

# **Design of Stable Power-Recycling Cavities**

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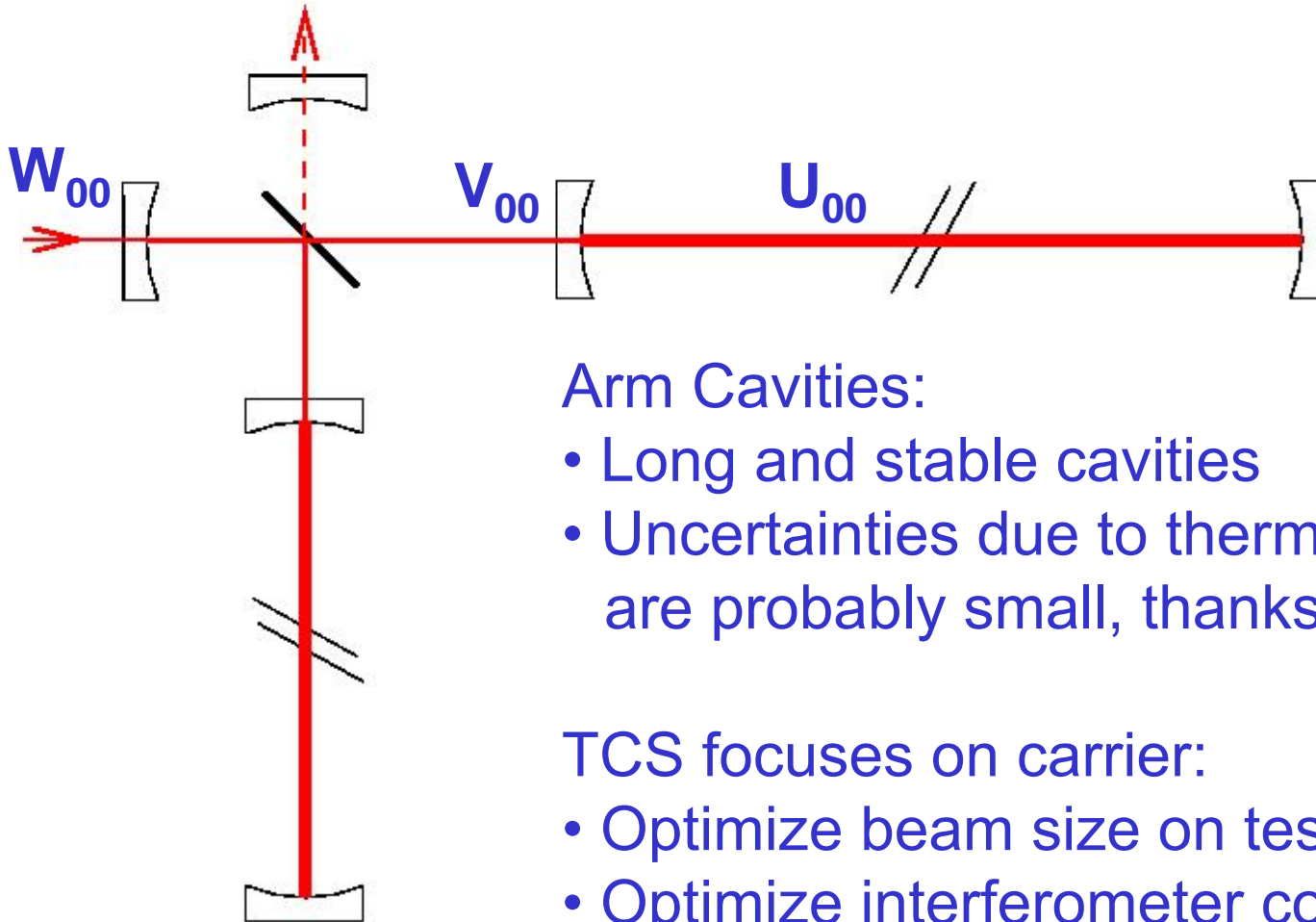
**10/05/2005**



**UNIVERSITY OF  
FLORIDA**



- Stable vs. unstable recycling cavities
- Design of stable recycling cavity
- Design drivers
  - Spot size
  - Vacuum envelope
  - Seismic Isolation
  - Flexibility in mode matching
  - Alignment
  - Modulation frequency / linewidth effects
- Conclusions/Outlook

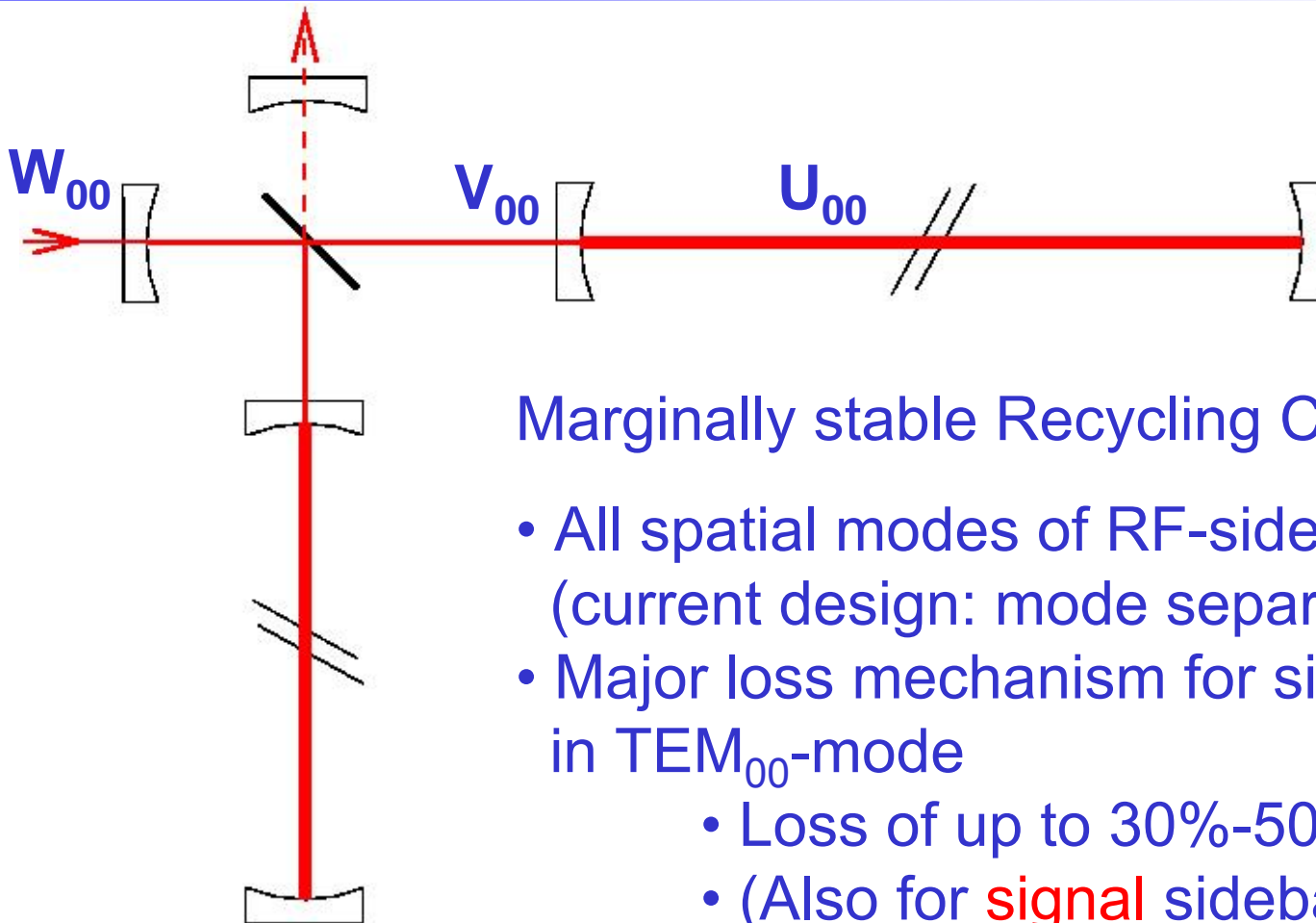


### Arm Cavities:

- Long and stable cavities
- Uncertainties due to thermal lensing are probably small, thanks to TCS

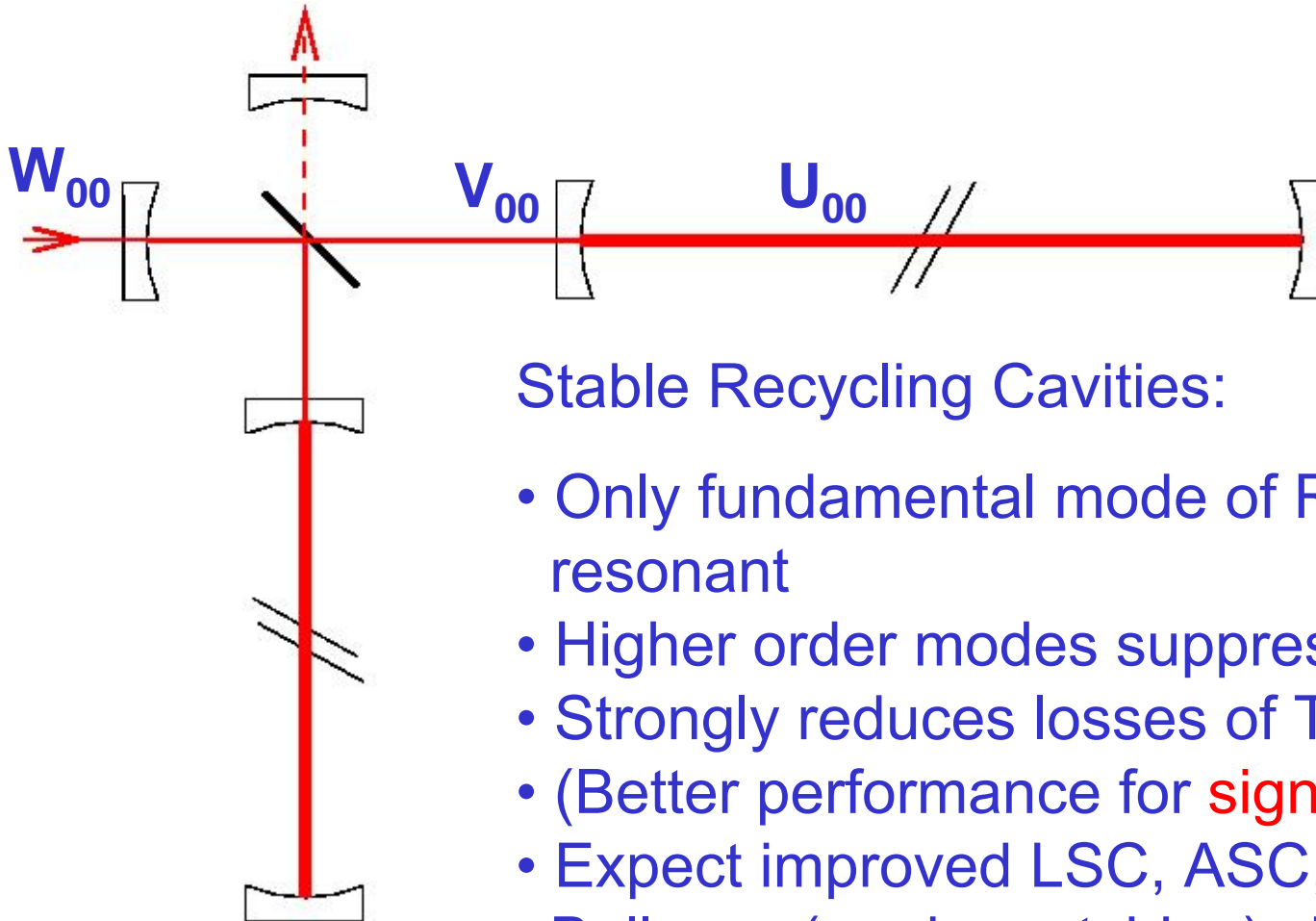
### TCS focuses on carrier:

- Optimize beam size on test masses
- Optimize interferometer contrast
- Optimize mode matching(?)



### Marginally stable Recycling Cavities:

- All spatial modes of RF-sidebands resonant (current design: mode separation  $\approx 4$  kHz)
- Major loss mechanism for sidebands in  $TEM_{00}$ -mode
  - Loss of up to 30%-50%
  - (Also for **signal** sidebands!)
- Impact on LSC and ASC



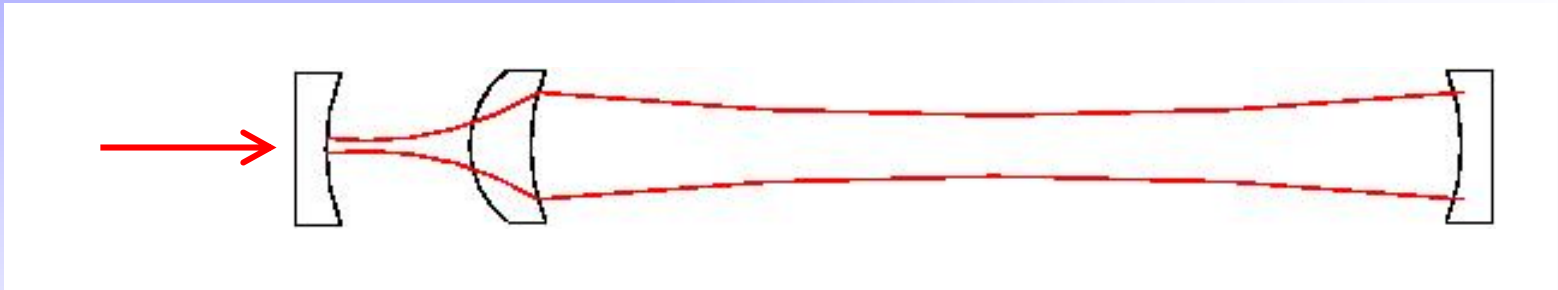
### Stable Recycling Cavities:

- Only fundamental mode of RF-sidebands resonant
- Higher order modes suppressed
- Strongly reduces losses of  $TEM_{00}$ -mode
- (Better performance for **signal** sidebands)
- Expect improved LSC, ASC, and even Bullseye (mode matching) signals
- Interferometer will be much easier to understand and debug

How? (mirror needed inside the Rayleigh range of the modes)

Solution 1:

- Lens in ITM substrate



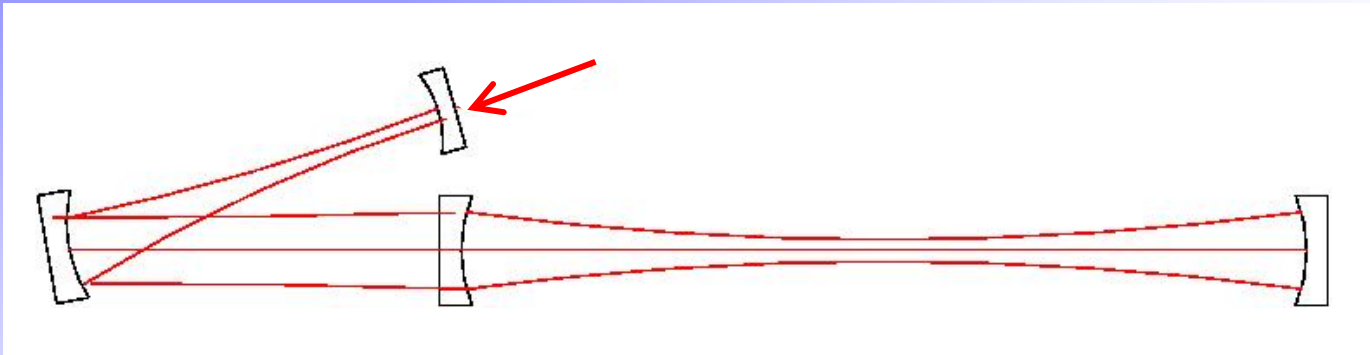
**Problem:**

Divergence angle:  $\alpha \sim 6 \text{ cm} / 8 \text{ m} \sim 7 \text{ mrad}$

→ Waist:  $w_0 = \lambda / \pi \alpha \sim 50 \text{ } \mu\text{m}$

Creates sub mm beam size on  
Recycling mirror ( $\sim 290 \text{ GW/m}^2$ )

- Two mirror Recycling cavity

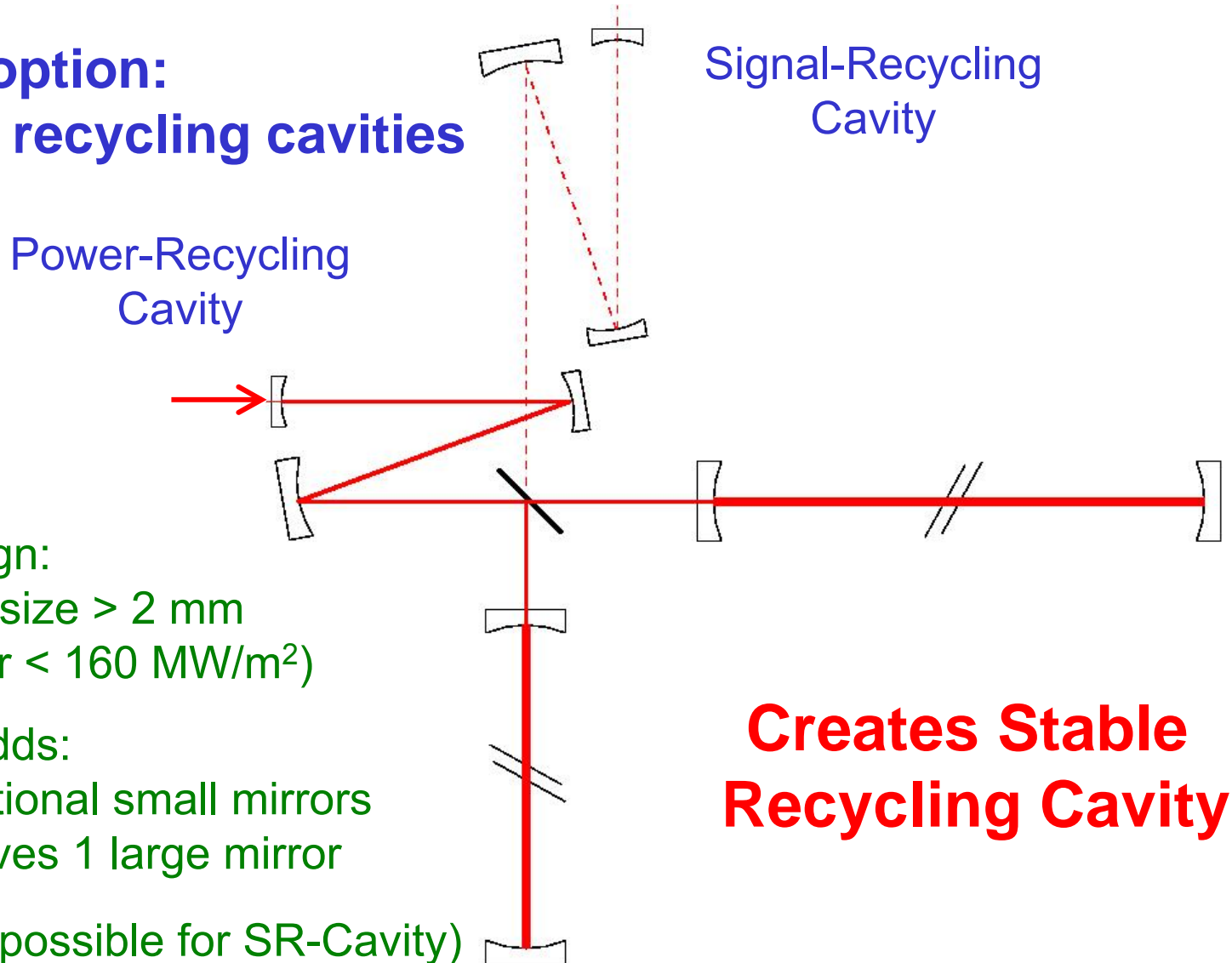
**Problem:**

Divergence angle:  $\alpha \sim 6 \text{ cm}/16 \text{ m} \sim 4 \text{ mrad}$

→ Waist:  $w_0 = \lambda/\pi\alpha \sim 90 \text{ }\mu\text{m}$

Creates sub mm beam size on  
Recycling mirror ( $\sim 80 \text{ GW}/\text{m}^2$ )

### Third option: folded recycling cavities



This design:

- Beam size  $> 2$  mm  
(Power  $< 160$  MW/m<sup>2</sup>)

Design adds:

- 2 additional small mirrors
- Removes 1 large mirror

(Same is possible for SR-Cavity)

**Creates Stable  
Recycling Cavity**



- ✓ Spot Size
- Vacuum envelope
- Seismic Isolation
- Flexibility in mode matching
- Alignment
- Modulation frequency / linewidth effects
- ...

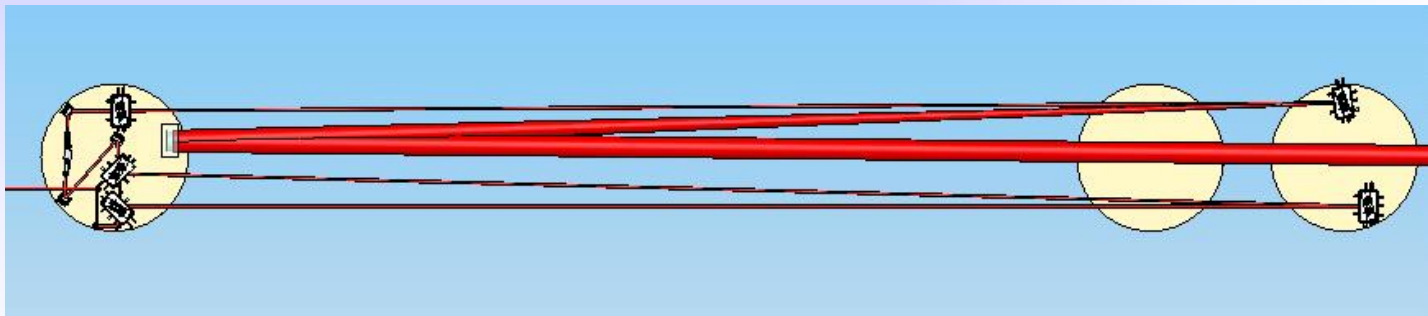
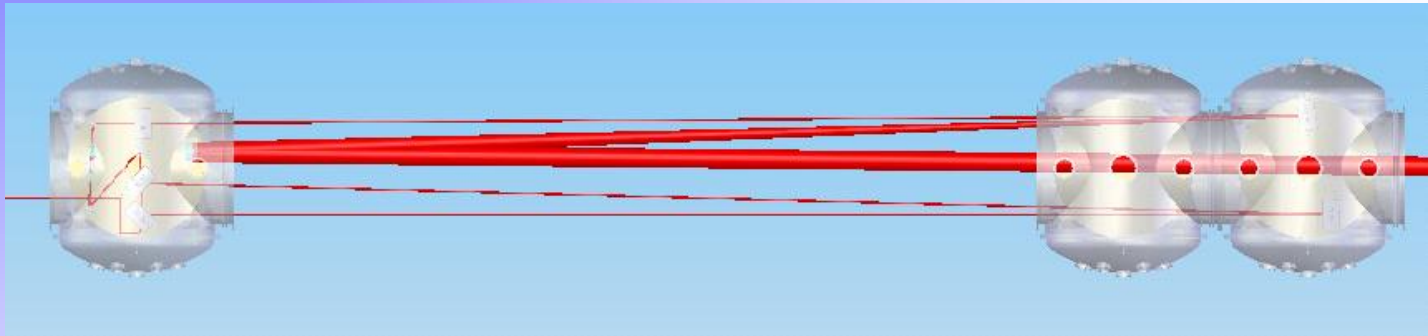


# Vacuum Envelope

Top View:

HAM 1

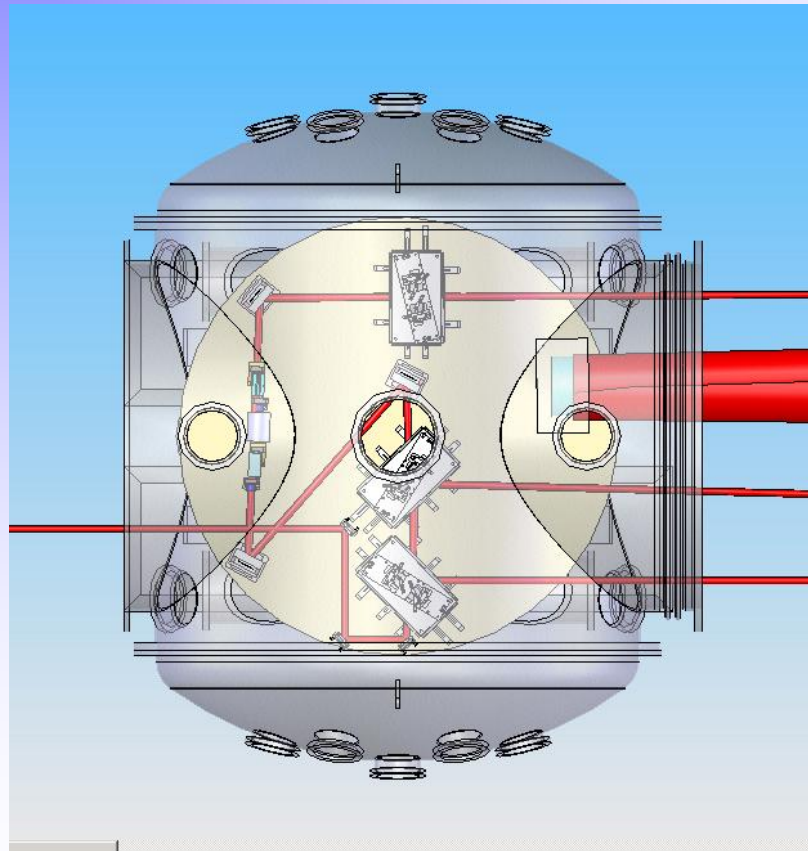
HAM2 HAM3





# Vacuum Envelope

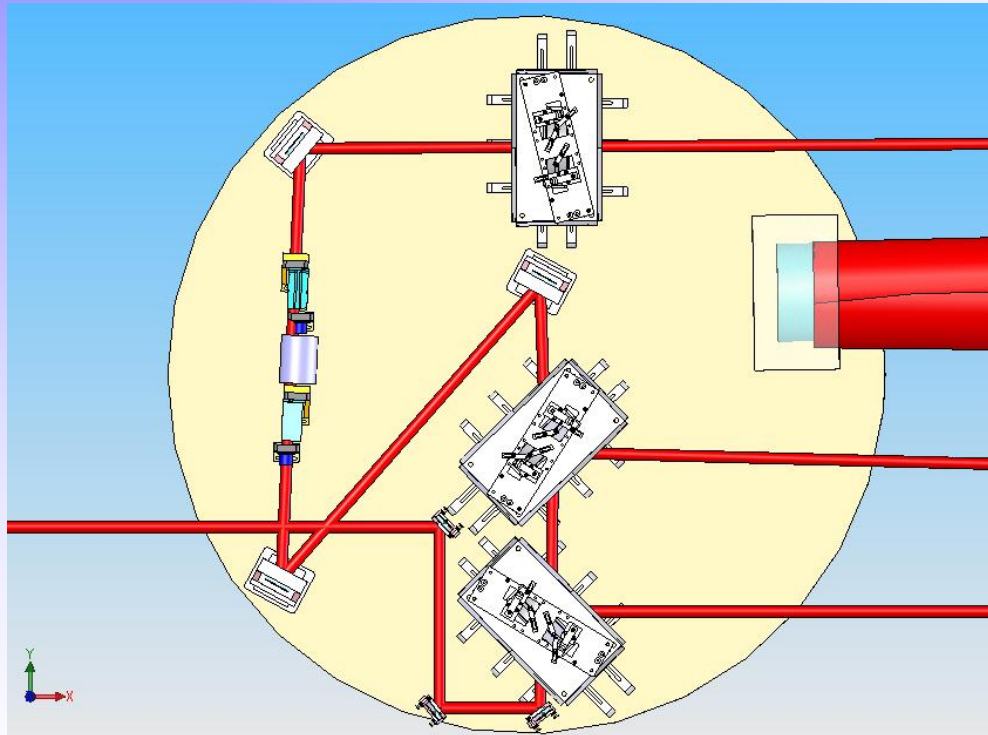
## Top View: HAM 1





# Vacuum Envelope

## Top View: HAM 1



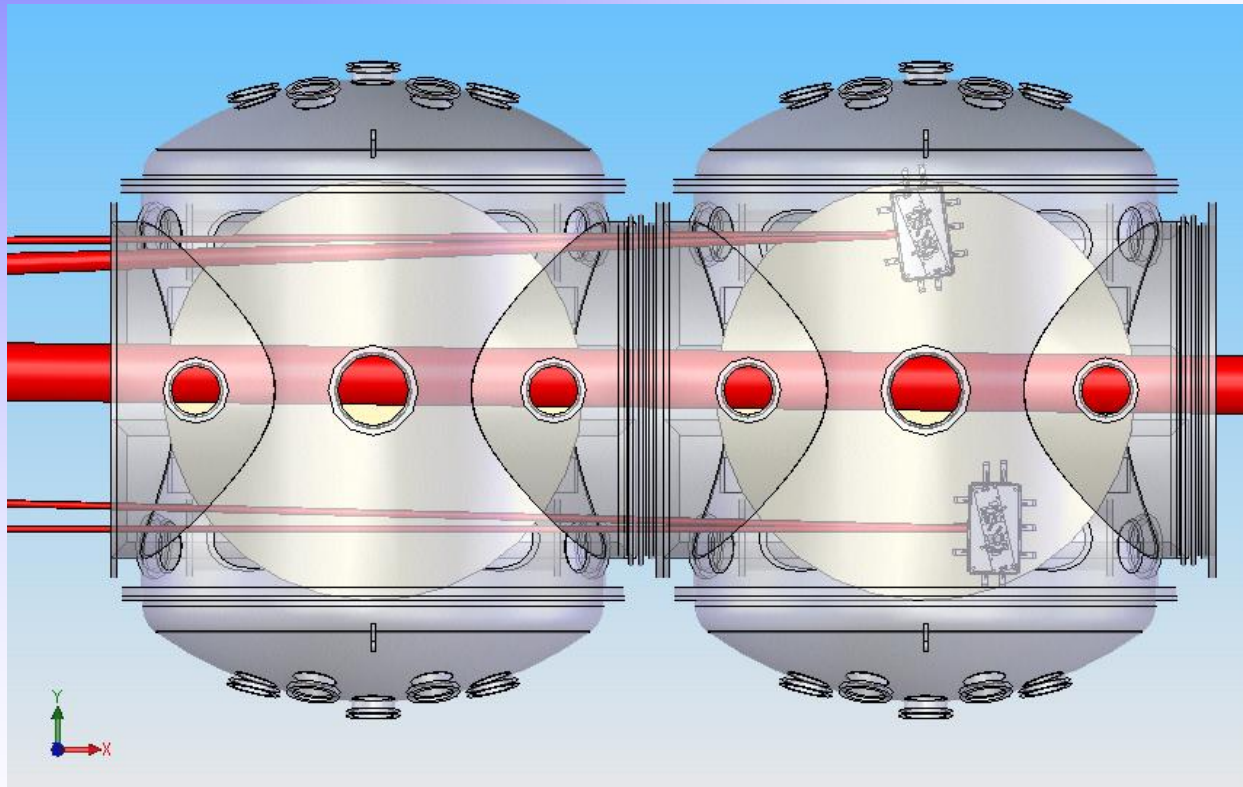


# Vacuum Envelope

## Top View

HAM 2

HAM 3



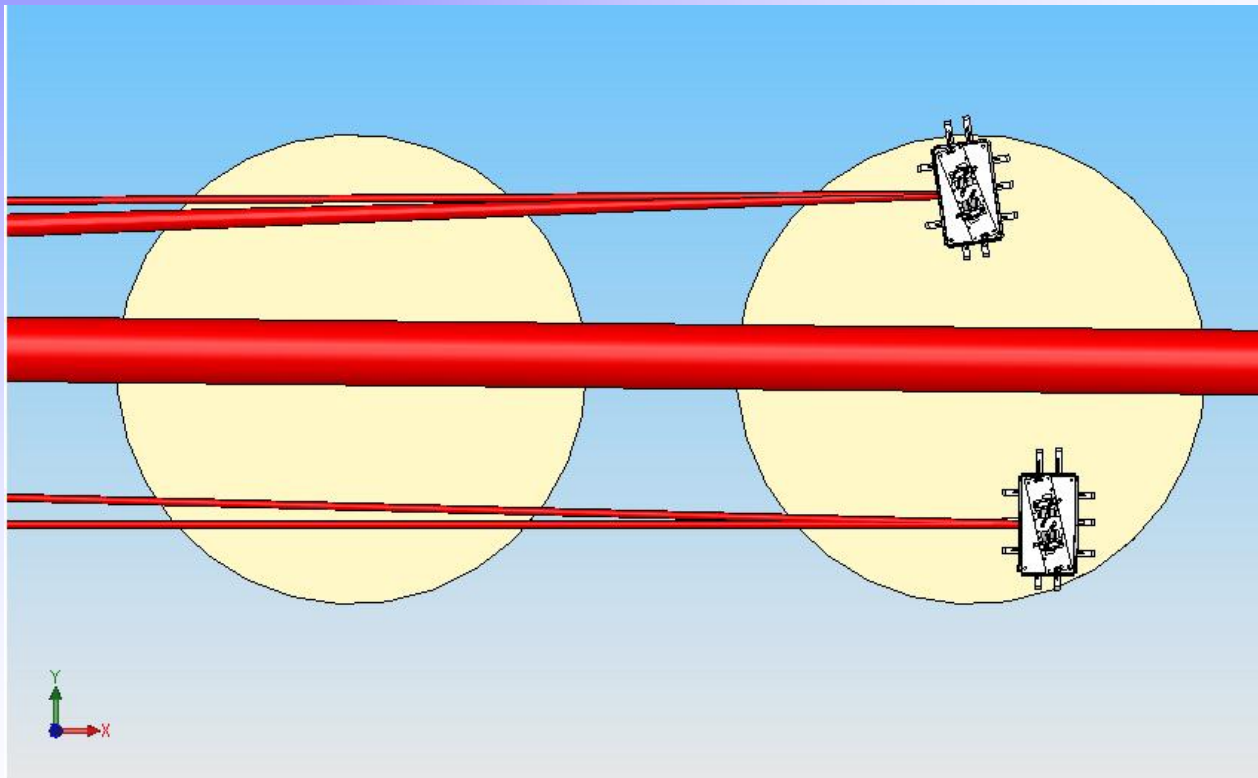


# Vacuum Envelope

## Top View

HAM 2

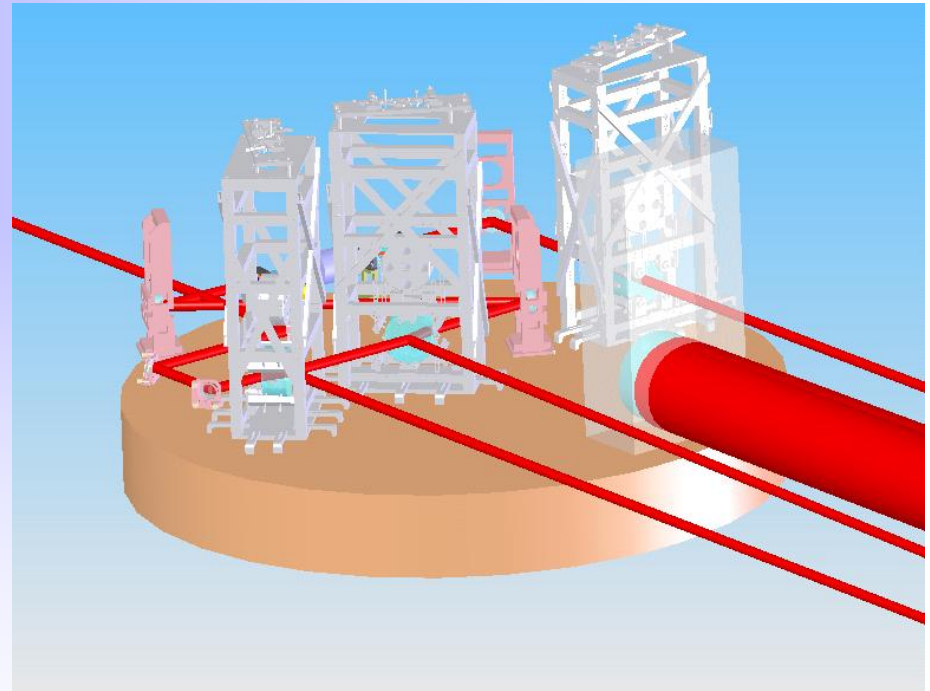
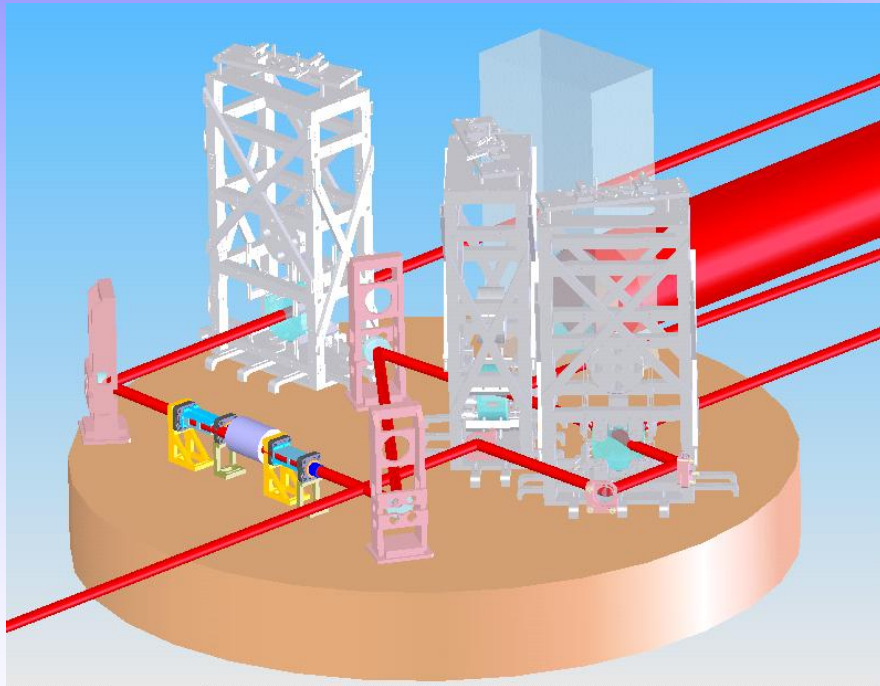
HAM 3





# Vacuum Envelope

## Side Views from HAM 1



- ✓ Spot Size
- ✓ Vacuum envelope
- Seismic Isolation
- Flexibility in mode matching
- Alignment
- Modulation frequency / linewidth effects
- ...



Requirements on single PR-mirror <sup>1</sup> :

- $3 \times 10^{-16}$  m/rHz
  - Driven by sensitivity to frequency noise

Target stability:

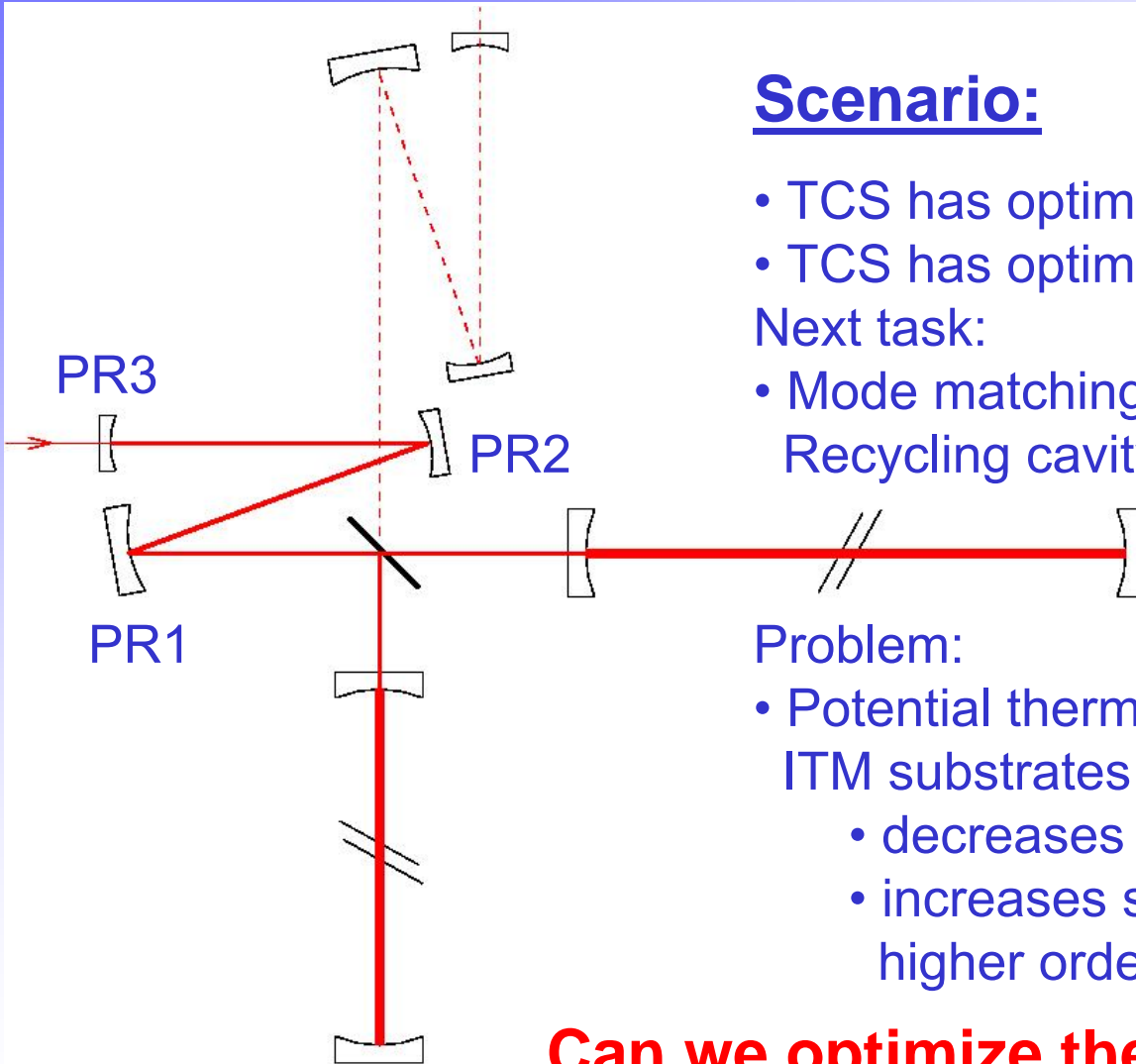
- $3 \times 10^{-17}$  m/rHz
  - Same suspension as Mode cleaner mirrors (triple pendulum)

Necessary changes for New Recycling cavity:

- Move large PR substrate in triple pendulum to MMT3 location
- First small PR mirror in MC-triple pendulum on IO-table
- Second small PR mirror in MC-triple pendulum on PR-table
- Mode matching from MC into Recycling cavity might add two additional small mirrors (single pendulum suspension)

<sup>1</sup> Sources: Seismic Isolation Subsystem Design Requirements Document E990303-03-D  
Advanced LIGO Systems Design T010075-00-D

- ✓ Spot Size
- ✓ Vacuum envelope
- ✓ Seismic Isolation
- Flexibility in mode matching
- Alignment
- Modulation frequency / linewidth effects
- ...



### Scenario:

- TCS has optimized beam size in arms
- TCS has optimized contrast in MI

Next task:

- Mode matching between Recycling cavity and arm cavities.

Problem:

- Potential thermal lens in BS and/or ITM substrates which
  - decreases mode matching
  - increases scattering into higher order modes

**Can we optimize the mode matching after we know the thermal lens ?**

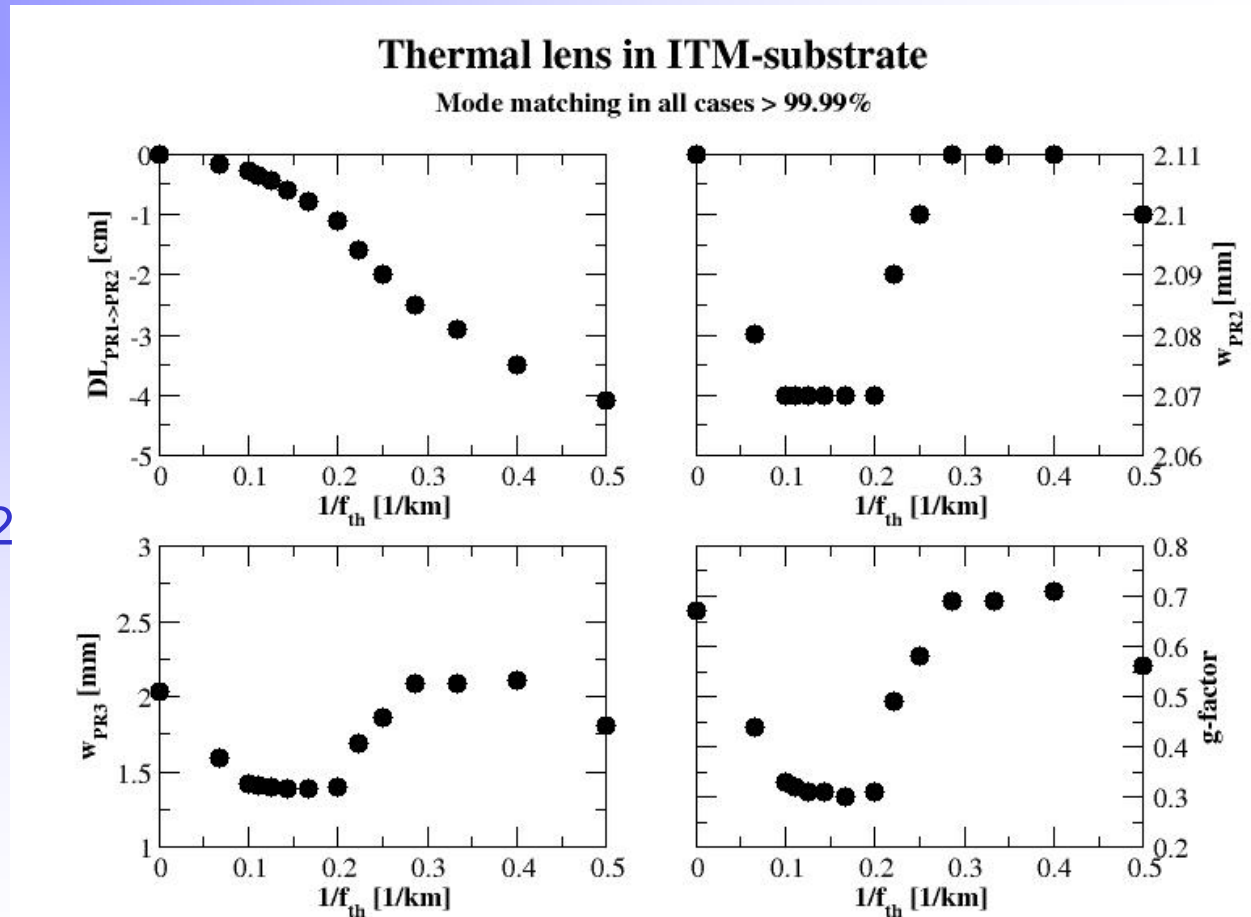
Can we optimize the mode matching after measuring the thermal lens?

Yes!

Even without changing the length of the recycling cavity

How?

- Change distance between PR1 and PR2 until mode matching is optimized
- Compensate change in the length by moving also PR3

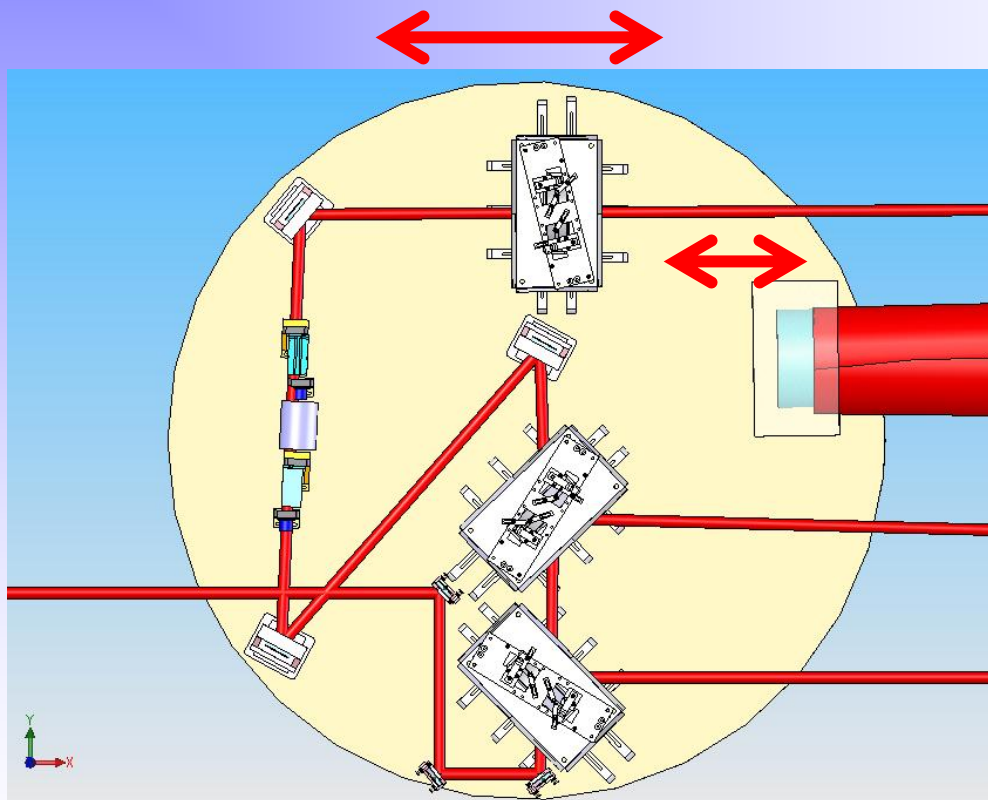


Alternative: Adaptive mode matching with thermally induced focal length changes

## Vacuum Envelope mode matching PR1, PR3

### Top View:

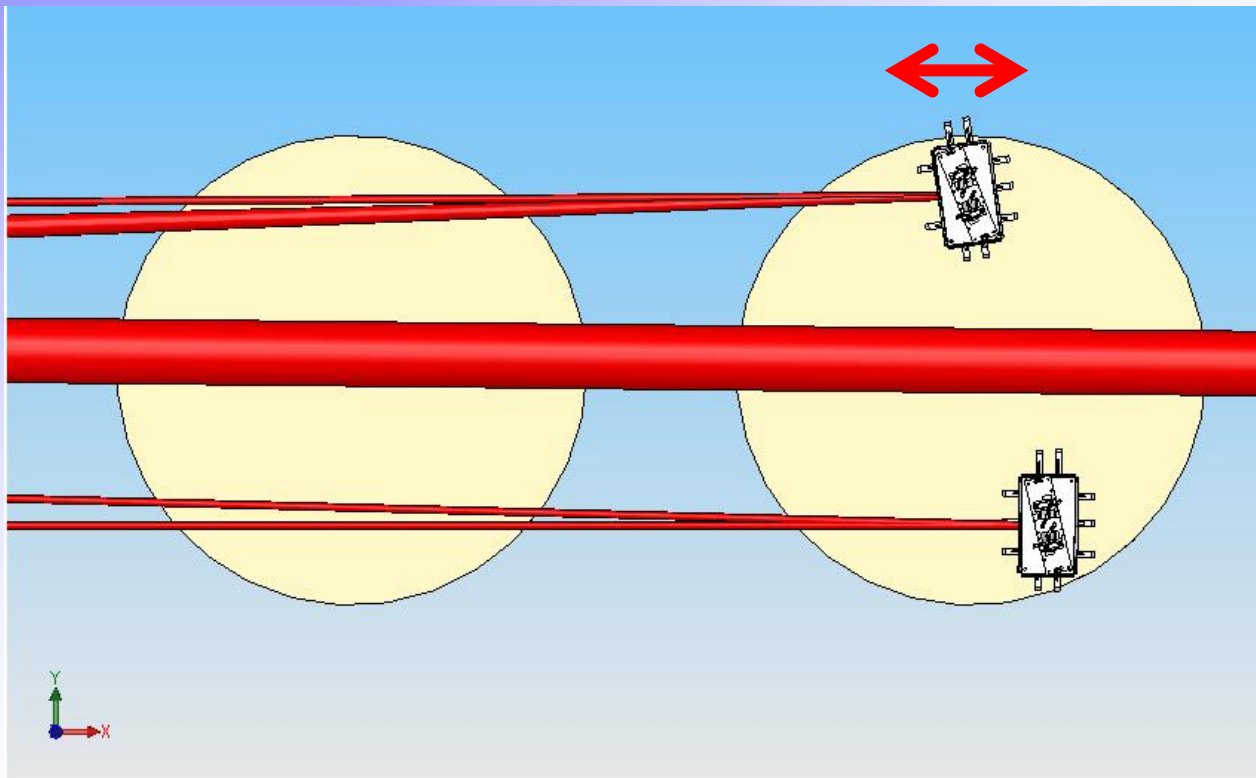
Plenty of space for mode matching adjustments



# Vacuum Envelope mode matching PR2

## Top View

Plenty of space for mode matching adjustments

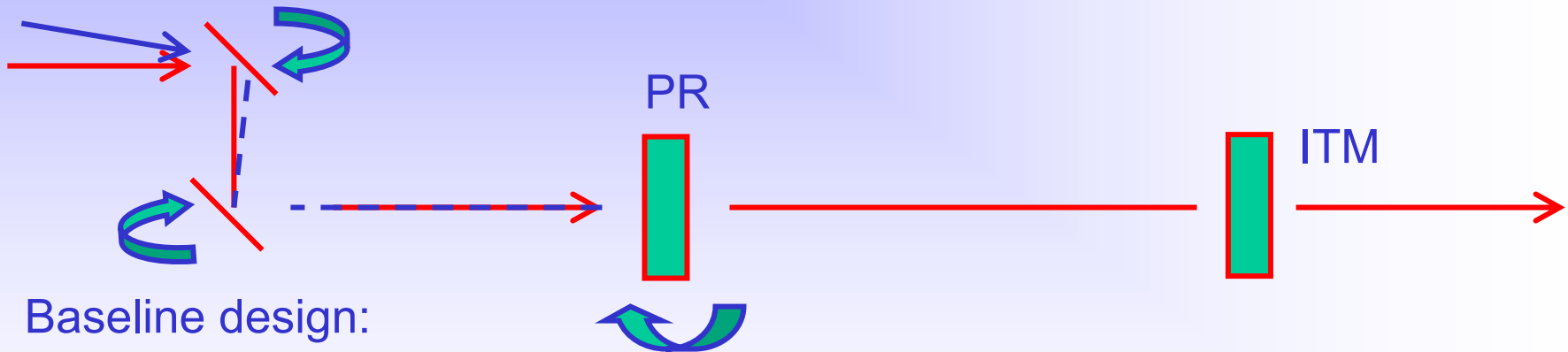


- ✓ Spot Size
- ✓ Vacuum envelope
- ✓ Seismic Isolation
- ✓ Flexibility in mode matching
- Alignment
- Modulation frequency / linewidth effects
- ...

Question:

Do we need to worry about additional alignment d.o.f as we have now more mirrors?

- Arm cavities are equal, no difference
- Any difference in Recycling Cavity?



Baseline design:

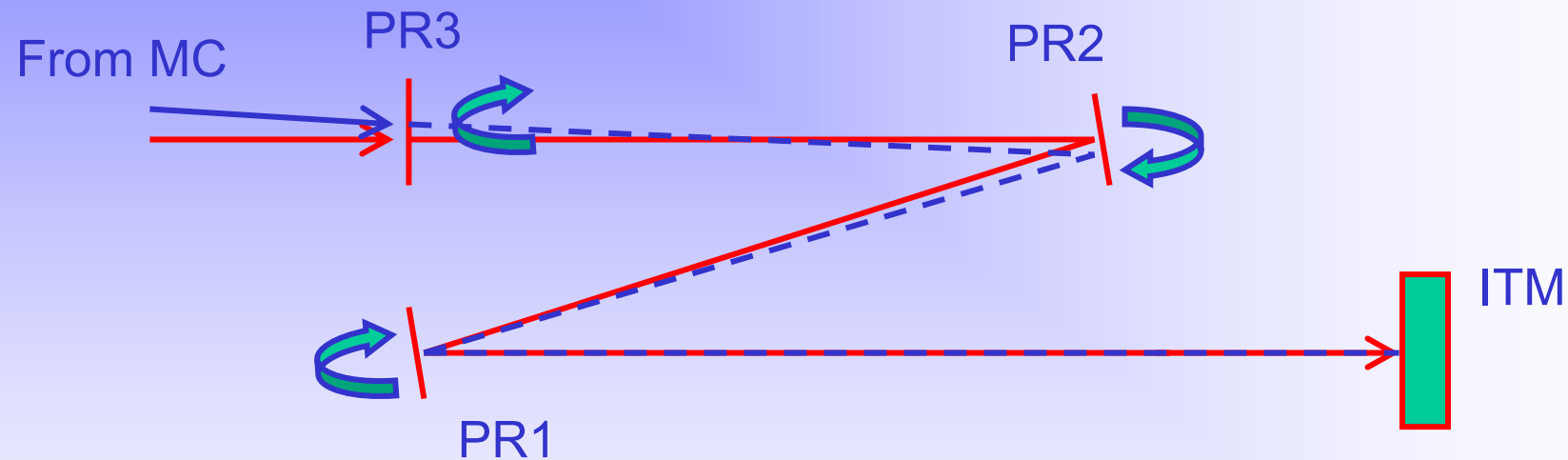
- Align orientation of PR
- Align propagation direction and position of Input beam

Total: 3 d.o.f. in horizontal and 3 d.o.f. in vertical direction



Alignment defined by arm cavity:

- Find position on PR1
- Propagation direction from PR1 to ITM1



Change in Input beam also requires adjustment of 3 d.o.f. in horizontal and 3 d.o.f. in vertical direction!

Other Option: Align input beam and only one of the PR mirrors.

## Alignment sensing matrix: (Work in progress)

- Calculate alignment sensing matrix for Advanced LIGO with and without stable recycling cavities

## Intermediate (premature) results:

For Baseline Design:

- Difficult to distinguish between PR and ITM tilts (same Gouy phase)

For New Design:

- Same problem between PR1 and ITM tilts
- Easy to distinguish between PR2, PR3 tilts and ITM tilts

## Preliminary conclusion:

Advantage for new design: Larger linear range in ASC-signals

Disadvantage: ?

- ✓ Spot Size
- ✓ Vacuum envelope
- ✓ Seismic Isolation
- ✓ Flexibility in mode matching
- ✓ Alignment
- Modulation frequency / linewidth effects
- ...

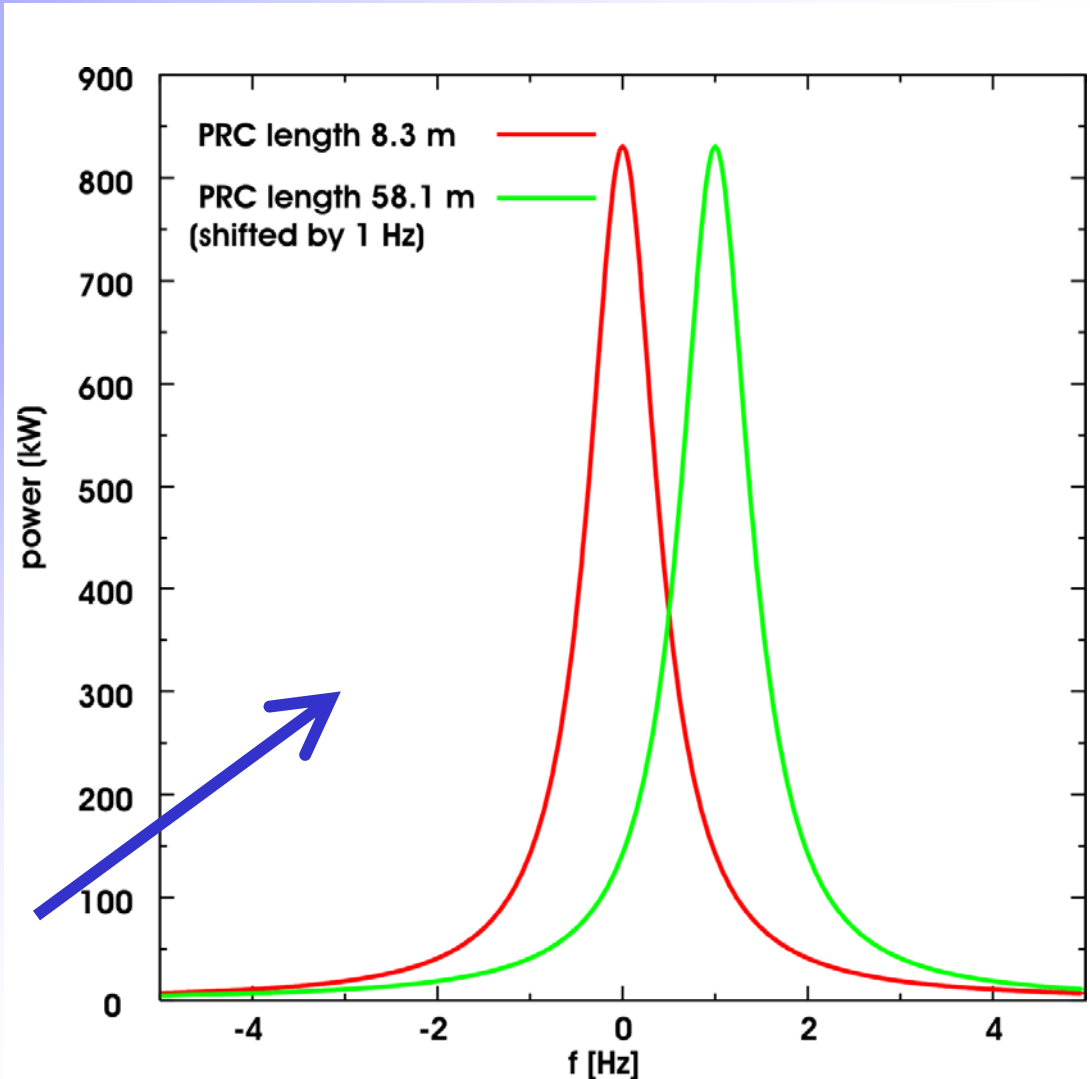
### Modulation frequency requirements

- 180 MHz must pass through MC and PRC and 9 MHz must be anti-resonant for the PRC (dictated by length of MC = 16.6m,  $FSR_{MC} = 9$  MHz)
- The vacuum envelope changes length of PRC from 8.3 m to  $8.3 \text{ m} + 3 \cdot (16.35 \text{ m} \pm x)$  (x must be small to fit in HAM chamber)
- With  $x = 0.25 \text{ m} \Rightarrow FSR_{MC} = 3.5 * FSR_{PR}$   
 $FSR_{PR} = 2.57 \text{ MHz}$

- Does changing the length of the PRC have any influence on the linewidth of the coupled power recycling / arm cavity?
- No, the finesse of the Arm cavities dominate the PRC:

$$\Delta \nu_{PRC} = \Delta \nu_{ArmC} \frac{1 - |\tilde{r}_{ArmC}(0)|^2}{2}$$

- No influence of PRC length
- Power vs. frequency in the x-Arm cavity for both PRC length in a finesse plot:



### Stable Recycling Cavity (SRC):

- Suppresses higher order modes of the RF-sidebands
- Increases Power in fundamental mode of sidebands
- (?) Improves alignment sensing (larger linear range of ASC signals)
- Adds flexibility for mode matching

### Baseline Recycling Cavity:

- Fewer Components (SRC has more small mirrors, one less large mirror)
- Fewer triple suspensions

### Costs:

- Hardware costs probably higher for stable recycling cavity
  - Should fit in current vacuum envelope
- Expect shorter commissioning time for stable recycling cavity design
  - Higher order mode contamination often limits diagnostics