



**LIGO**

# Minimizing the Resonant Frequency of MGAS Springs for Seismic Attenuation System in Low Frequency Gravitational Waves Interferometers

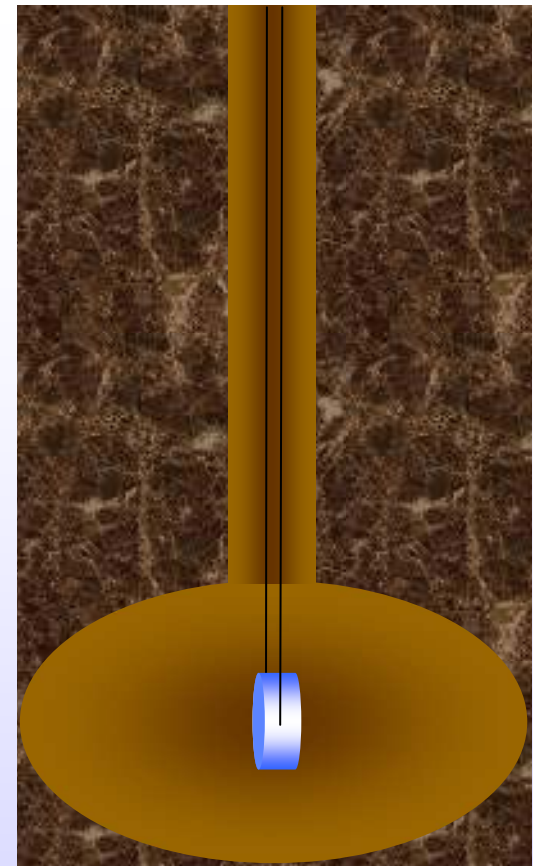
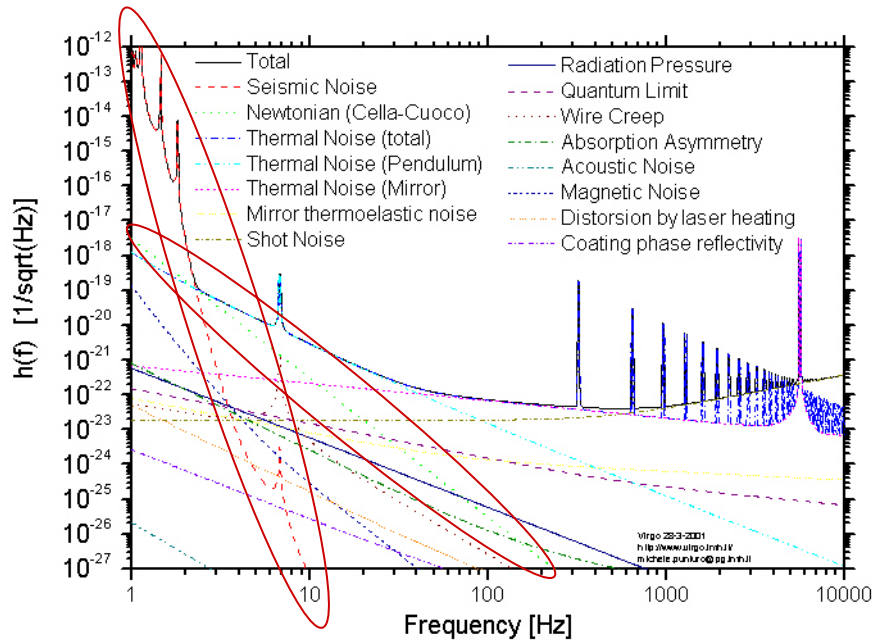


CALTECH



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Riccardo De Salvo, Barbara Simoni

# Motivations

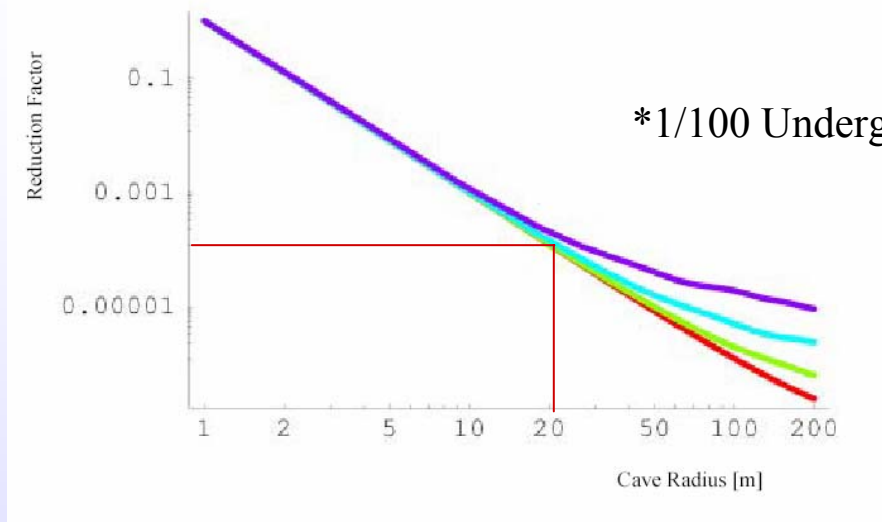


Ground Based Interferometer are Limited by Newtonian Noise under 10 Hz

Seismic Attenuation was Designed to Match that Limit

Recent Calculations Show the Possibility of Suppression of Newtonian Noise by Suspending the Test Masses in Deep Caves

# Cella Suppression of Newtonian Noise



Giancarlo Cella Draft

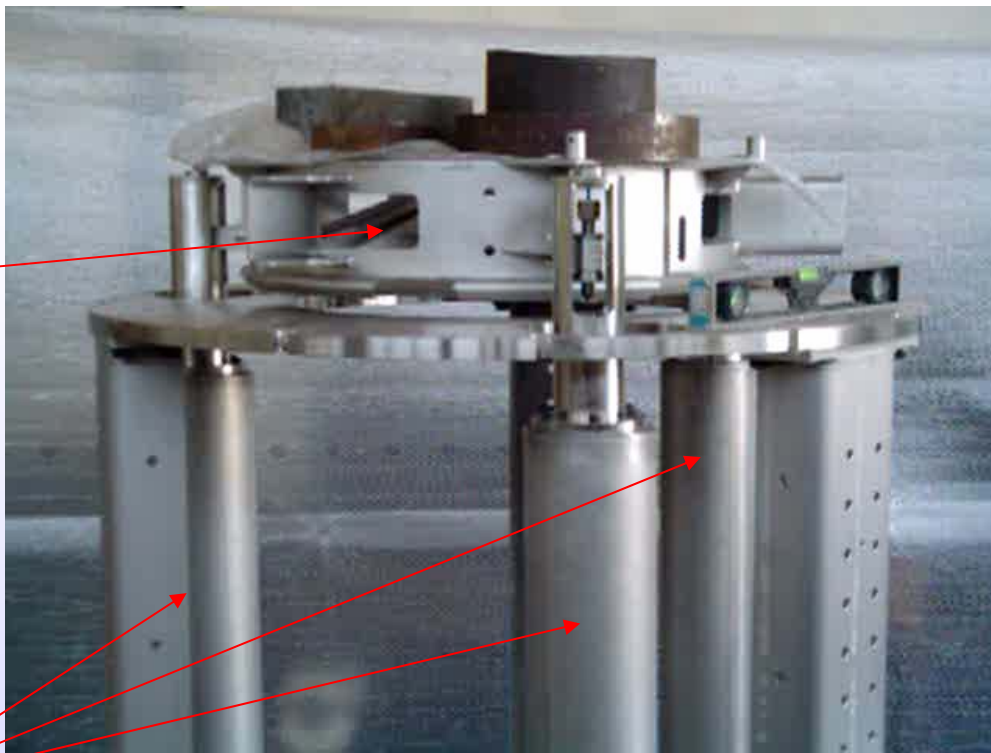
Suppression of NN by a Factor of  $10^{-6}$  in Amplitude, 30 in Frequency  
Seismic Attenuation Must be Redesigned to Match the New Limit



Horizontal Achievable with Longer Wires in Wells  
Vertical Attenuation Requires New Development

# Horizontal Attenuation

Filter

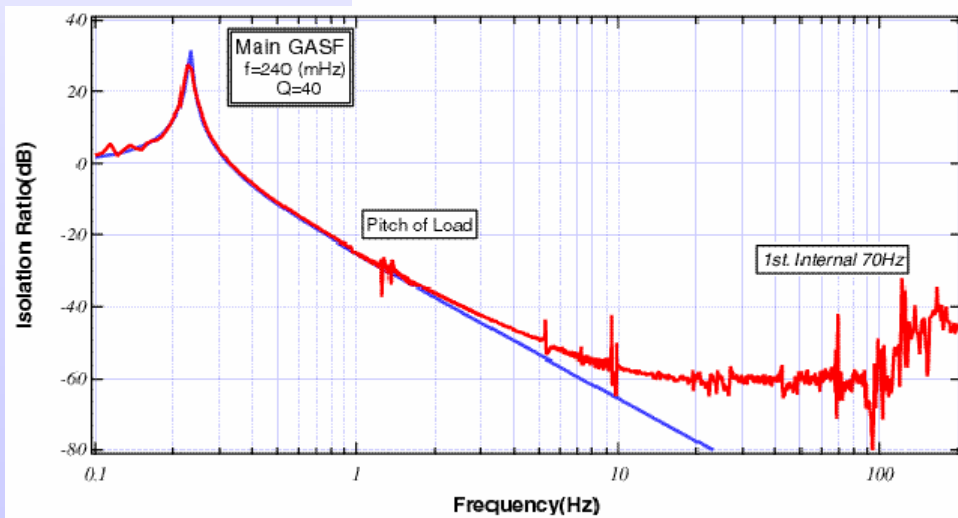
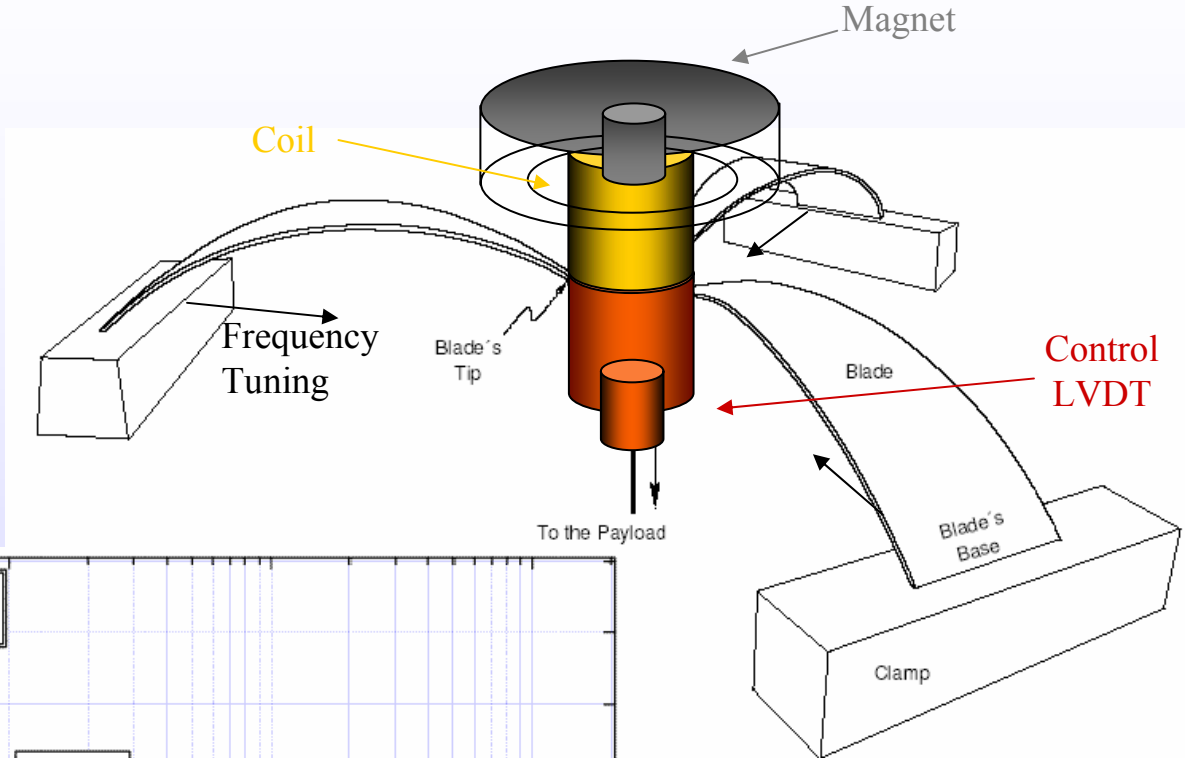


Inverted Pendula





# Existing MGAS Spring



Practical Limit "200mHz

Method to Lower the Resonant Frequency below the Mechanical Limitations

Simulated Noise

# Apparatus Schematics

Mechanical Actuator

Actuator

Blade

Control LVDT

Signal 1

Filter to ground LVDT

Signal 2

Ground to Payload LVDT

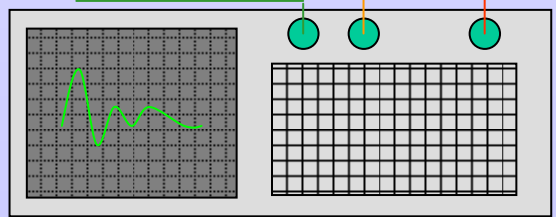
Signal 3

Load

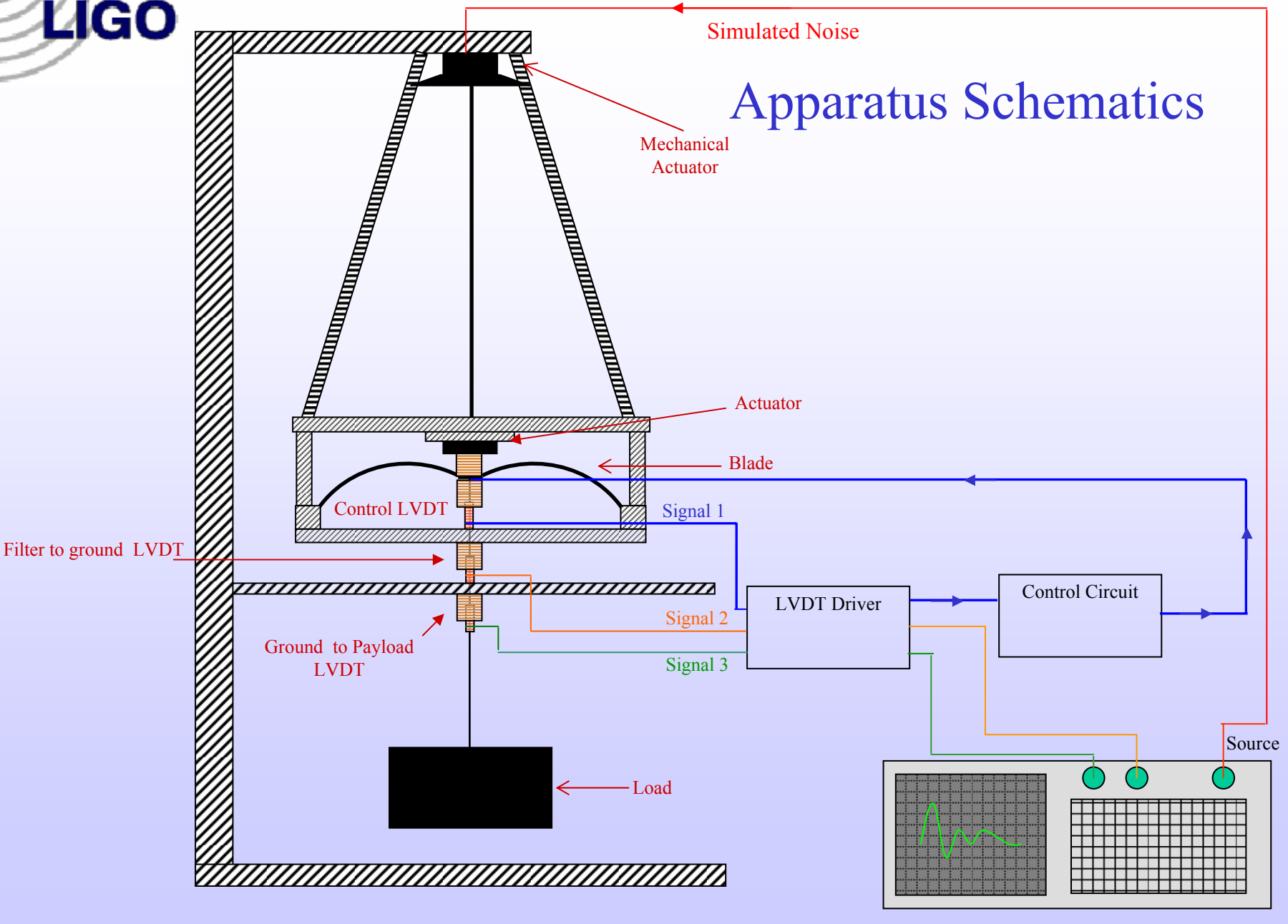
LVDT Driver

Control Circuit

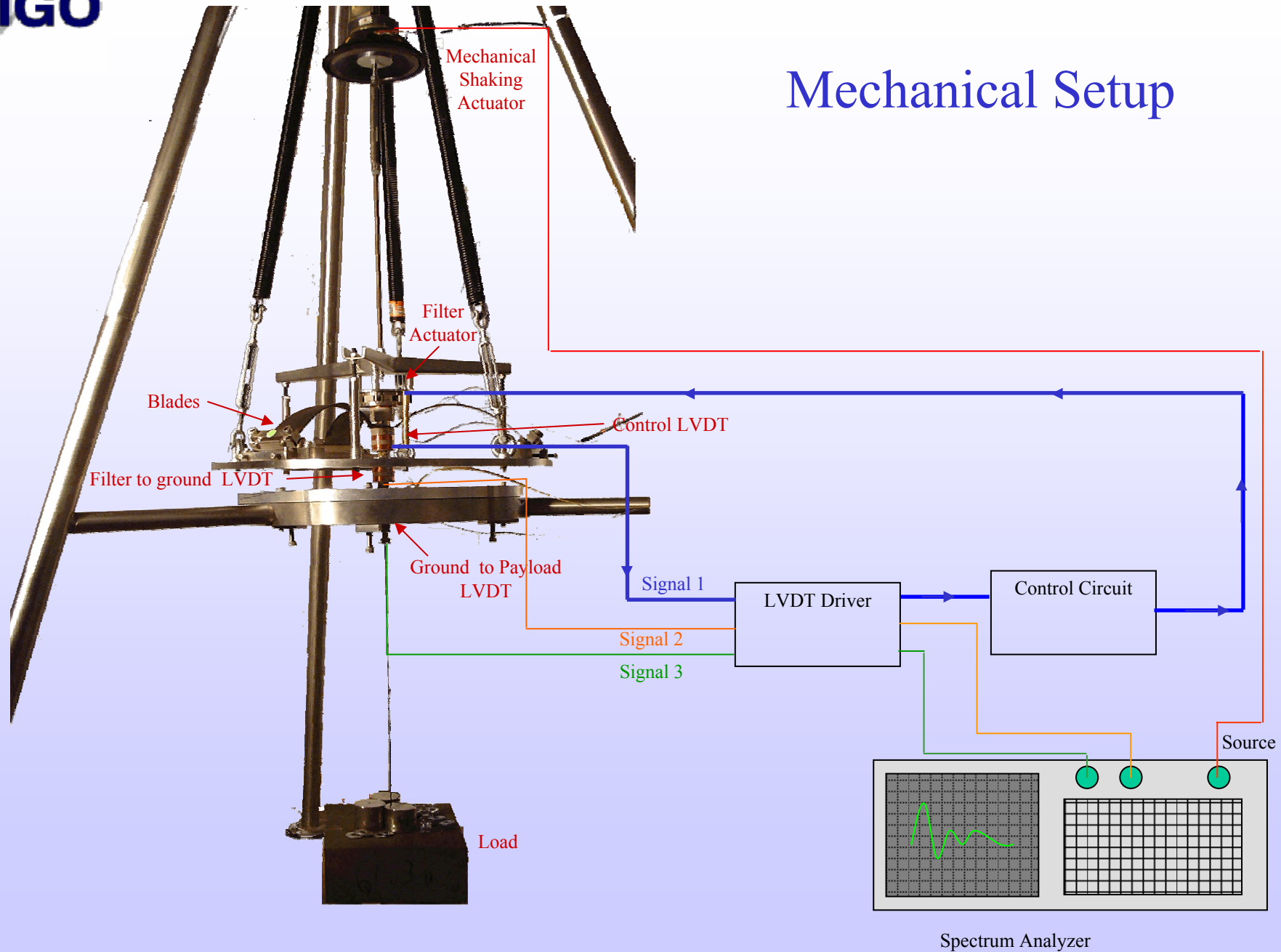
Source

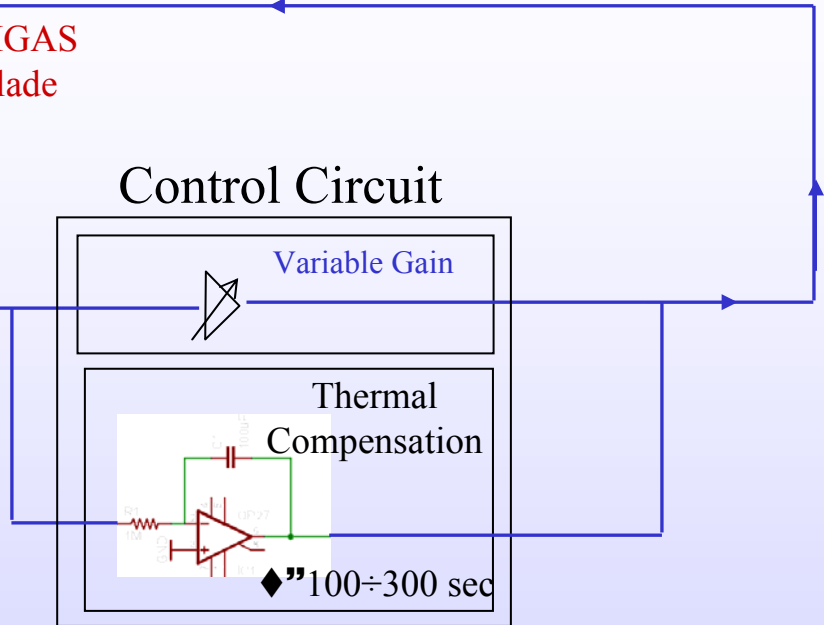
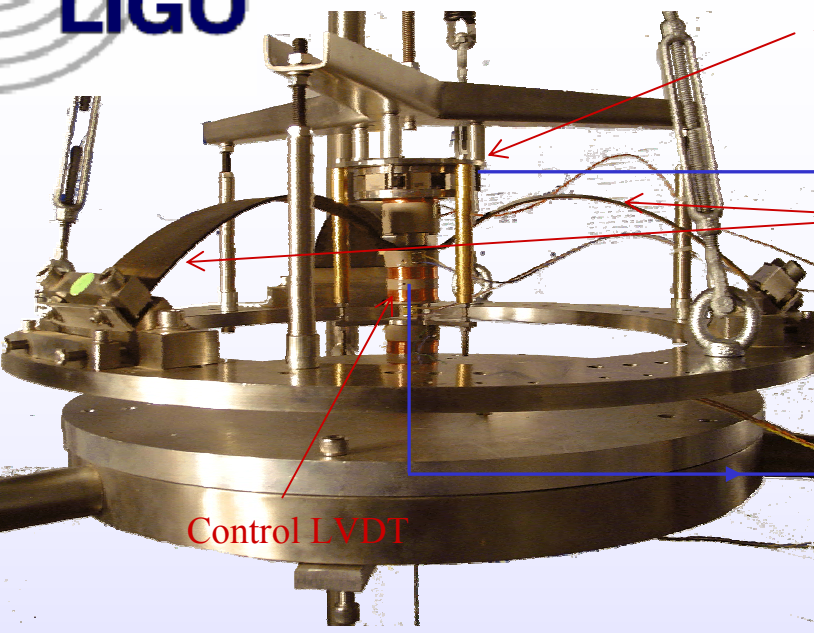


Spectrum Analyzer



## Mechanical Setup





- LVDT
- Variable Gain
- Amplificator-Voice Coil



Tunable spring in parallel with MGAS spring

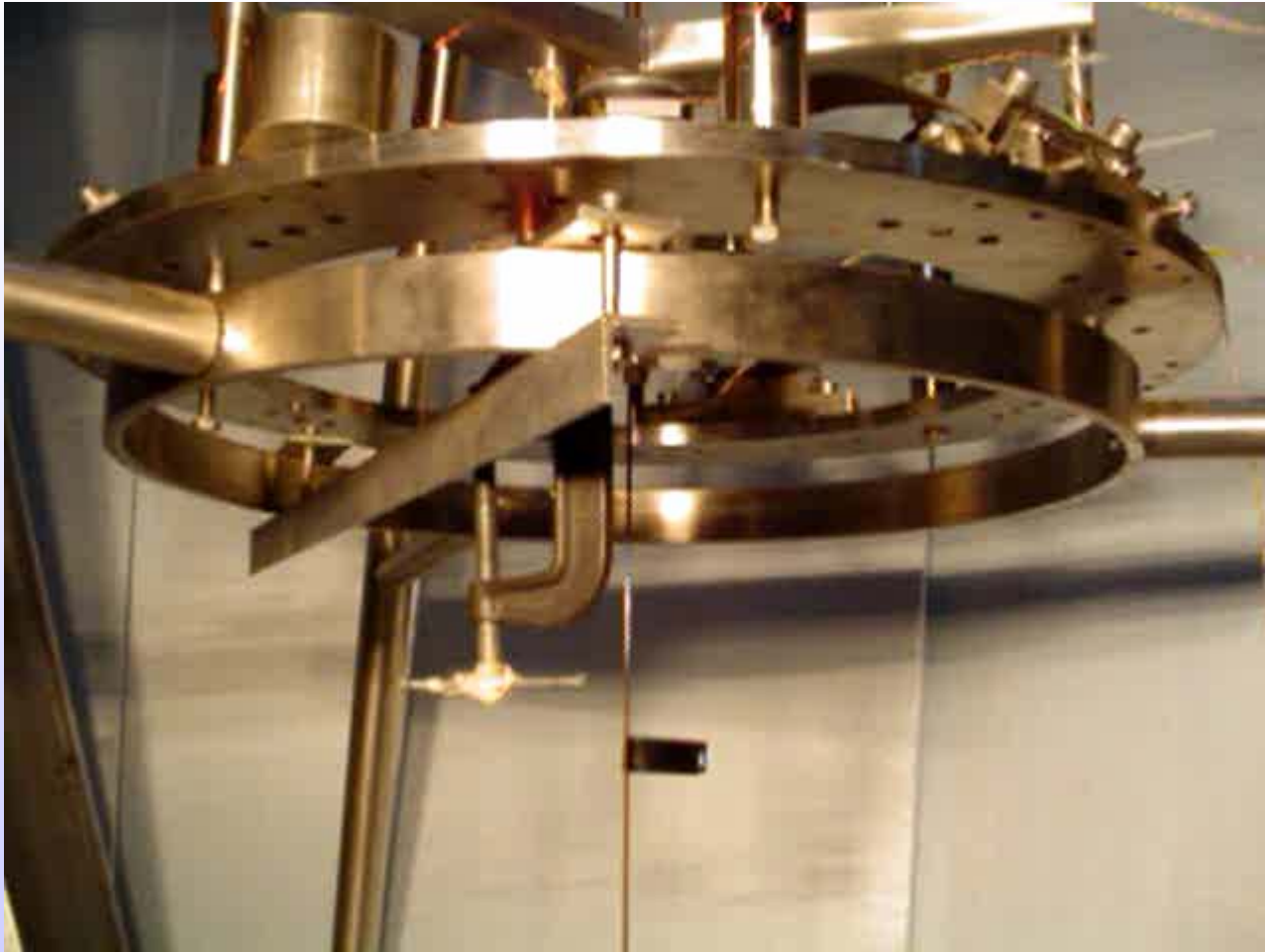
( Set Point Integrator



Thermal Drift Correction)

MGAS already neutralize > 90% of cantilever spring stiffness

Circuit corrects the last few per cent of stiffness and stabilizes performance



Payload

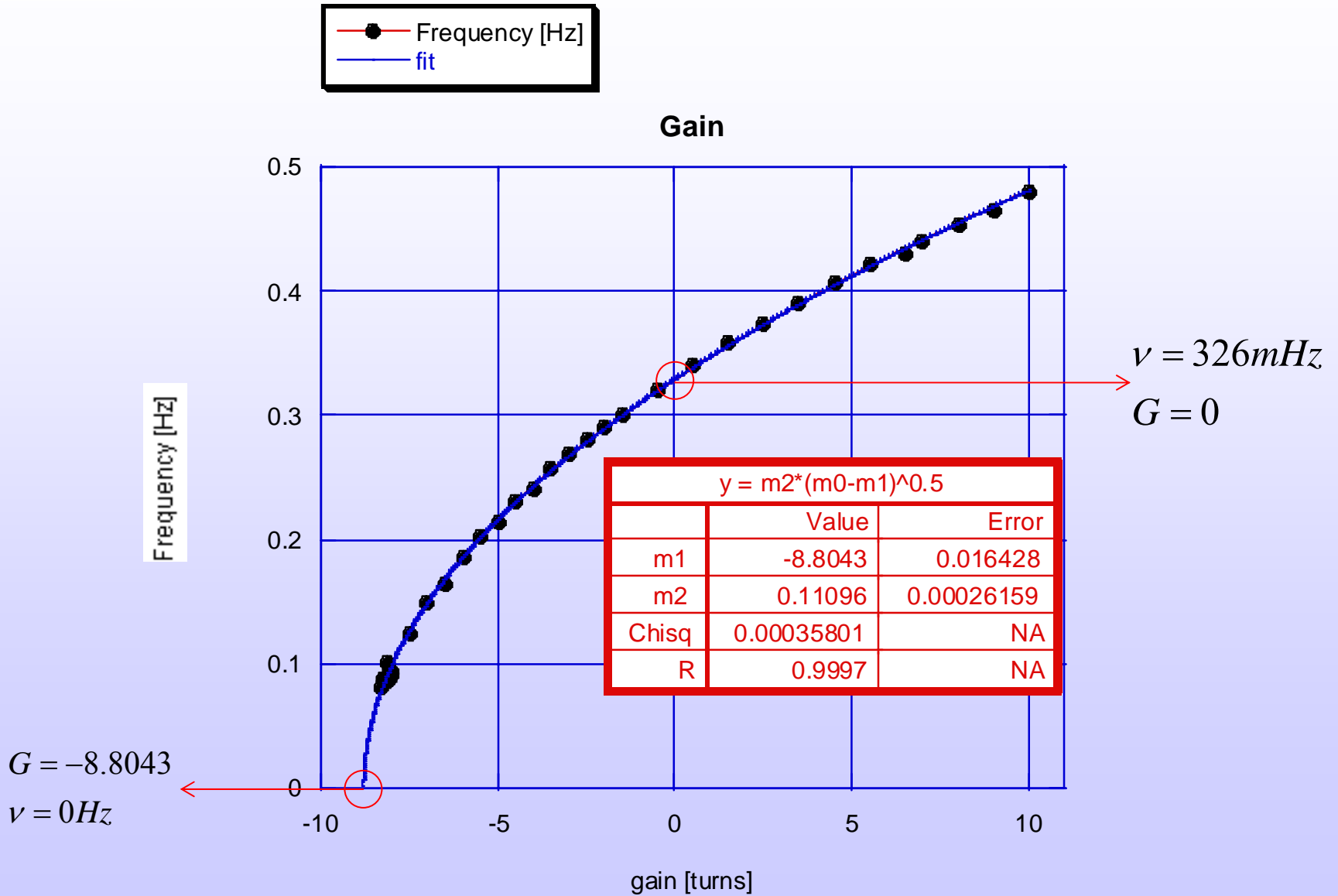


# Characterization Work

- Determination of the Working Point
- Circuit Calibration
- Frequency behavior as a function of the Gain
- Q Factor Analysis
  - Impulse Response
  - Frequency Response

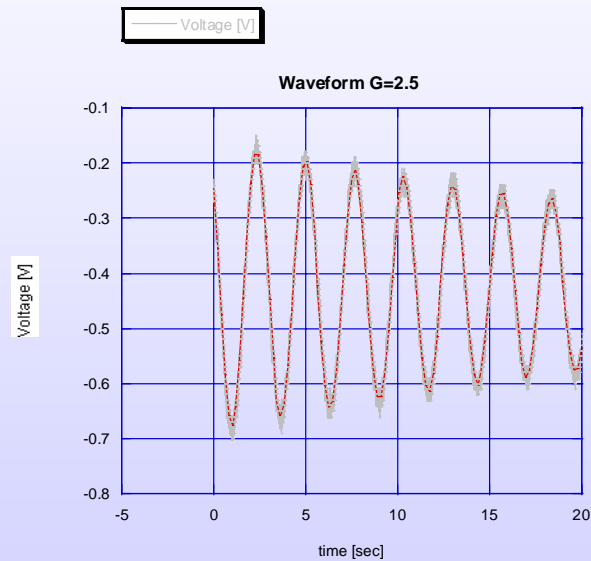


After fixing the vertical height to the minimum frequency point we change the Gain to find the **frequency behavior vs. gain**



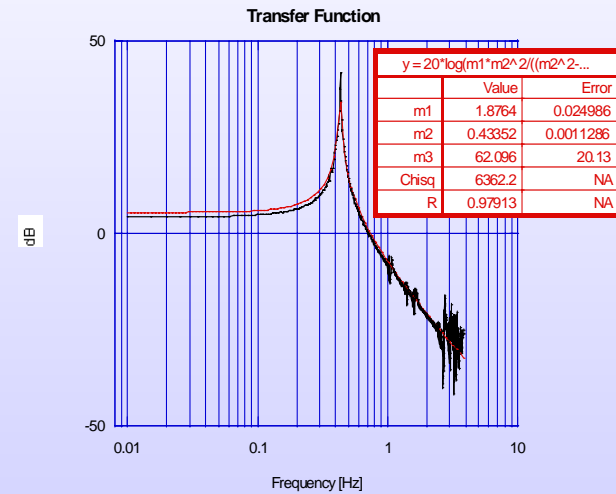
# Q Factor Analysis; Two Methods

Fitting the Damped Exponential in Free Oscillations



$$Q = \tau \cdot \nu$$

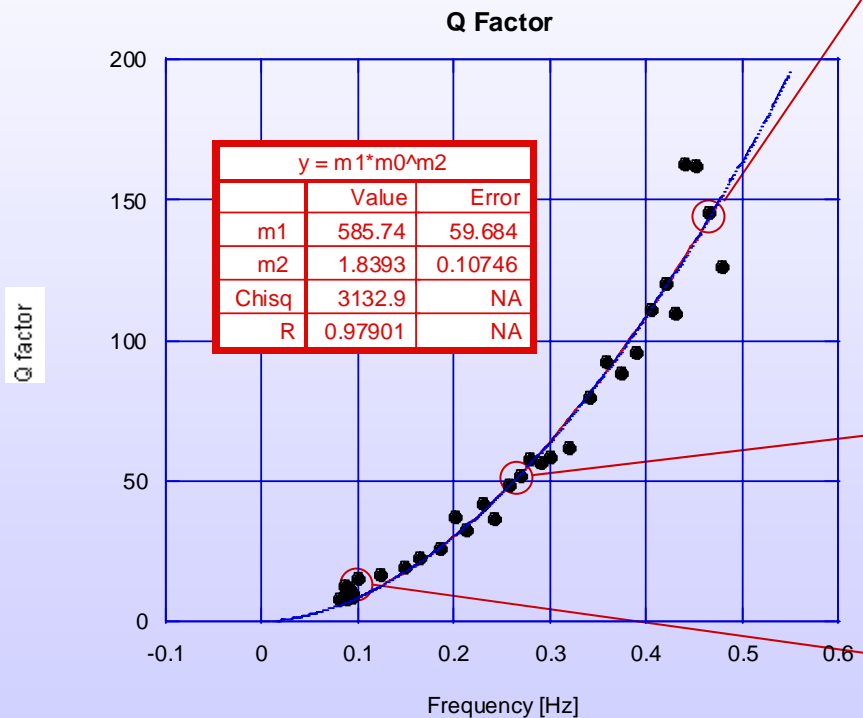
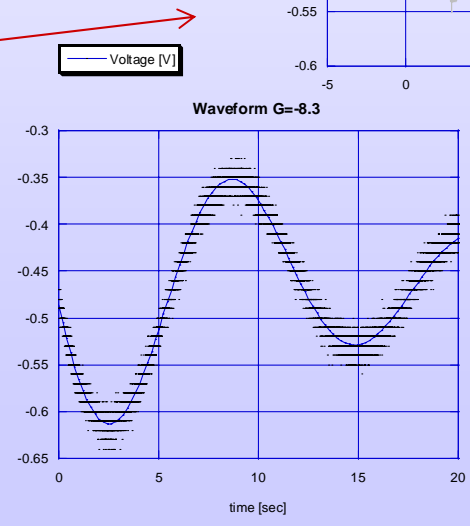
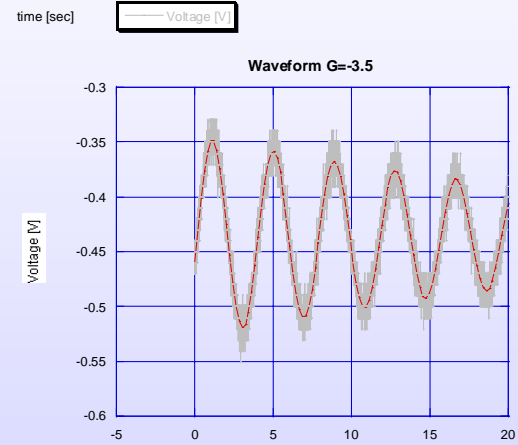
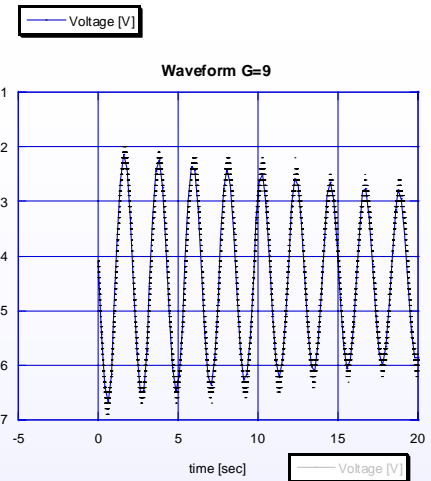
Fitting the Resonant Width in the Transfer Function



$$Q = \frac{f_0}{\Delta f}$$

# Impulse Response

$$Q_{factor} = \tau \cdot \nu$$

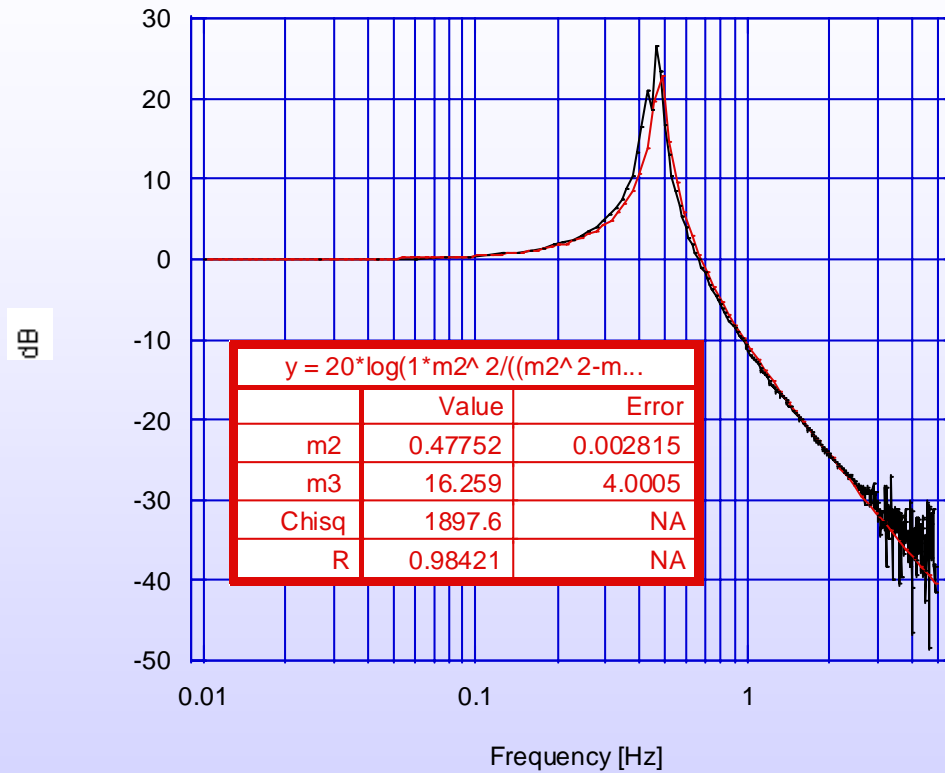


y = m1*m0^m2		
	Value	Error
m1	585.74	59.684
m2	1.8393	0.10746
Chisq	3132.9	NA
R	0.97901	NA

$$y = c_0 + c_1 \cdot \left( \cos(2\pi\nu t + \varphi) \cdot e^{-t/\tau} \right)$$

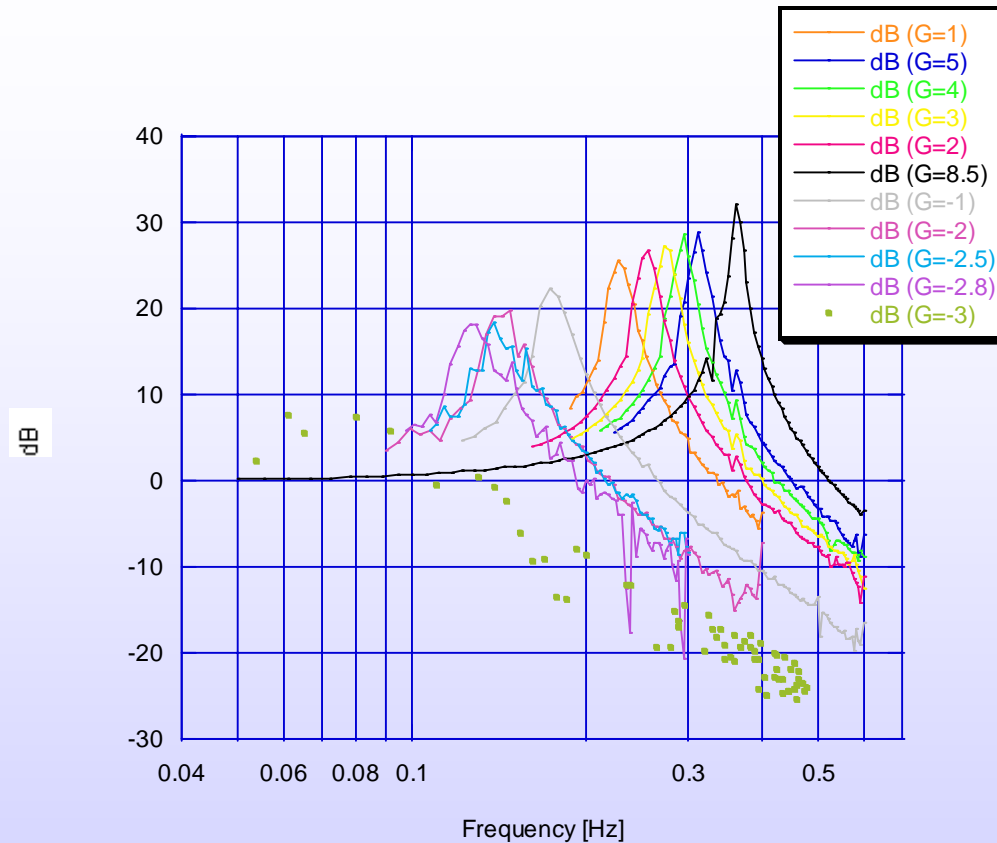
# Transfer Function Measurement

(filter body to payload)



$$f(\nu) = 20 \log \left( \frac{H_0 \cdot \nu_0^2}{\sqrt{\left( (\nu_0^2 - \nu^2)^2 + \frac{\nu^2 \nu_0^2}{Q^2} \right)}} \right)$$

## Transfer Function with Different Gain values

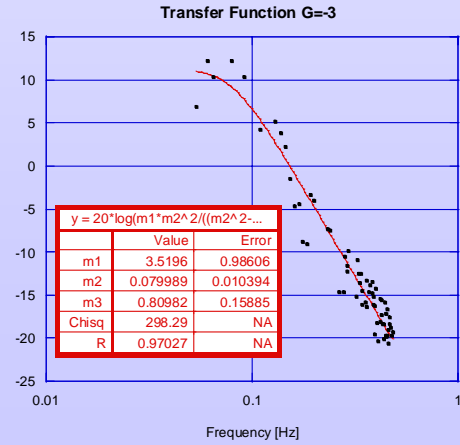
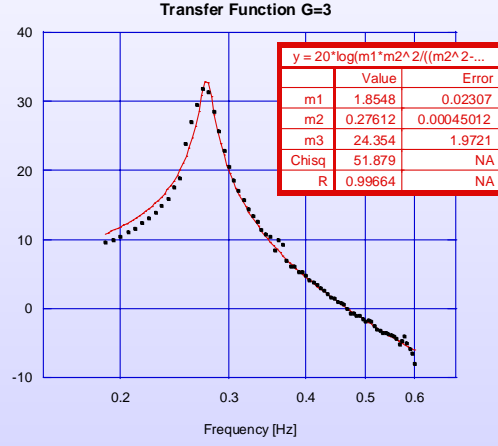
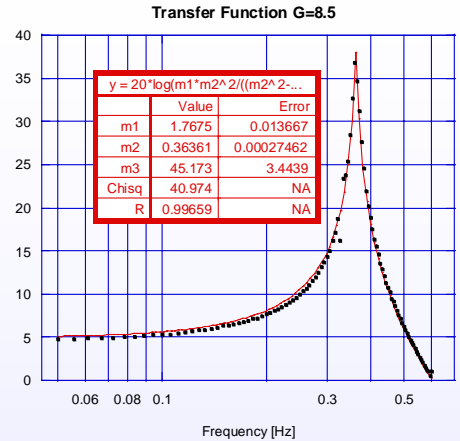
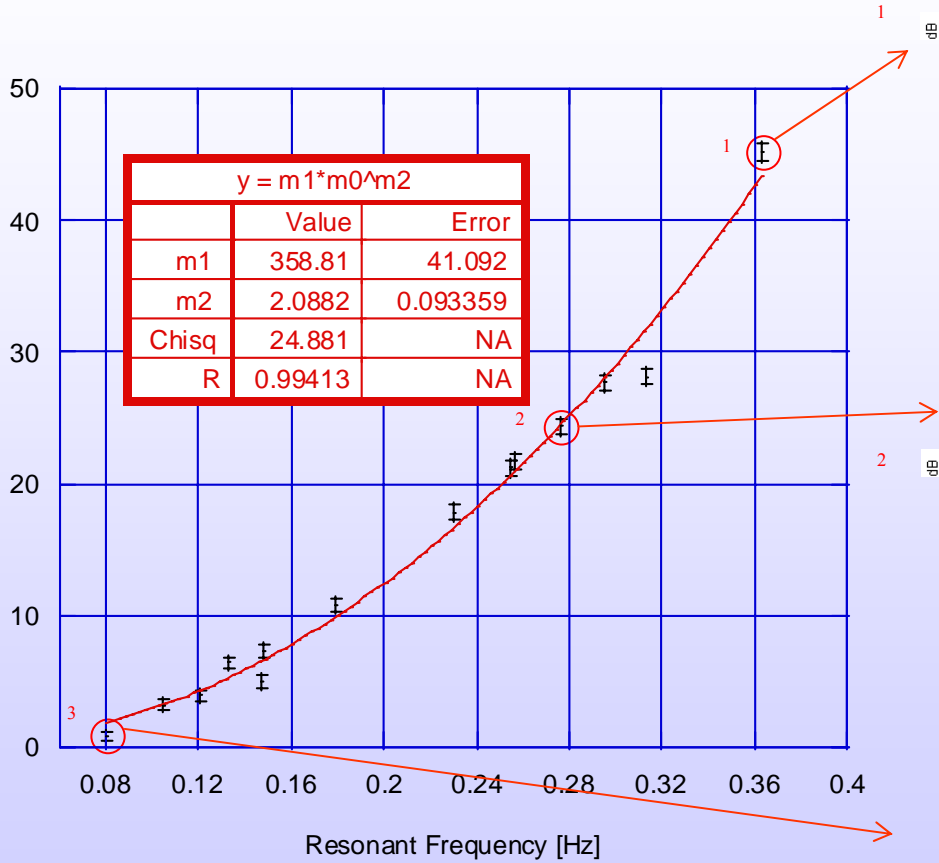


## Lowering the system stiffness

As the Transfer Function is shifted to lower frequencies,

The Q factor decreases

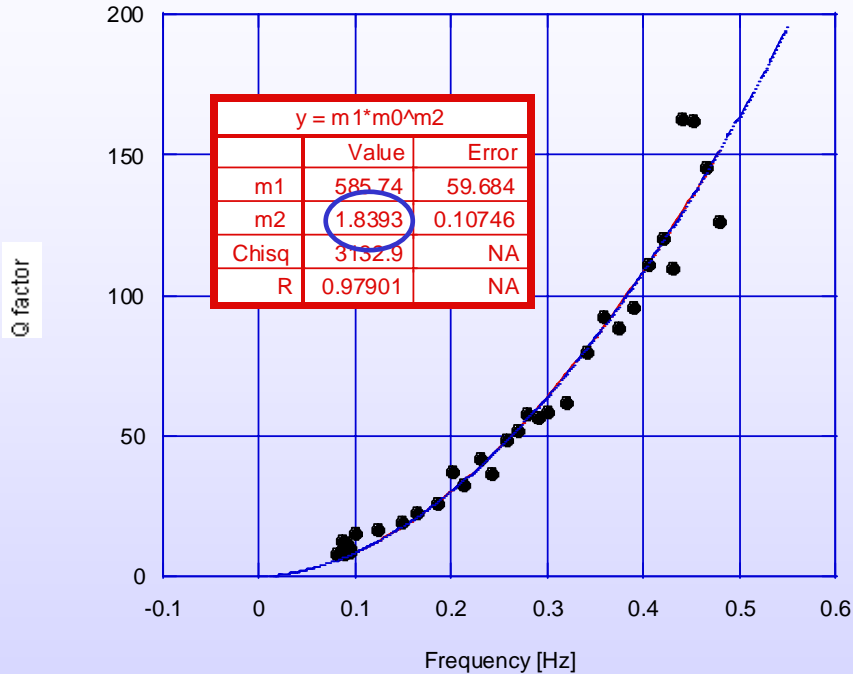
Q factor



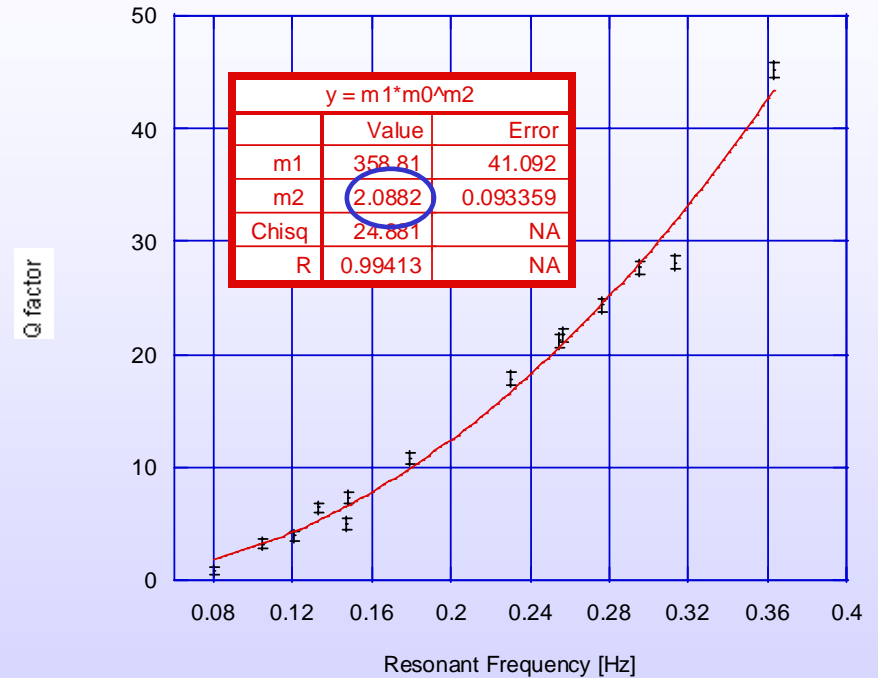


## Impulse Response

Q Factor



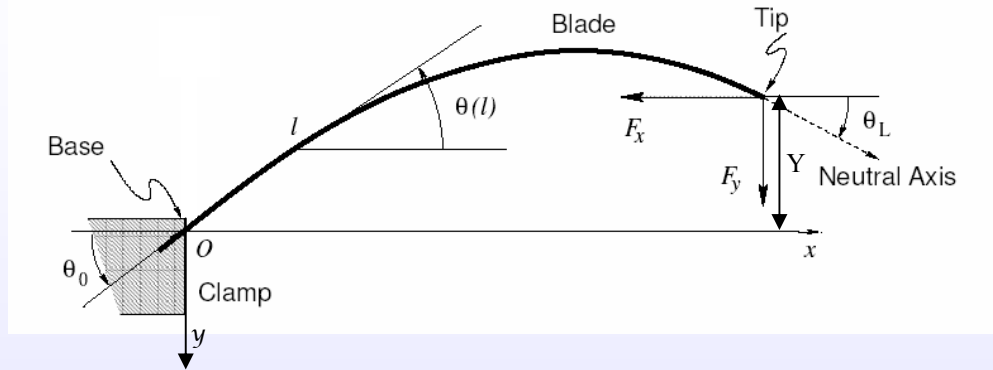
## Frequency Response



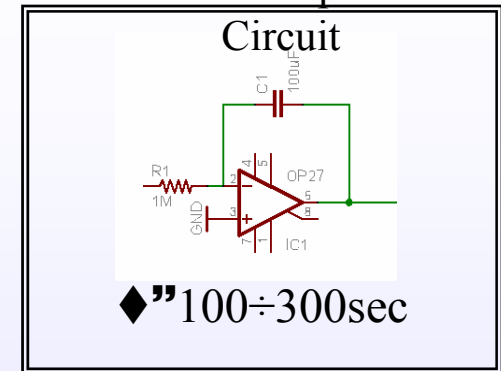
Both methods show a **quadratic** behavior for the Q factor

**Implies structural, non viscous, damping**

# Need for Thermal Compensation



## Thermal Compensation



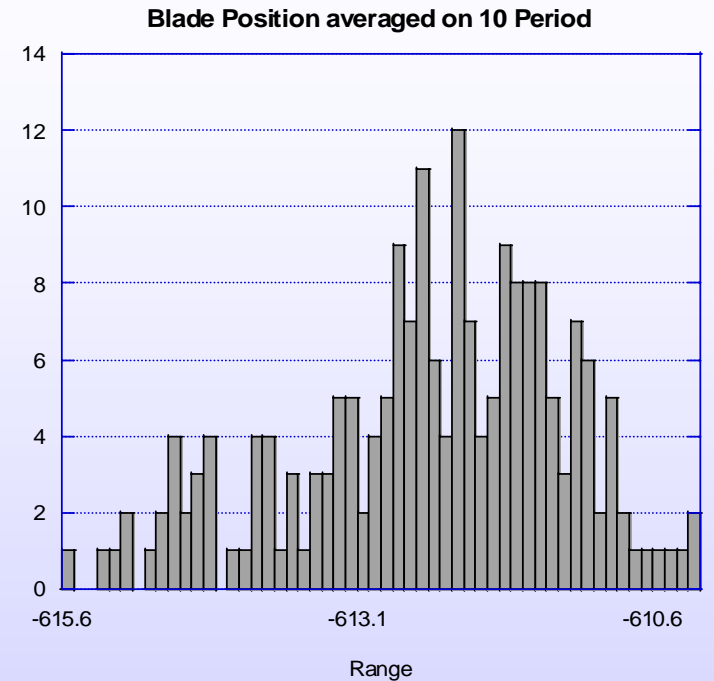
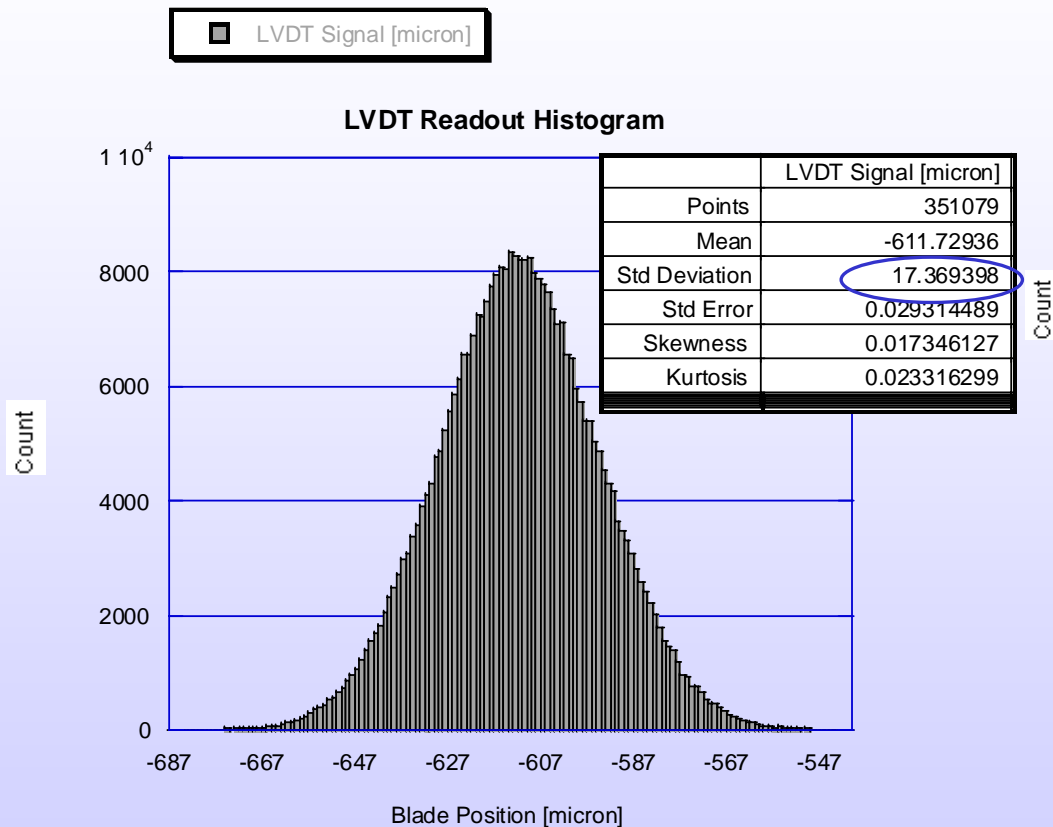
$$\frac{dY}{dT} : -\frac{g}{L\omega_y^2} \alpha_E$$

Where  $\alpha_E$  is the thermal expansion coefficient given by the Young's modulus

Virginio Sannibale et al.

The large thermal dependence of the blade working point with temperature, at low stiffness, makes it practically impossible to obtain very low resonant frequencies

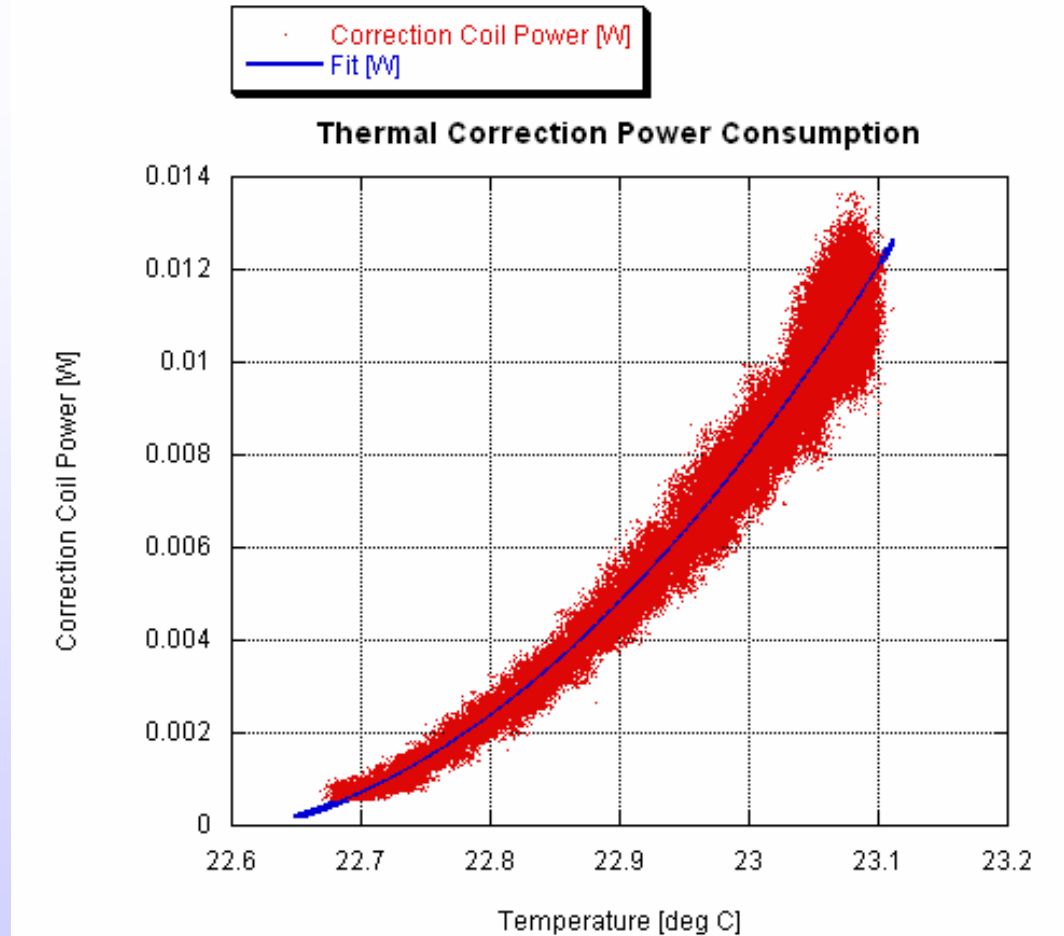
# Overnight Blade Tip Position stability Integrated on 10 Period



	Blade Position [micron] averaged 100 sec and decimated
Mean	-612.4834
Std Deviation	1.1317328
Variance	1.2808192
Std Error	0.08042875
Skewness	-0.51884154
Kurtosis	-0.25288313

These residuals are mainly the r.m.s. 100 mHz oscillator resonance excited by the seismic activity

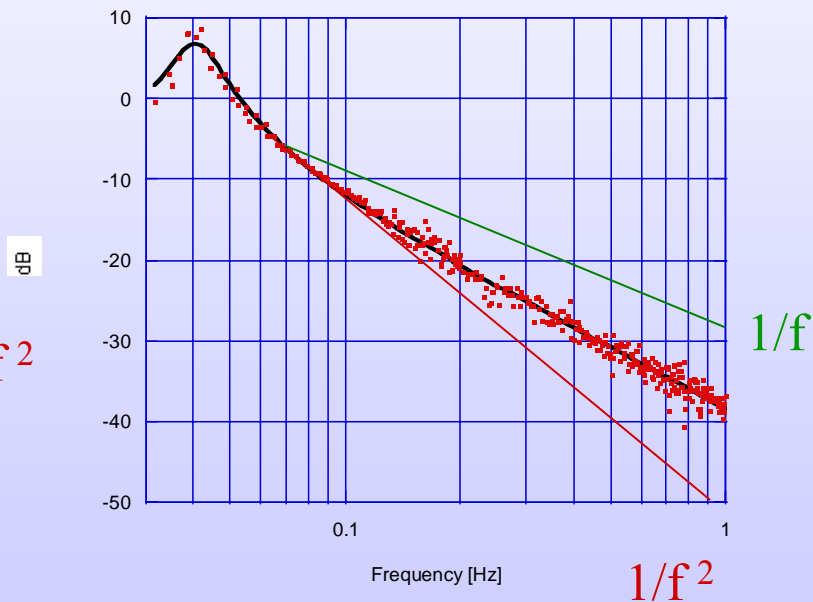
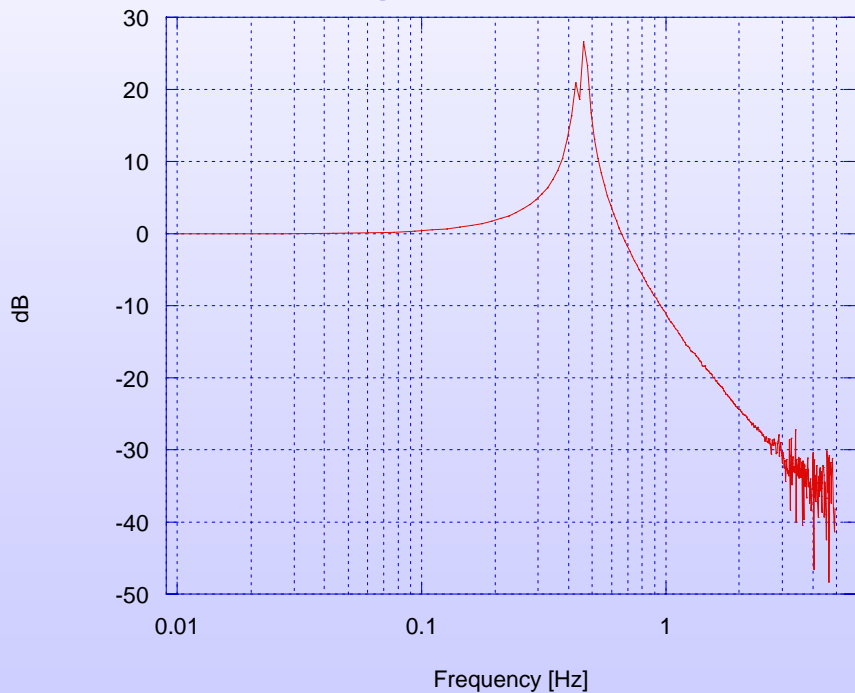
# Power Considerations



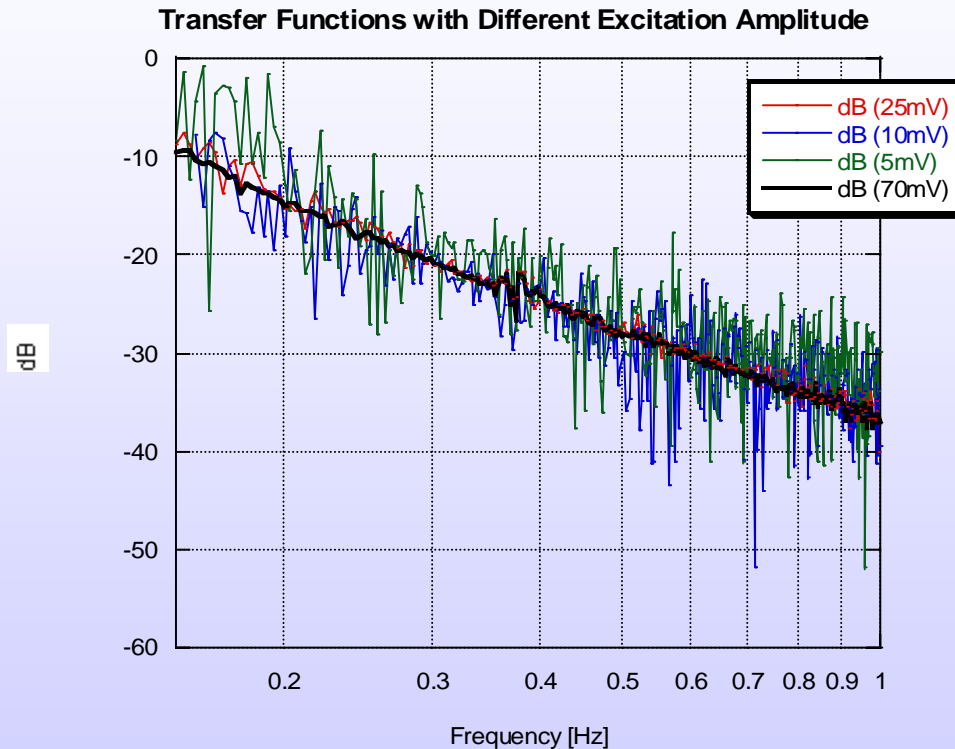
The Power consumption is of the order of "10mW

## 1. Slower Slope in the Lower Frequency Transfer Function Measurements

Right  $1/f^2$  Behavior



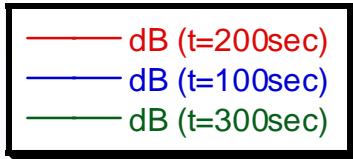
# Transfer Function Measurements with different Excitation Amplitude



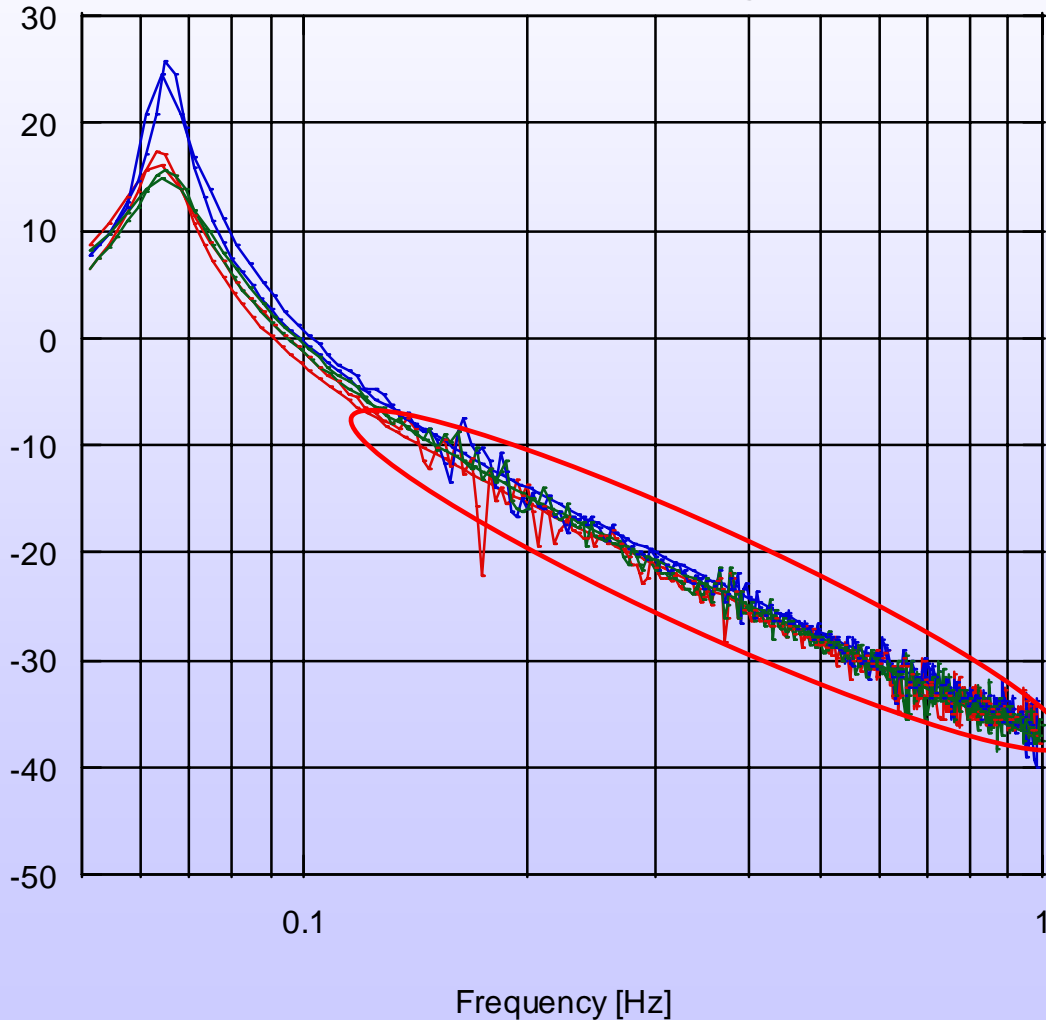
The slope does not change



# Transfer Function Slope for Different Integration Times



Transfer Function with Different Integration Times

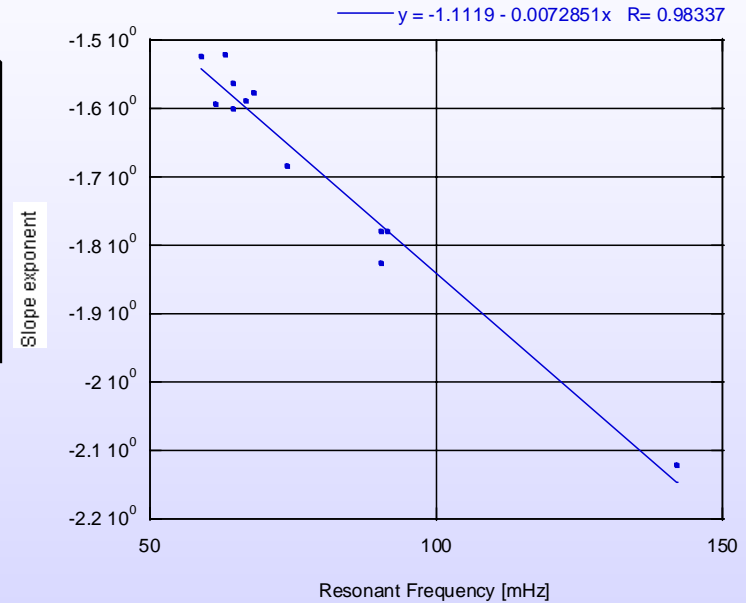
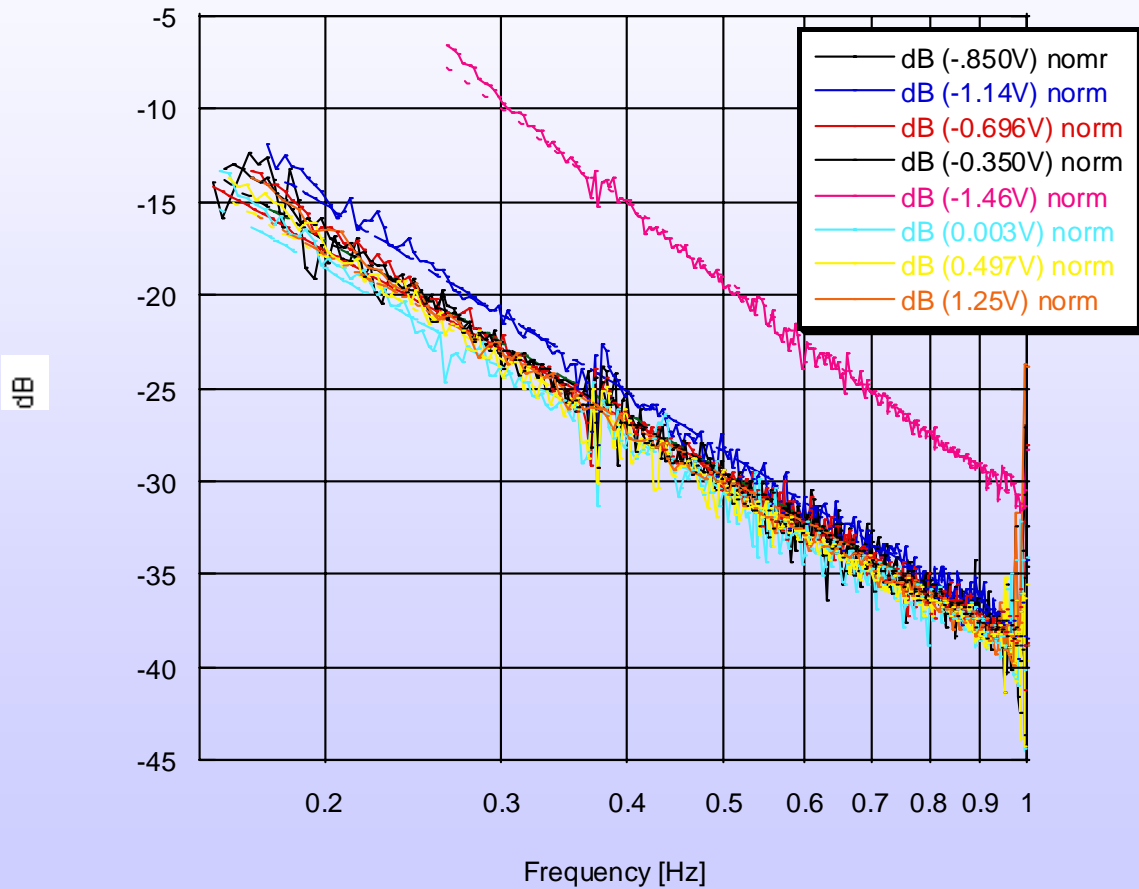


The Slope does not depend on the integration time

dB

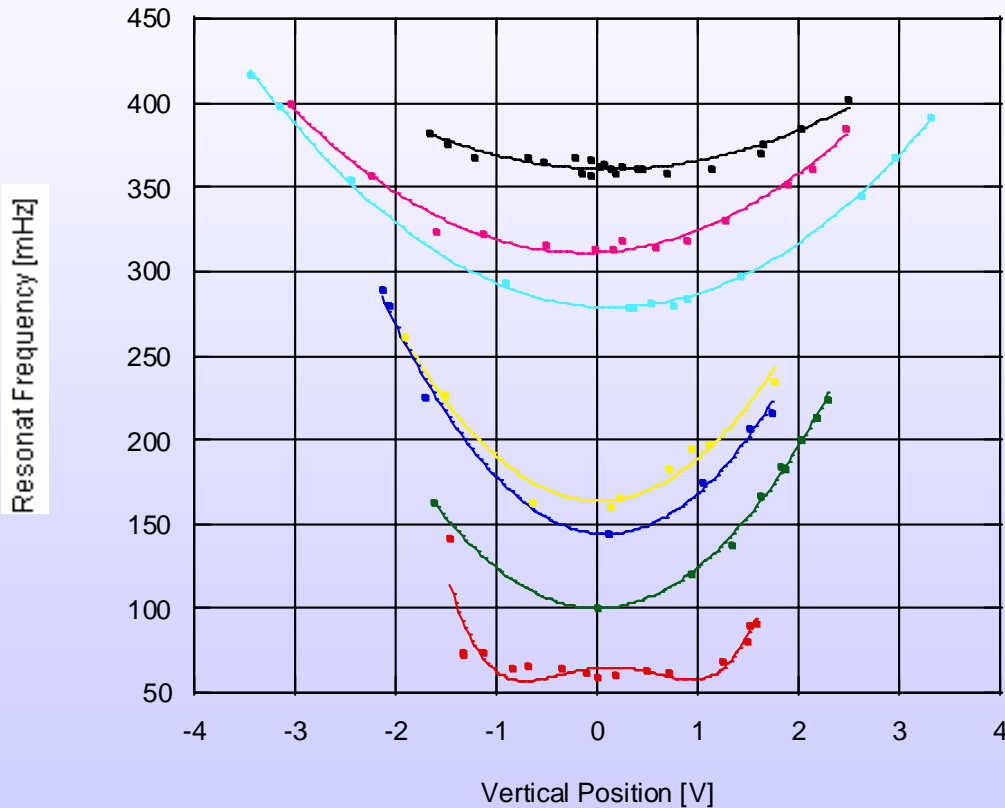
# Slope for Different Vertical Positions

Transfer Function measurements for different vertical positions



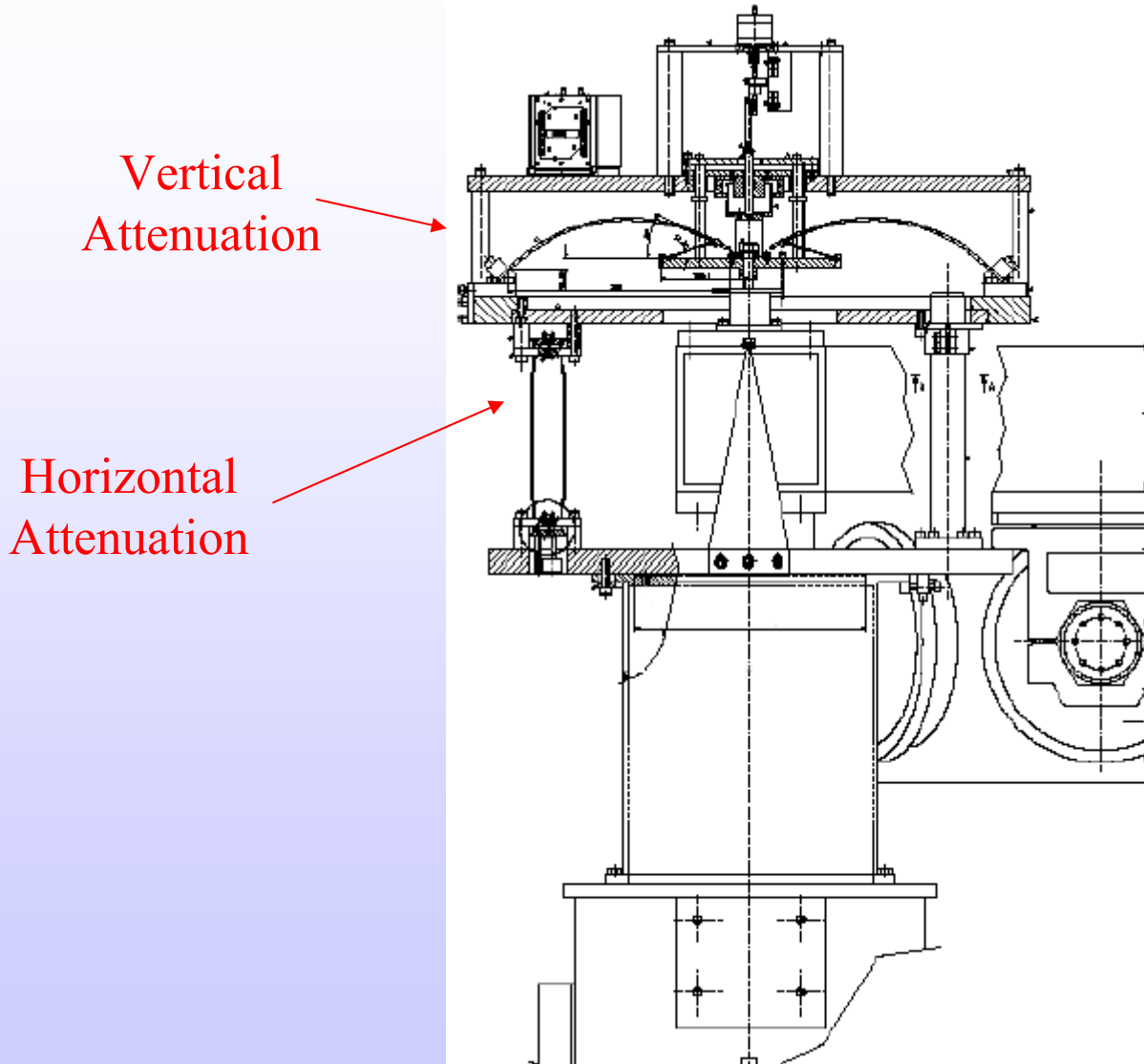
Need for more investigations

# Second anomaly founded



- So far the working point to frequency dependence has always been observed to be hyperbolic, getting narrower at lower frequency
- At lower frequency we find a departure from the hyperbolic behavior (the fit in the bottom data set is a fourth power polynomial)
- We suppose that higher order effect may be taking over when the anti-spring gets close to fully neutralize the spring constant
- The newly observed behavior is coincidental with the departure from  $1/f^2$  of the attenuation transfer function
- We do not know yet if the two anomalous effects are correlated.

# Is this useful for LIGO??



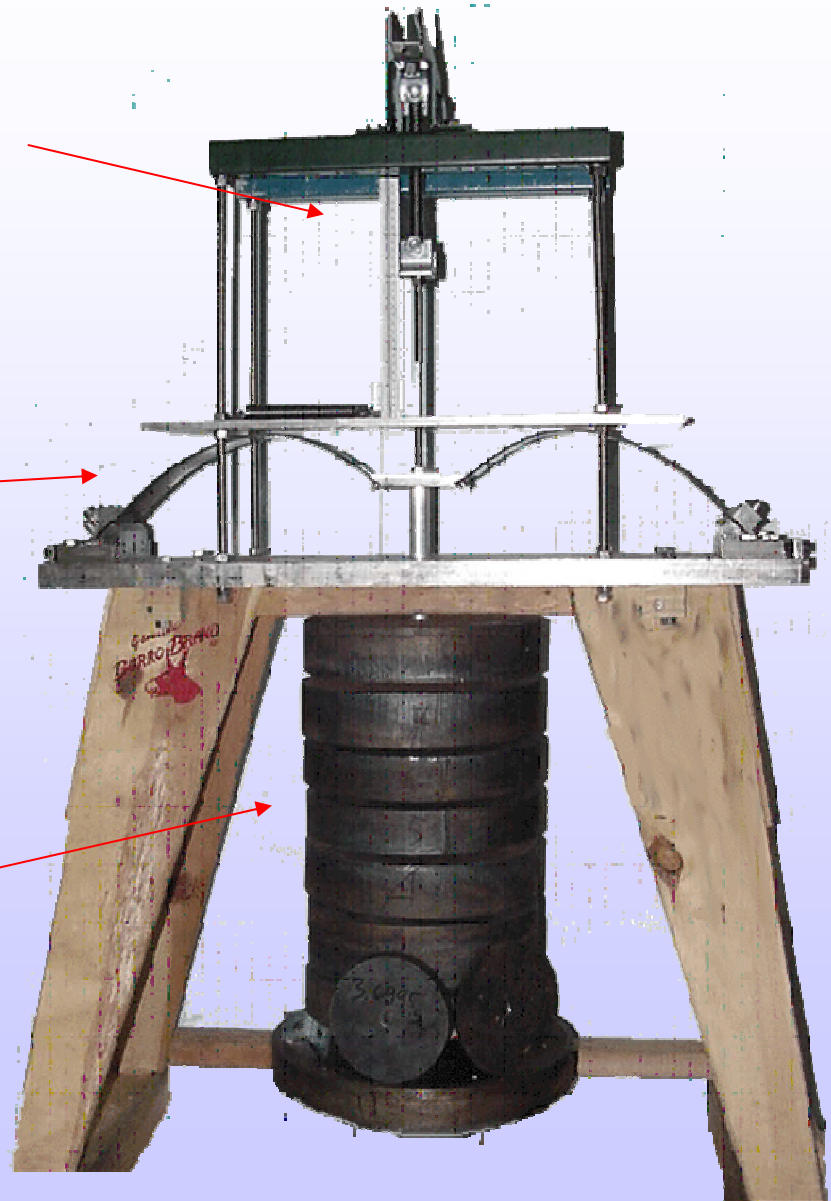
the LIGO Deep Fall Back solution prototype for one-pier preattenuators

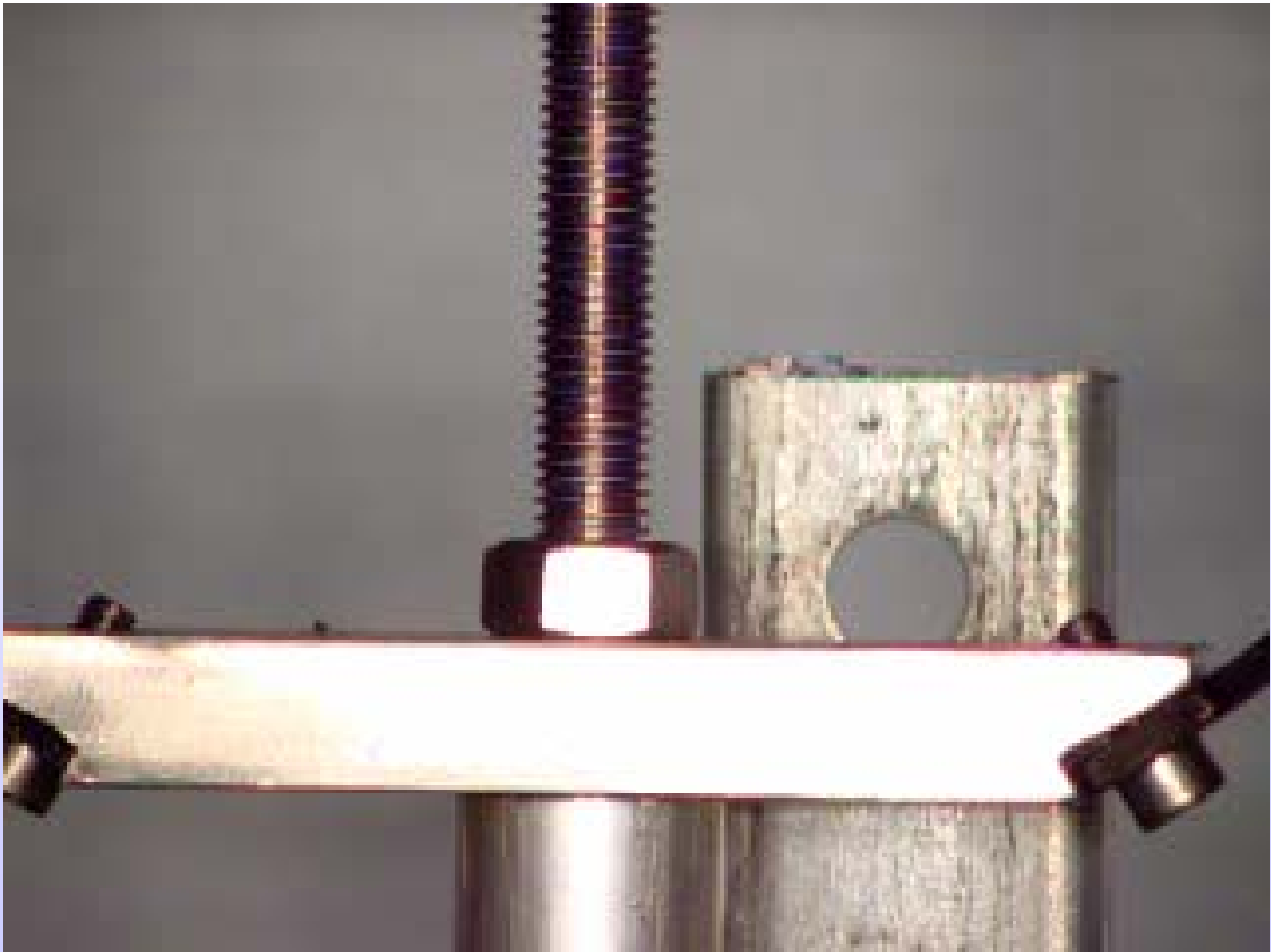
# DFBS prototype

Bellow equivalent springs

Cantilevers

350 Kg Payload





Real time



## DFBS Prototype

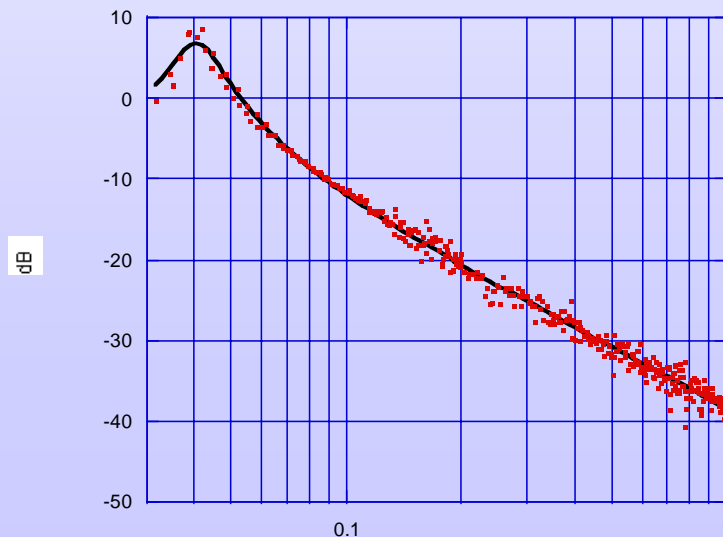
So far driven down to 120mHz despite the additional springs (4/3 of the equivalent bellow stiffness) in fully passive configuration



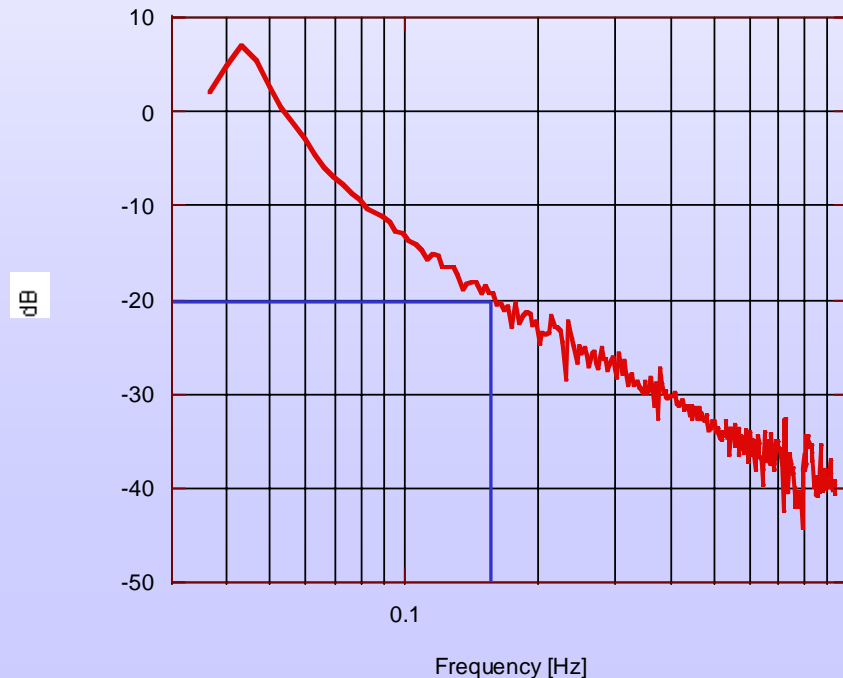
Expect  $\leq 30\text{mHz}$  if tuned with electromagnetic anti-spring

attenuation plateau at  $10^{-3}$  proven on preceding prototypes (expect similar performance)

- This development of Electromagnetic Correction Springs was designed to boost the Low Frequency attenuation performance of Geometric Anti Springs for **future Underground Low Frequency Gravitational Wave Interferometric Detectors** (Horizontal Attenuation was always easily available)
- This development allows for further depression of seismic perturbations, beyond the performance of the Superattenuators, reaching down to 1 Hz and even below.



- The retrofitting of this technology on existing system like the LIGO deep fall back pre-isolator solution may allow the introduction of attenuation factors as large as one thousand for frequencies above 1 Hertz
- Sizeable attenuation at the micro seismic peak at 150 mHz can be obtained as well



## Next Steps

- Find the source of the less than  $1/f^2$  behavior
- Repeat the Measurements with Accelerometers
- Study and Reduce the Control Circuit Noise Improving some of its Performances (Yanyi Chen)
- Make a Mechanical Thermal Compensation
- Use this Seismic Attenuation System on the Mexican Hat Interferometer (Barbara Simoni)

