of Voxel_{I,J}
- Fit mode to wavefront distortion

Off axis viewing angle, θ

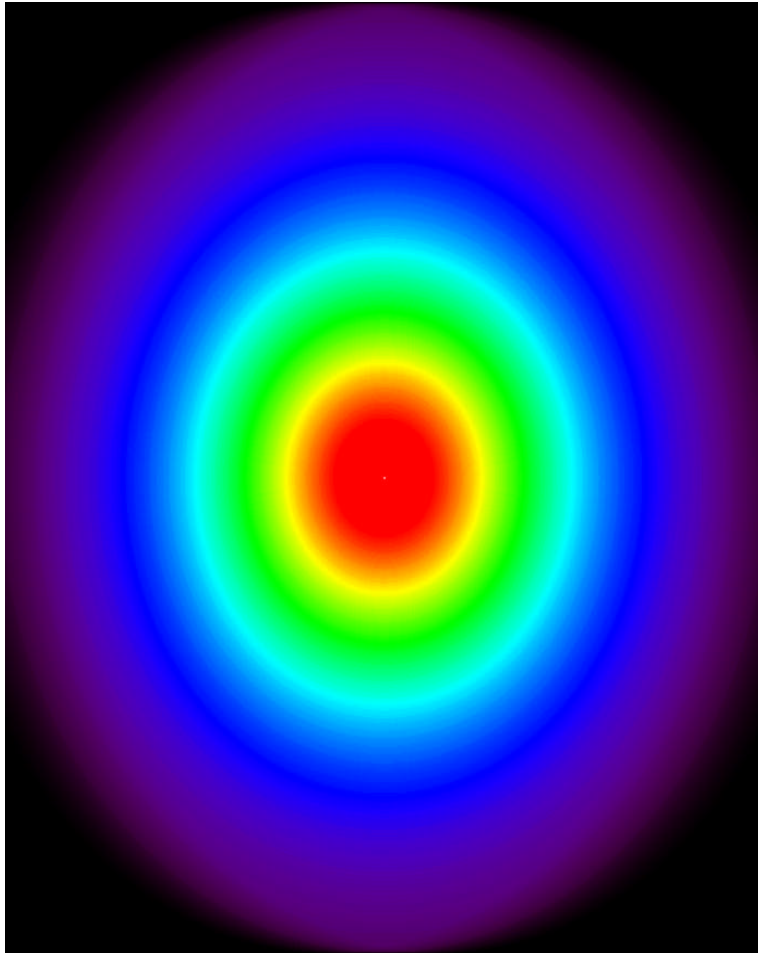
Experimental Objectives

- Demonstrate that tomographic sensor works
- Validate results with independent high precision on-axis interferometer
- Experiment constructed to mimic distortion in Advanced LIGO

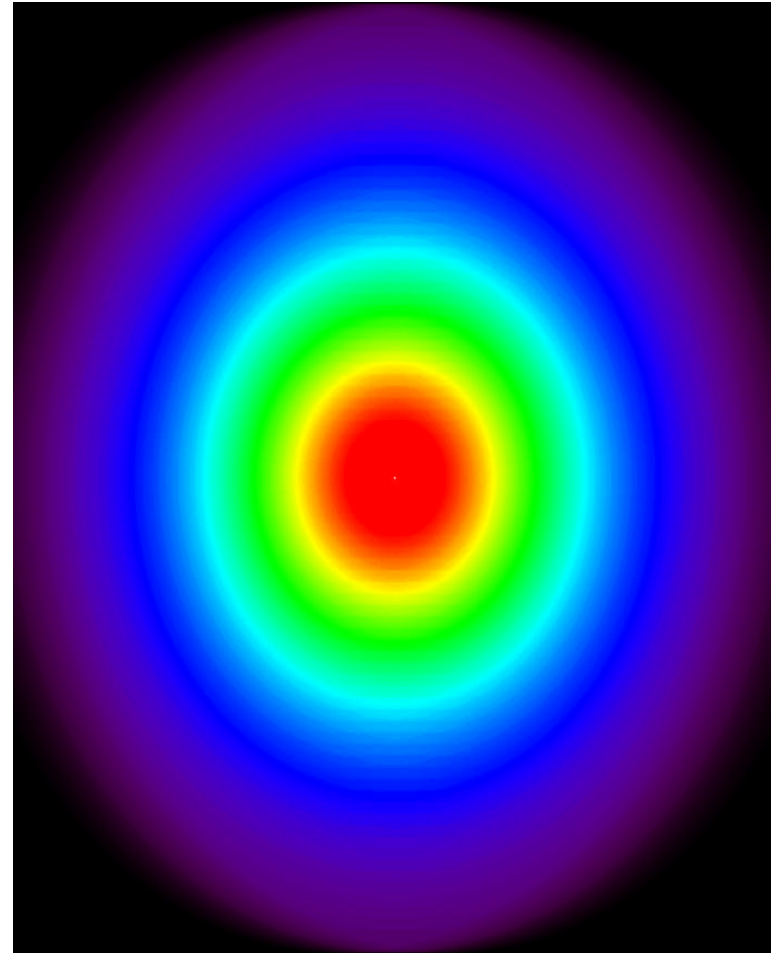
Experiment to Show Sensor Works



Simulation of Experiment Results

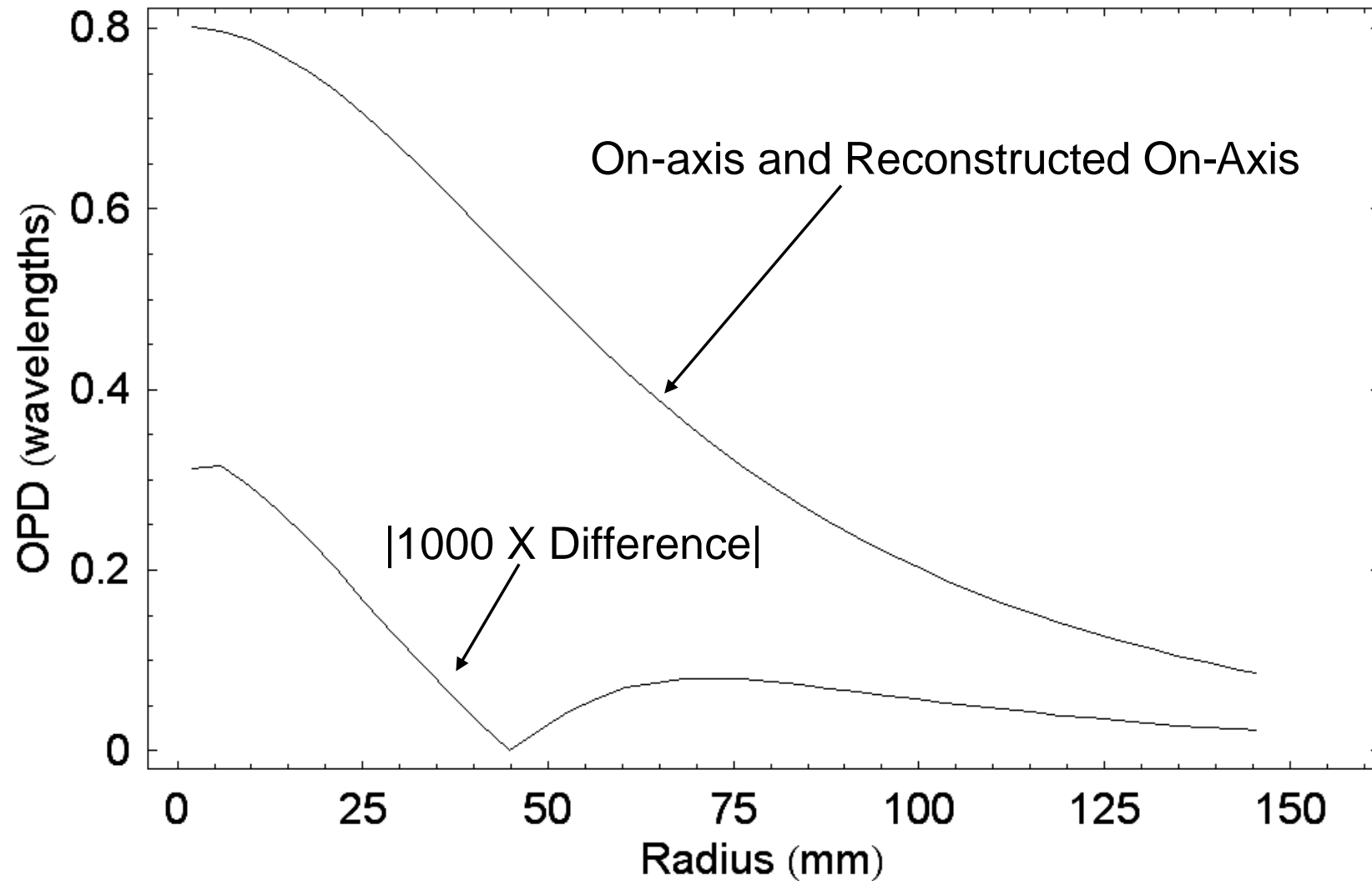


Original off-axis OPD

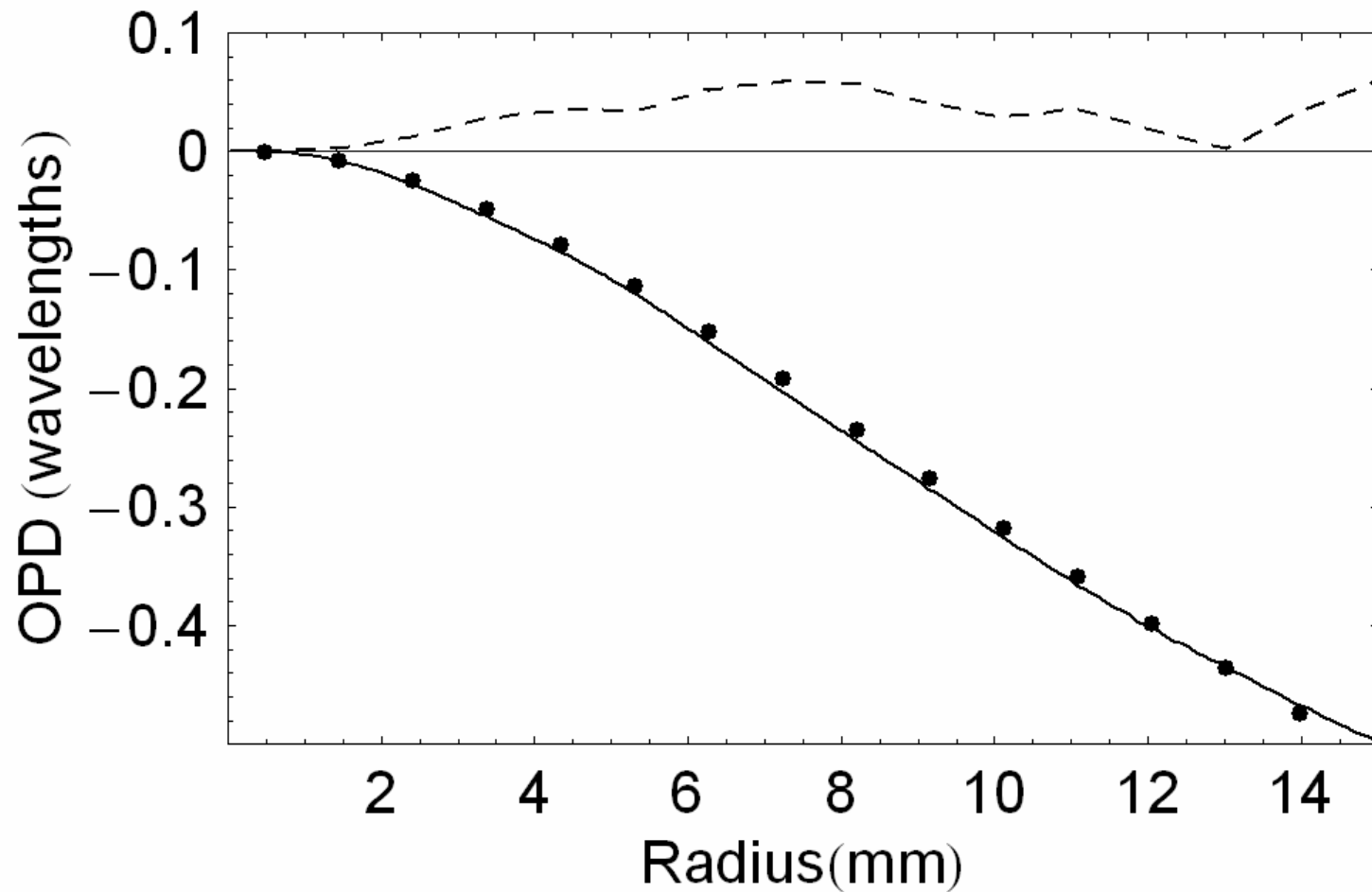


Best fit with voxel projections

Simulation shows Tomographic Analysis is Accurate



Off axis reconstruction agrees exactly with on axis interferometer



Dashed line: 5 x absolute difference, dots: reconstruction

Conclusion

- Hartmann sensor has accuracy and sensitivity required for advanced interferometers
- Current RMS Noise of sensor $\sim \lambda/1100$
- Advantageous for both **on axis** and **off axis**
- Voxel analysis shown to be accurate
- Initial experimental results are promising
- Can extend to non-cylindrically symmetric distributions – use multiple views and azimuthal voxelation
- Ideal for active feedback servo systems

