



Status of LIGO Simulation

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- ◆ End to End simulation

- » Overview
- » Physics
- » Simple example

- ◆ Past

- » Lock acquisition

- ◆ Present

- » Noise simulation

- ◆ Future

- » Advanced LIGO

- ◆ Scientists

- » Hiro Yamamoto
- » Matt Evans
- » Biplab Bhawal
- » Virginio Sannibale 1/3
- » Luca Matone
 - LHO liaison

- ◆ Programmers

- » Bruce Sears
- » Melody Araya



LIGO End to End Simulation

the motivation

- ◆ Assist detector design, commissioning, and data analysis
- ◆ To understand a complex system
 - » *back of the envelope is not large enough*
 - » **complex hardware** : pre-stabilized laser, input optics, core optics, seismic isolation system on moving ground, suspension, sensors and actuators
 - » **feedback loops** : length and alignment controls, feedback to laser
 - » **non-linearity** : cavity dynamics to actuators
 - » **field** : non-Gaussian field propagation through non perfect mirrors and lenses
 - » **noise** : mechanical, thermal, sensor, field-induced, laser, etc : amplitude and frequency : creation, coupling and propagation
 - » **wide dynamic range** : $10^{-6} \sim 10^{-20}$ m
- ◆ **As easy as back of the envelope**



E2E perspective

- ◆ e2e development started after LIGO 1 design completed (1997 ~)
- ◆ LIGO 1 lock acquisition was redesigned successfully using e2e by M.Evans (2000 ~ 2001)
- ◆ Major on going efforts for LIGO I (2001 ~)
 - » Realistic noise of the locked state interferometer
 - » Effect of the thermal lensing on the lock acquisition
 - » Effect of the train and logging activity at LLO to lock acquisition and lock stability
- ◆ Efforts for Advanced LIGO (2000 ~)
 - » Development of optics and mechanics modules
 - » Trying to expand users who can contribute
 - A.Weinstein (CIT), J.Betz Wieser (MIT), M.Rakmanov (UF), M.Malec (GEO)



End to End Simulation overview

- ◆ General purpose GW interferometer simulation framework
 - » Generic tool like matlab or mathematica
 - » Time domain simulation written in C++
 - Speed and flexibility
 - » Optics, mechanics, servo, ...
 - time domain modal model, single suspended 3D mass.
 - analog and digital controller - ADC, DAC, digital filter, etc
- ◆ End to End simulation environment
 - » Simulation engine - modeler, modeler_freq
 - » Description files defining what to simulate - Simple pendulum ~ full LIGO (constituent files are called “box files” or simply “boxes”)
 - » Graphical Editor to create description files - alfi
- ◆ LIGO I simulation packages
 - » Han2k : used for the lock acquisition design
 - » SimLIGO : to assist LIGO I commissioning



End to End Simulation

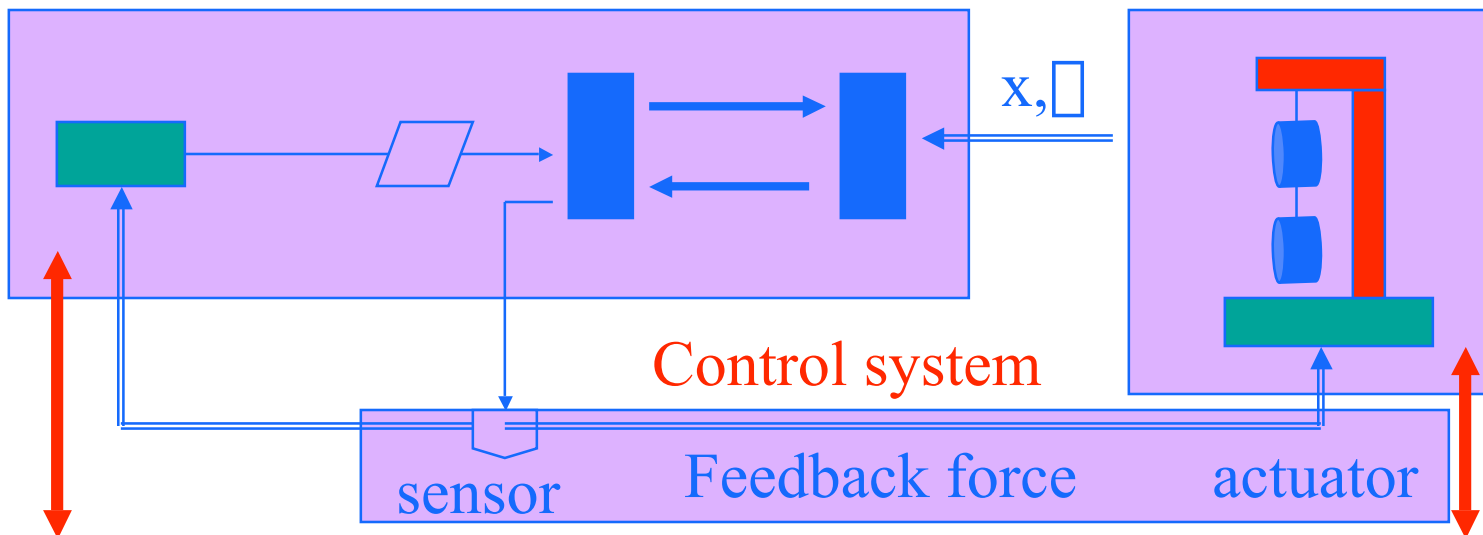
e2e vs matlab

	e2e	matlab
General purpose calculator	Laser+2 mirrors = FP	1+2 = 3
Language	Easy construction of LIGO like opto-mechanical system	Quick prototyping of wide variety of problems
Built-in function	Primitive modules : Mirror, michelson cavity, 3d mass, digital_filter, etc FUNC - expression parser	math functions, strings, graphics, etc
User programs	Execute box files in modeler, (compound module)	execute m-files in matlab
GUI	Alfi	simulink

End to End Simulation

coarse view

Laser Optics system Mechanical system

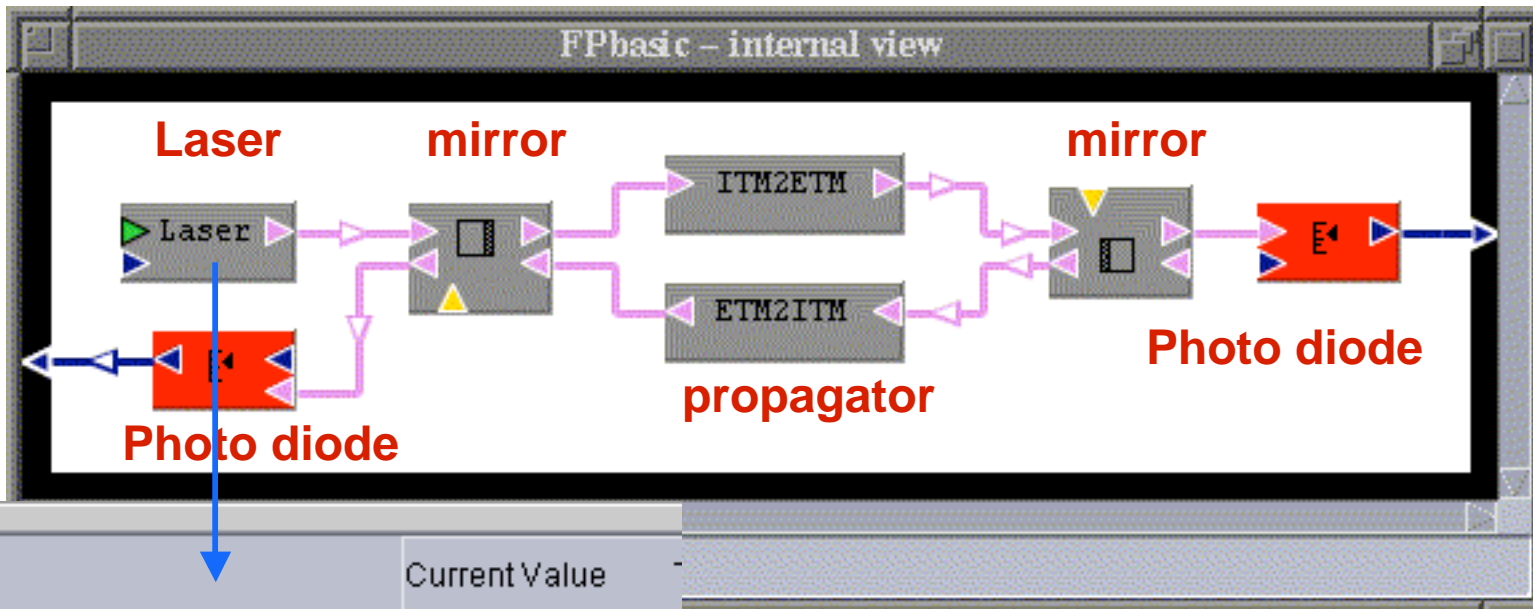


- Time domain modal model
- Objects : laser, mirror, photo diode, ...
- Any planar interferometer
 - Fabry-Perot, Mode cleaner, LIGO I,
 - Advanced LIGO, ...

- Transfer function using Digital filter
- Single Suspended mirror
- Mechanical Simulation Engine (object-oriented)



e2e Graphical Editor



	Current Value
lambda	DEFAULT
waist_size_X	w0
waist_size_Y	w0
distance_waist_X	z_dist
distance_waist_Y	z_dist
angle_resolution	DEFAULT
compute_mismatch_curvature	DEFAULT
max_mode_order	1



Status of LIGO Simulation



e2e primitives

Mirror module - an example

```
struct field  
{ double amps[n];  
  int mode;  
  int polarization;  
  double waistPos;  
}
```

Mass position and orientation

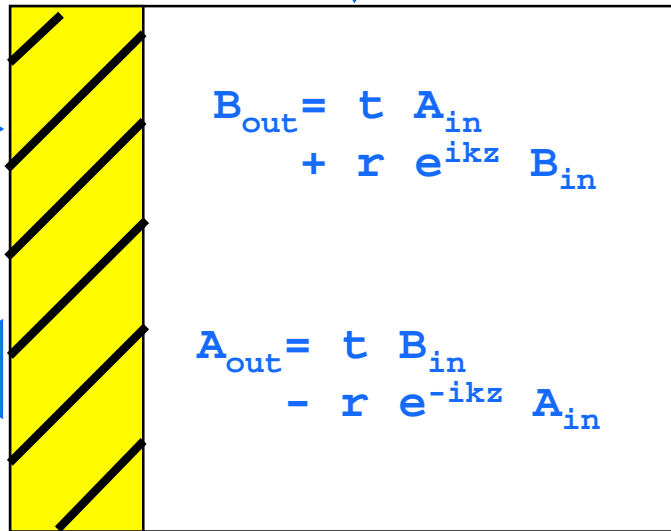
```
struct clamp  
{ double x, y, z;  
  double thetax,...  
  int statusBits;  
}
```

Input field to coated side

output field from coated side



A



B

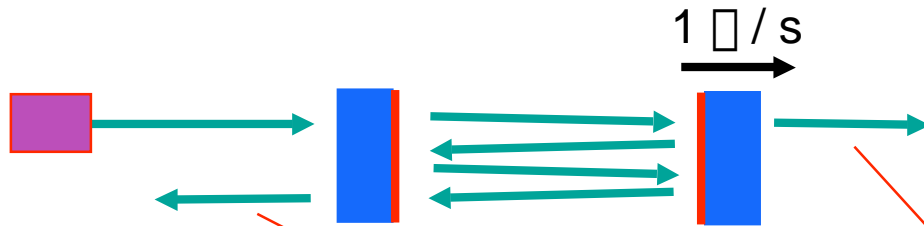
output field from substrate side

Input field to substrate side

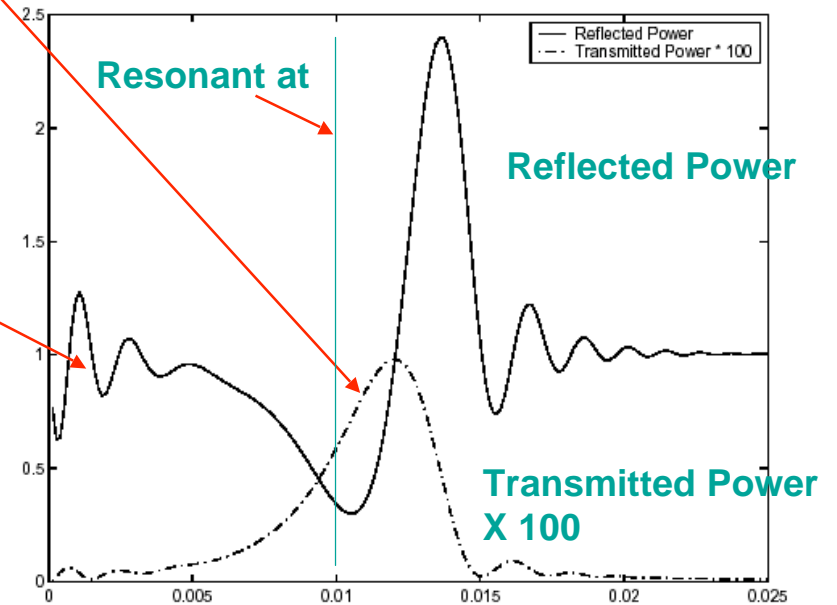
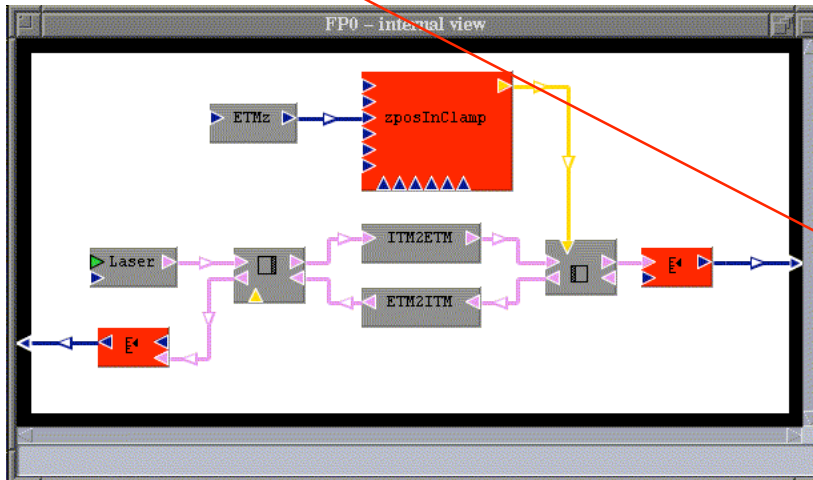
Static parameters : Reflectivity, transmittance, surface curvature, etc

e2e example - 1

Fabry-Perot cavity dynamics



$$ETMz = -10^{-8} + 10^{-6} t$$

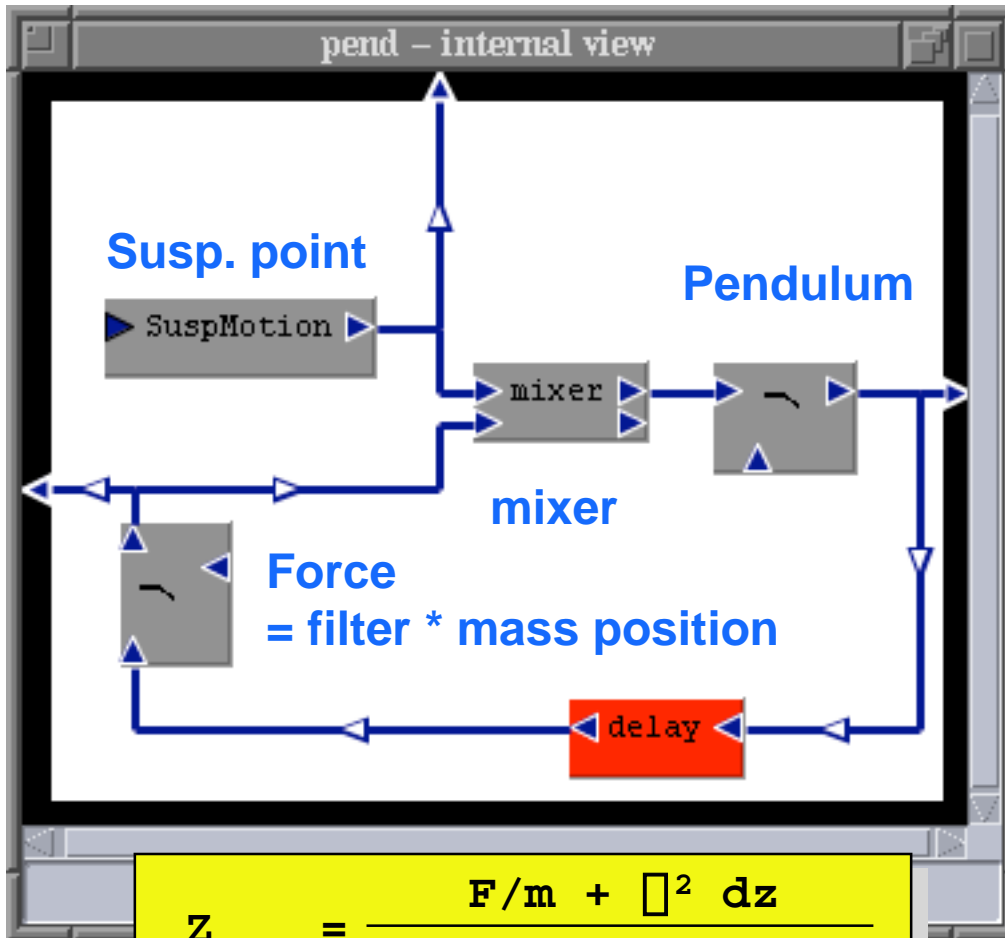


Power = 1 W, $T_{ITM}=0.03$, $T_{ETM}=100\text{ppm}$,
 $L_{\text{cavity}} = 4000\text{m}$



e2e example - 2

Suspended mass with control



$$Z_{\text{mass}} = \frac{F/m + \ddot{z}}{s^2 + a s + \omega^2}$$

Suspension point

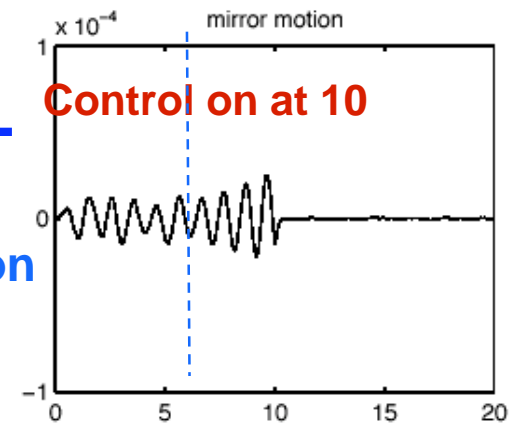
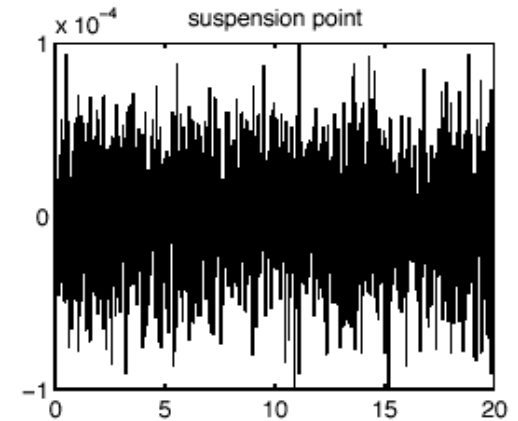


Pendulum res. at 1Hz

Force



Mass position





FUNC primitive module - command liner in GUI -

- ◆ GUI is not always the best tool
- ◆ FUNC is an expression parser, based on c-like syntax
- ◆ all basic c functions, `bessel`, `hermite`
- ◆ special functions : `time_now()`, `white_noise`,
`digital_filter(poles, zeros)`, `fp_guoyphse(L,R1,R2)`, ...
- ◆ predefined constants : `PI`, `LIGHT_SPEED`, ...
- ◆ inline functions : `leng(x,y) = sqrt(x*x+y*y)`; `L = leng(2,3)`;

mixer module

```
gain = -5; lockTime = 10;  
out0 = if ( time_now()<lockTime , in0, in0+gain*in1 );
```



e2e physics

Time domain simulation

- ◆ Analog process is simulated by a discretized process with a very small time step ($10^{-7} \sim 10^{-3}$ s)

- ◆ Linear system response is handled using digital filter

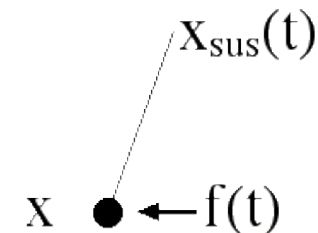
- » e2e DF = PF's pziir.m (bilinear trans (s->z) + SOS) + CDS filter.c

- » Transfer function -> digital filter

- » Pendulum motion

- » Analog electronics

$$x = \frac{1}{s^2 + \zeta s + \omega_0^2} \frac{f}{m} + \omega_0^2 x_{sus}$$



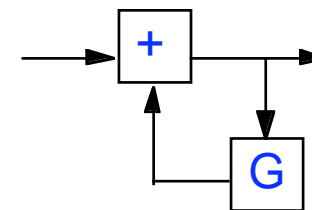
- ◆ Easy to include non linear effect

- » Saturation, e.g.

- ◆ A loop should have a delay

- » Need to put explicit delay when needed

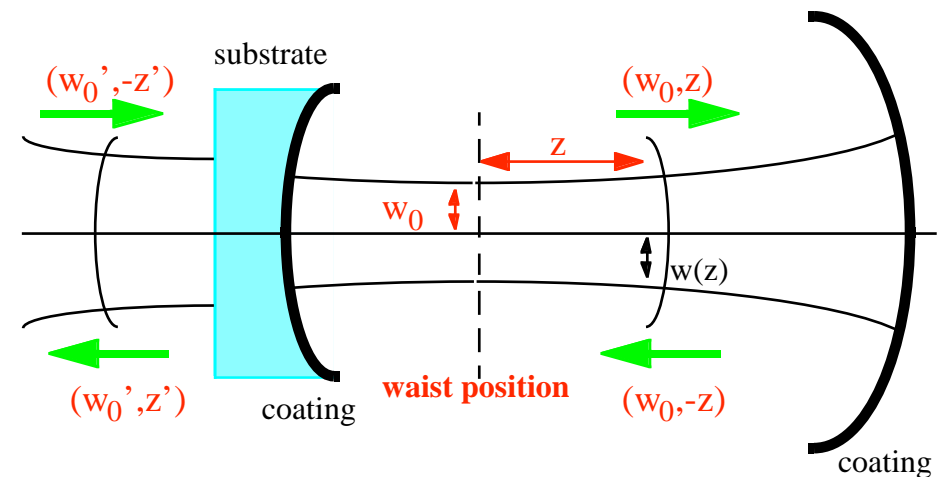
- » Need to choose small enough time step



e2e physics

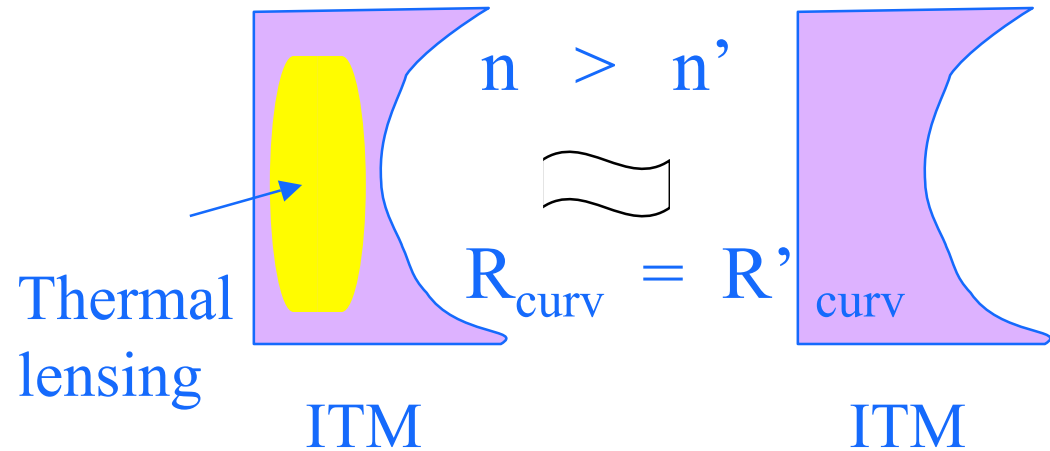
Fields and optics

- ◆ Time domain modal model
 - » field is expanded using Hermite-Gaussian eigen states
 - » number of modes $(n+m) \leq 4$ for now, no limit in the future
- ◆ Reflection matrix
 - » tilt
 - » vertical shift
 - » curvature mismatch
- ◆ Completely modular
 - » Arbitrary planar optics configuration can be constructed by combining mirrors and propagators
- ◆ Photo diodes with arbitrary shapes can be attached anywhere
- ◆ Adiabatic calculation for short cavities for faster simulation

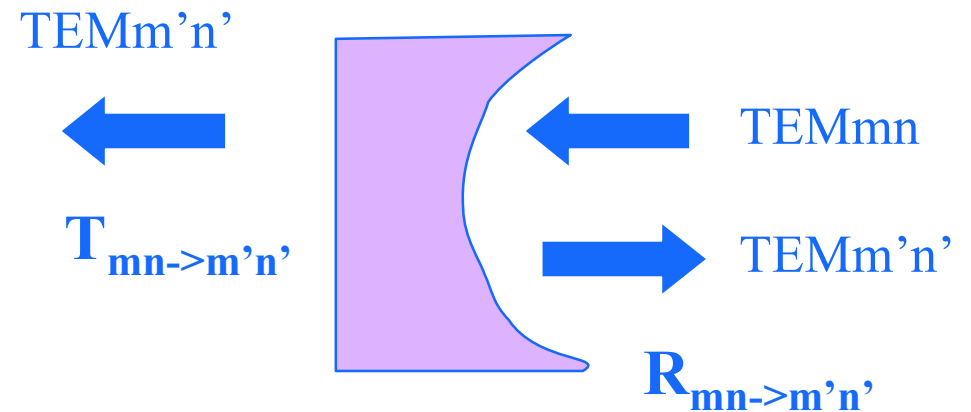


e2e physics optics imperfection

- ◆ Simple lens model
 - » LIGO 1
 - lock, mode mixing



- ◆ Mode decomposition matrix - tbd
 - » LIGO 1
 - actual mirror phase map
 - more accurate
 - » Adv. LIGO



e2e physics Mechanics simulation

(1) Seismic motion from measurement

- » correlations among stacks
- » fit and use psd or use time series

(2) Parameterized HYTEC stack

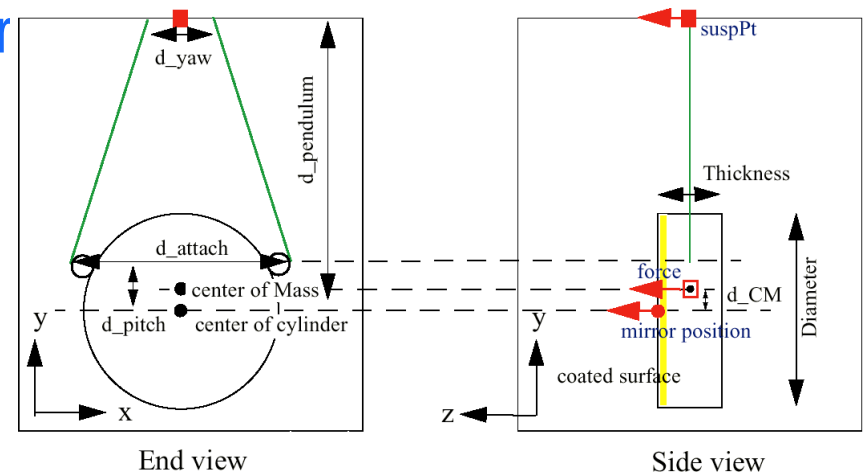
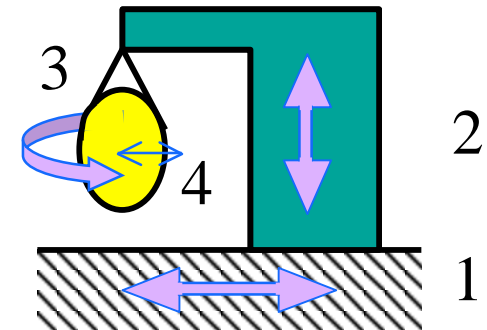
- » Ed Daw

(3) Simple single suspended mirror

- » M.Rakmanov, V.Sannibale
- » 4/5 sensors and actuators
- » couple between LSC and ASC

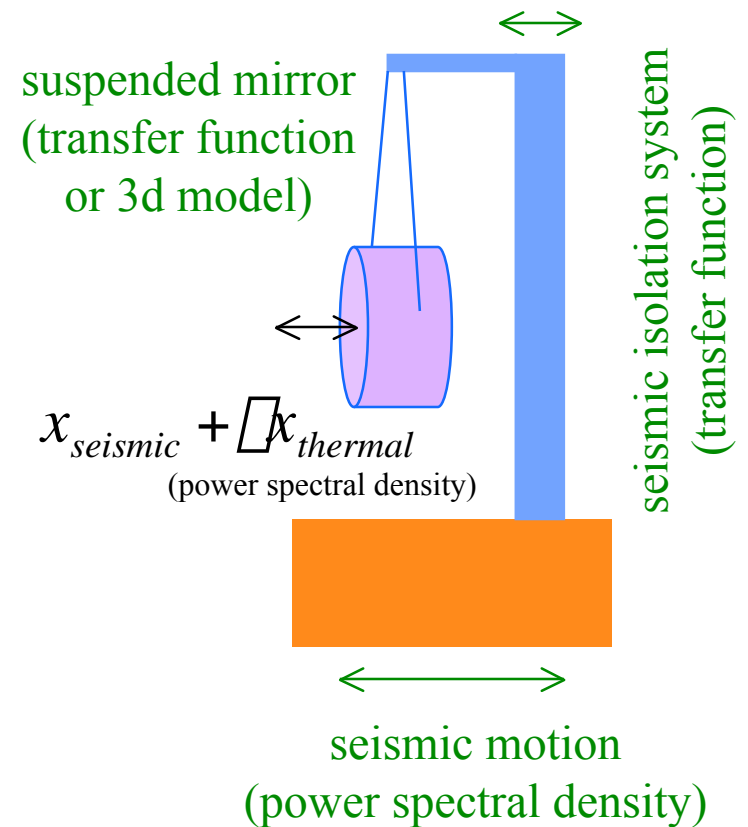
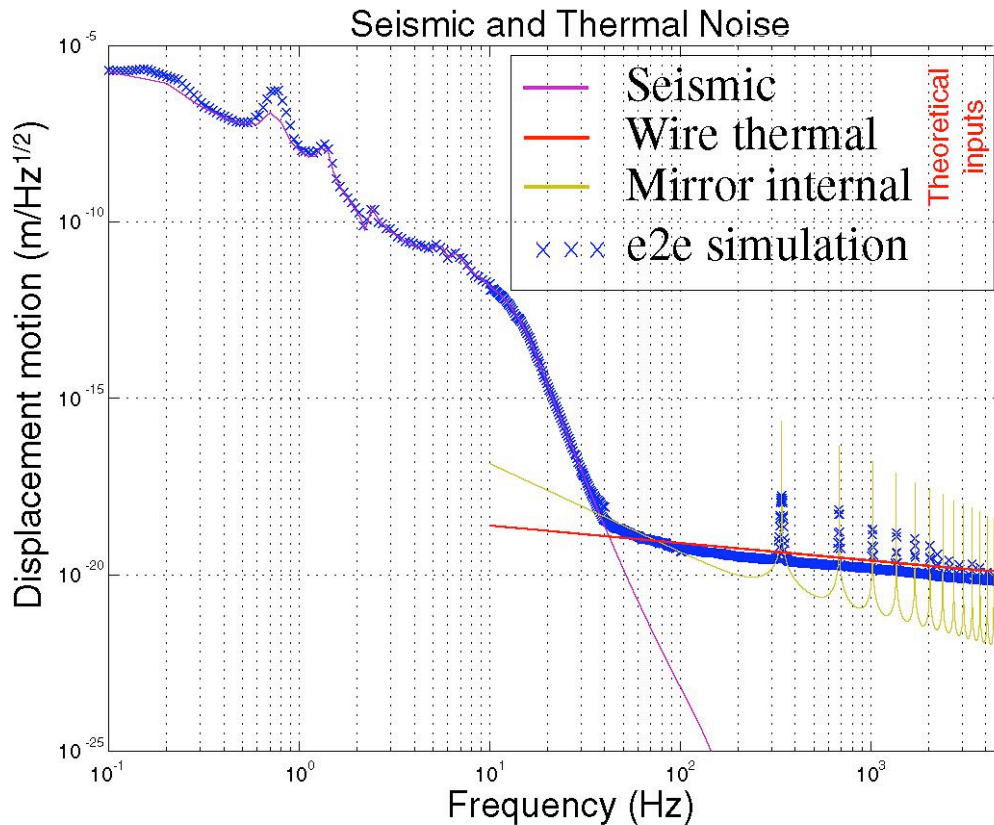
(4) Thermal noise added in an ad hoc way

- » using Sam Finn's model



Mechanical noise of one mirror

seismic & thermal noises





Sensing noise

Shot noise for an arbitrary input

Average number of photons

$$n_0(t) = \frac{\int P(t) \cdot \int t}{h \cdot \int}$$

Actual integer number of photons

$$n(t) = \text{Poisson}(n_0(t))$$

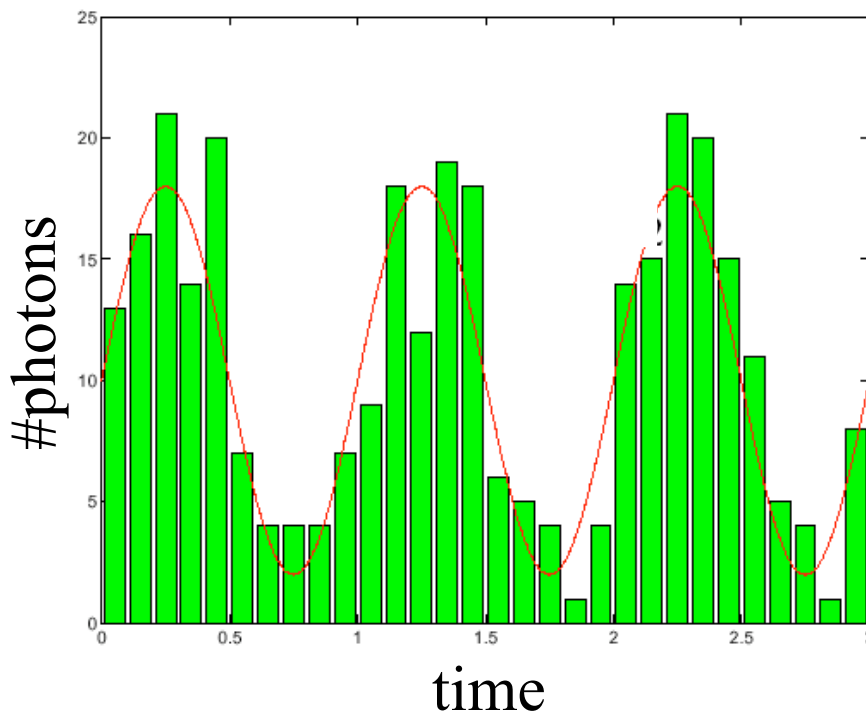
Simulation option

Shot noise can be turned on or off for each photo diode separately.

— Average number of photons by the input power of arbitrary time dependence



Actual number of photons which the detector senses.





First LIGO simulation

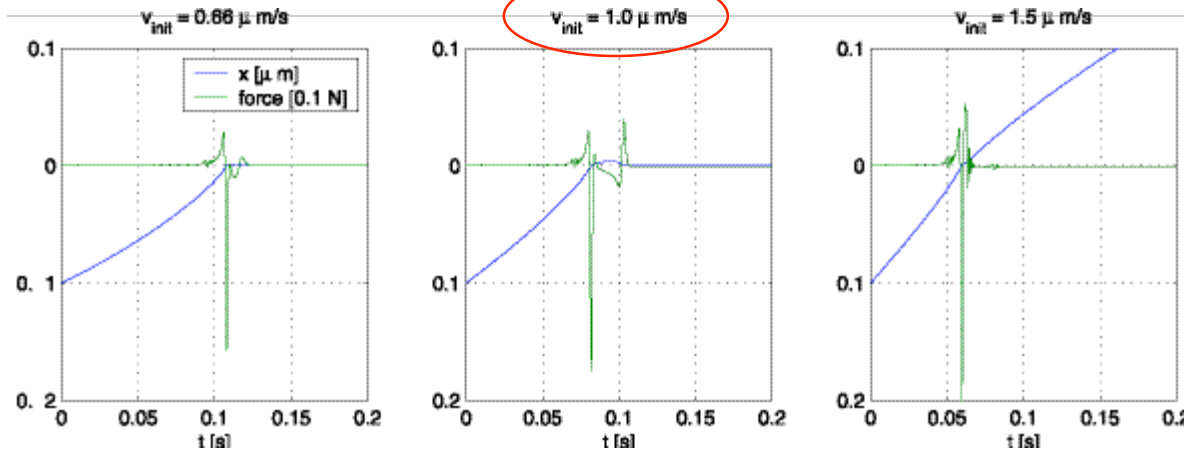
Han2k

- ◆ Matt Evans Thesis
- ◆ Purpose
 - » design and develop the LHO 2k IFO locking servo
 - » simulate the major characteristics of length degree of freedom under 20 Hz.
- ◆ Simulation includes
 - » Scalar field approximation
 - » 1 DOF, everywhere
 - » saturation of actuators
 - » Simplified seismic motion and correlation
 - » Analog LSC, no ASC
 - » no frequency noise, no shot noise, no sensor/actuator/electronic noise

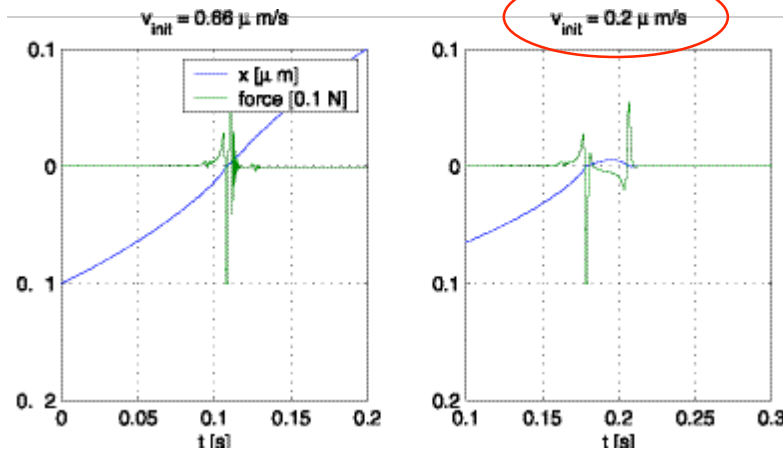
Fabry-Perot

ideal vs realistic

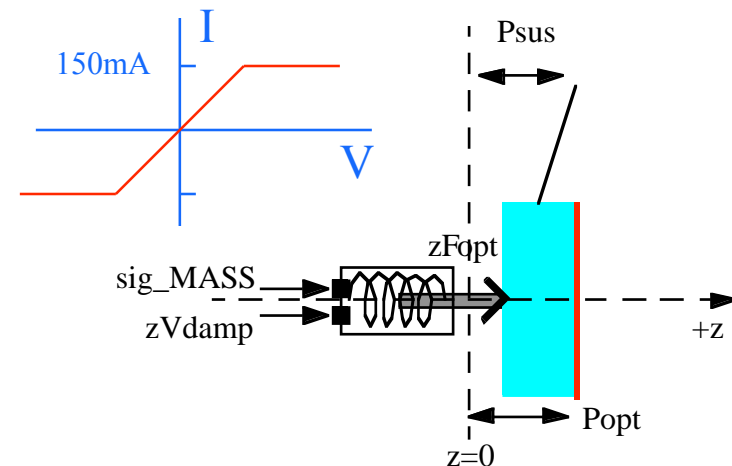
ideal



realistic



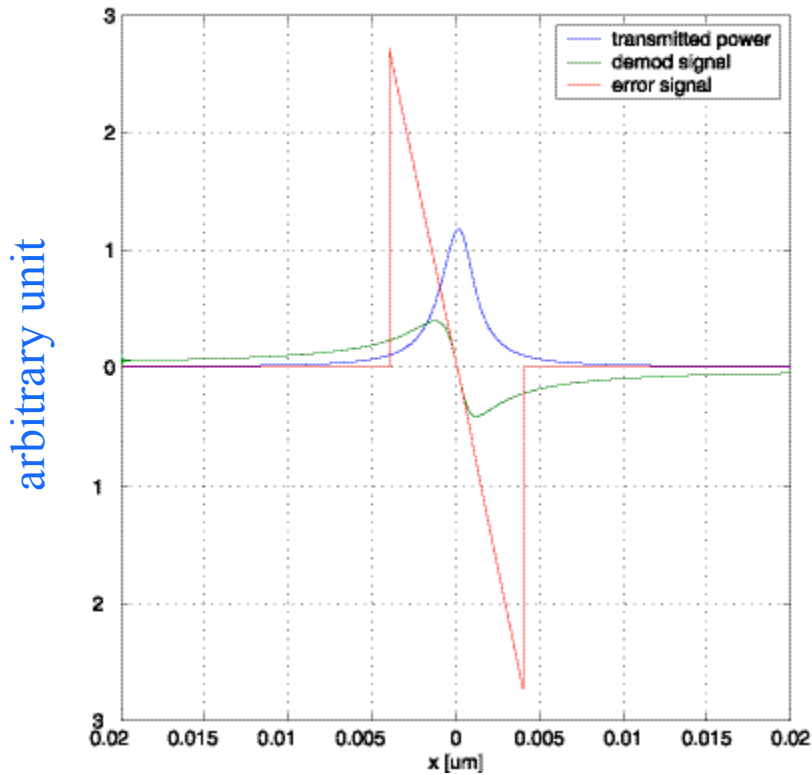
Linear Controllers:
Realistic actuation modeling plays a critical role in control design.



Fabry-Perot

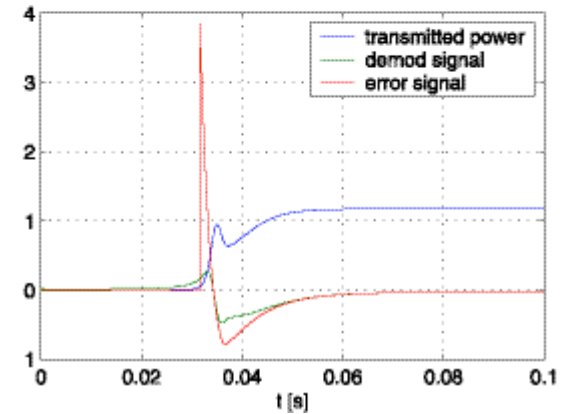
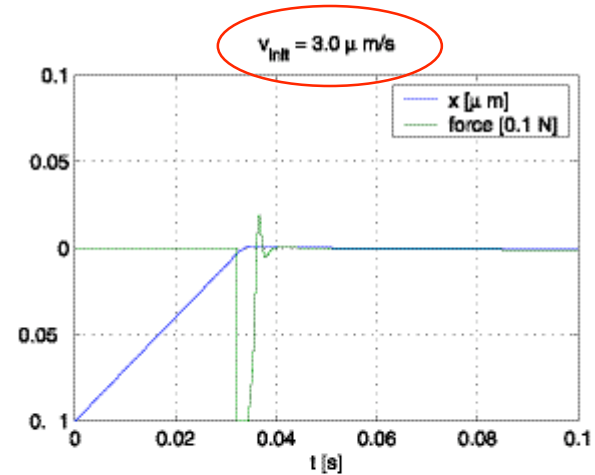
Error signal linearization

$$S = \frac{S_{PDH}}{|A_{tr}|^2} = \left[\frac{r_{ETM}}{t_{ETM}^2} \sin \right]$$



arbitrary unit

arbitrary unit

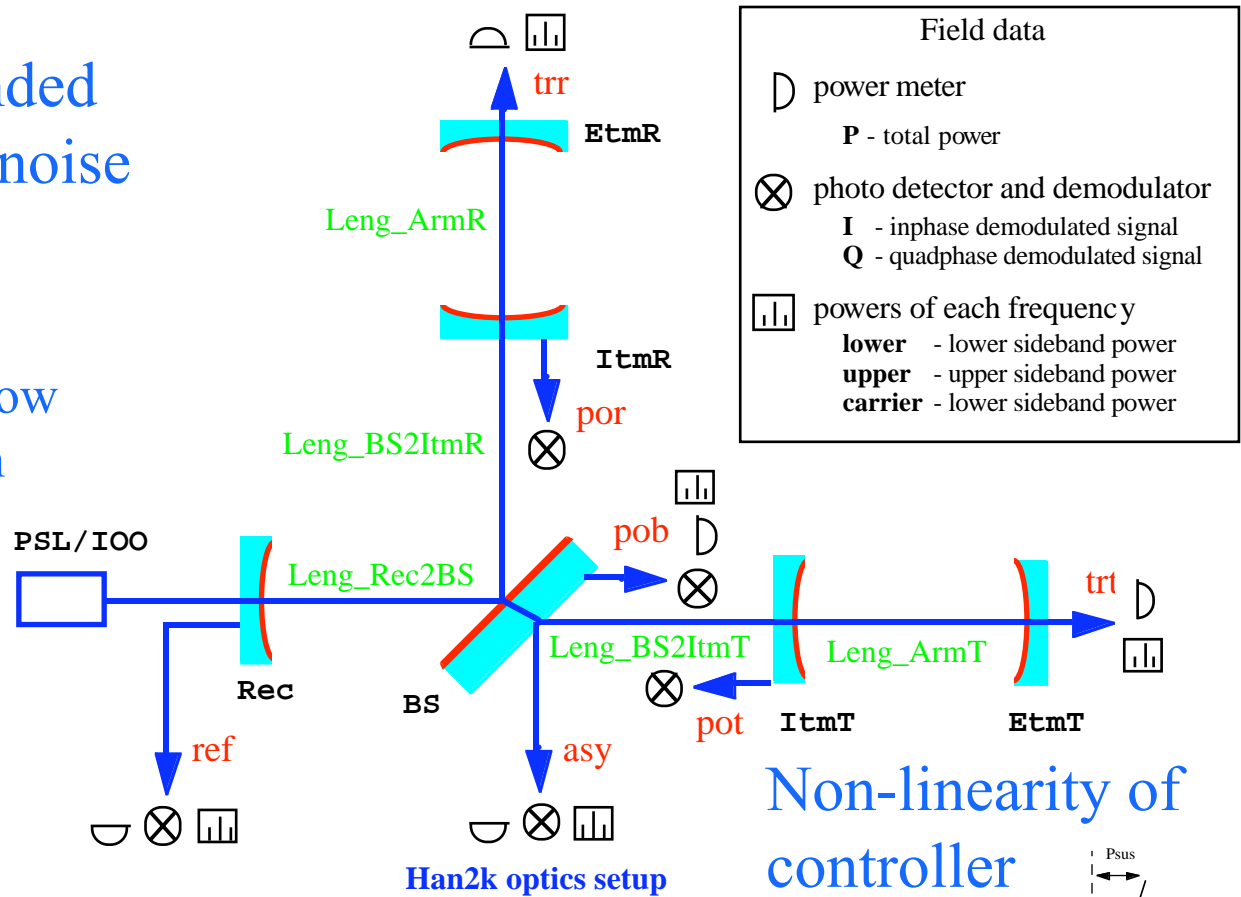
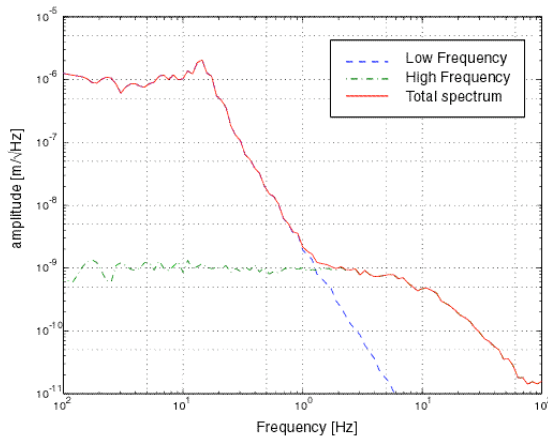




Hanford 2k simulation setup

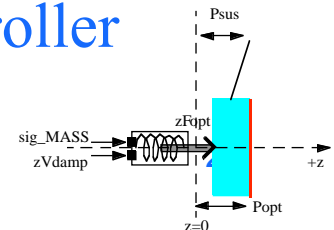
6 independent suspended mirrors with seismic noise

corner station :
strong correlation in the low frequency seismic motion



Han2k optics setup

Non-linearity of controller

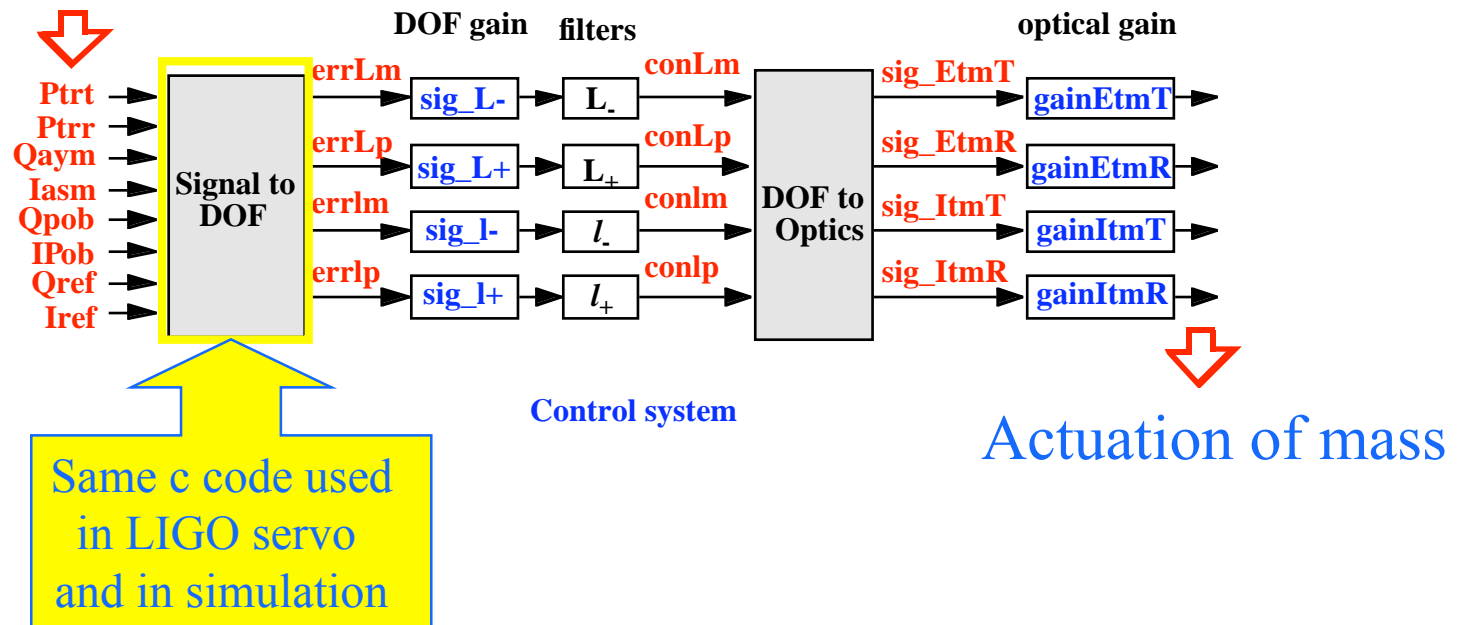




Automated Control Matrix System

LIGO T000105 Matt Evans

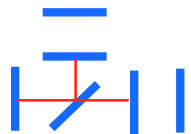
Field signal



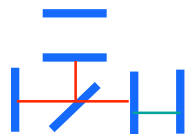
Multi step locking



State 1 : Nothing is controlled. This is the starting point for lock acquisition.



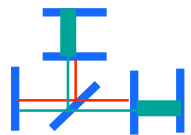
State 2 : The power recycling cavity is held on a carrier anti-resonance. In this state the sidebands resonate in the recycling cavity.



State 3 : One of the ETMs is controlled and the carrier resonates in the controlled arm.



State 4 : The remaining ETM is controlled and the carrier resonates in both arms and the recycling cavity.



State 5 : The power in the IFO has stabilized at its operating level. This is the ending point for lock acquisition.



Lock acquisition

real and simulated

Figure 1. LHO 2k IFO data

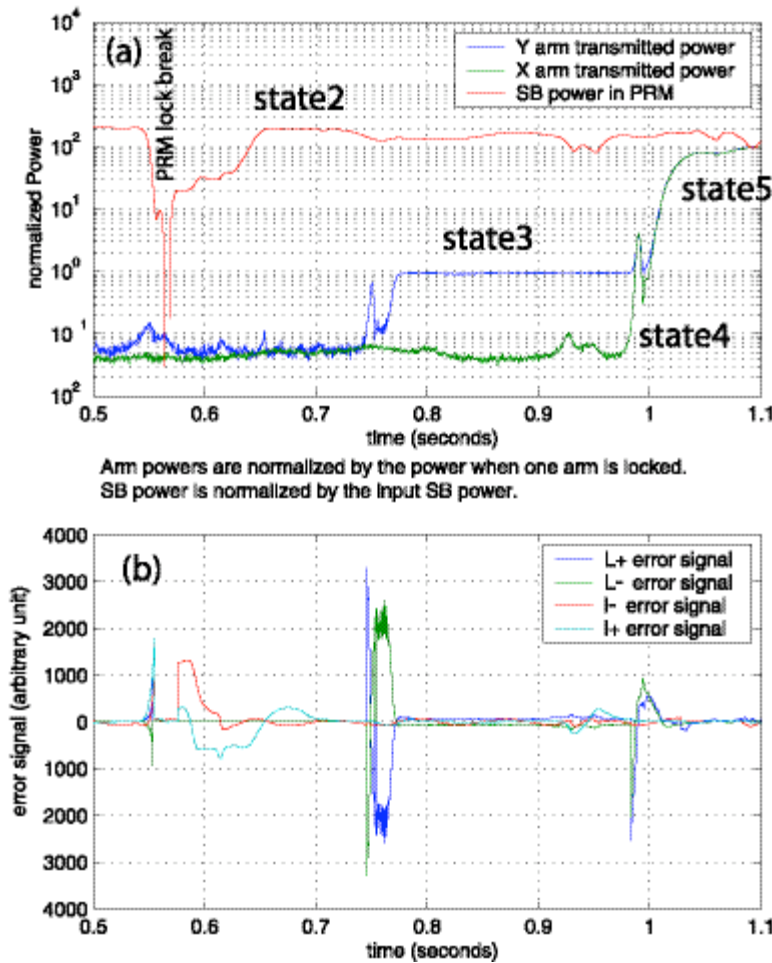
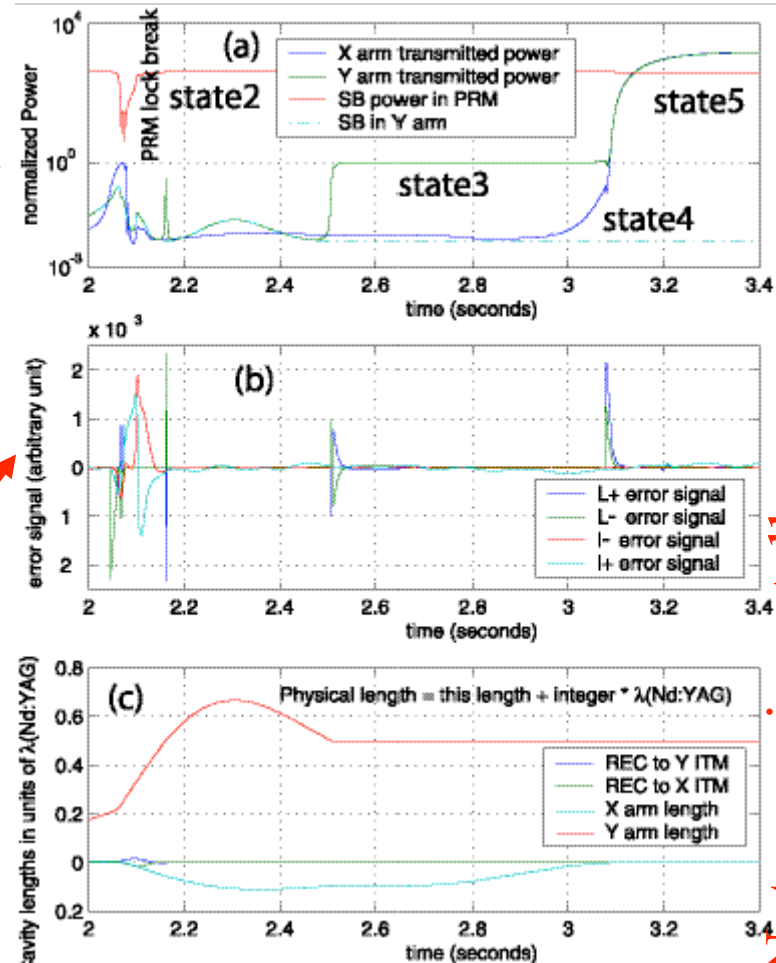


Figure 2. Simulated signal



observable

Not experimentally observable



LIGO Second generation LIGO simulation

SimLIGO

- ◆ Assist noise hunting, noise reduction and lock stability study in the commissioning phase
- ◆ Performance of as-built LIGO
 - » effect of the difference of two arms, etc
- ◆ Noise study
 - » Non-linearity
 - cavity dynamics, electronic saturations, digitization, etc
 - » Bilinear coupling
- ◆ Lock instability
- ◆ Sophisticated lock acquisition
- ◆ Upgrade trade study



SimLIGO

A Detailed Model of LIGO IFO

- ◆ Modal beam representation
 - » alignment, mode matching, thermal lensing
- ◆ 3D mechanics
 - » Correlation of seismic motions in corner station
 - » 6x6 stack transfer function
 - » 3D optics with 4/5 local sensor/actuator pairs
- ◆ Complete analog and digital electronics chains with noise
 - » Common mode feedback
 - » Wave Front Sensors
 - » “Noise characterization of the LHO 4km IFO LSC/DSC electronics” by PF and RA, 12-19 March 2002 included



SimLIGO

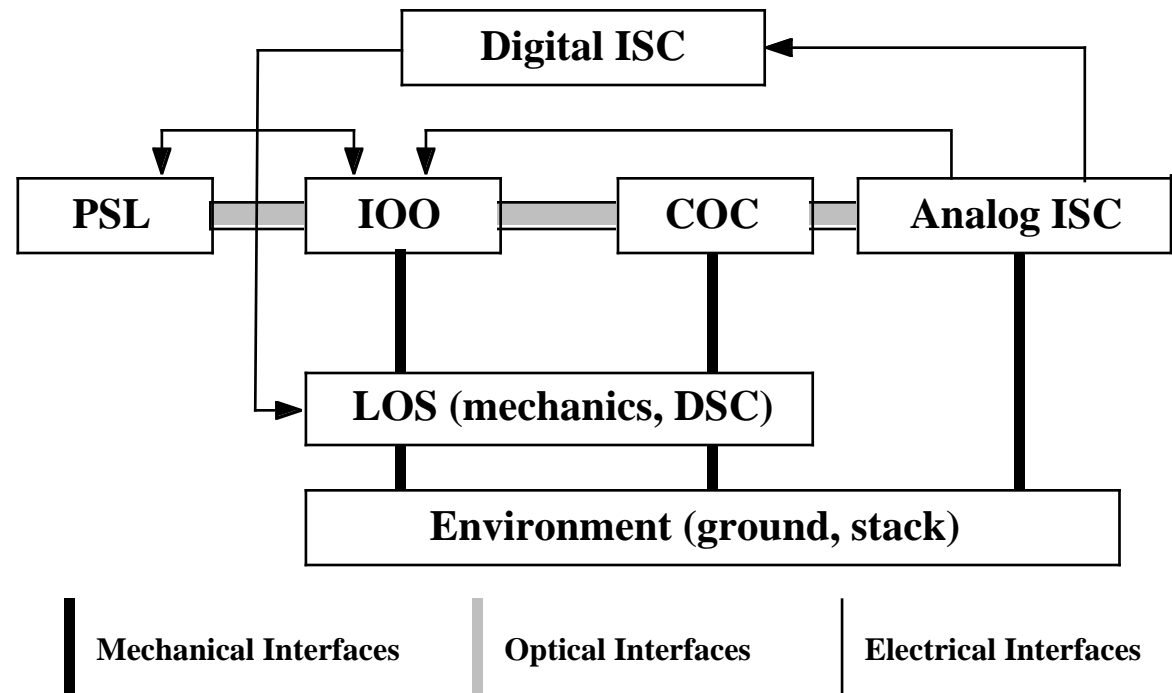
Noise sources

- ◆ All major noise sources
 - » seismic, thermal, sensing, laser frequency and intensity, electronics, mechanical
- ◆ IFO
 - » optical asymmetries (R, T, L, ROC)
 - » non-horizontal geometry (wedge angles, earth's curvature)
 - » phase maps
 - » scattered light
- ◆ Mechanics
 - » wire resonances, test mass internal modes
- ◆ Sensor
 - » photo-detector, whitening filters, anti-aliasing
- ◆ Digital system
 - » ADC, digital TF, DAC
- ◆ Actuation
 - » anti-imaging, dewhitening, coil drivers



SimLIGO

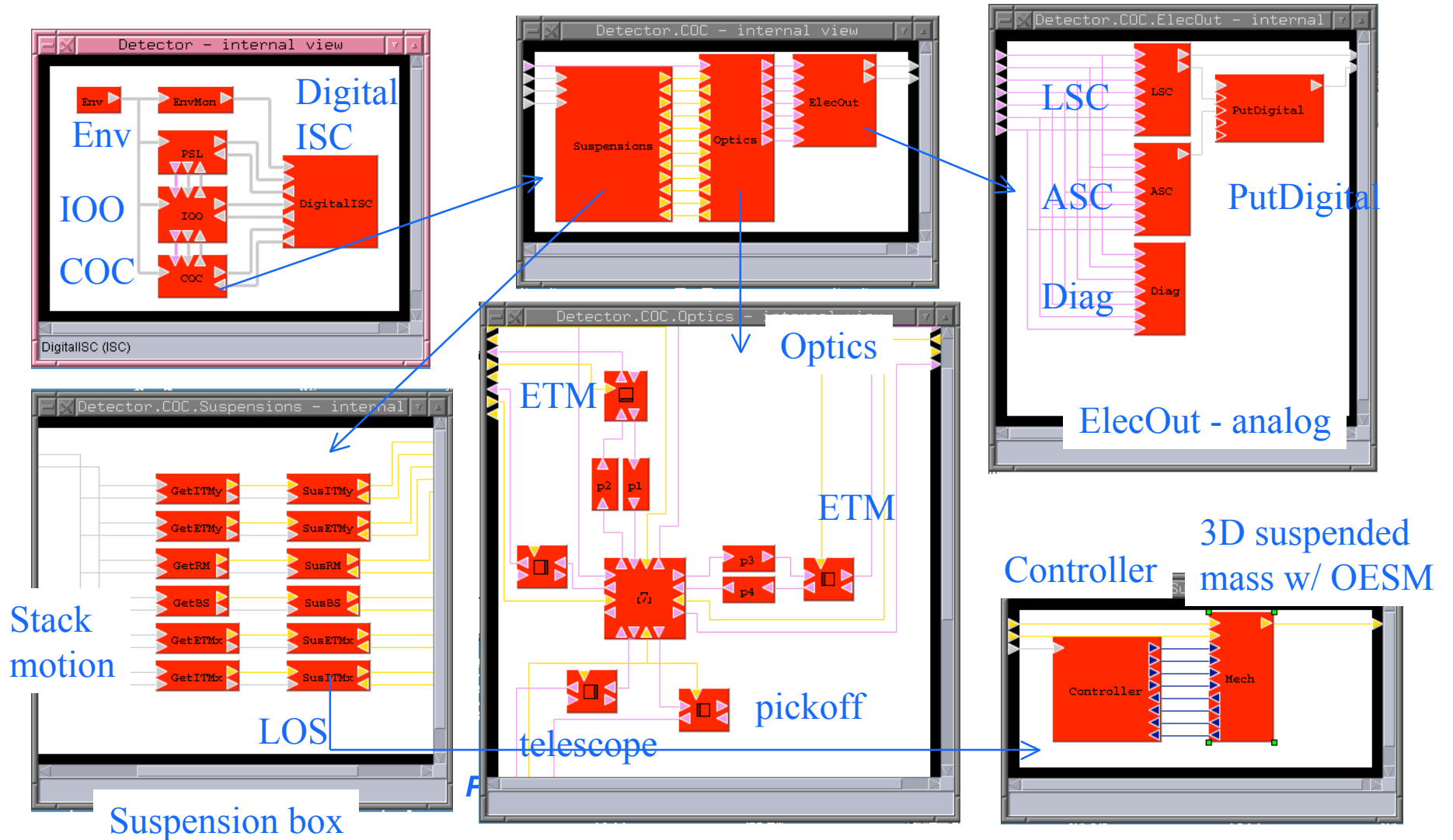
System structure





SimLIGO

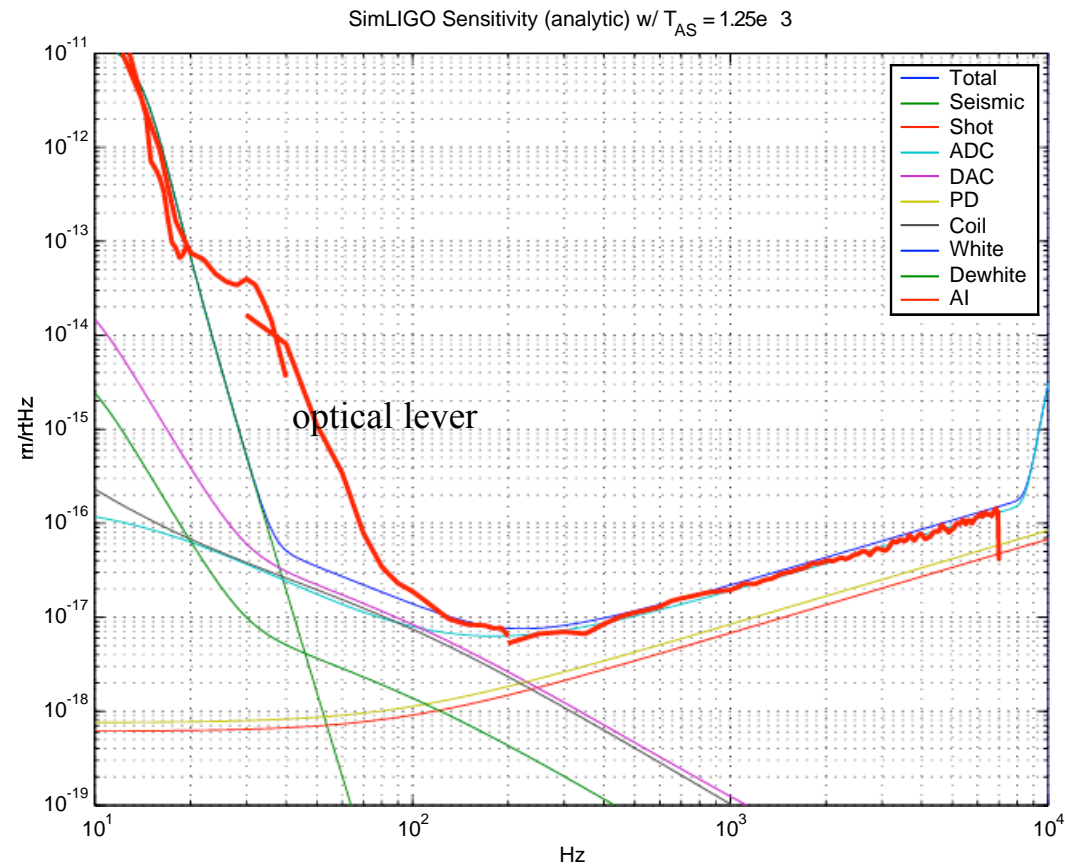
more realistic LIGO simulation





SimLIGO

Noise components

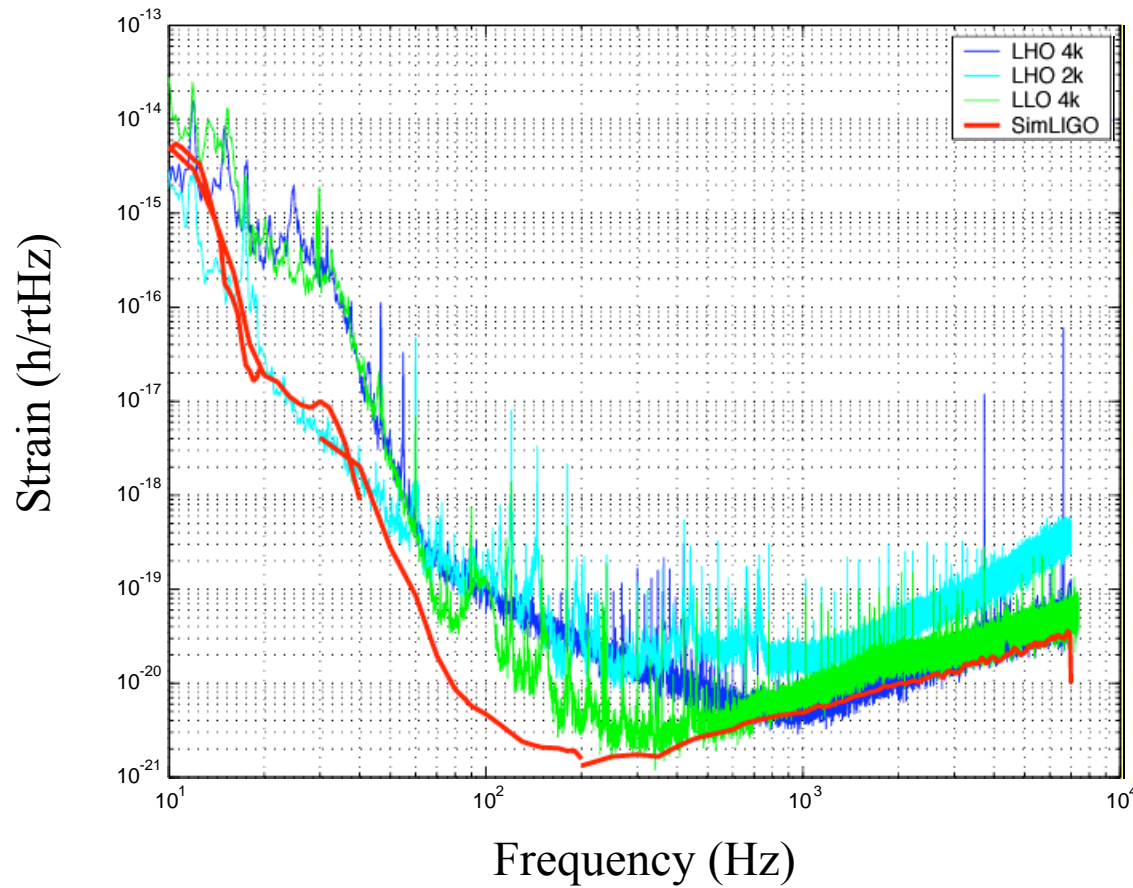




LIGO data vs SimLIGO

Triple Strain Spectra - Thu Aug 15 2002

rana-1029490757.pdf



SimLIGO simulates a IFO with all final design subsystems with current measured noises

data and simulation out of date



SimLIGO

sensitivity curve

- ◆ Calculated from a time series of data
 - » Major ingredients of the real LIGO included
 - » Interferometer, Mechanics, Sensor-actuator, Servo electronics
 - » Known noises
 - » Signal to sensitivity conversion
- ◆ Demonstration of the capability to simulate the major behavior of LIGO
 - » Reliable tool for fine tuning a complex device
 - » Almost any assumptions can be easily tested - at least qualitatively
 - » Trade study
 - » Subsystem design
 - » ...



LIGO simulation without programming

- ◆ Package distributed

- » SimLIGO box files
- » auxiliary files
 - macro files, run instructions, support apps
- » matlab files for easy analysis of e2e outputs
- » `modeler < run.in` to generate time series and psds
- » **5 lines in unix terminal to generate the sensitivity curve**

- ◆ Macro files - text file

- » lengths and mirror quantities
- » noise : on-off
- » control : on-off
- » shaking mirrors : length and angle - linear, periodic, random
- » configurations : FP, PRM, full LIGO



SimLIGO

what's TDB - we do

- ◆ Simulation code improvements
 - » Add physics
 - mirror phase map, radiation pressure, scattering noise, etc
 - » Improve existing physics simulation
 - better field-optics implementation, etc
 - » Code improvements
 - better data manipulation, speed, multi thread, etc
- ◆ SimLIGO
 - » Update common mode servo
 - » Better mechanical system model
 - » Lock acquisition support



SimLIGO

what's TDB - we need help

- ◆ LIGO 1 hardware/software data **NEEDED**
 - » Seismic data
 - only LHO data now
 - S.Yoshida (SLU) is helping us
 - » Noise data
 - updated noises of laser frequency, amplitude, electronic, etc
 - » Updated servo design
- ◆ **More USERS**
 - » why simulation is useful
 - » how simulation can be used



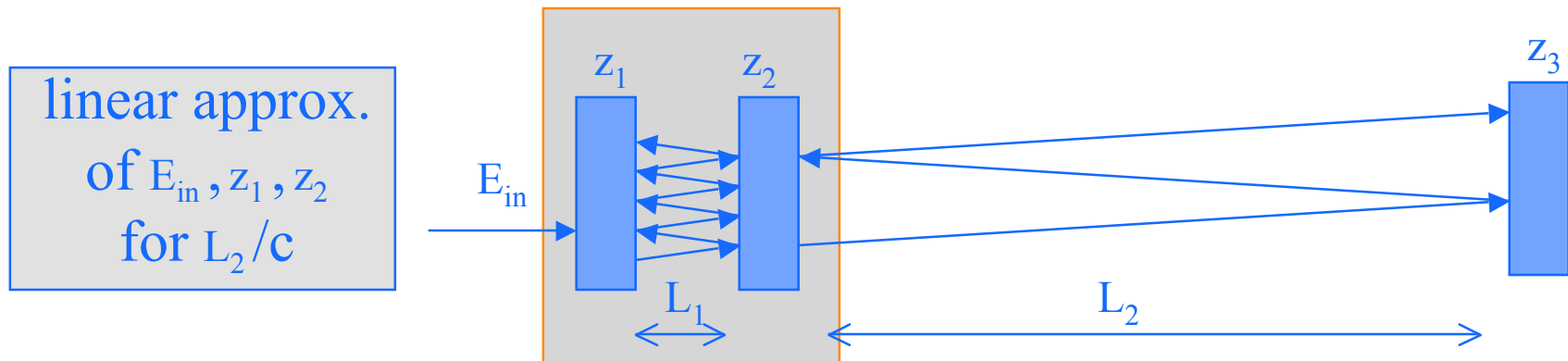
Future work Advanced LIGO

- ◆ Optics and Field
 - » Fast simulation of dual recycling configuration
 - » Thermal lensing effects
 - » Method handling complex profile field - more sophisticated modal model or FFT?
- ◆ Mechanics
 - » Simulation of quad pendulum
 - » Interfacing with stack models by other group
- ◆ Noises
 - » thermo elastic
 - » radiation pressure, ...
- ◆ Others
 - » “seismic noise whitening”, otherwise, 64 bit real is not enough
 - » speedup



Dual recycling cavity simulate FAST

- ◆ Can be simulated today, but slow...
- ◆ simulation time step = cavity length / speed of light
- ◆ Module based on an approximate calculation of fields in a short cavity runs 500 ($\sim L_2 / L_1$) faster than simulation using primitive mirrors.
- ◆ M.Rakmanov (UF) worked on a dual recycling cavity formulation and did its validation using matlab and e2e primitive optics. Not completed.





Mechanical Simulation Engine(MSE)

- ◆ Delivered by Dr.G.Cella of Univ.Pisa
 - » C++ mechanics class library
 - » Developed for LIGO based on his work at Virgo
- ◆ Fully three dimensional model
- ◆ Modular design with flexibility
- ◆ Time domain and frequency domain simulation
- ◆ Easy integration with the optics and control parts of the End to End model
- ◆ Interface to external models, like stack models by other group



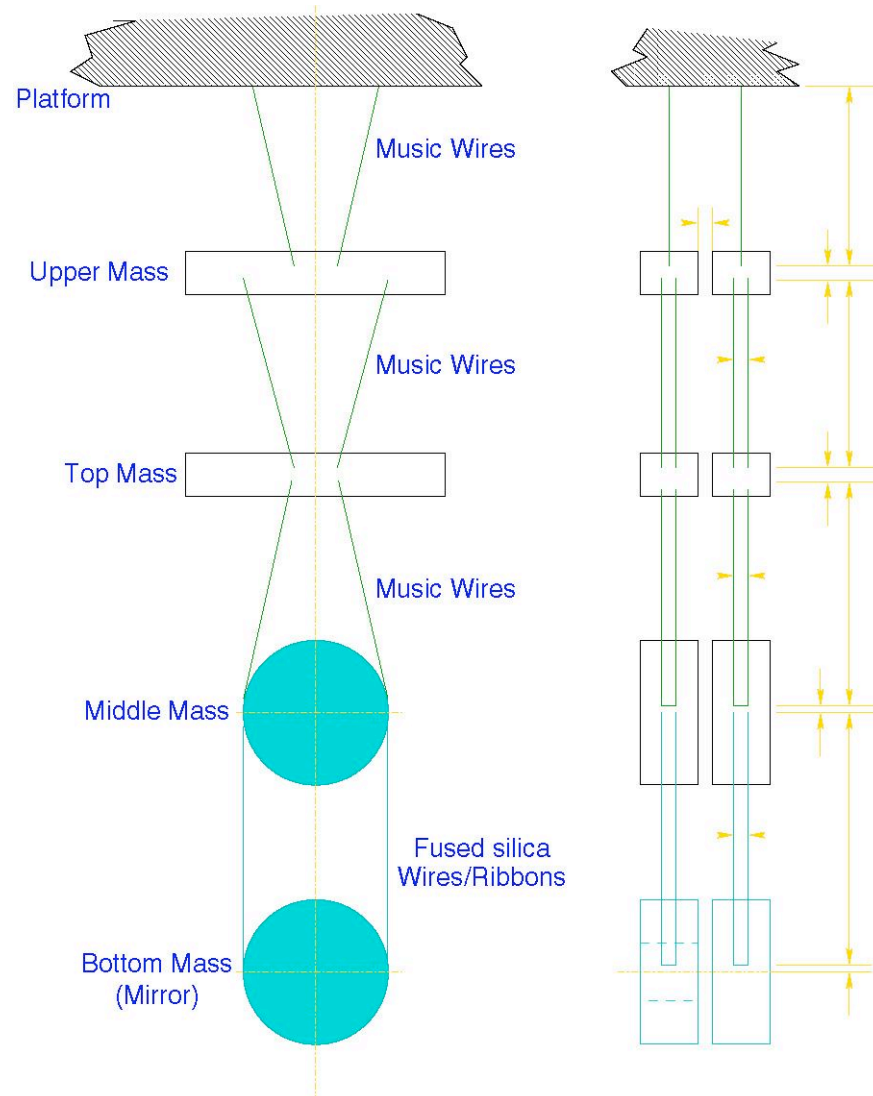
Quadruple Pendulum

- ◆ Virginio Sannibale based on MSE (1/3 of his time)
- ◆ The two chains of the quadruple pendulum suspension implemented.
- ◆ Main geometrical parameters of each element included.
- ◆ Complete three-dimensional simulation. All the geometrical possible couplings can be taken into account.
- ◆ Rigid body D.O.F. completely described.
- ◆ Internal mode implementation in progress (wire violin mode, blade, ...)
- ◆ Small oscillation or a linear regime.
- ◆ Viscous Damping for the longitudinal modes.
- ◆ Force actuators can be placed anywhere.
- ◆ Not completed



Adv. LIGO Mechanics

Quadruple Pendulum structure

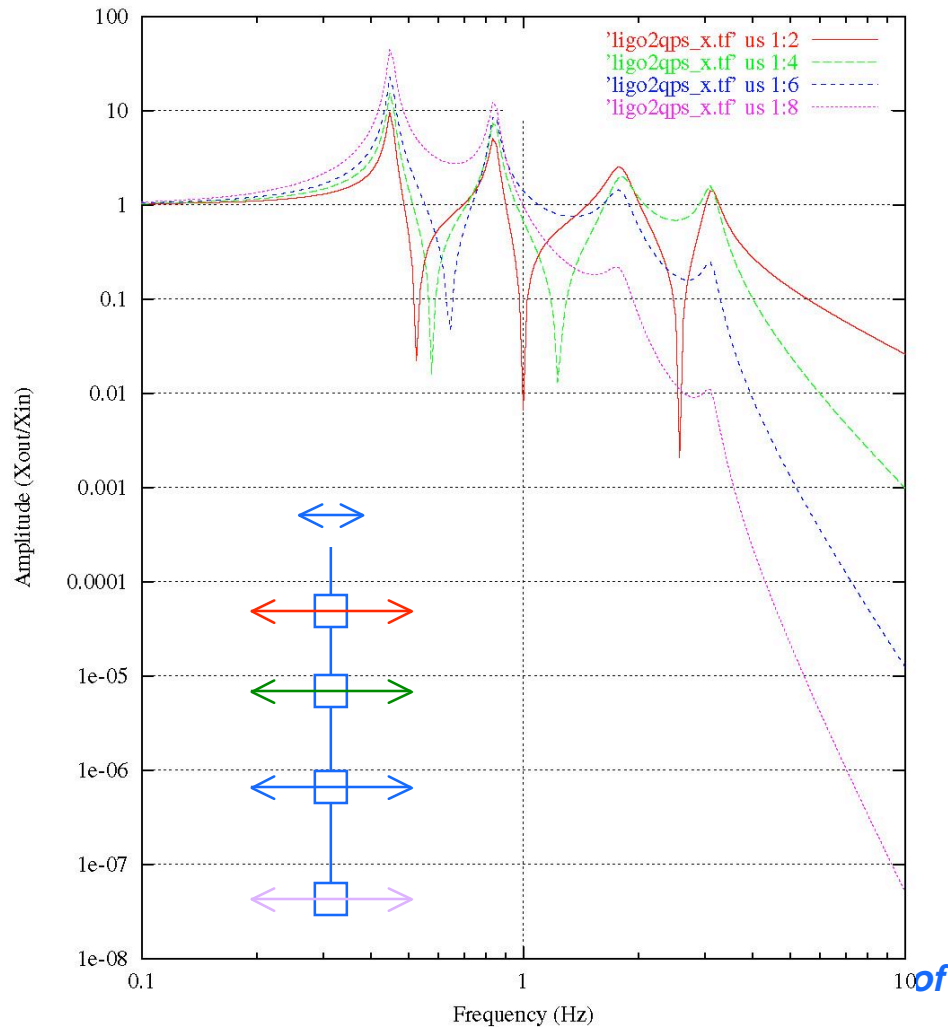




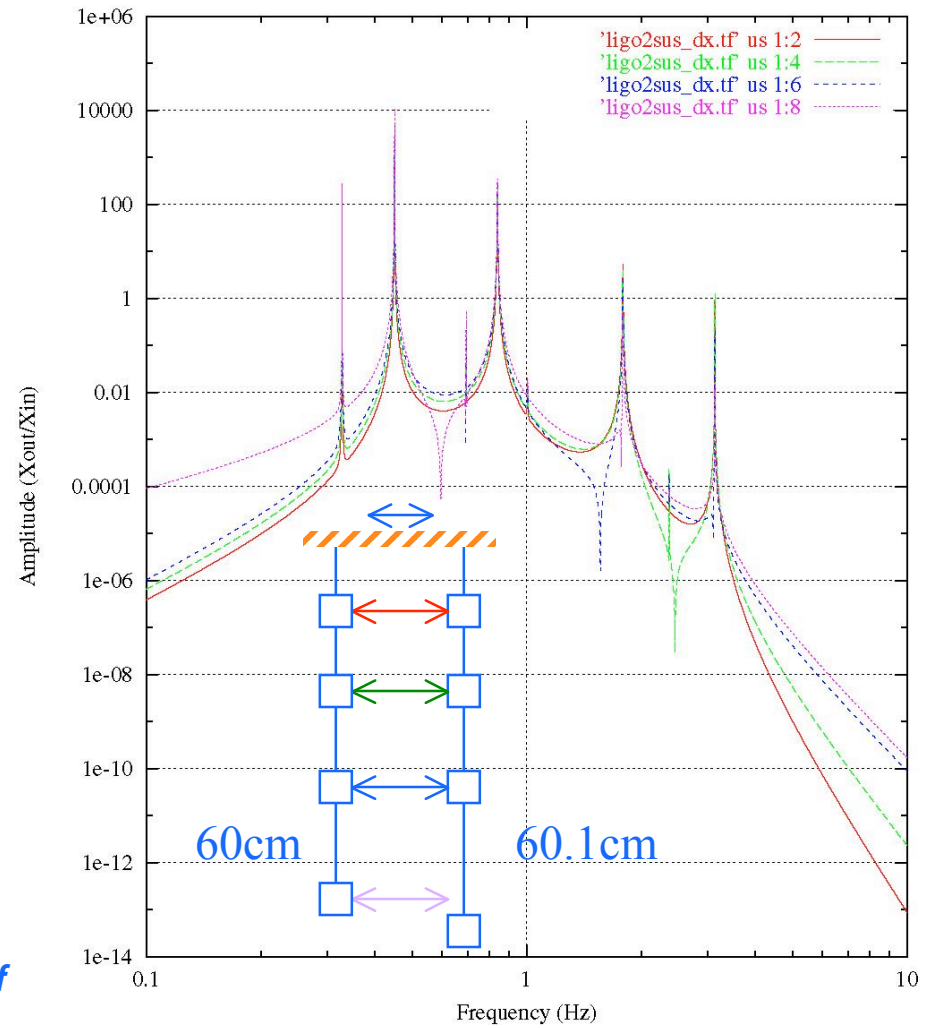
Adv. LIGO Mechanics

Transfer functions

LIGO-II Quadruple Pendulum Longitudinal Transmissibility: Amplitude



LIGO-II Suspension: Differential Longitudinal Transm., Amplitude





Information about End to End simulation package

- ◆ Platform supported
 - » JAVA 1.4, gcc 2.95.2
 - » Sun Solaris, Intel Linux, MacOSX (tbd)
- ◆ Homepage
 - » www.ligo.caltech.edu/~e2e/
- ◆ e2e tarbal downloadable from e2e homepage
 - » e2e-version.tar.gz, SimLIGO.tar.gz, Han2k.tar.gz
- ◆ Documentations
 - » all downloadable from e2e homepage
 - » Han2k users manual
 - » SimLIGO
 - 1) System structure, 2) How to guide, 3) Physics (to be completed)
- ◆ Maillist
 - » ligo-e2e-announce, physics, GUI, programming