

LASER INTERFEROMETER GRAVITATIONAL WAVE OBSERVATORY  
- LIGO -  
CALIFORNIA INSTITUTE OF TECHNOLOGY  
MASSACHUSETTS INSTITUTE OF TECHNOLOGY

<b>Document Type</b> <b>LIGO-T980054-00 - D</b> 6/15/98
<b>PO Beam Waist Size and Location on the ISC Table</b>
Michael Smith

*Distribution of this draft:*

This is an internal working note  
of the LIGO Project.

**California Institute of Technology**  
**LIGO Project - MS 51-33**  
**Pasadena CA 91125**  
Phone (626) 395-2129  
Fax (626) 304-9834  
E-mail: info@ligo.caltech.edu

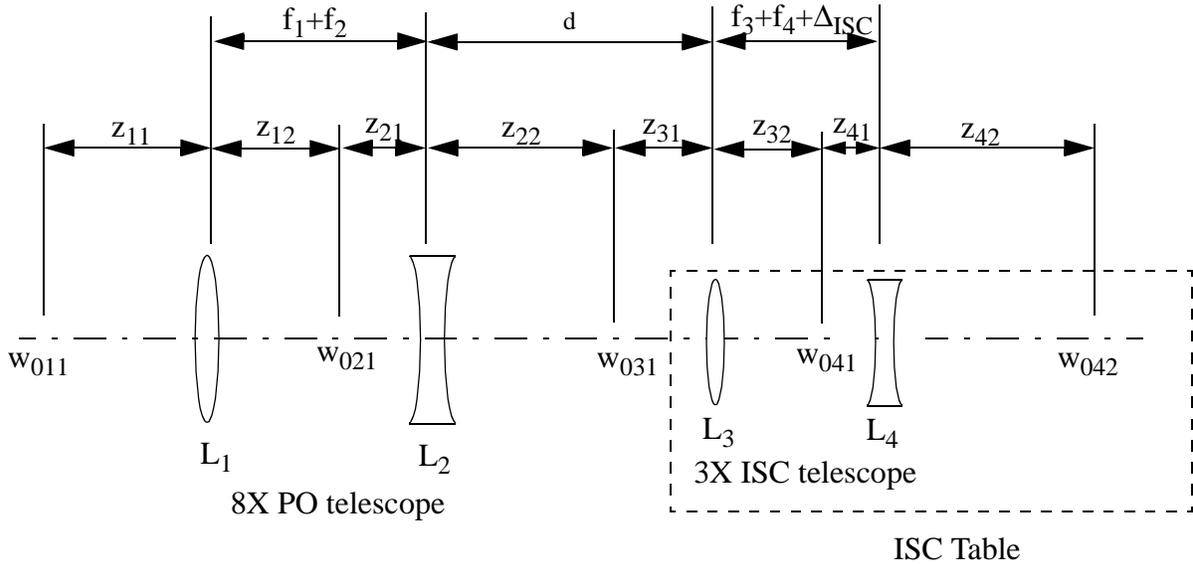
**Massachusetts Institute of Technology**  
**LIGO Project - MS 20B-145**  
**Cambridge, MA 01239**  
Phone (617) 253-4824  
Fax (617) 253-7014  
E-mail: info@ligo.mit.edu

WWW: <http://www.ligo.caltech.edu/>

LIGO DRAFT

# 1 OVERVIEW

The PO beam waist location on the ISC table can be varied by defocusing the ISC telescope. An optical schematic drawing of the PO beam optical train, which includes the 8X reflective telescope inside the vacuum housing and the 3.3X ISC telescope on the ISC optical table is shown in Figure 1. The input beam waist is inside the IFO, approximately 900 m from the PO telescope. The ISC telescope is separated from the PO telescope by approximately 3 m. The input beam waist is transformed by the lens train to an output beam waist of size  $w_{042}$ , located in the vicinity of the ISC table at a distance  $z_{42}$  from the end of the ISC telescope.



**Figure 1: Optical schematic of PO beam optical train**

The size and location of the output beam waist can be determined by using Gaussian beam transformation theory.

## 2 GAUSSIAN BEAM TRANSFORMATION THEORY

An analysis of the dependence of the output beam waist and location on the defocusing of the ISC telescope was made using the following parameters.

### 2.1. Telescope Parameters

#### PO Telescope

primary focal length, $f_1$	1524 mm
secondary focal length, $f_2$	-190.5 mm

input beam waist position, $z_{11}$	$9 \times 10^5$ mm
input beam waist parameter, $w_{011}$	36.4 mm
distance to ISC telescope, $d$	3000mm

### ISC Telescope

primary focal length, $f_3$	251.8 mm
secondary focal length, $f_4$	-74.172 mm

## 2.2. Gaussian Beam Transformation Equations

$$z_{12} := f_1 + f_1^2 \cdot \frac{(z_{11} - f_1)}{\left[ (z_{11} - f_1)^2 + \left( \pi \cdot \frac{w_{011}^2}{\lambda} \right)^2 \right]}$$

$$w_{012} := \left[ \frac{1 \cdot \left( 1 - \frac{z_{11}}{f_1} \right)^2}{w_{011}^2} + \frac{1 \cdot \left( \pi \cdot \frac{w_{011}}{\lambda} \right)^2}{f_1^2} \right]^{-0.5}$$

$$w_{021} := w_{012}$$

$$z_{21} := f_1 + f_2 - z_{12}$$

$$z_{22} := f_2 + f_2^2 \cdot \frac{(z_{21} - f_2)}{\left[ (z_{21} - f_2)^2 + \left( \pi \cdot \frac{w_{021}^2}{\lambda} \right)^2 \right]}$$

$$w_{022} := \left[ \frac{1 \cdot \left( 1 - \frac{z_{21}}{f_2} \right)^2}{w_{021}^2} + \frac{1 \cdot \left( \pi \cdot \frac{w_{021}}{\lambda} \right)^2}{f_2^2} \right]^{-0.5}$$

LIGO-DRAFT

$$w_{031} := w_{022}$$

$$z_{31} := d - z_{22}$$

$$z_{32} := f_3 + f_3^2 \cdot \frac{(z_{31} - f_3)}{\left[ (z_{31} - f_3)^2 + \left( \pi \cdot \frac{w_{031}^2}{\lambda} \right)^2 \right]}$$

$$w_{032} := \left[ \frac{1 \cdot \left( 1 - \frac{z_{31}}{f_3} \right)^2}{w_{031}^2} + \frac{1 \cdot \left( \pi \cdot \frac{w_{031}}{\lambda} \right)^2}{f_3^2} \right]^{-0.5}$$

$$w_{041} := w_{032}$$

$$z_{41}(\Delta \text{ ISC}) := f_3 + f_4 + \Delta \text{ ISC} - z_{32}$$

$$z_{42}(\Delta \text{ ISC}) := f_4 + f_4^2 \cdot \frac{(z_{41}(\Delta \text{ ISC}) - f_4)}{\left[ (z_{41}(\Delta \text{ ISC}) - f_4)^2 + \left( \pi \cdot \frac{w_{041}^2}{\lambda} \right)^2 \right]}$$

$$w_{042}(\Delta \text{ ISC}) := \left[ \frac{1 \cdot \left( 1 - \frac{z_{41}(\Delta \text{ ISC})}{f_4} \right)^2}{w_{041}^2} + \frac{1 \cdot \left( \pi \cdot \frac{w_{041}}{\lambda} \right)^2}{f_4^2} \right]^{-0.5}$$

LIGO-DRAFT

### 2.3. Results: Output Beam Waist Size and Location

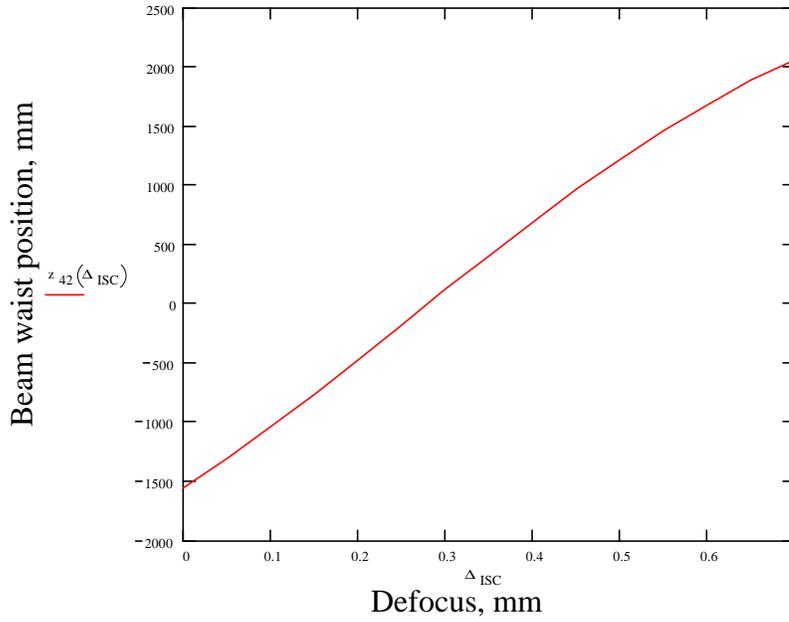


Figure 2: Beam waist position versus ISC defocus, d=3000mm

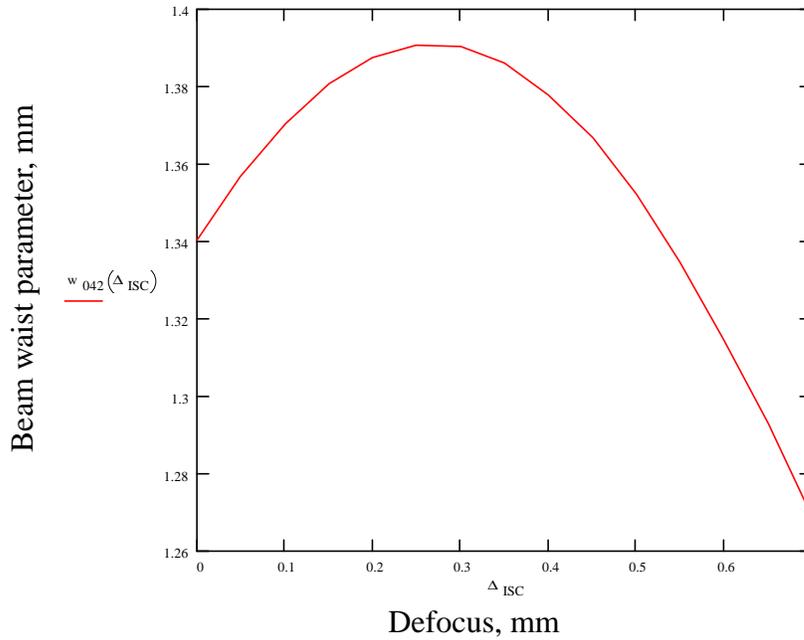


Figure 3: Beam waist size versus ISC defocus, d=3000mm

LIGO-DRAFT