

# ***Study of the thermal noise caused by inhomogeneously distributed loss***

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# *0. Abstract*

(1) Our **experiments** show that ...

when the loss is distributed **inhomogeneously**

**the traditional method** to estimate thermal noise is **invalid**.

(2) The thermal noise of

**mirror with inhomogeneous loss**

was calculated using **new valid methods**.

# *Contents*

*1. Introduction*

*2. Experimental check of  
estimation methods*

*3. Calculation of thermal noise  
of the mirror  
with inhomogeneous loss*

*4. Summary*

# 1. Introduction

- Thermal noise of mirror

  - fundamental noise of GW detectors

  - It is **important** to estimate thermal noise

- Modal expansion

  - traditional method to estimate thermal noise

(thermal noise of system)

=  $\Sigma$  (thermal noise of **each resonant mode**)

However ...

new estimation methods (**direct approaches**)

suggest that modal expansion is **invalid**

when the loss is distributed **inhomogeneously**.

- **Direct approaches** (Levin, Nakagawa, Tsubono)

  - **without** modal decomposition

○ Suggestion of **direct approaches**

————→ **Serious problem !**

However, this problem **has not been**  
**researched fully.**

This problem is **main theme of this speech.**

○ The **two topics** of this speech

(1) **Experimental check** of estimation methods

**modal expansion** : **invalid**

**direct approach** : **valid**

(2) Estimation of thermal noise of

**the mirror with inhomogeneous loss**

using **direct approaches**

# 2. Experimental check of estimation methods

## 2-1. Outline

- Experimental check of modal expansion and direct approaches

—————→ Measurement of the thermal noise of the mirror with inhomogeneous loss

- Direct measurement of thermal noise of real mirror: difficult

(i) Mechanical model of mirror : drum

(ii) Measurement of mechanical response

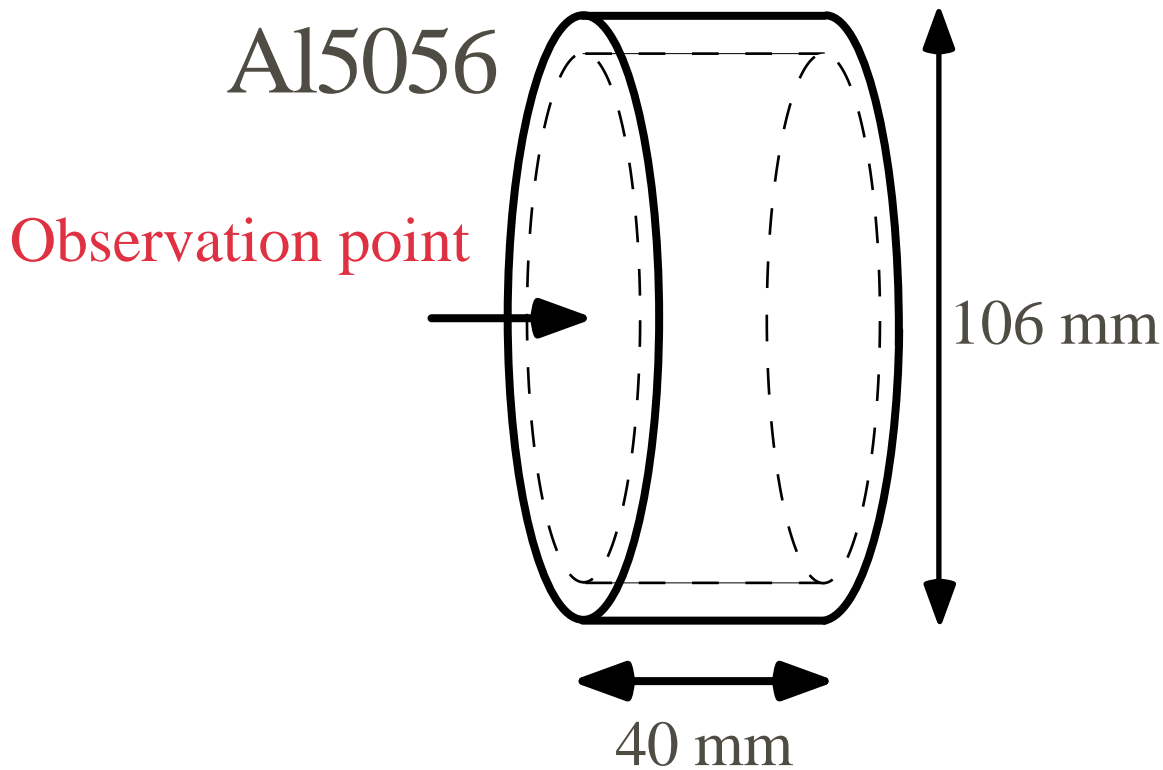
—————→ Fluctuation-dissipation theorem

first experimental check

using oscillator like mirrors

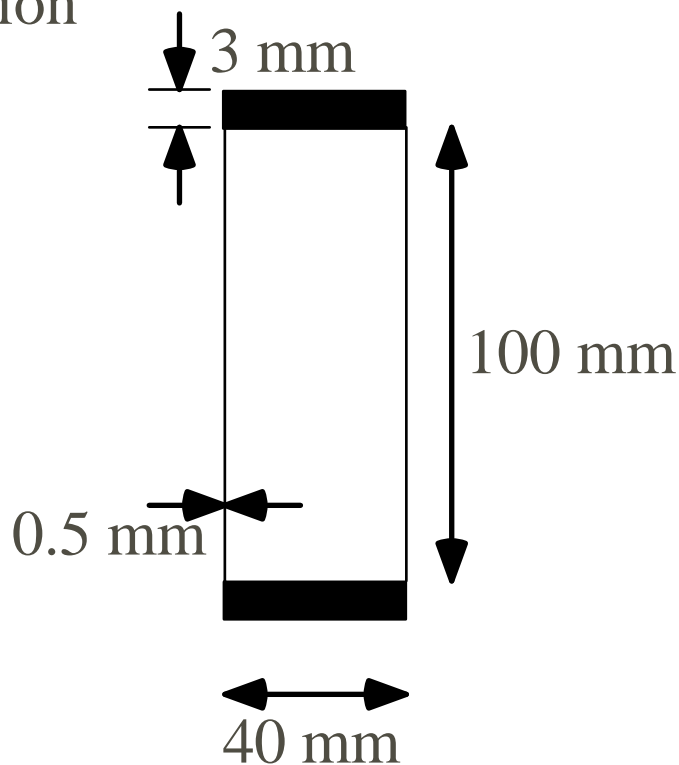
## 2-2. Experiment

○ drum



Observation band : lower than resonant frequencies

● Cross section





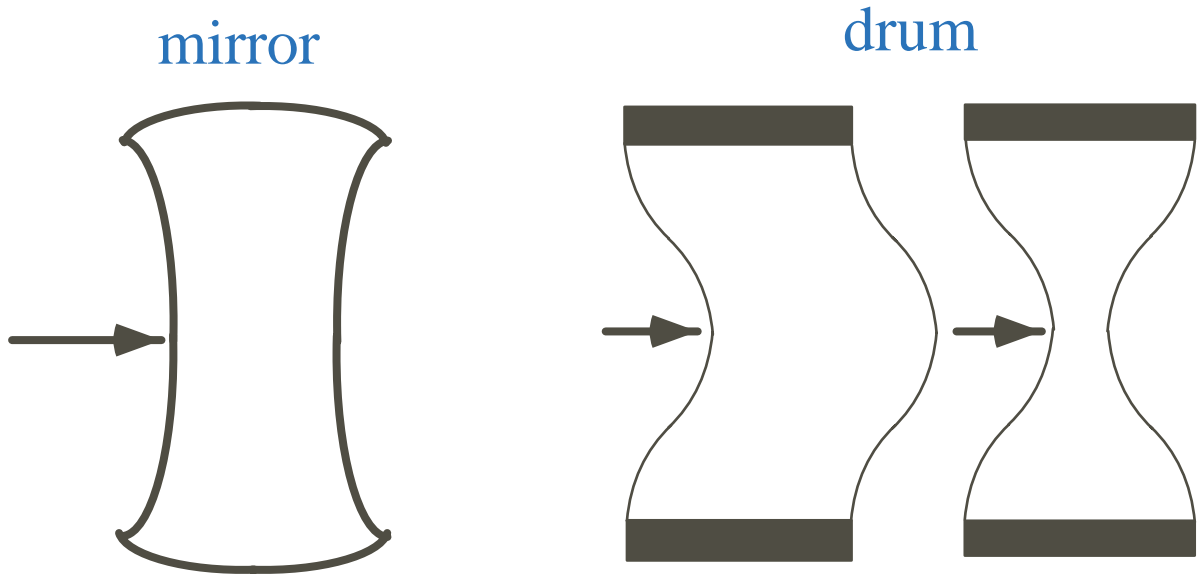
10cm

Drum (front view)



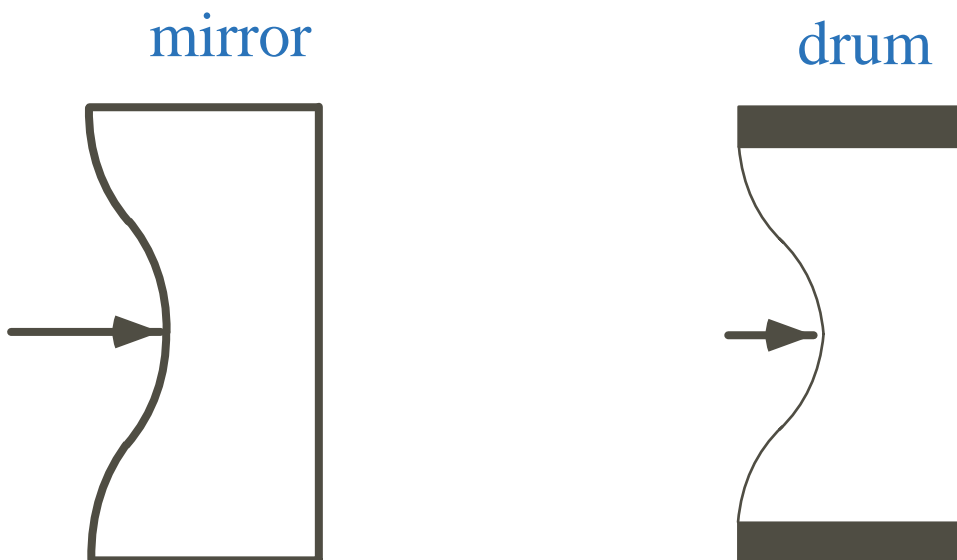
● comparison between **mirror** and **drum**

(1) At resonant frequencies



**Both sides** vibrate.

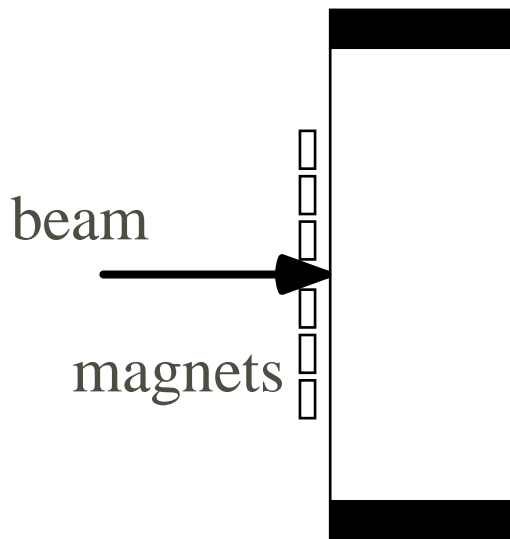
(2) In observation band ( $\ll$  resonant frequencies)



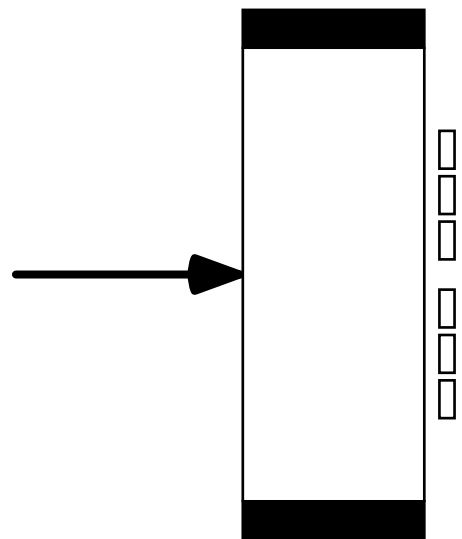
**Only one side** vibrates.

● loss distribution

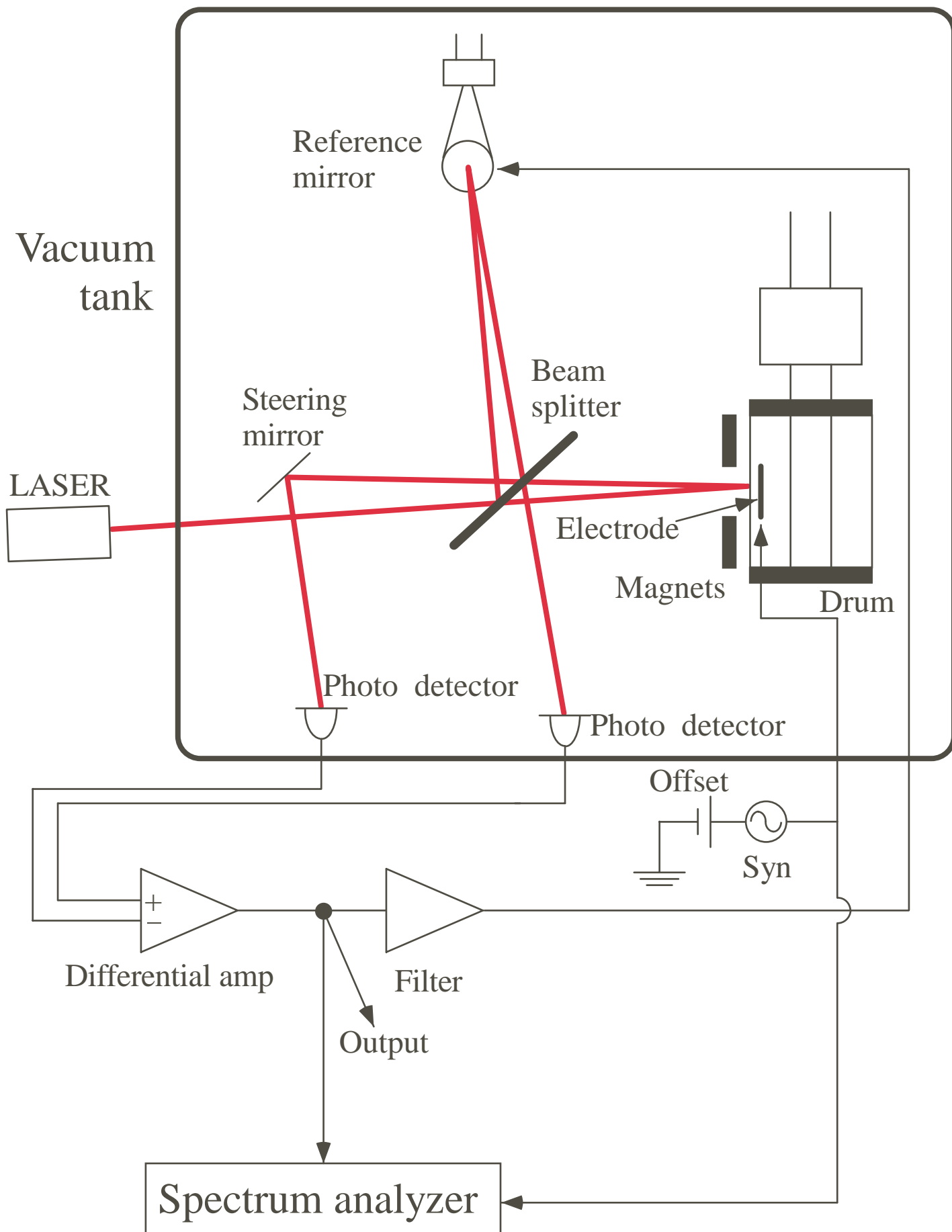
Front disk

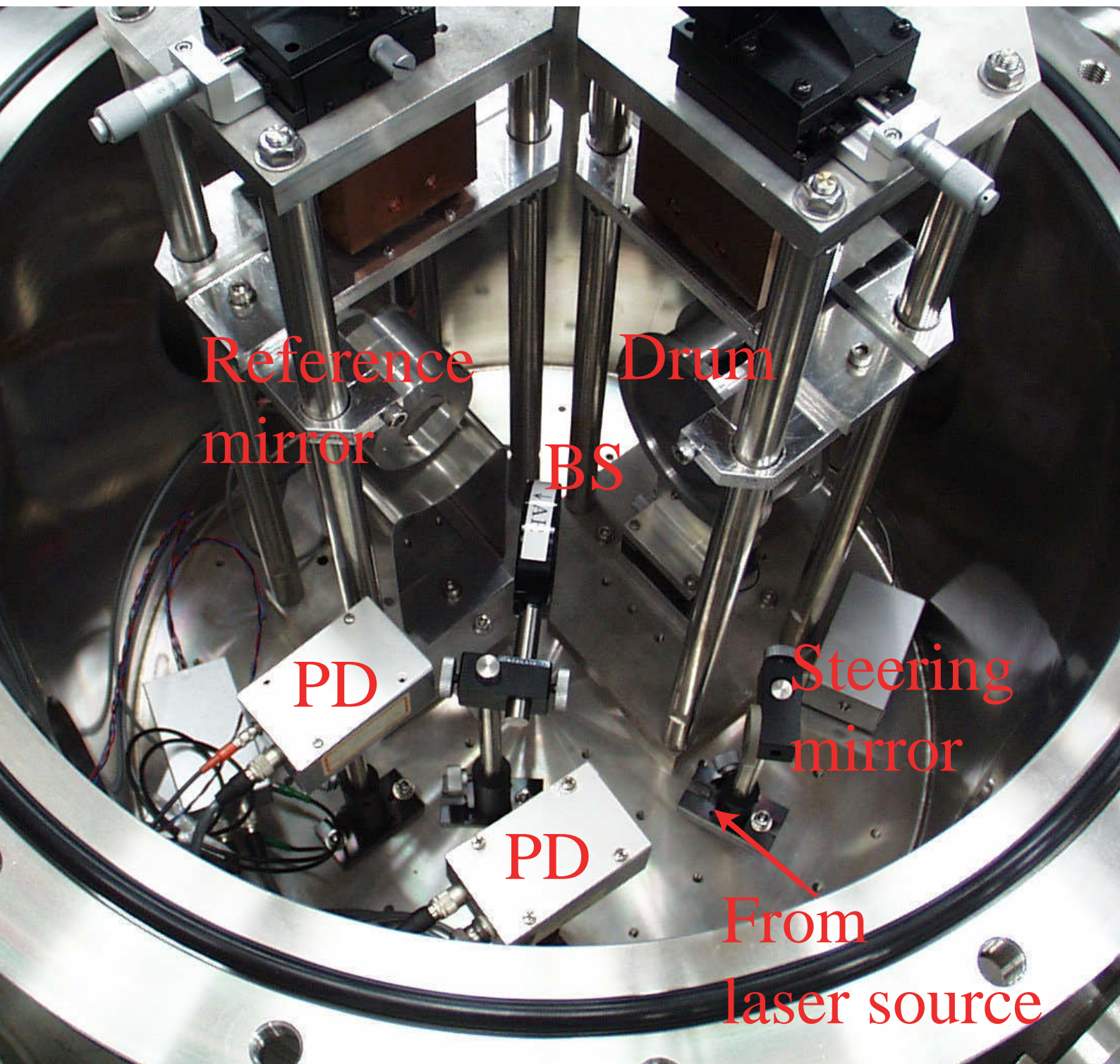


Back disk



# ○ Experimental apparatus



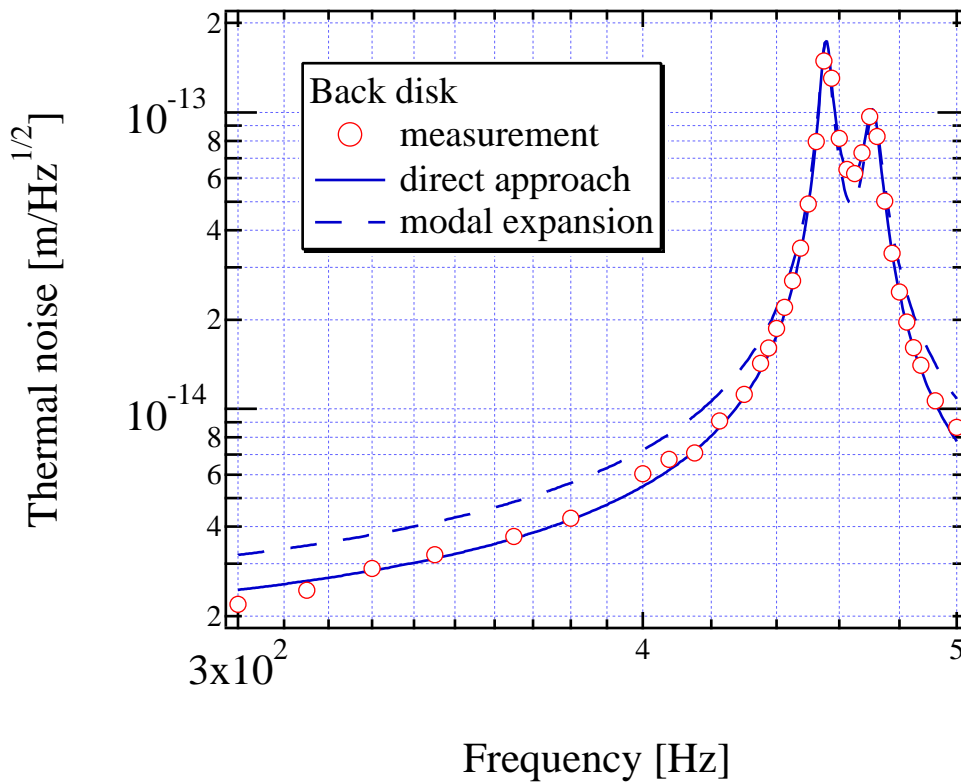
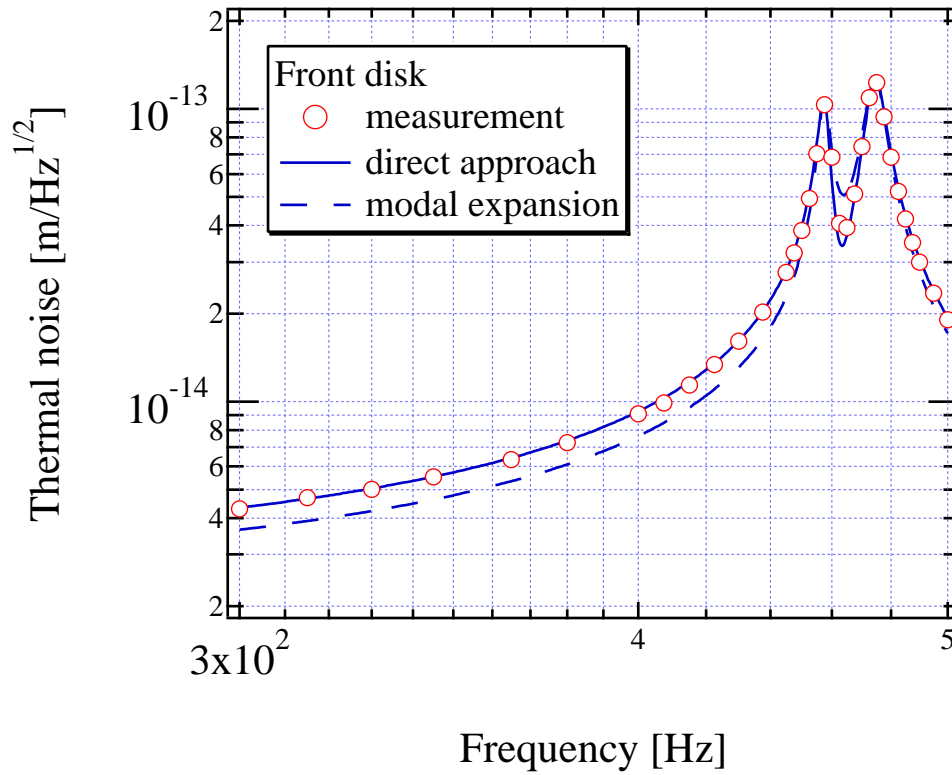


Interferometer  
in vacuum tank

# 2-3. Results

direct approach: valid

modal expansion: *invalid*



○ Why is modal expansion invalid ?

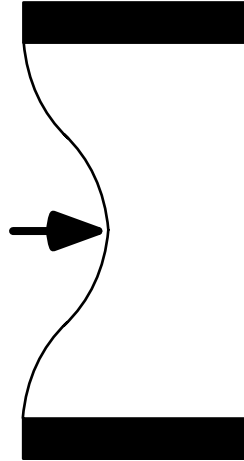
(1) **real** thermal noise

Fluctuation-dissipation theorem :

power of thermal motion

**is proportional to dissipated energy**

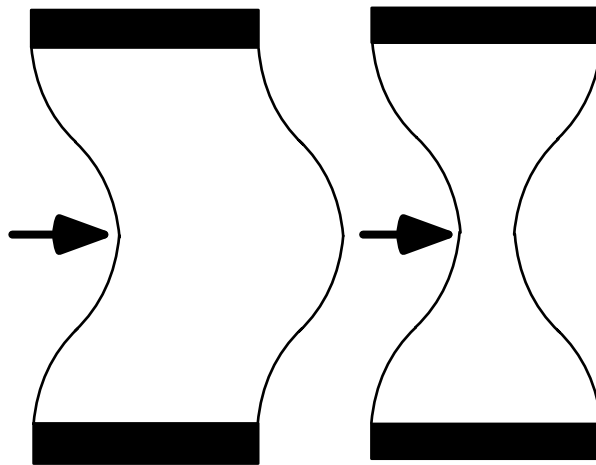
observation band  $\ll$  resonant frequency



**Only one side** vibrates.

loss : **Front** disk  $>$  **Back** disk

(2) **modal expansion** (summation of resonant mode)



**Both sides** vibrate.

loss : **Front** disk  $=$  **Back** disk

# *3. Calculation of thermal noise of the mirror with inhomogeneous loss*

## *3-1. Outline*

The thermal noise of **real** mirror  
**with inhomogeneous loss**

is calculated using **direct approach**.

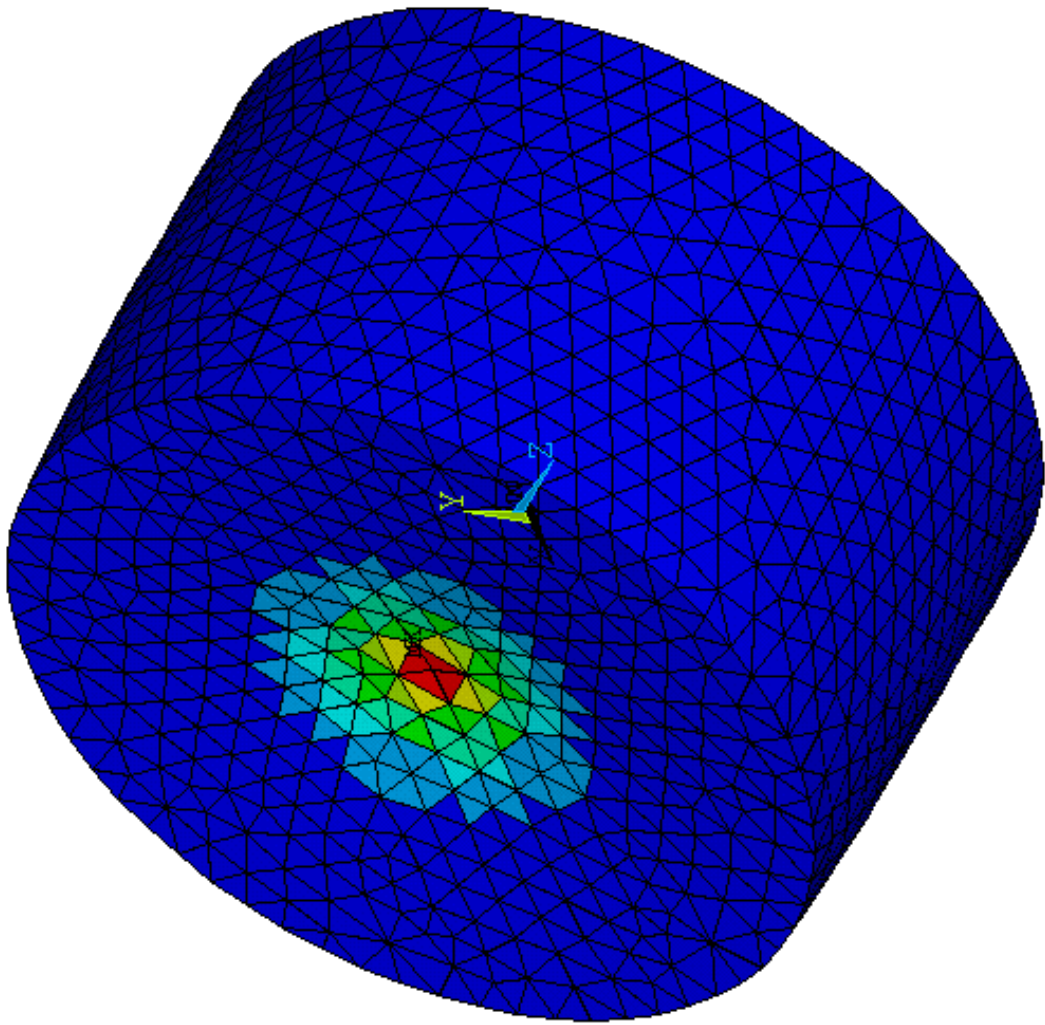
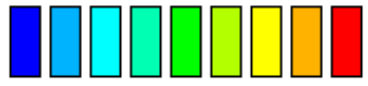
Calculation : difficult

—————▶ **Finite element method**



ANSYS 5.3  
MAR 26 2000  
20:32:50  
ELEMENT SOLUTION  
STEP=1  
SUB =1  
TIME=1  
SENE

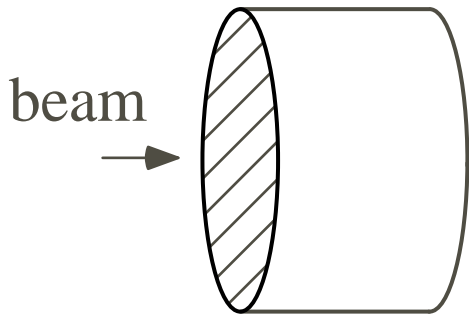
DMX = .195E-09  
SMN = .128E-16  
SMX = .775E-13  
.128E-16  
.862E-14  
.172E-13  
.258E-13  
.344E-13  
.431E-13  
.517E-13  
.603E-13  
.689E-13  
.775E-13





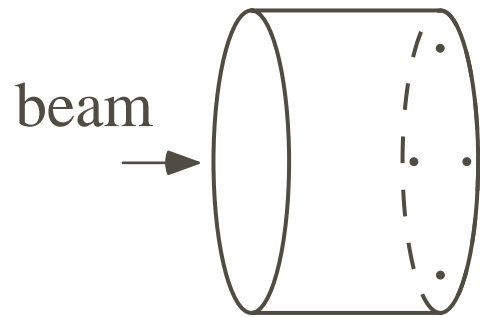
## 3-2. Loss distribution

two extreme case



Coating

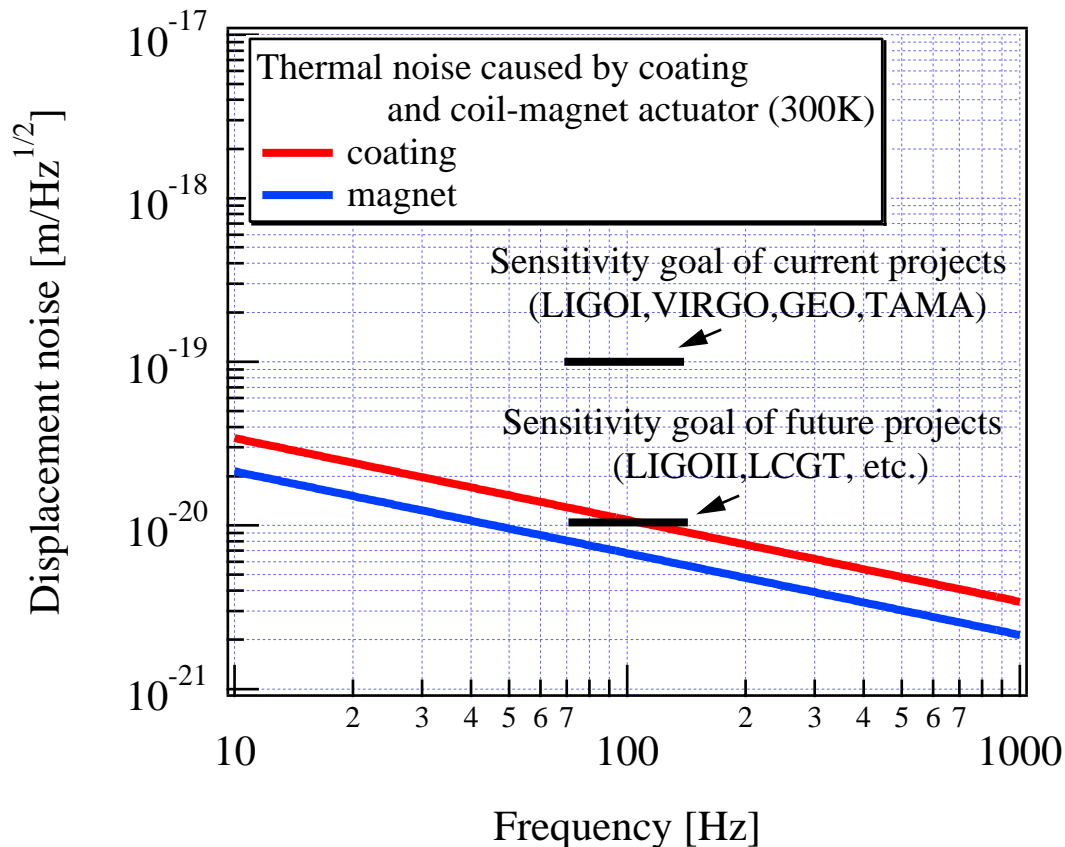
(thermal noise)  
>(modal expansion)



Coil-magnet  
actuator

(thermal noise)  
<(modal expansion)

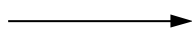
## 3-3. Results



In future projects ...

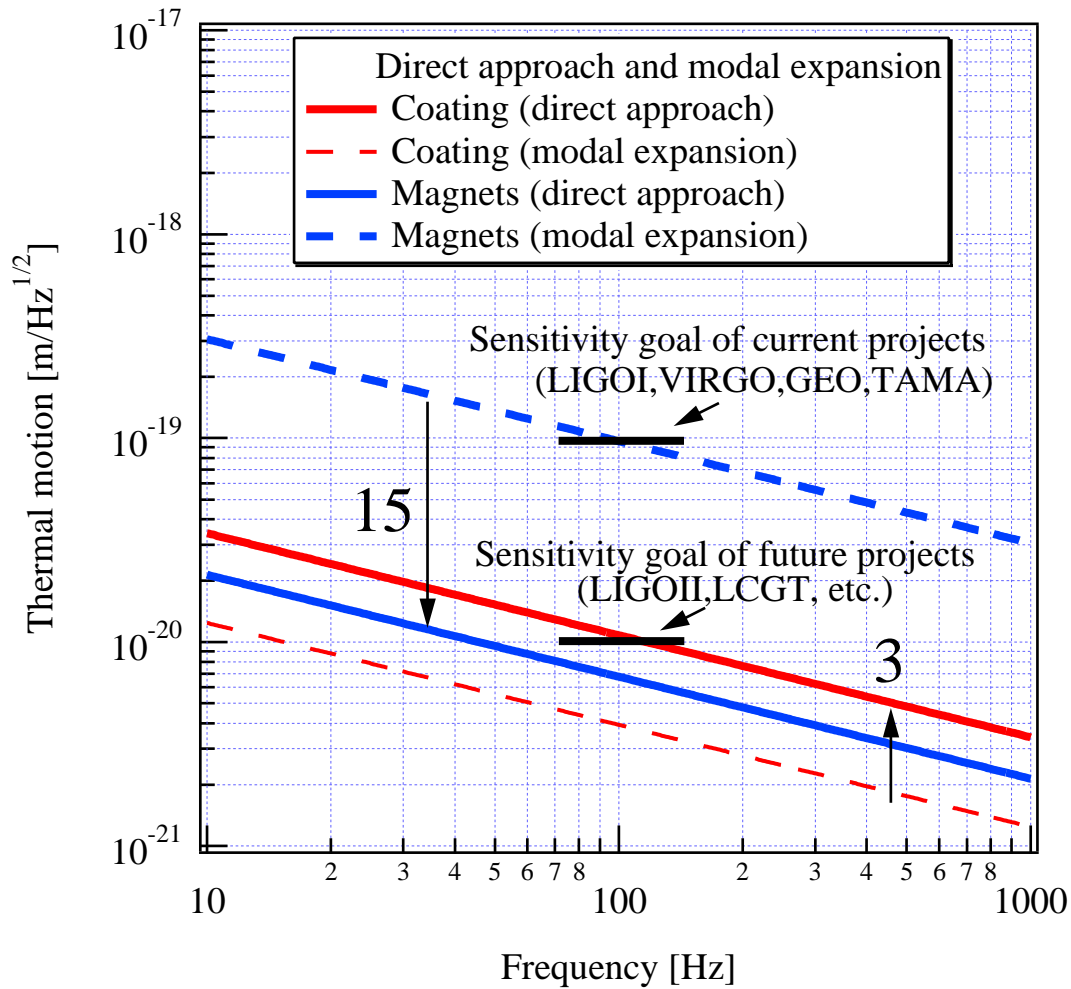
coating and magnet : **comparable** with goal

low loss coating and actuator ?



cooling ?

# Direct approach and modal expansion



coating : 3 times

magnet : 1/15 times

large difference

between the thermal noise

and modal expansion

# 4. Summary

(1) Our experiments show that ...

when the loss is distributed **inhomogeneously**

**modal expansion** (**traditional** method) is **invalid**.

**direct approaches** (**new** methods) are **valid**.

(2) The thermal noise of **mirror with inhomogeneous loss** is calculated using **direct approaches**.

**coating and actuator** : **comparable** with goal of **future** projects

**large difference** between **thermal noise** and estimation of **modal expansion**