



**An additional  
Low Frequency  
Gravitational Wave  
Interferometric Detector  
for Advanced LIGO?**

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Riccardo DeSalvo

California Institute of Technology

Pasadena April fool's 2003

LIGO-G030165-00-R

# Scientific motivations

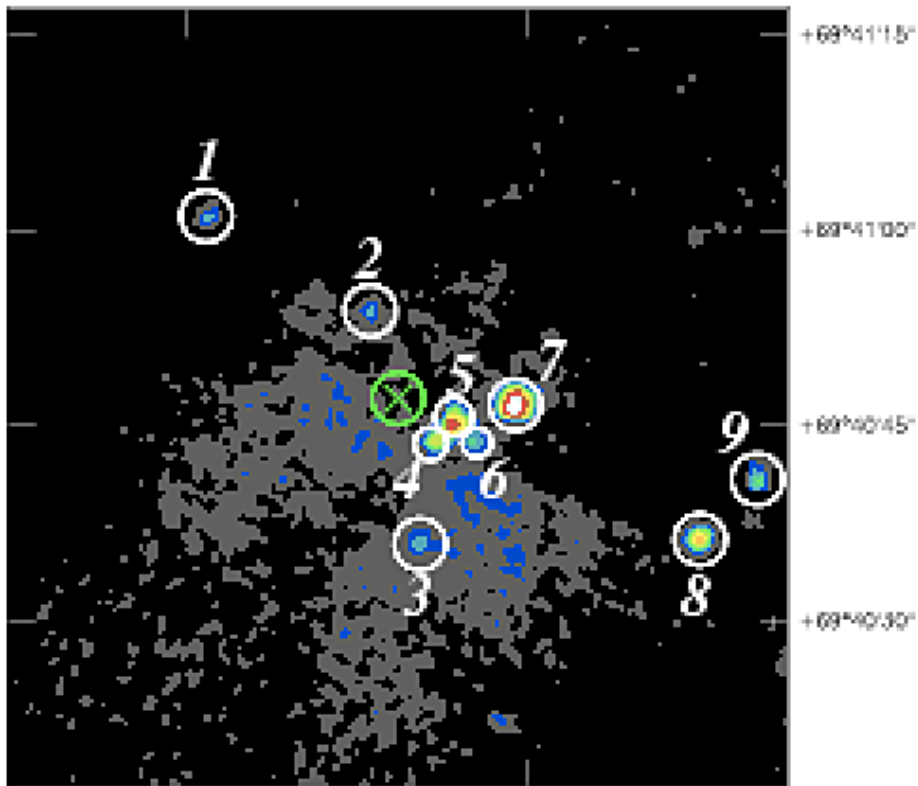
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- New observations performed after the design of Adv-LIGO indicate the presence of new possible LF GW sources
- Data summary from Cole's Miller based on X-ray and optical observations of galaxies and globular clusters including Chandra's observations of X-ray sources
- <http://www.astro.umd.edu/~miller/IMBH/>
- [http://online.kitp.ucsb.edu/online/bhole\\_c02/miller/oh/05.html](http://online.kitp.ucsb.edu/online/bhole_c02/miller/oh/05.html)

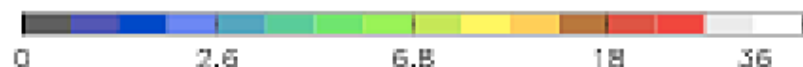
# LIGO Chandra's observations of M82

Matsumoto et al.

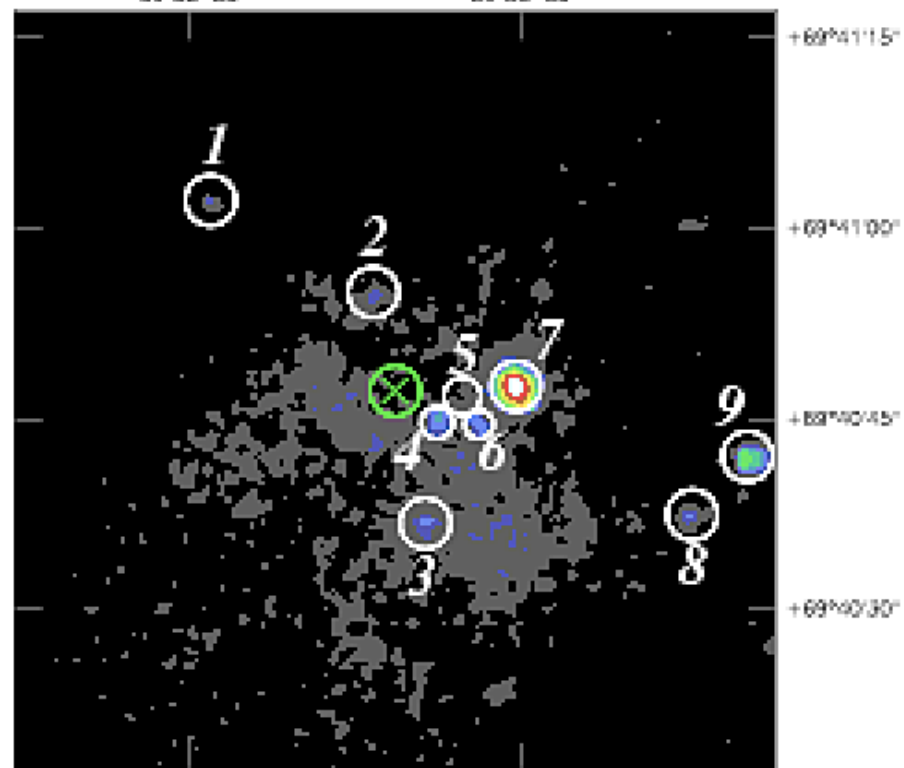
M82  
CHANDRA HRC HRC-I Exposure: 2788 s  
09°55'55" 09°55'50"



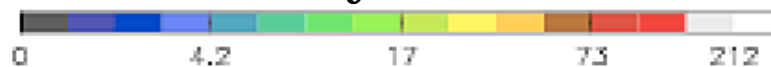
28 October 1999



M82  
CHANDRA HRC HRC-I Exposure: 17684 s  
09°55'55" 09°55'50"



20 January 2000



# Chandra's observations

## Matsumoto et al.

- Observed x-ray sources in globular clusters
- Eddington mass of sources  $30 \sim 10^3$  s.m.
- Emission implies a companion
- So many companions imply high density in the cluster (optically observed)
- High density implies frictional braking
  - Kinetic energy tends to be equalized in encounters, fat guys get slowed
- Many clusters have the same pattern

# What do I gather from globular cluster observations

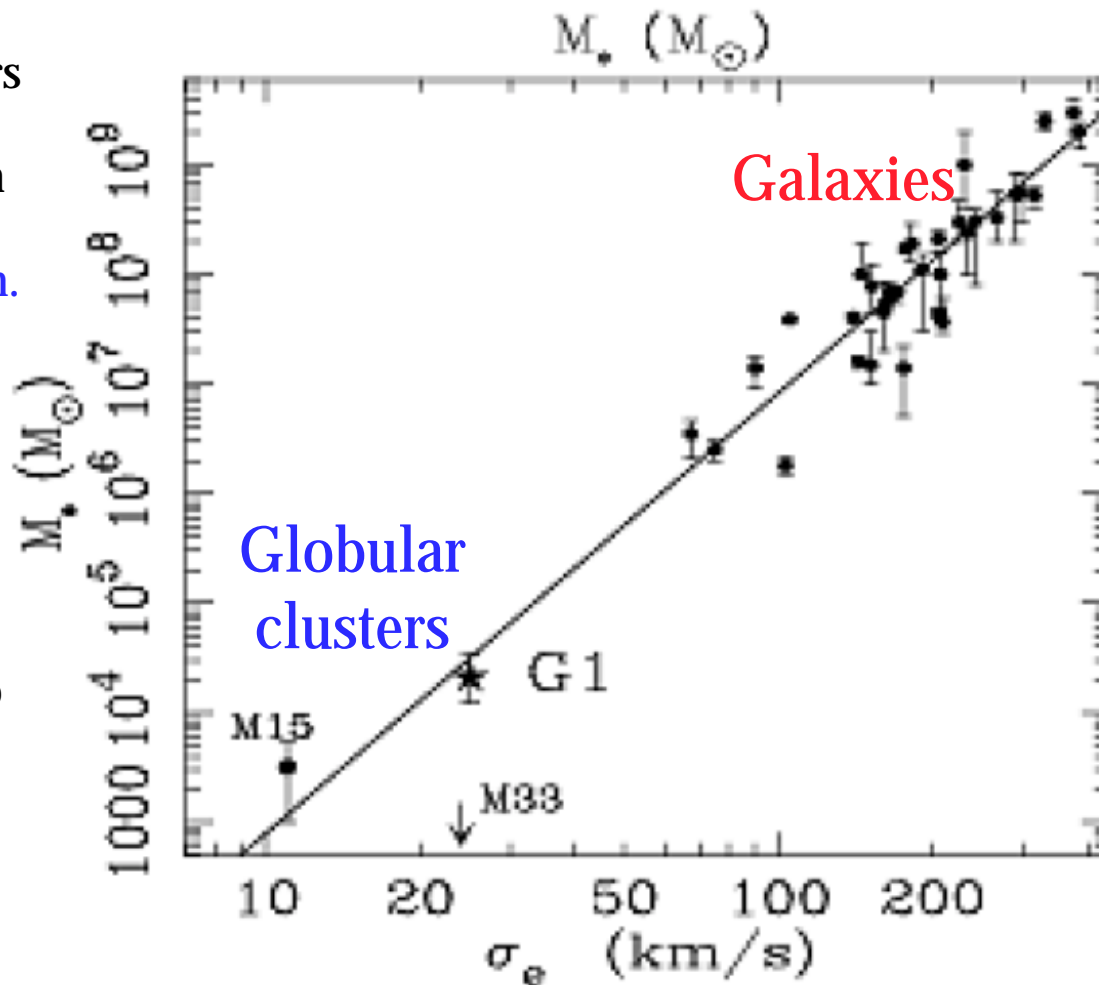
- Stars above 50 s.m. directly evolve in BH (collapsars)
- Stars below 20-30 s.m. (above 8) rapidly ( $\sim 10-15\text{My}$ ) go supernova and leave behind 1.4 s.m. NS
  - (In between (30-50 s.m.) smaller BH are generated)
- Stars >50 s.m. slow down by dynamical friction ( $\tau=10\sim 50\text{My}$ ) and sink to the center of the cluster where they may be induced to merge
  - In encounters kinetic energy gets equalised, heavy masses get slowed
  - Density of  $\sim$  million stars per cubic parsec observed
  - Mass segregation occurs
- Smaller stars ( $<8$  s.m., including NSs) collect the kinetic energy, get accelerated and may be dispersed out of the cluster

# What do I gather from globular cluster and galaxy observations

1. The only electromagnetically visible BH are those accreting from companion star.
  - The accretion stage is short ( $\sim 10\text{My}$ )
  - Why so many are visible?
  - Frequent Encounters of binaries with singles tend to tie and tighten up the bigger guy and fling out the smaller of the three
2. X-ray sources compatible with several 30 to 1000 s.m. BH per galaxy are observed by Chandra and XMM, many more may lurk
3. Velocity dispersion in globular cluster centers imply presence of IMBH or BH clusters

# LIGO Optical observations: inspirals may be ongoing at a catalyzed pace

- In some Globular clusters the speed distribution of stars is compatible with central concentrated and invisible mass  $\sim 10^3$  s.m.
- Either a single, a binary or a cluster of BH must be at the center
- (Note: Statistics increased with respect to this figure)





# LIGO Optical observations: inspirals may be ongoing at a catalyzed pace

- In some Globular clusters the speed distribution of stars is compatible with central concentrated and invisible mass  $\sim 10^3$  s.m.

Either a single, binary or cluster of BH must be at the center

- (as well as the other BH observed farther away from the center)

- Swirl is observed in the core stars around that hidden mass
- But frictional braking would rapidly eliminate the observed swirl!
- Core stars around central BH cluster can be swirled up while hardening the massive binaries at the center (controversial but growing evidence)
- A BH cluster must be present and being hardened
- And will coalesce at rapid rate!  $\ll 10\text{My}$  !!!!
- Is this a Smoking gun?



# What is relevant for GW observations

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- Useful chirp for heavier masses ends at 30 to 100 Hz
  - Available signals start above 20+20 s.m.
    - Close to ISCO the orbits are relativistic and difficult to make templates (still lower effective frequency range for detection)
  - L.F. sensitivity necessary to trigger with optimal filters
- ~10 of BH-BH inspiral events per year are expected
- GW Signals from massive BH will carry farther than NS
  - We will map galaxy clusters farther away than NS-NS inspirals

# Consequences

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- Do we have evidence that low frequency sensitivity is of astrophysical interest?
- Of course yes!
- Is the present Advanced LIGO best suited to cover the new possible sources indicated by Chandra and other optical observations?
- Not without some significant changes
  - 10% power / different finesse
  - Fused Silica instead of Sapphire mirrors (bulk TN)
  - Supersized, double weight mirrors (coating TN)
  - Double length suspensions (susp. TN)

# Consequences

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- Note:
- Adv-LIGO is designed to be broadband and to cover a different class of sources and goes as low in frequency as practical as possible while focusing on the higher frequency end
- by specializing interferometer design is it possible to do better at either HF or LF than a single instrument in a single configuration can.
- It is practically impossible to optimally cover both ends with a single design
- Separate design lead to better optimizations.

# Consequences

---

- Do we need a low frequency companion for Advanced LIGO to cover the new possible sources indicated by Chandra and other optical observations?
- Of course yes!
  - Note:
  - Adv-LIGO is designed to cover a different class of sources and goes as low in frequency as practical as possible while focusing on the higher frequency end
  - It is practically impossible to cover both ends with a single design
  - Separate design lead to better optimizations.

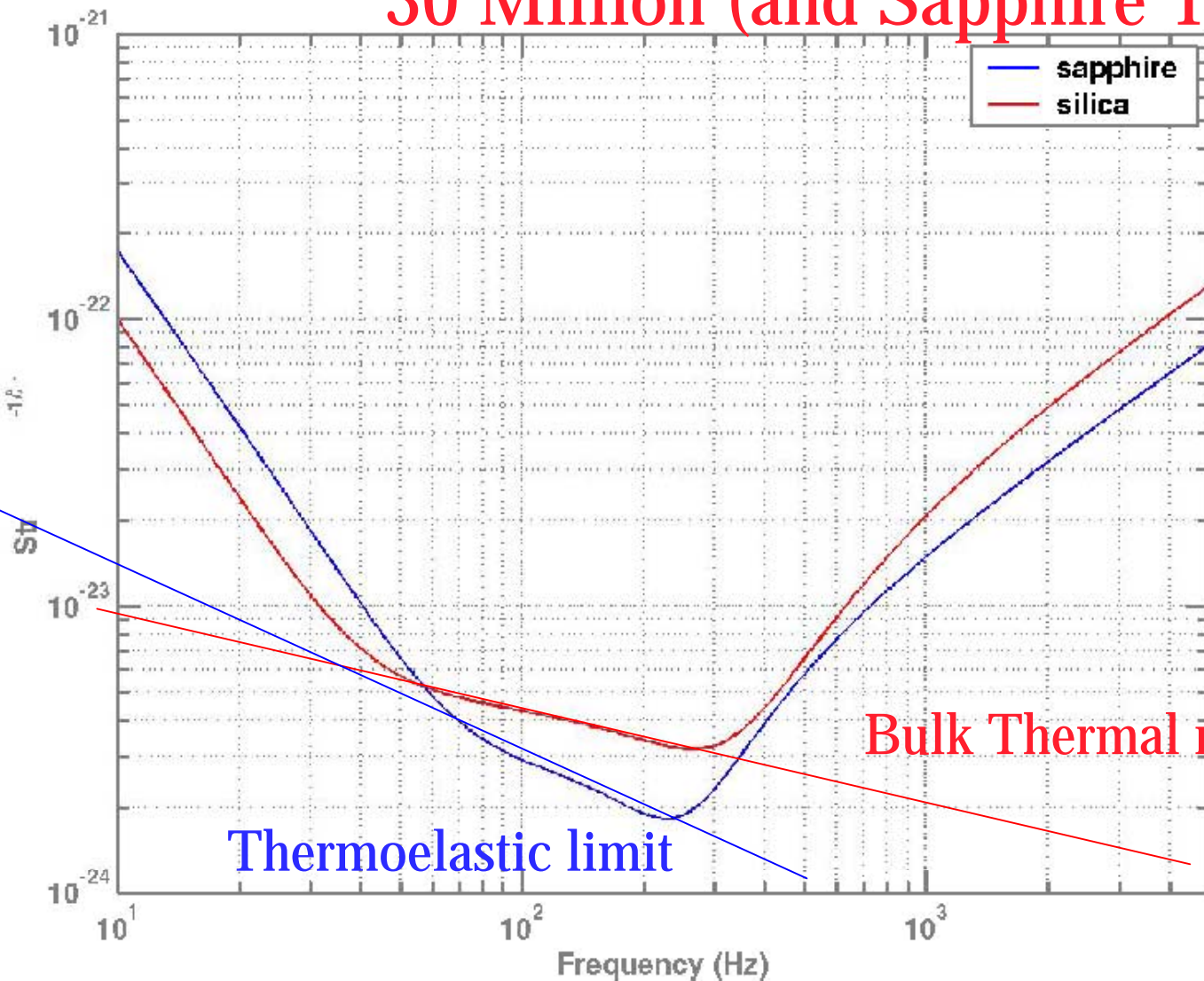
# Question

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- Can we technically build and operate an interferometer at Lower Frequency than Adv-LIGO?



This curve was drawn when Fused silica was believed to have a Q-factor of 30 Million (and Sapphire T-E limited)



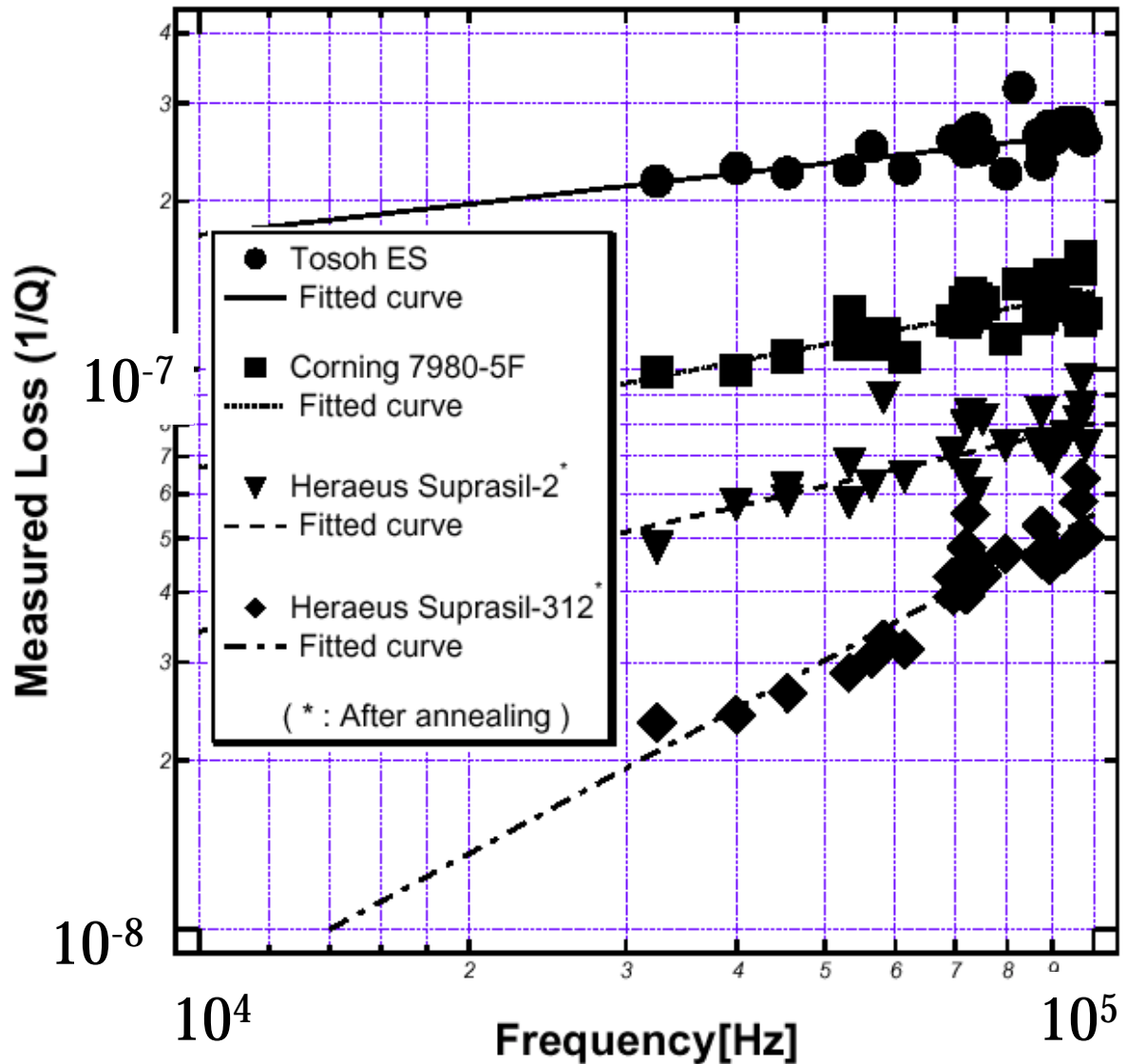
# The new TN situation

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- Now the bulk F.S. TN floor is crumbling.
- Two measurements:
- Kenji's Q- factor measurements
- Fused Silica have been observed to be capable of Q factors at and above 200 Million (Gregg Harry, Steve Penn)
  - Note: Sapphire show equally high Q factors but, unfortunately, the fact is irrelevant because of the thermo-elastic effect

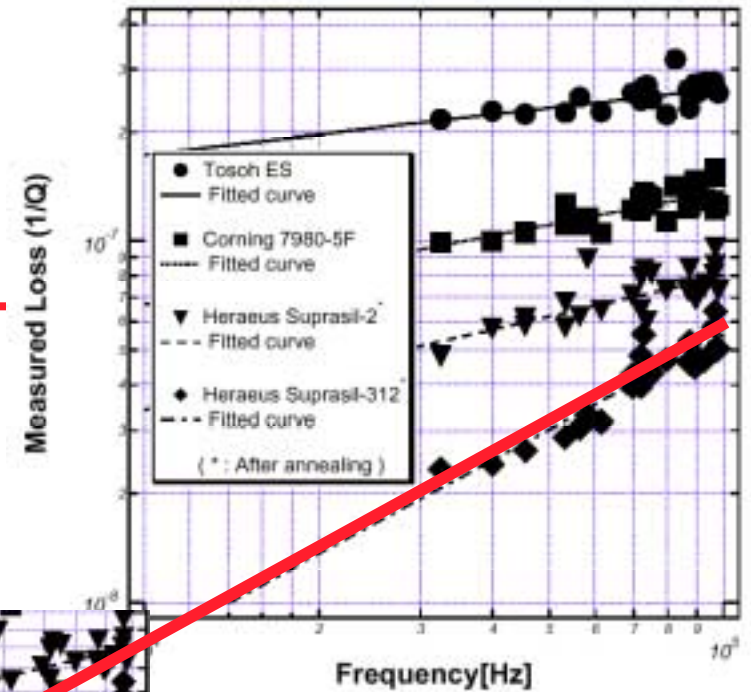
The Q-factor improves at lower frequency

How much better does it get at 100 Hz?



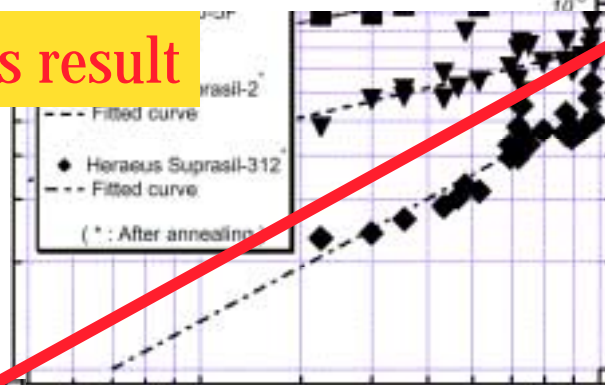


Let me cheat for a moment



$10^3$  Hz

Steve and Gregg's result

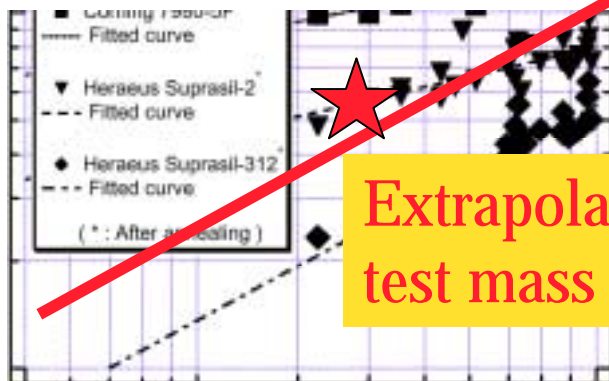


Surface and Coating losses?

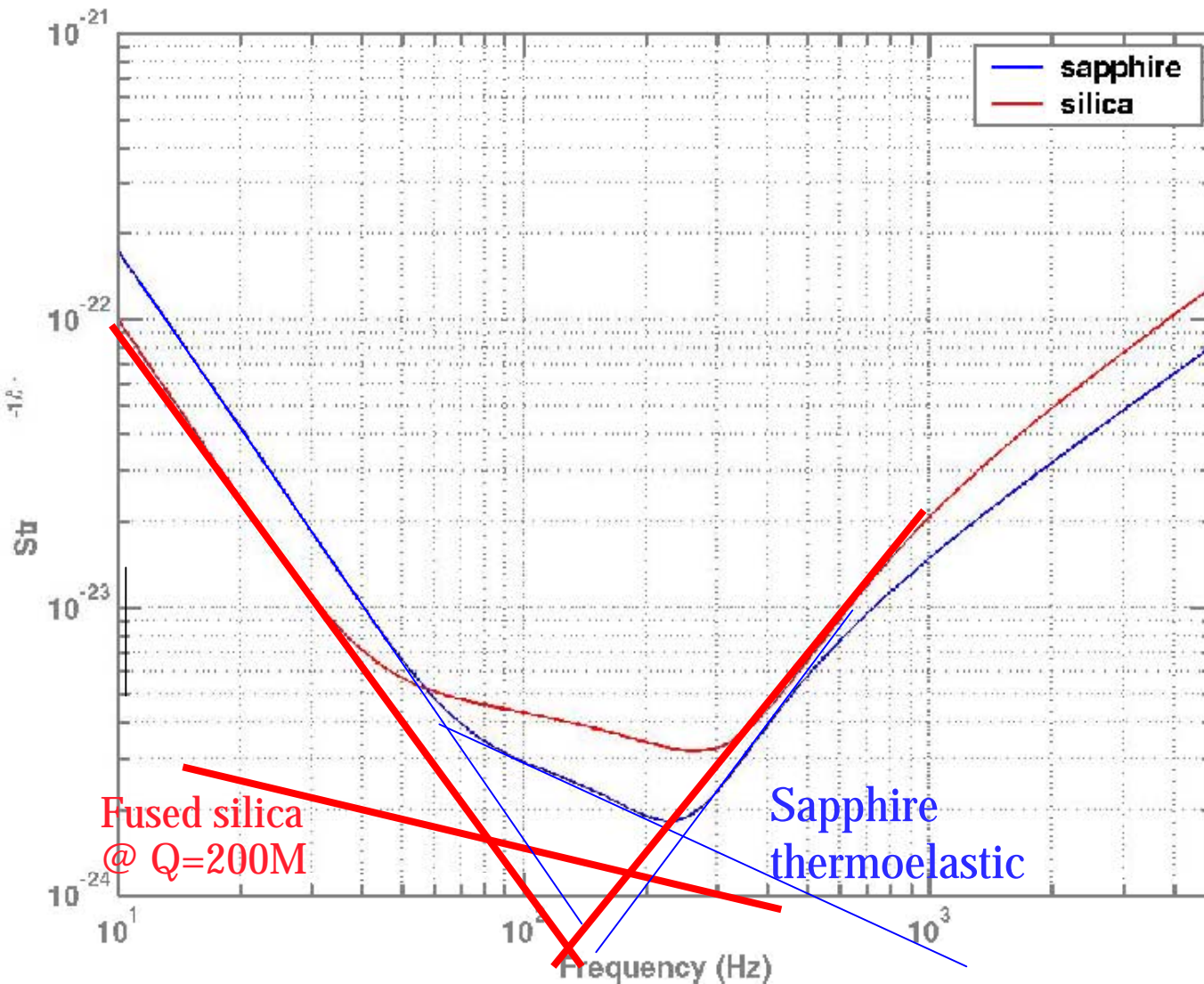
$10^{-9}$   
 $10^4$  Hz

Extrapolated to test mass shape

Where are the substrate losses at  $f \sim 100$  Hz?



# What can we expect?.



Coating TN  
Disregarded!

This opens the road  
To LF

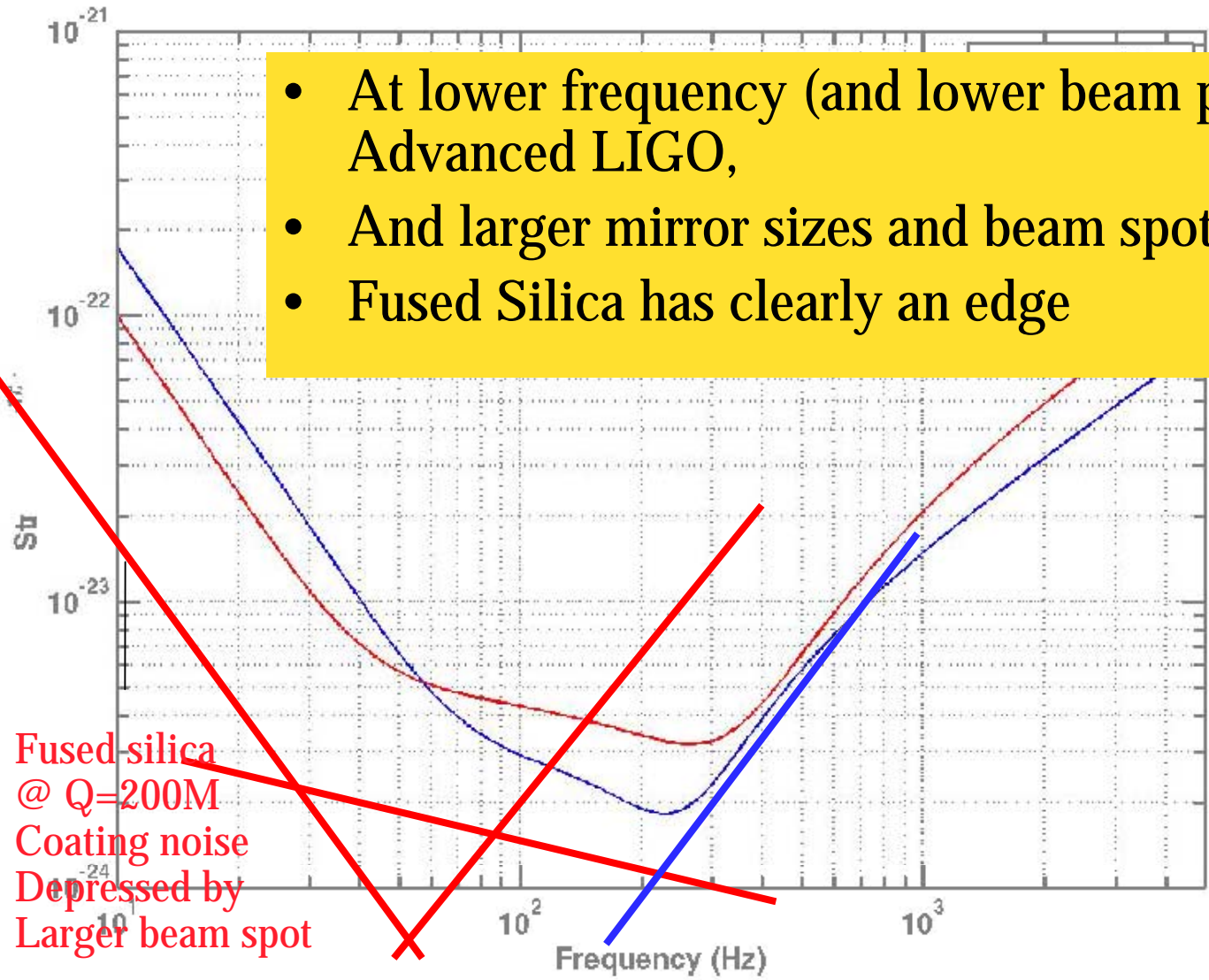
Note: At high Frequency  
Sapphire is preferable  
because of power  
dissipation limitations  
for Fused Silica<sub>18</sub>

# Implications at L.F.

- Fused silica allows for much lower thermal noise floor at L. F. if coating problem is solved
- The lower beam power can be tolerated.
  - No need for the higher thermal conductivity of Sapphire.
- Fused silica marginal for Adv-LIGO mirror size and power level
- At frequencies lower than Adv. LIGO (and larger beam sizes) the beam power problem rapidly disappears  $\sim 1/f^2$
- The limit will be given by coating thermal noise.
- Advanced coatings and Large spot sizes are the solution to offset this limit
  - Coating thermal noise  $\sim (\text{spot diameter})^{-1}$

# Resuming

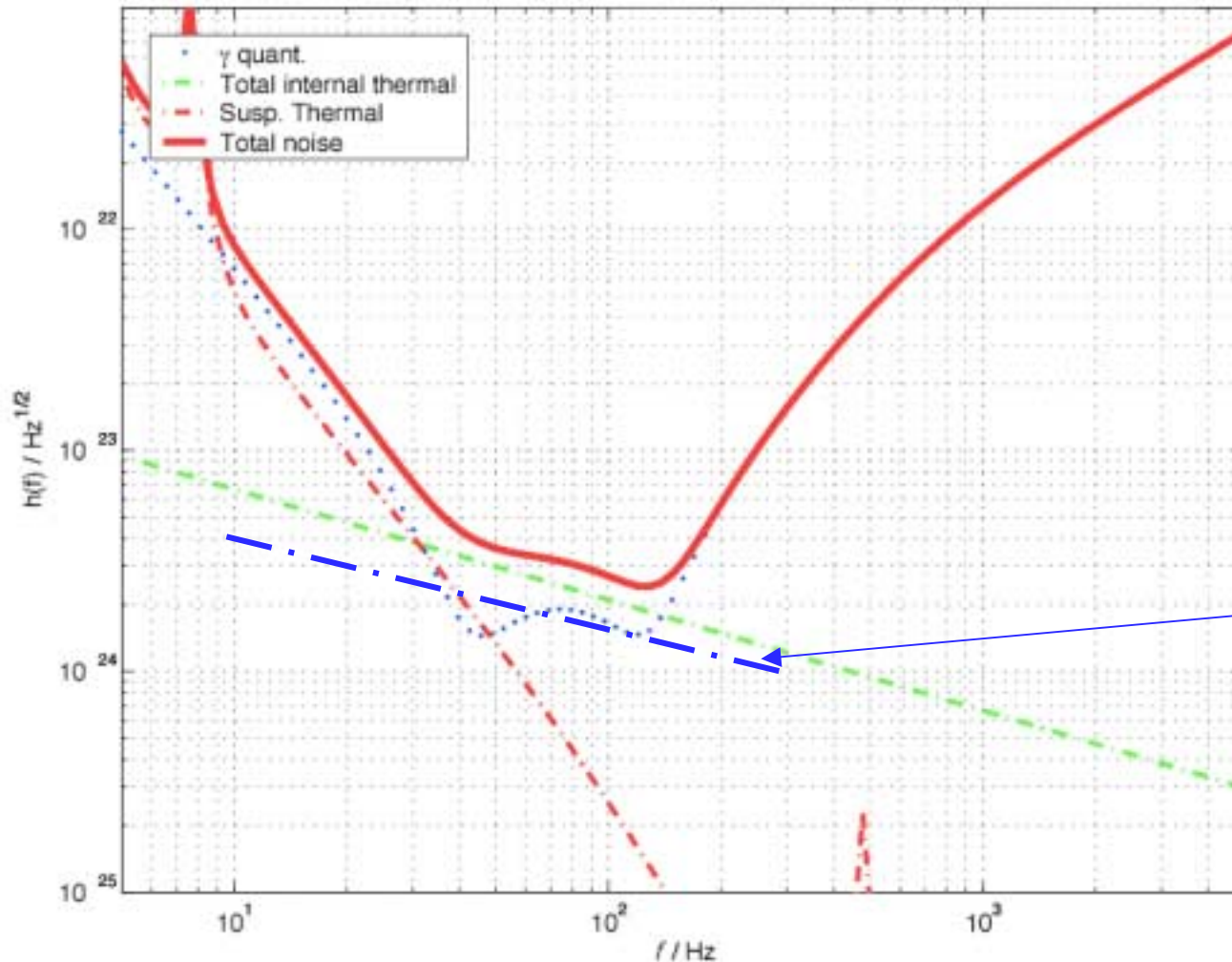
- At lower frequency (and lower beam power) than Advanced LIGO,
- And larger mirror sizes and beam spots
- Fused Silica has clearly an edge



Fused silica  
 @ Q=200M  
 Coating noise  
 Depressed by  
 Larger beam spot

1/2 Freq. => 1/4 power  
 2x Spot => 1/4 p. dens.

# Bench and Kenji's estimations



- 12 cm beam spot,
- $1 \cdot 10^{-4}$  coating phi,
- 500 million silica Q,
- 5 Hz seismic wall

Coating TN limited

- In dashed: Kenji estimation for same parameters

# Cosmic reach LF-LIGO

Spot cm	coating $\phi$	silica Q Millions	BNS range Mpc
6	$5 \cdot 10^{-5}$	100	166
6	$1 \cdot 10^{-5}$	200	230
12	$1 \cdot 10^{-4}$	500	234
12	$5 \cdot 10^{-5}$	200	258

# Cosmic reach

NS inspiral 100 Mpc

Adv.LIGO optimized for ns insp.	S/N 6
LF-LIGO Opt.for 30+30sm insp.	S/N 9

t.b.c.

30+30sm inspiral,  
max reach at S/N 10

Adv.LIGO	770 Mpc
LF-LIGO	1150 Mpc

t.b.c.

Bench/G. Harry  
Adv-LIGO standard  
Config.  
Fused silica Q 200M

Parameter	LF LIGO	ADV LIGO
Seismic wall	6 Hz	10 Hz
Mass radius	215 mm	155 mm
Beam radius	12 cm	6 cm
Suspension l.	1.5 m	0.5 m

# Signal to noise at 200 MPc

Inspiral mass	Adv LIGO S/N	LF LIGO S/N
1.4+1.4	4	4.4
30+30	51.5	57.1
50+50	78.9	87.4

Q silica 50M (conservative)  
Coating Phi  $2 \times 10^{-5}$

A-LIGO seis. Wall @ 10 Hz  
Standard configuration

LF-L susp. Noise limited

Bench/Gregg Harry

- Assuming templates exist throughout the freq. range
  - At higher frequencies templates may not be available for the final merge and inspiral phase



# Signal to noise at 200 MPc

Inspiral mass	Adv LIGO S/N	LF LIGO S/N
1.4+1.4	4	4.4
30+30	51.5	57.1
50+50	78.9	87.4

**But much larger S/N are possible if the signal of both interferometers is combined!!**

- 
- Kip is running his own independent evaluation of merit for a LF LIGO companion.
  - To be cross checked

# Implications

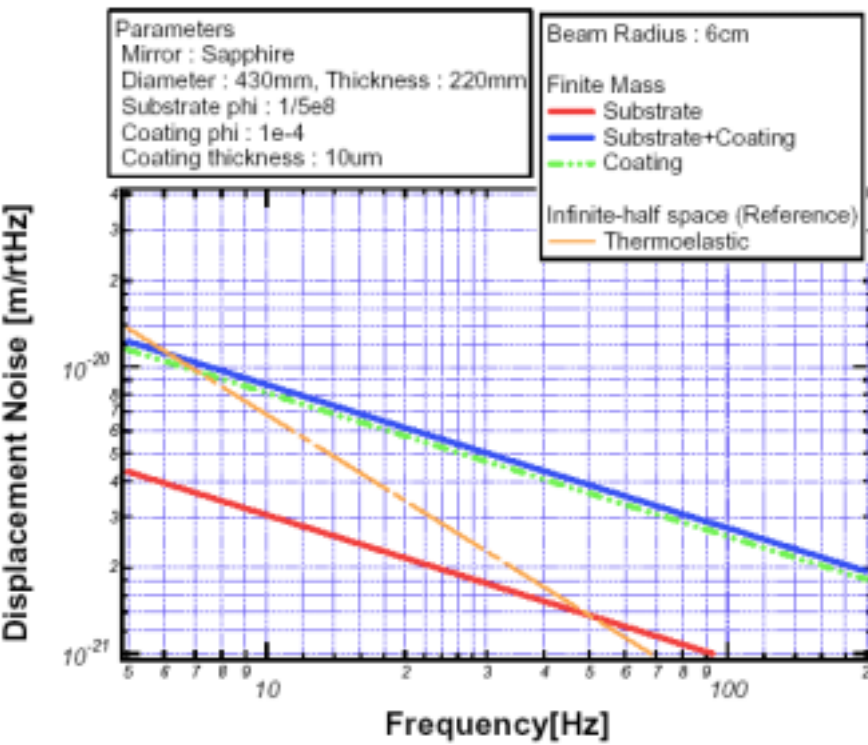
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- A Virgo-like interferometer to cover the low frequency region at LIGO would be mostly welcome
- Advantages
  - lower frequency region is better covered
  - Splitting up the frequency range between two different interferometers eases lots of design constraints and allows better performance from each
  - Advanced LIGOs are free to be narrow banded
  - For heavy massers, Adv.LIGO would be “triggered” by the LF optimal filter detection and can start disentangling final inspiral and merge signals

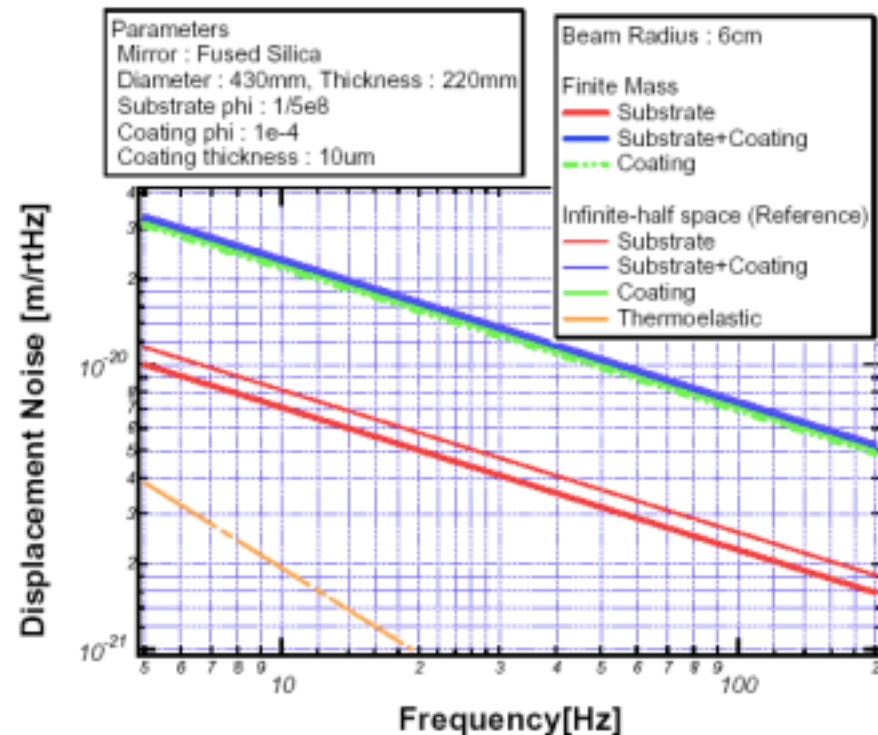
# LIGO Is Fused Silica better than Sapphire at low frequency?

- If we consider same geometrical size mirrors
- Sapphire is unbeatable!

Data from Kenji



030

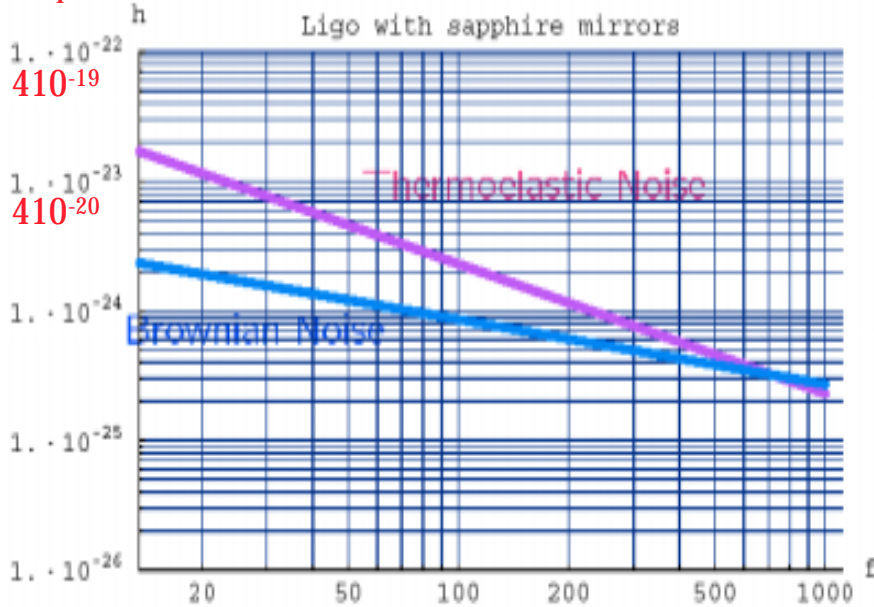


# LIGO Is Fused Silica better than Sapphire at low frequency?

- However, as soon as we consider reasonable sizes of sapphire (advanced-LIGO sizes)

Fused Silica immediately becomes competitive at LF Thermo-elastic noise of adv. LIGO mirrors Gauss spot (Erika)

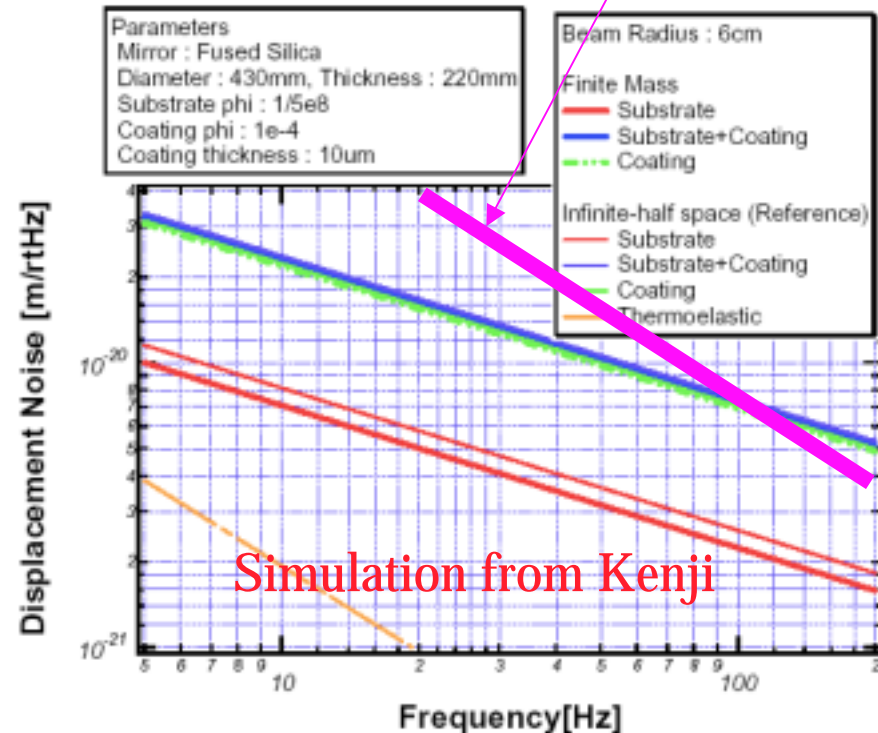
Displacement noise



Adv, LIGO simulation from Erika  
6 cm spot

$$Q_{\text{sapphire}} = 2 \times 10^8$$

030'

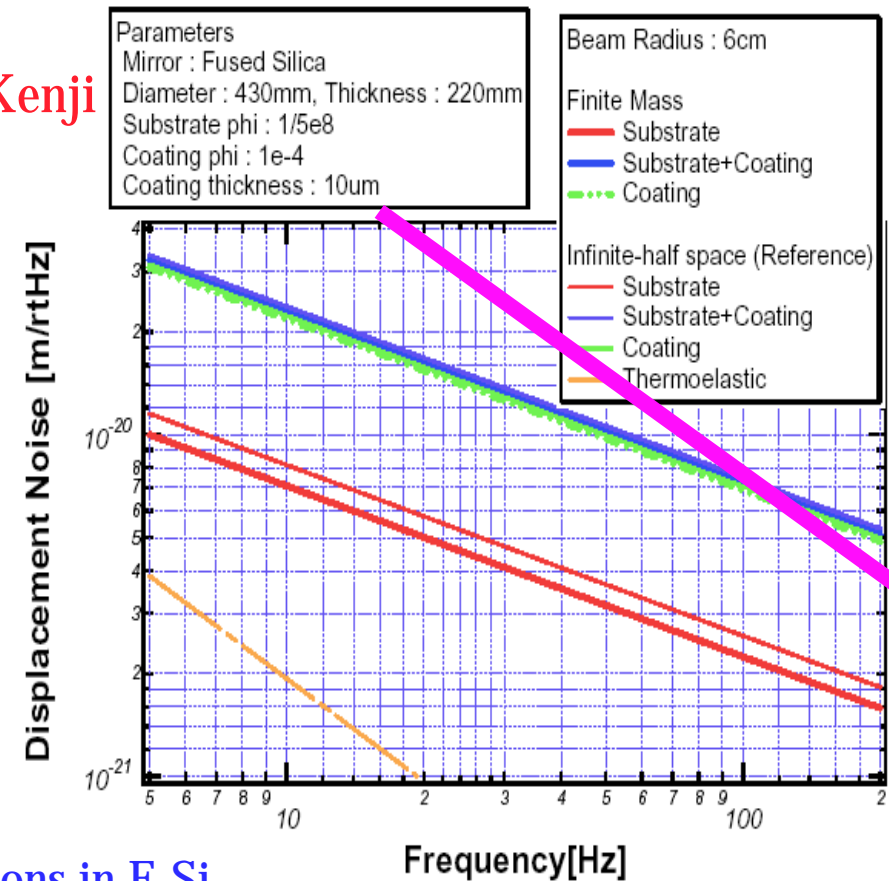
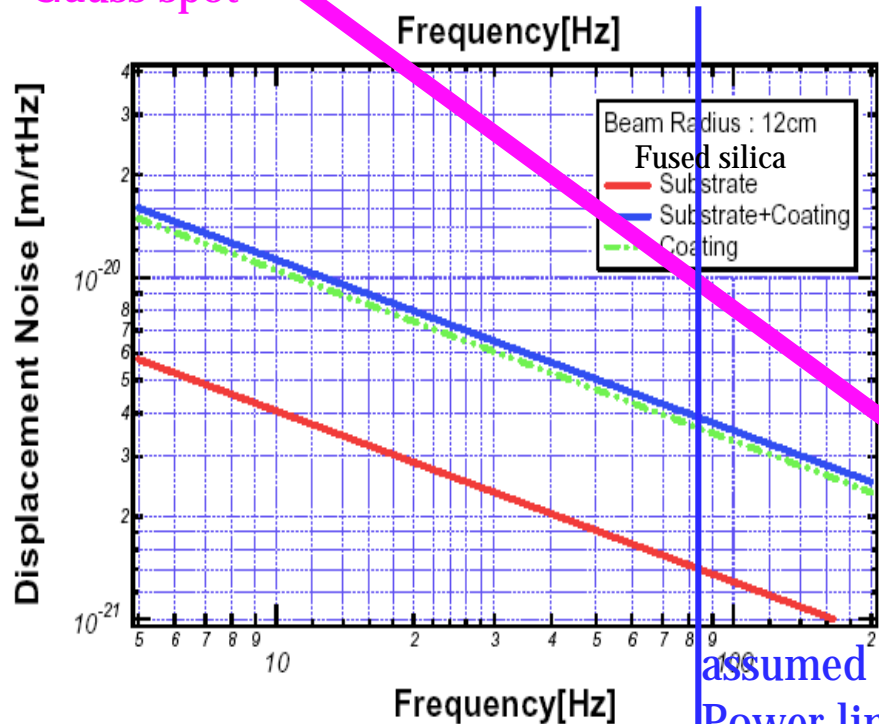


# LIGO Is Fused Silica better than Sapphire at low frequency?

- Even better with **larger spot sizes** allowable by larger fused silica mirrors and softer suspensions

Thermo-elastic noise of  
adv. LIGO mirrors  
Gauss spot

Simulation from Kenji



assumed 30 Hz  
Power limitations in F-Si

# How to mitigate the coating noise problem

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- Can use bigger masses and larger beam spots to counter both coating thermal noise and power limitations (and depress radiation pressure fluctuations)
- Bonus: larger bottom of the canyon
- Tighter alignment requirements are possible with lower frequency suspensions and hierarchical controls (Virgo scheme).
- Note, possible advances in coating loss angle not included

# How to mitigate the coating noise problem 2

*Ligo Seminar  
February 2003*

*Erika D'Ambrosio  
Ligo Laboratories, Caltech*

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## Scaling law for $w$

Standard Thermal Noise:  $S_{coupled}(f) \sim w^{-1}$

Thermodynamical Fluctuations:

$$S_{coupled}(f) \sim w^{-3} \iff \langle \delta x^2 \rangle = \alpha^2 \delta T^2 \left[ \frac{K_{th}}{C_p \tau} \right]$$

Coating Mechanical Loss:  $S_{coupled}(f) \sim w^{-2}$

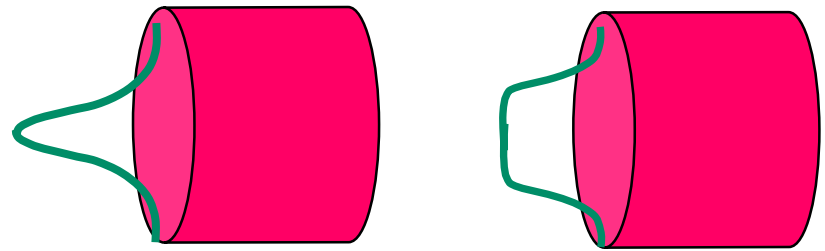


# How to mitigate the coating noise problem 3

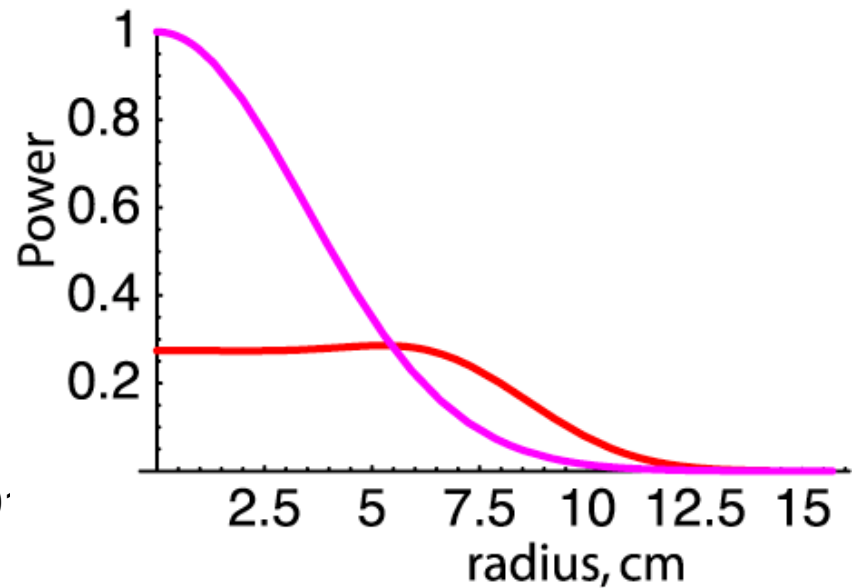
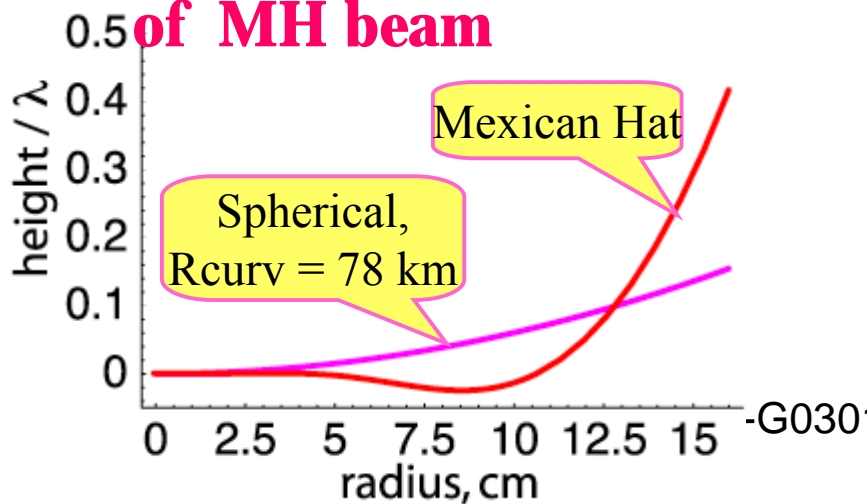
Mexican hats proposed by Kip Thorne et al. are a solution

<http://www.ligo.caltech.edu/docs/G/G030137-00/>

- A Flat-topped beam averages over bumps much more effectively than a Gaussian beam.



- MH mirror shape: matches phase fronts of MH beam**

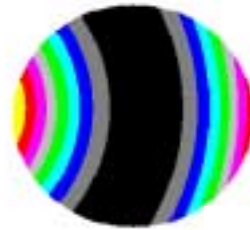
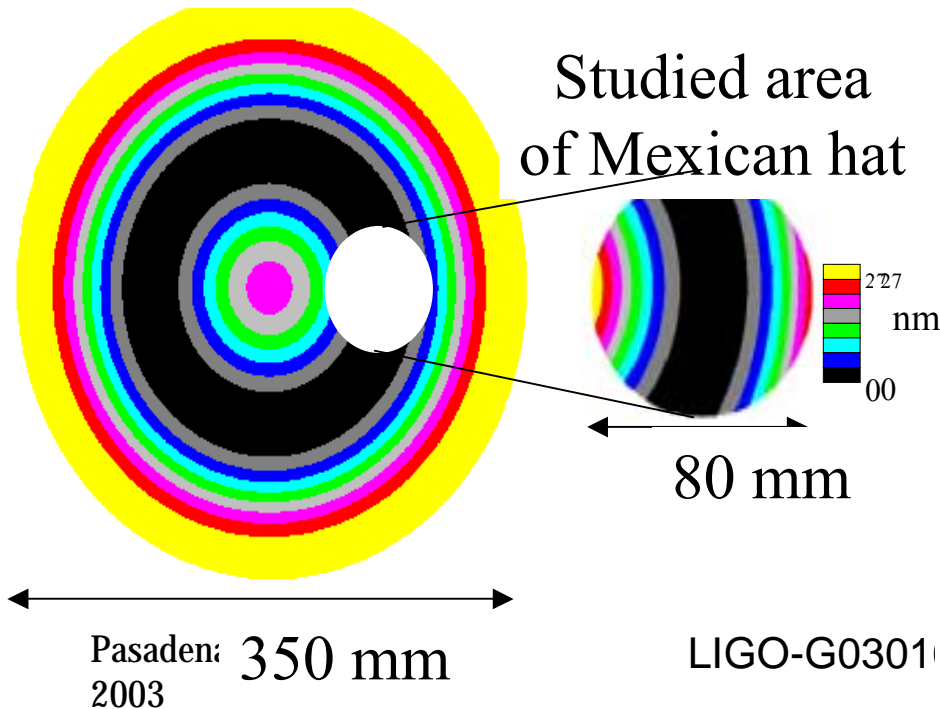


## How to mitigate the coating noise problem 4

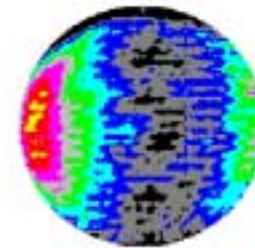
And J.M. Mackowsky shows that they are relatively easy to make

<http://www.ligo.caltech.edu/docs/G/G030115-00/>

Top view of a Mexican hat

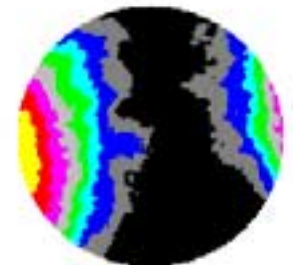
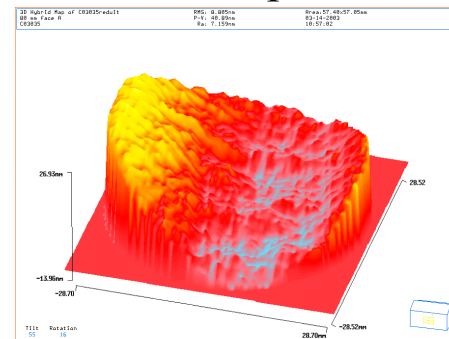


Theoretical mexican hat



Simulation of the corrective coating

Experimental mexican hat



## How much larger?

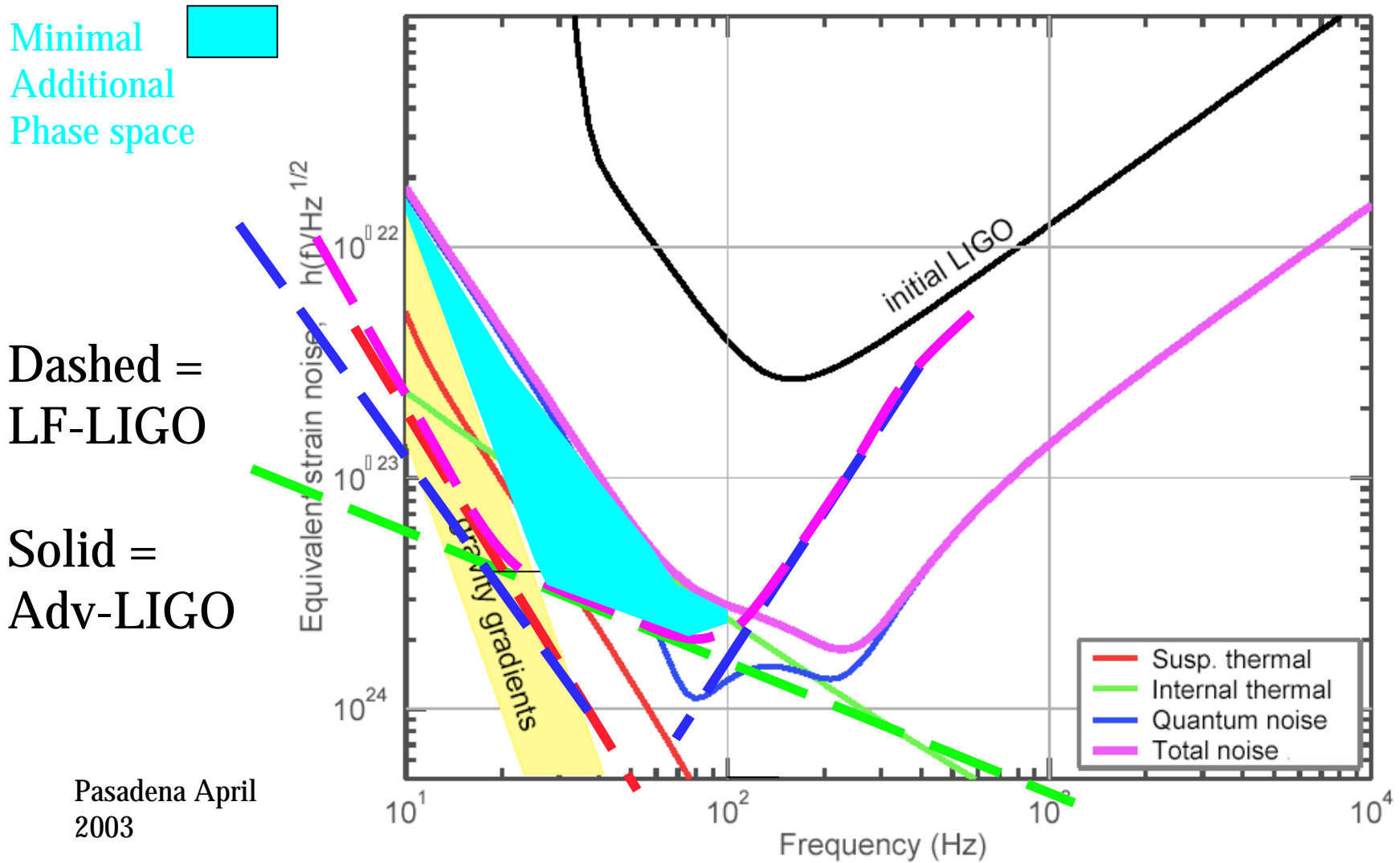
- The larger mirrors discussed are feasible today
  - 75 Kg fused silica
  - 430 mm diameter
  - Have a bid from Heraeus

## Does gravity gradient negate the advantages?

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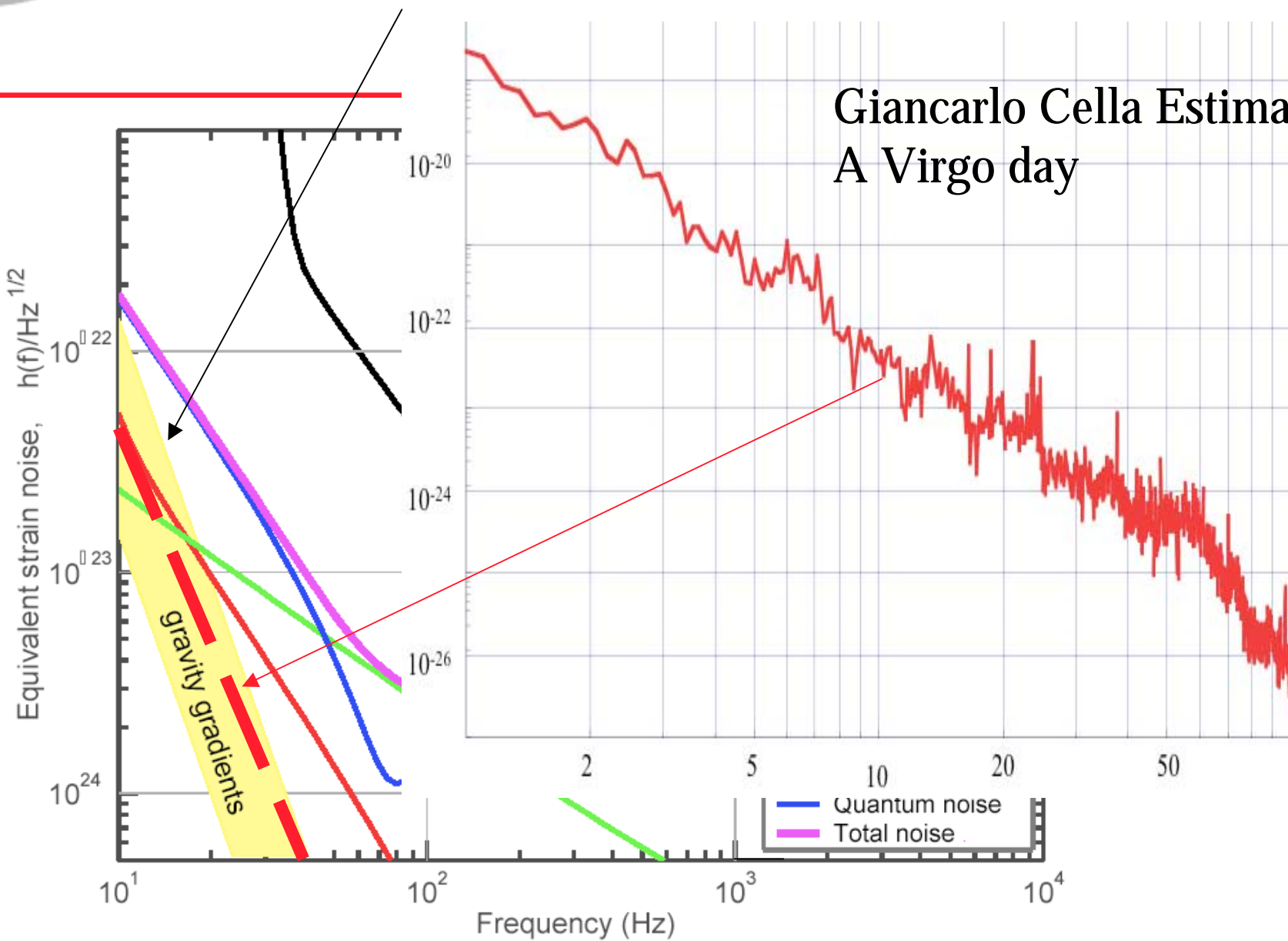
- With longer mirror suspensions (1-1.5m) the suspension thermal noise is pushed at lower frequency
- Gravity gradient gets uncovered
- Can start testing GG subtraction techniques
- Note:  
Clearly for the future will need to go underground to fight GG
- But even aboveground there is so much clear frequency range to allow substantial detection improvements

# Is gravity gradient going to stop us?





Adv-LIGO estimation based on worse of best 90%  
Of data stretches, including transients!



# Comments on GG

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- G.C. Cella evaluations give similar results
- Even if the GG was to be low only in windless nights, it would be worth having the listening capability 50% of the time
- LF-LIGO would give us the opportunity to test GG subtraction techniques

# Comments on GG

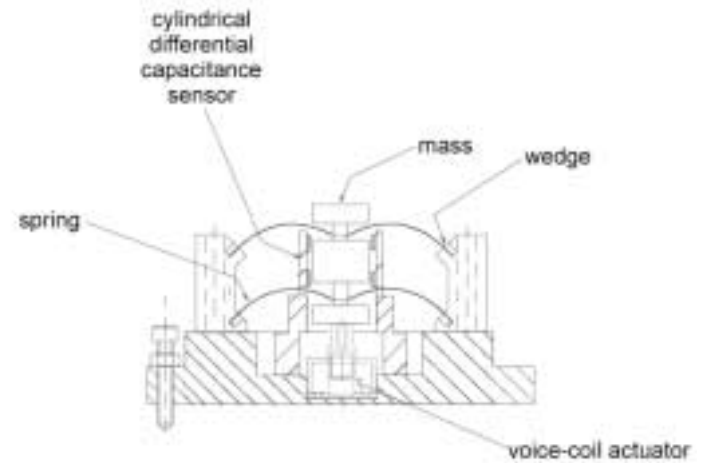
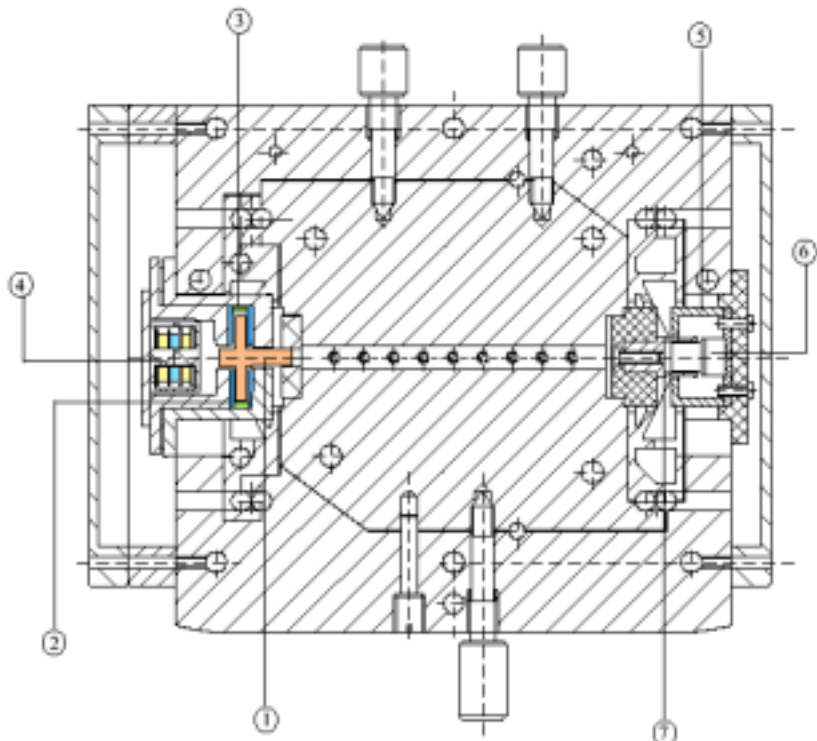
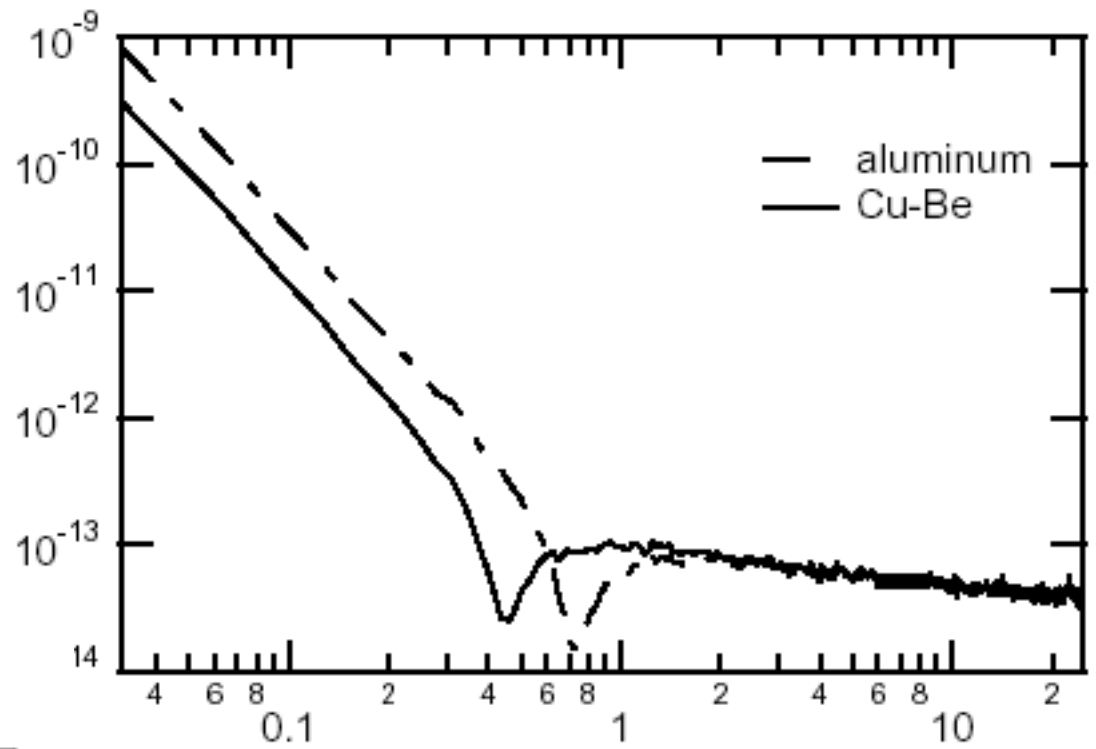
- Main contribution to GG is the moving soil/air interface.
- Simple matrix of surface accelerometers can allow up to x10 improvement
  - (work in Pisa)
- Then more difficult







Displacement Noise ( $\text{m}/\text{Hz}^{1/2}$ )



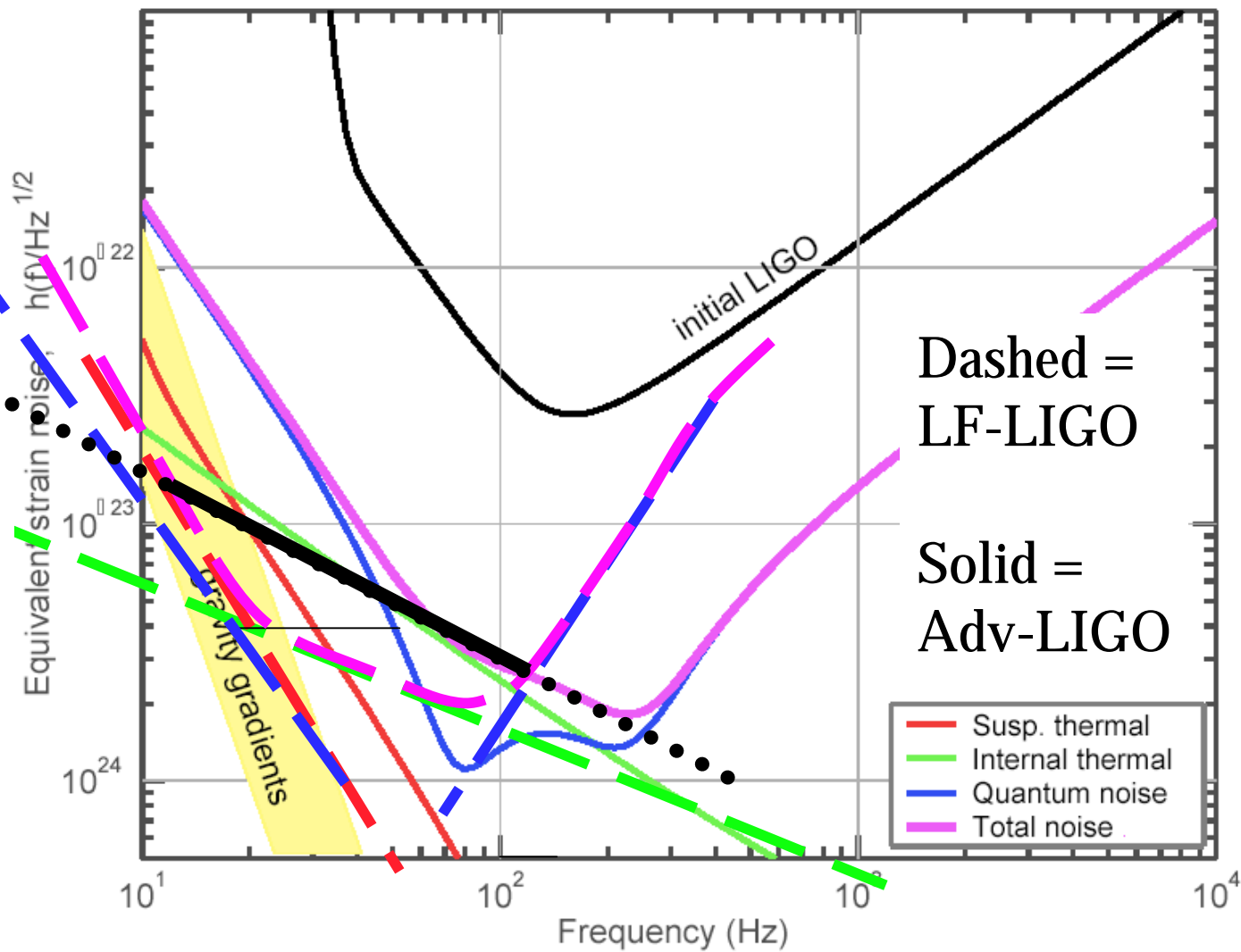
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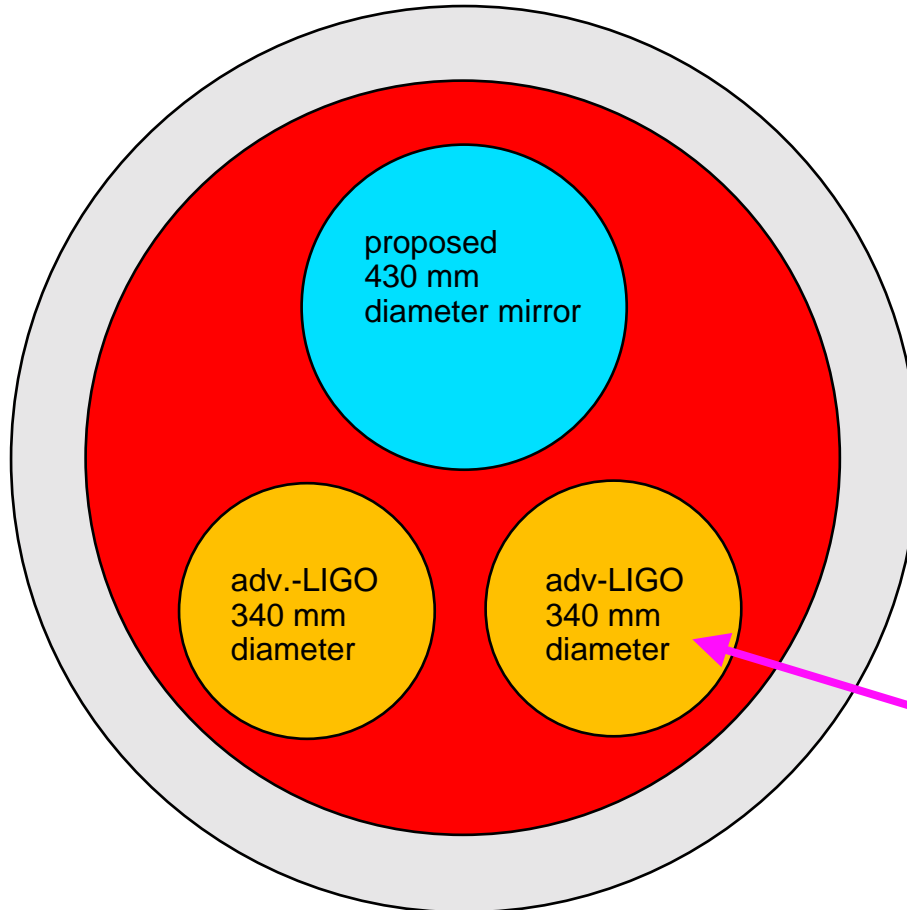
# Is gravity gradient going to stop us?

50+50 sm  
inspiral at  $z=2$

We can  
possibly re-  
cover all the  
yellow band



# Can we accommodate a LF Adv-LIGO

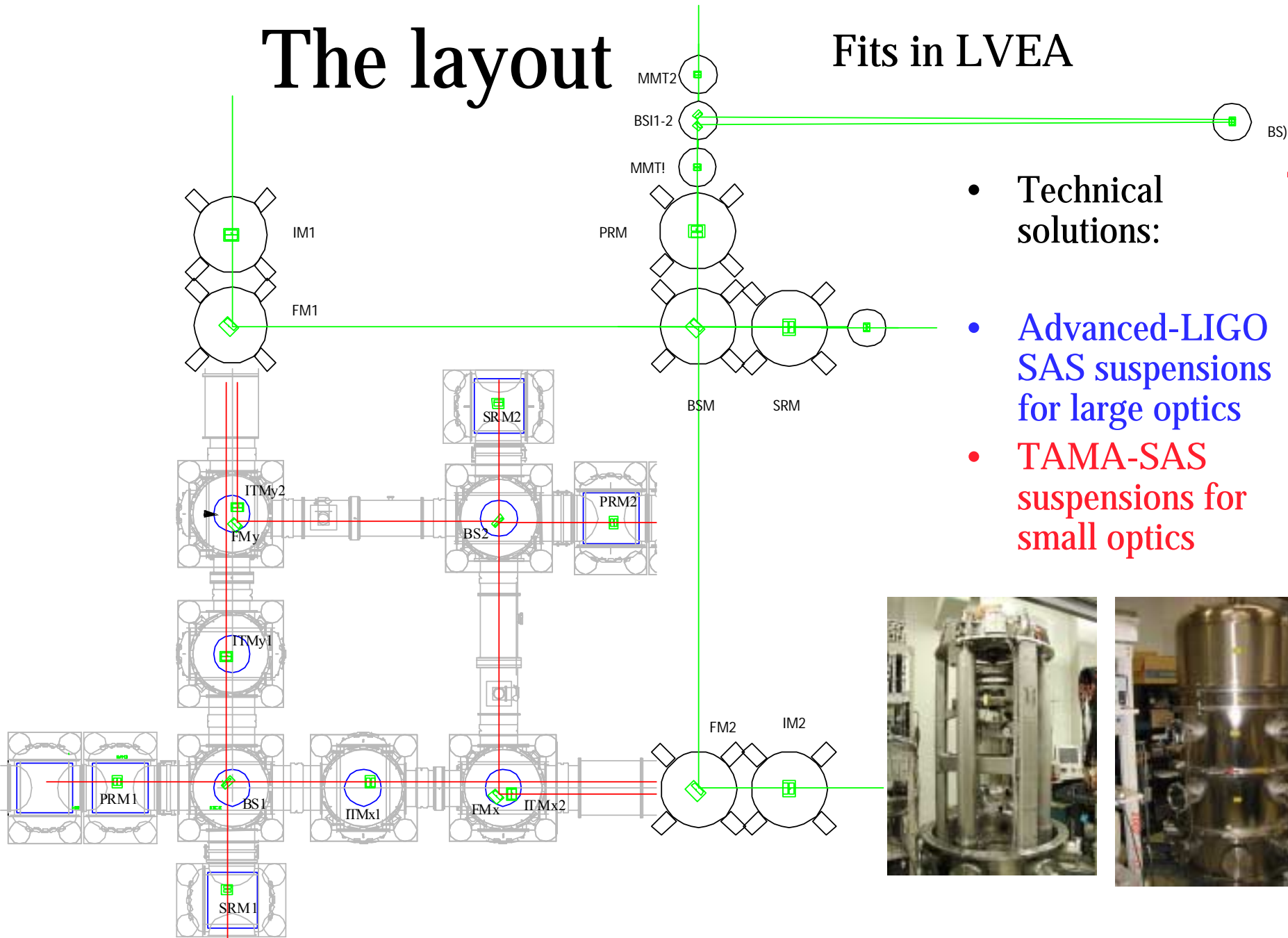


- There is space in the beam pipe just above and forwards of the Adv-LIGO mirrors

• Advanced LIGO nominal beam positions

# The layout

## Fits in LVEA



- Technical solutions:

- Advanced-LIGO SAS suspensions for large optics
- TAMA-SAS suspensions for small optics



# L F Int. Characteristics

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- Shorter SAS
- Longer mirror suspensions
  - Suspension T.N. freq. cut  $\sim 1/\sqrt{L}$
- **Everything hanging down**

Auxiliar suspended tables above beam line for pickoff, etc.

- **Stay out of the way of Adv. LIGO**

# Do we need a new design?

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- **Virgo optical and control design is nearly optimal,**
  - The **Virgo interferometer** is (or soon will be) fully validated.
  - Will only need minor improvements and some simplifications
- **Laser can be the same as LIGO (lower power)**
- **Seismic Attenuation and Suspensions**
  - large optics: already developed for advanced LIGO (downselected at the time)
  - Small optics: use TAMA-SAS design
  - Both well tested

All components off the shelf and tested.

**Technically we can build it almost immediately**

# When and where to implement LF LIGO?

- Cannot disrupt Adv-LIGO operations
- Above the Adv.-LIGO beamline => must be installed forward of Adv-LIGO
- At least all the main mirror vacuum tanks must, but probably all of the interferometer should, be installed at the same time as Adv-LIGO

# Can we afford a LF Adv-LIGO

- LSC and Advanced LIGO have decided not to pursue the L.F. option to focus on different possible sources, and dedicated all available sources to it
- A L.F. interferometer can be done only with external support
- A LF brother for Adv-LIGO would be a **simpler and cheaper interferometer.**
- There may be interest for EGO to make new interferometers in the LIGO facility before making a new generation IF in a new facility.
- **Seismic and suspension** design is available using the **inexpensive, existing, and well validated**, SAS and Virgo concept
- There is space in the existing facilities,
  - except the end stations at Hanford and small buildings for mode cleaner.



# Can we afford a LF Adv-LIGO

- Estimation of project costs:

Color code: Prices per unit **Price per interferometer**

Cost source

- |   |                  |               |
|---|------------------|---------------|
| • Large Vacuum tanks (2 m diameter ~Virgo design)       | 0.4 Meu          | Actual Cost   |
| • Large SAS tower (including control electronics)       | .25 Meu          | A.C./Bids     |
| • Mirrors   | 0.3 Meu          | Bids          |
| • 7 or 8 systems(vacuum+SAS+mirror) per interferometer  | <b>7.6 Meu</b>   |               |
| • Small vacuum tank and TAMA-SAS suspensions            | 0.2 Meu          | A. C. + Bids  |
| • 6 to 8 needed per interferometer                      | <b>1.6 MeU</b>   |               |
| • Small optics  | <b>0.2 Meu</b>   | Est.          |
| • Laser   | <b>0.5 Meu</b>   | rec. LIGO     |
| • Gate valves   | 0.1 Meu          | A.C.          |
| • 4 to 6 needed   | <b>0.6 Meu</b>   |               |
| • New buildings for end station and mode cleaner, each: | 0.5 MUS\$        | Est. F. Asiri |
| • 1 needed in LA (MC), 3 in WA (end station and MC)     | <b>1.0 MUS\$</b> |               |
| • Design  | <b>0.3 Meu</b>   | Est./A.C.     |
| • Various   | <b>3.0 Meu</b>   | Est.          |
| • Total per interferometer                              | <b>14.8 Meu</b>  |               |
| • Spares (1 set optics)                                 | <b>4.0 Meu</b>   |               |

# Can we afford a LF Adv-LIGO

- We are talking of **15 to 20 M US\$** per interferometer **for components**
- **Manpower** we can estimate a staff of **20 persons for 5 years for one interferometer, 30 persons for 2 interferometers**
  - Partly from Europe in part from the States.
  - 100,000US\$ per person/year, **for 1 interferometer 10 MUS\$**  
**for 2 interferometers 15 MUS\$**
- **Estimated Total**
- **for one interferometer 30 MUS\$**
- **for two interferometers 50 MUS\$**

# Can we afford **not to** introduce a LF brother for Adv-LIGO

- Clearly the newly observed BH are important and compelling potential GW sources for a LF interferometer
- Not going LF means forgoing the study of the genesis of the large galactic BH believed to be central to the dynamics of galaxies and forgoing mapping the globular clusters in our neighborhood

# Conclusions

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- Adv-LIGO is designed for broadband over a different set of possible sources and consequently does not cover well the Low Frequency range as well as an IFO exclusively targeted at this range
- Ignoring the LF range could be dangerous because it contains many juicy, and observed, GW signal generator candidates
- Redesigning Adv-LIGO to cover it would be awkward and take too long and it would uncover the equally important High Frequency range
- Adding a simple Low Frequency interferometer is the simplest and best choice!

# Implementation strategy

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- Gather a **composite study group**
- Since the resources will have to be both **external and harmonized** to the A-LIGO program  
the study group would have to be initially independent from LSC.
- **Go around the world with a hat**  
**see how many collaborators and additional millions of \$/Euro I manage to collect**