



Laboratoire Kastler Brossel
Physique quantique et applications

High sensitivity interferometric measurements in cryogenic environment: optomechanical correlations and laser cooling

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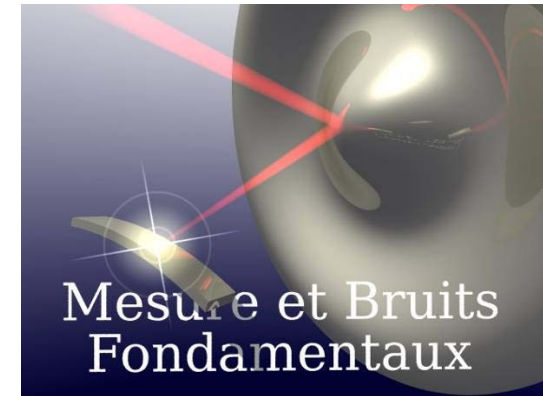
Antoine Heidmann

Pierre Verlot

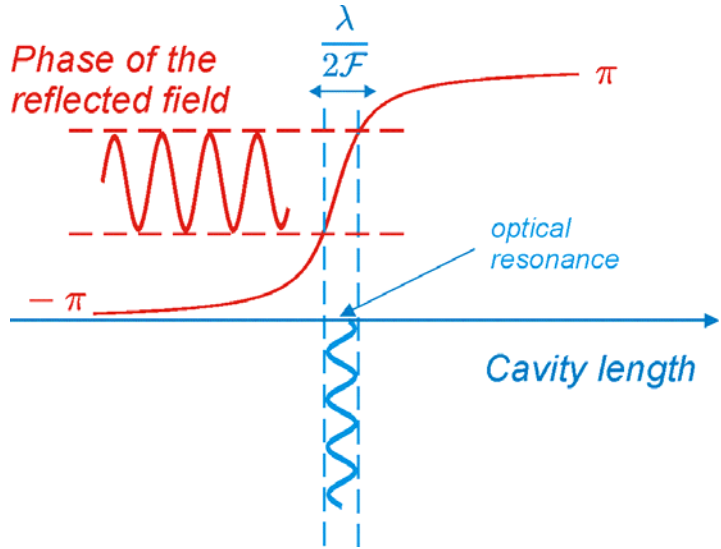
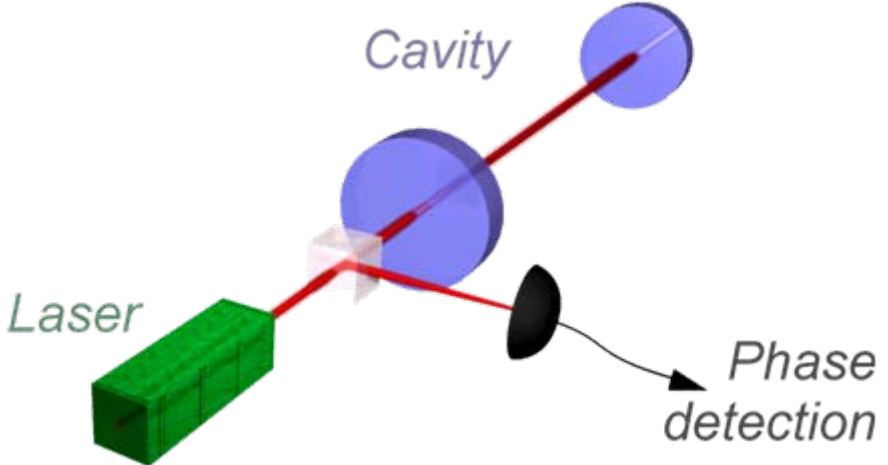
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Chiara Molinelli

Aurélien Kuhn



High-sensitivity displacement measurement



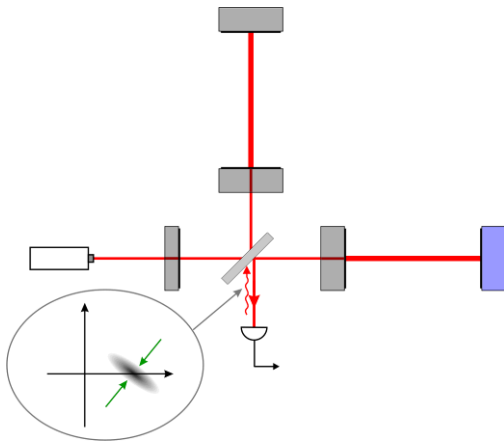
$$\delta\varphi_{\text{out}} = \delta\varphi_{\text{in}} + \frac{8n\mathcal{F}}{\lambda} (\delta x + \delta x_{\text{cl}} + \delta x_{\text{rad}})$$

(quantum) phase noise index fluctuations frequency noise signal (classical) position noise (quantum) radiation pressure noise

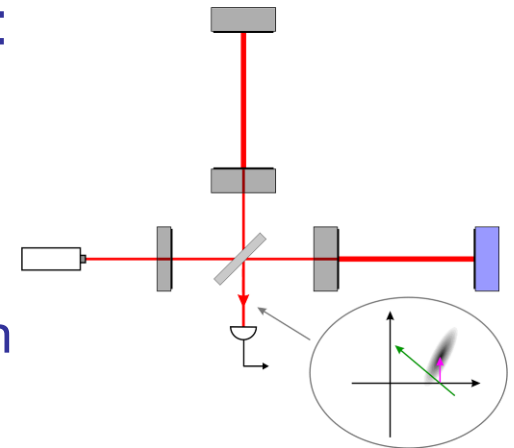
Quantum noise reduction

Many proposals to reduce quantum noises:

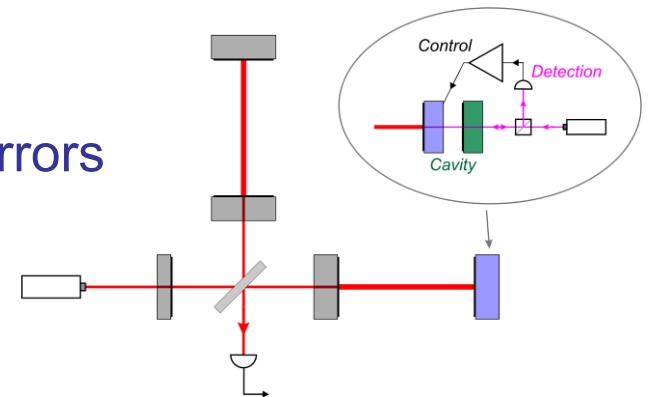
- Injection of squeezed states



- QND detection



- Quantum locking of mirrors



Objectives:

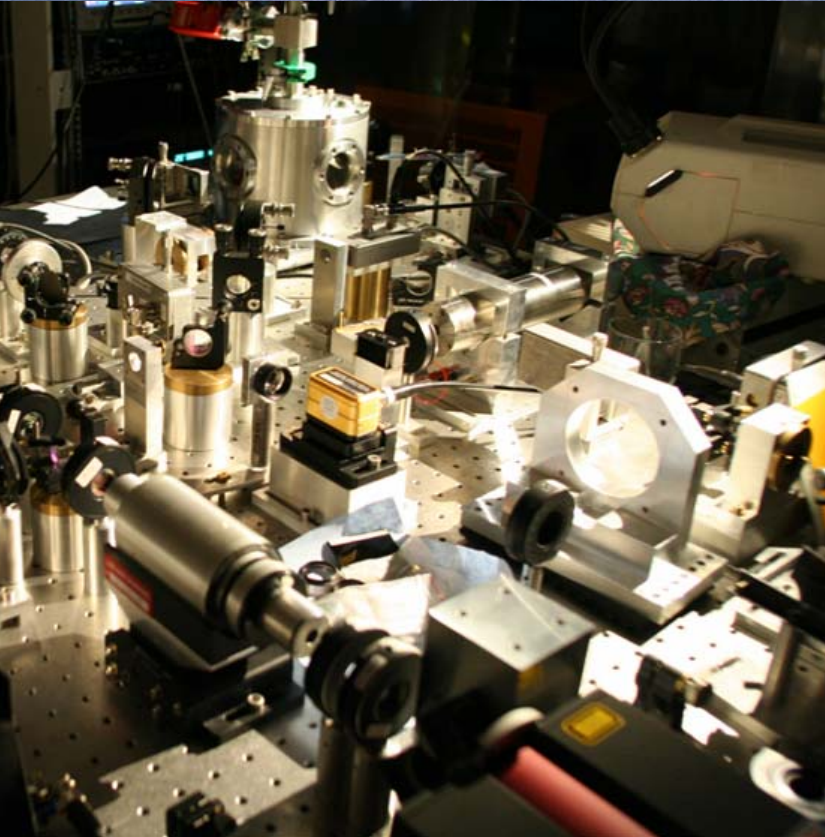
- Define the constraints in real interferometers
- Find efficient and robust schemes
- Perform experimental tests of quantum noises



High sensitivity interferometric measurements

Toward a QND measurement

Laser cooling of a microresonator



Experimental setup

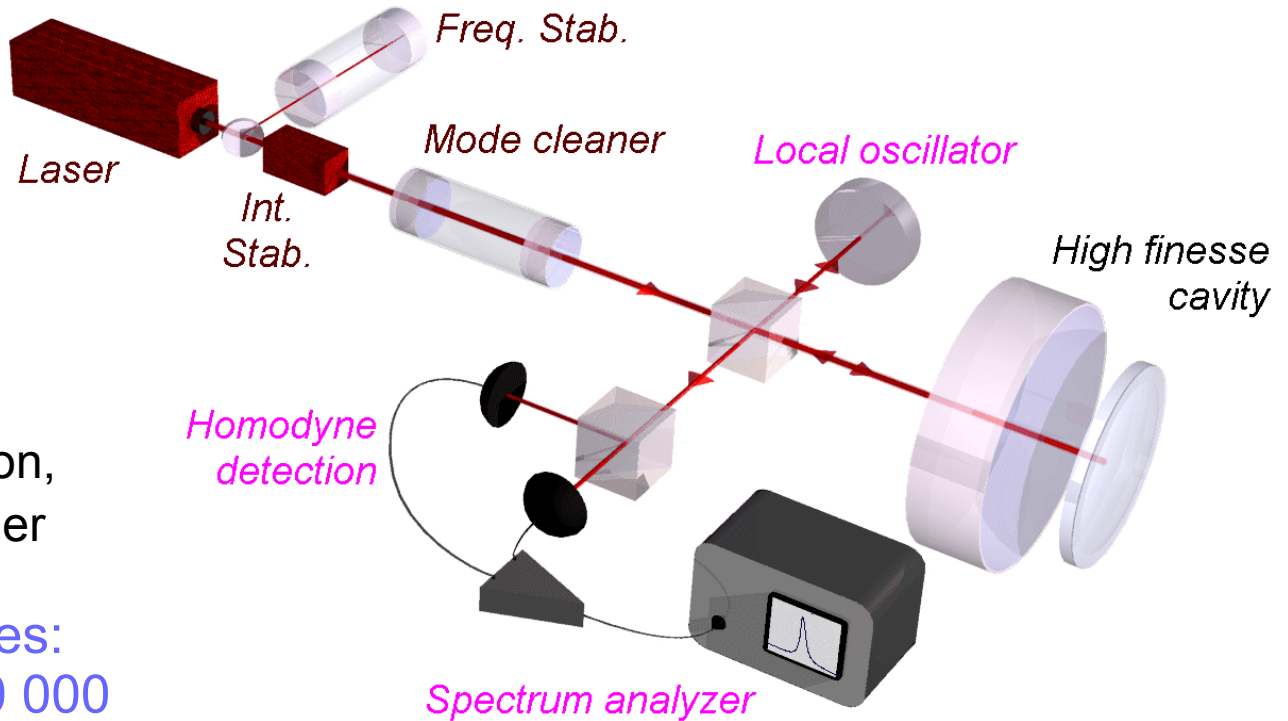
Measurement of mirror displacements with a high-finesse cavity

- Ultra stable laser source

Frequency and intensity stabilization, spatial mode cleaner

- High-finesse cavities: from 30 000 to 230 000

- Homodyne detection working at the quantum level



Observation of thermal noise

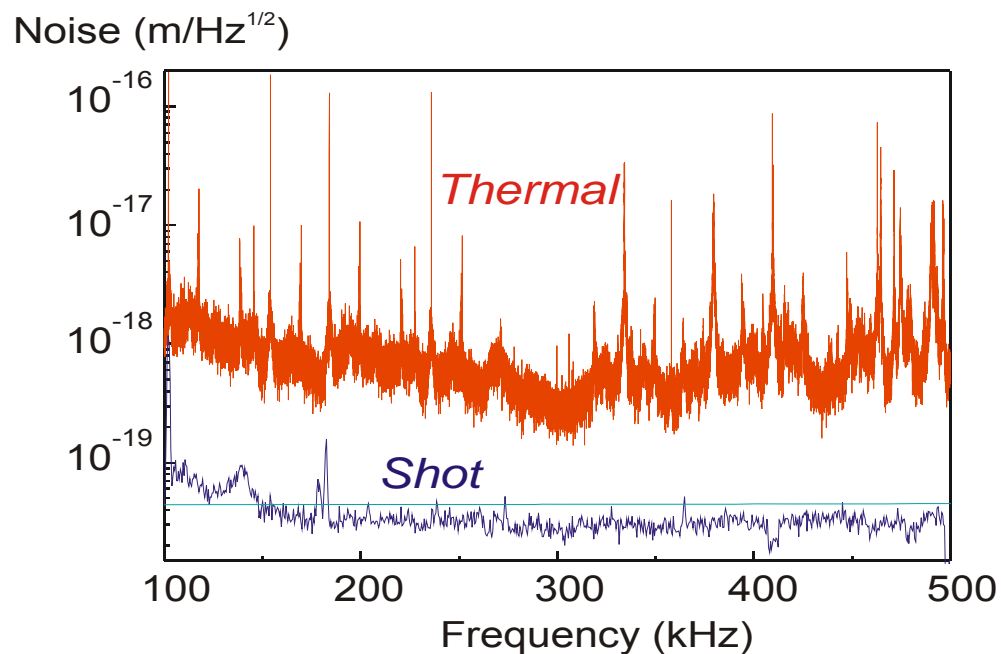


Optical coating made by the LMA
Cavity with a finesse 230 000

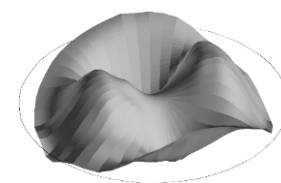
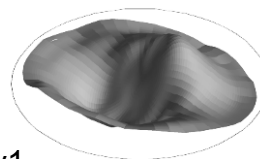
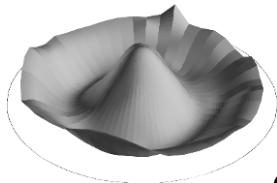
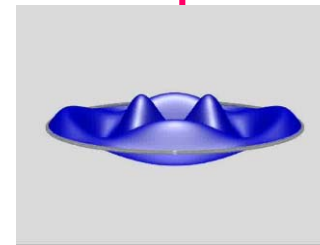
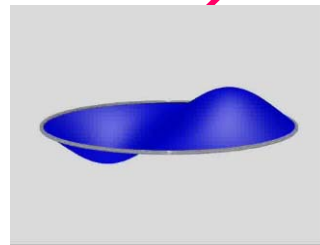
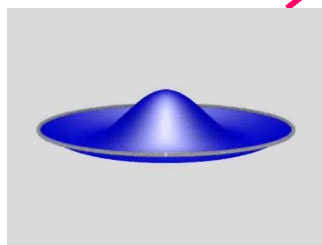
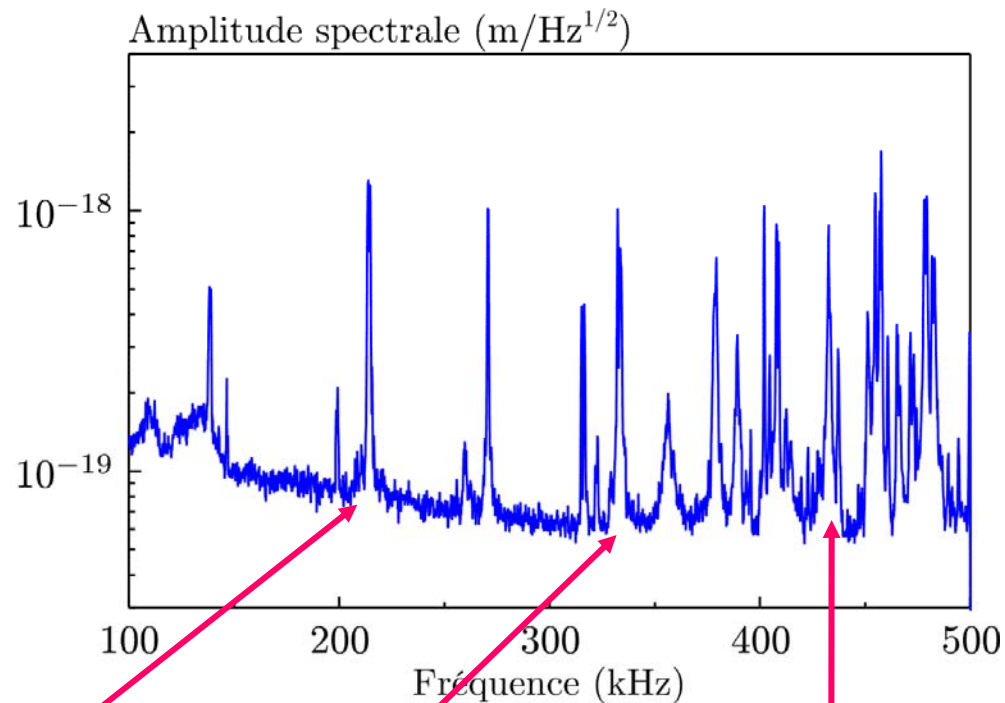
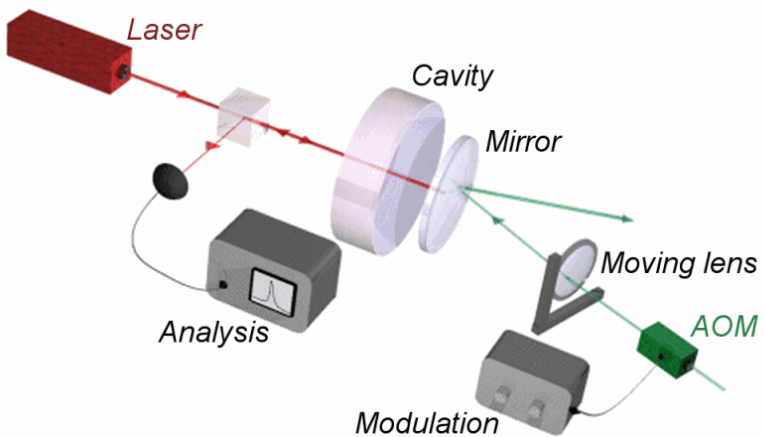
1 mW of incident power

Current sensitivity:

$$\delta x_{\min} = 3 \times 10^{-20} \text{ m}/\sqrt{\text{Hz}}$$



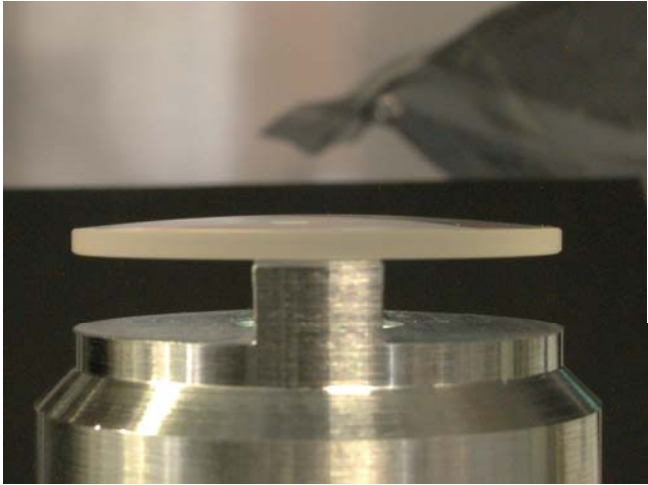
Characterization of internal modes



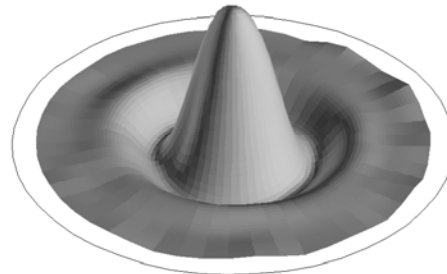
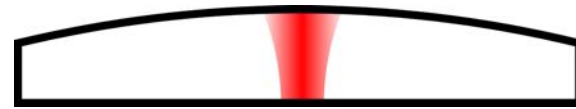
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Characterization of internal modes

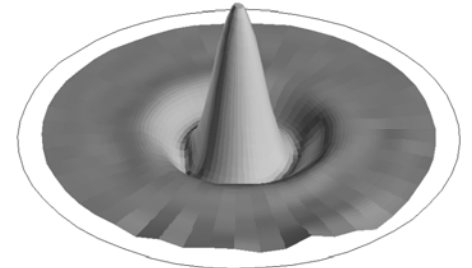
Plano-convex geometry



Gaussian structure of acoustic mode
Confinement at the center



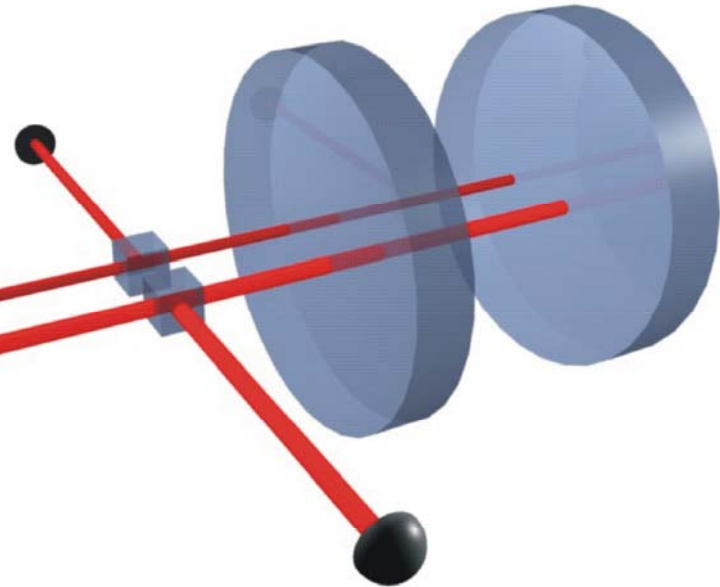
$npl = 100$



200

Effective mass of 20mg < 1% of total mass

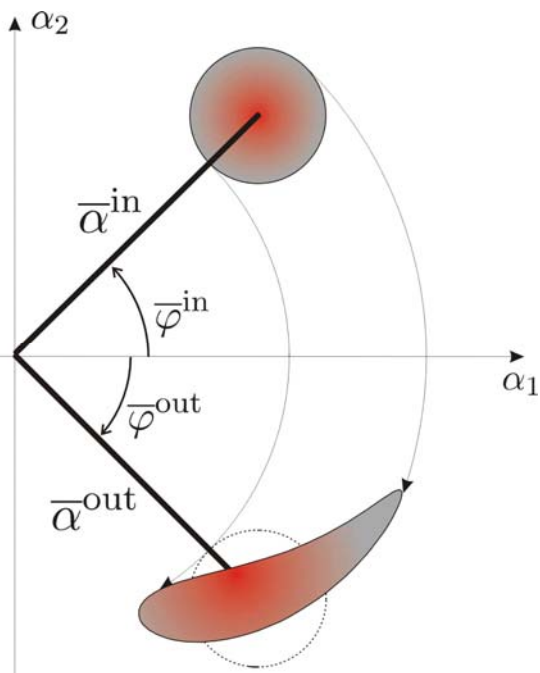
Mechanical Q factor up to 10^6



High sensitivity interferometric measurements

Toward a QND measurement

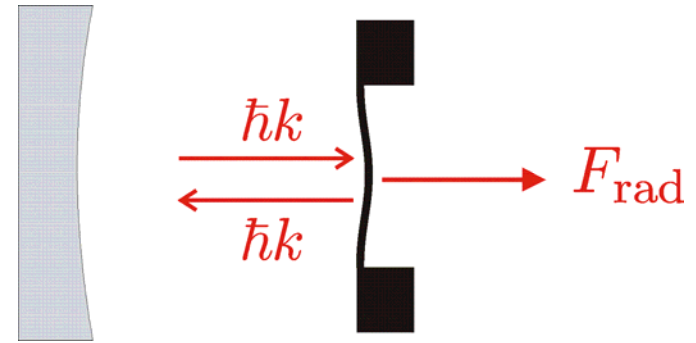
Laser cooling of a microresonator



Quantum optics and radiation pressure

Optomechanical effects in a cavity:

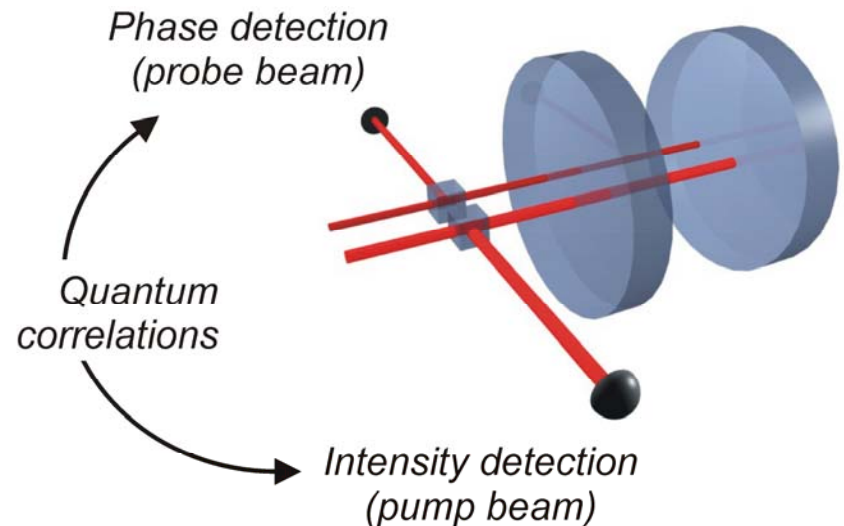
- Radiation pressure of light induces a mirror motion
- The mirror motion produces a phase-shift of the light



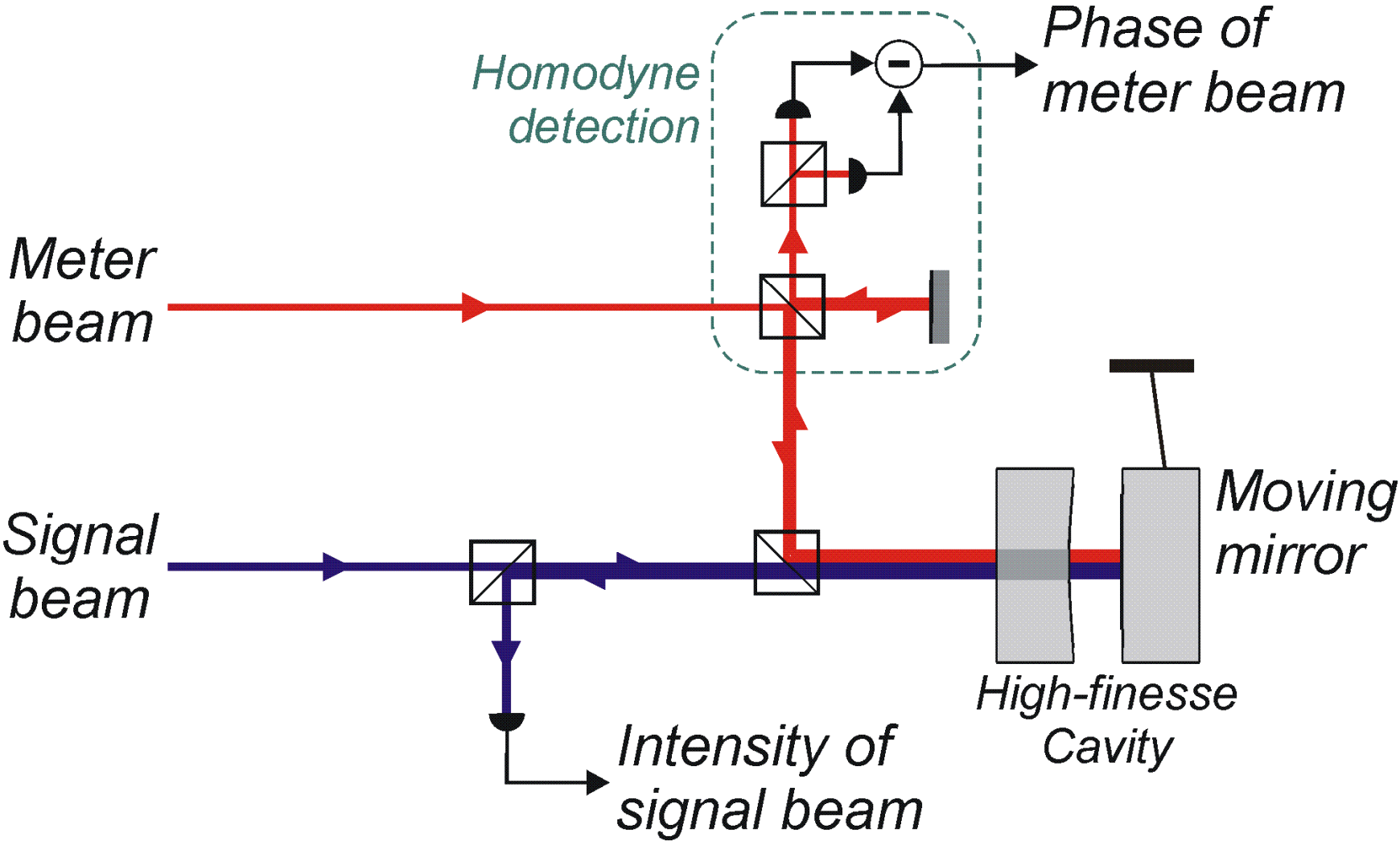
A moving mirror is equivalent to a nonlinear Kerr medium inserted in the cavity

→ Quantum optics experiments:

- Squeezed light generation
- Quantum Non Demolition measurement



Principle of the experiment



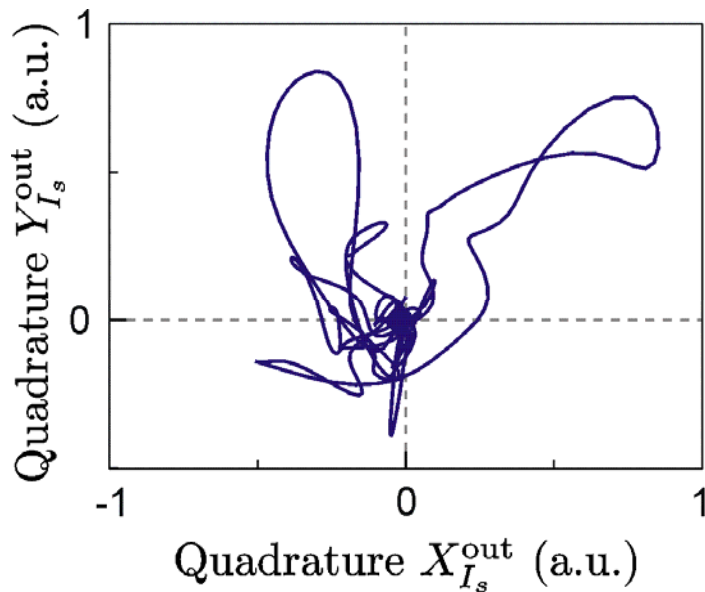
Experimental results

Intensity noise:

$$\delta I_s^{out}(t) = X_{I_s}^{out}(t) \cos(\Omega_c t) + Y_{I_s}^{out}(t) \sin(\Omega_c t)$$

Phase noise:

$$\delta \varphi_m^{out}(t) = X_{\varphi_m}^{out}(t) \cos(\Omega_c t) + Y_{\varphi_m}^{out}(t) \sin(\Omega_c t)$$

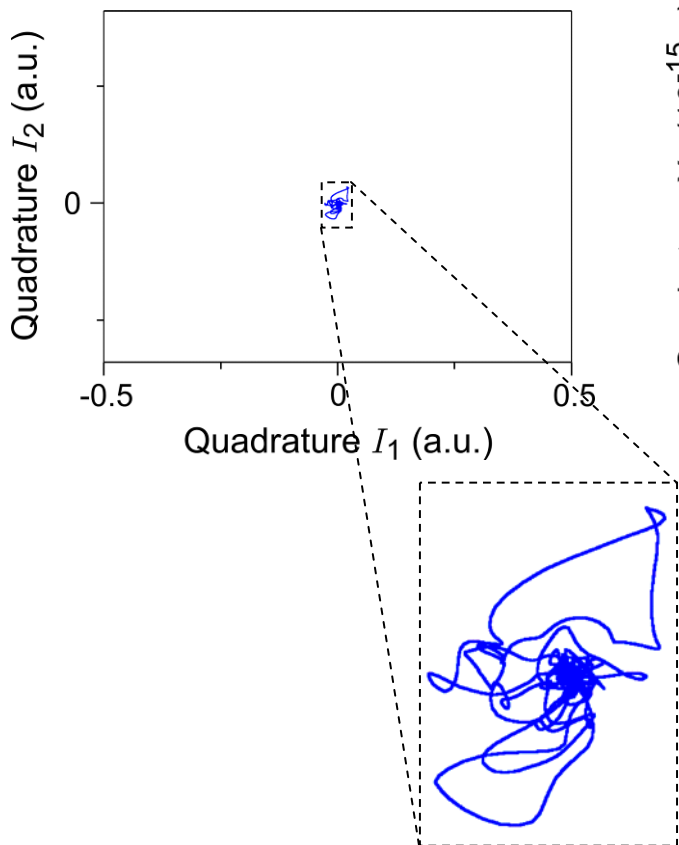


$$\delta x_t \ll \delta x_{rad} \rightarrow C_{I_s, \varphi_m} = \frac{|\langle \delta I_s^{out} \cdot \delta \varphi_m^{out*} \rangle|^2}{\langle |\delta I_s^{out}|^2 \rangle \langle |\delta \varphi_m^{out}|^2 \rangle} = 0.96$$

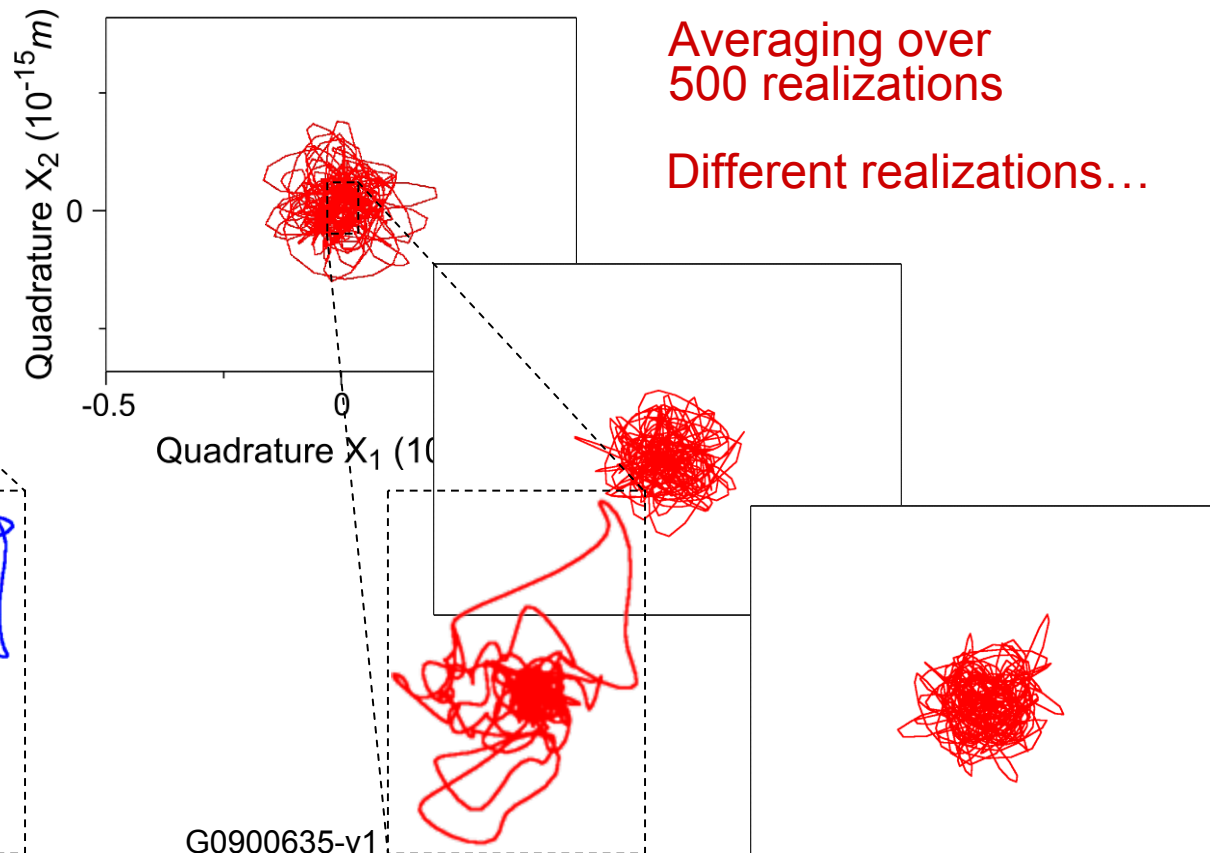
Observing quantum correlations?

$$\frac{\delta x_{\text{rad}}}{\delta x_T} \simeq 0.2$$

Signal intensity:

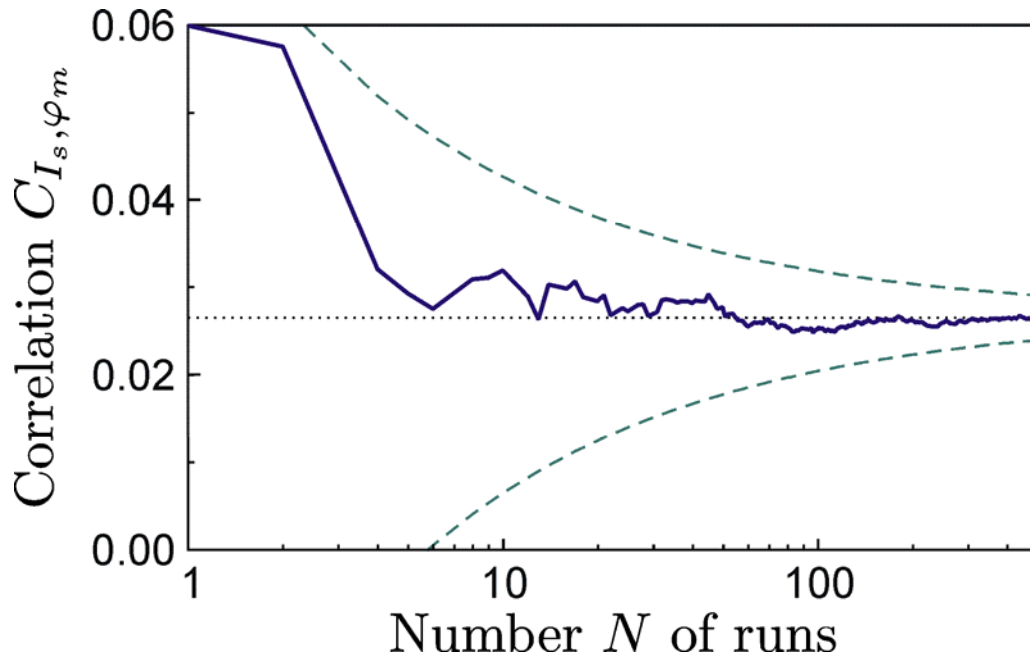


Displacements :



Detecting quantum correlations ?

Correlation function: $C_{I,\varphi} \simeq 0.03$ for $\frac{\delta x_{\text{rad}}}{\delta x_T} \simeq 0.2$

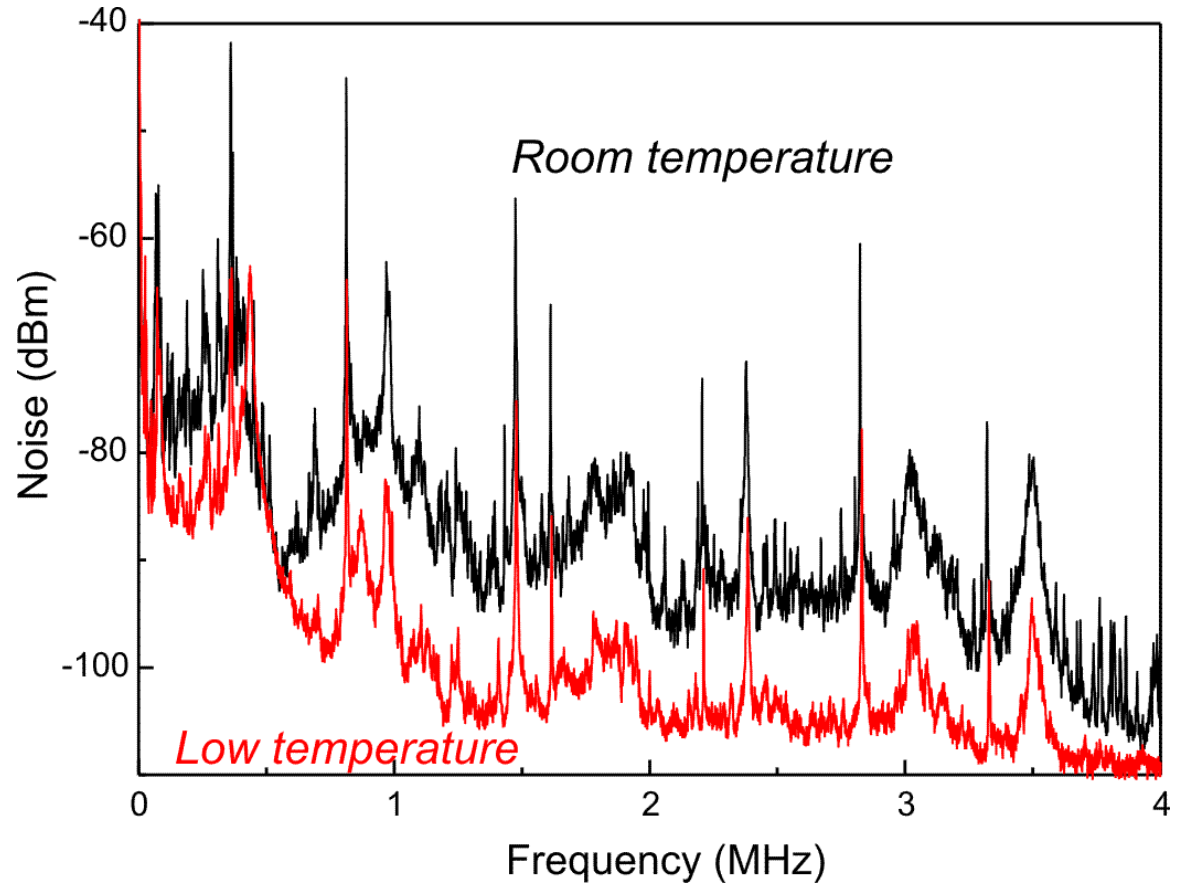


Quantum noise 2 orders of magnitude below but

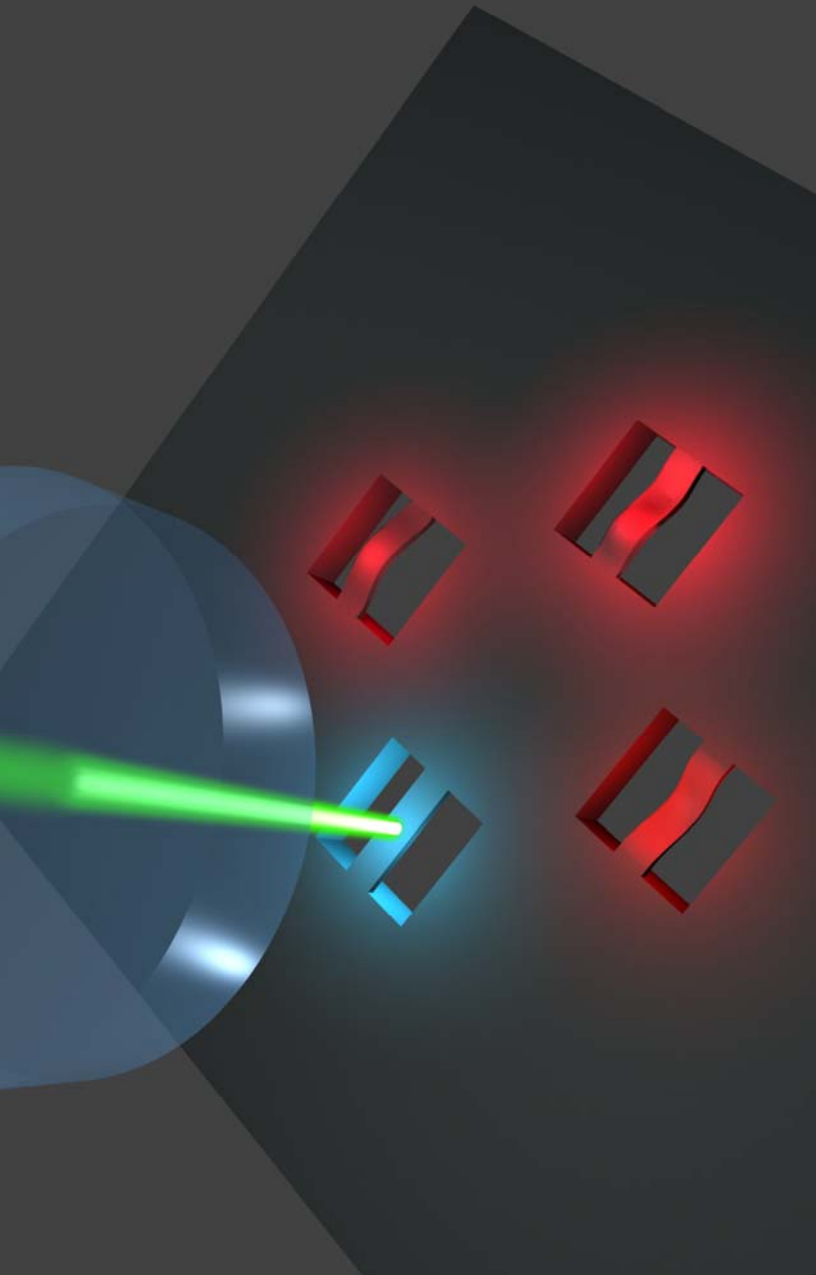
$$\frac{\delta x_{\text{rad}}}{\delta x_T} \simeq 0.1 \text{ at } 1 \text{ K}$$

Toward the observation of quantum correlations

Cryogenic operation



Thermal noise at low temperature (cryostat at 3.5 K) is reduced as compared to room temperature



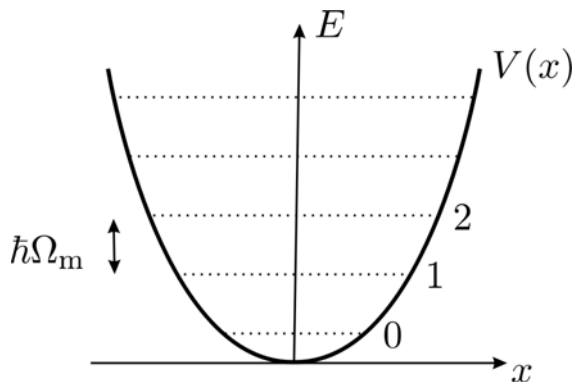
High sensitivity interferometric
measurements

Toward a QND measurement

Laser cooling of a microresonator

Reach the quantum regime of microresonator ?

Use the optomechanical coupling to reach and observe the quantum fundamental state of of macroscopic mechanical resonator



- Observation of residual quantum fluctuations:

$$M\Omega_m^2\Delta x^2 = \frac{\hbar\Omega_m}{2}$$

$$\Delta x \simeq 10^{-17} \text{ m}$$

$$(M \simeq 100 \mu\text{g}, \Omega_m/2\pi \simeq 1 \text{ MHz})$$

$|\psi(x)|^2$

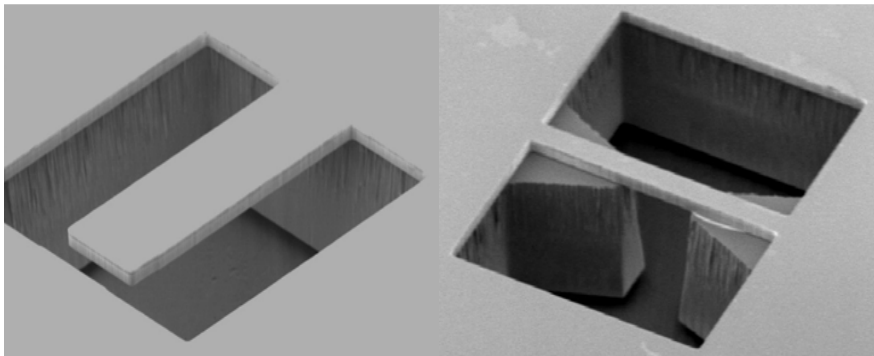


- Reach the quantum regime:

$$k_B T \leq \hbar\Omega_m \quad \begin{array}{l} 1 \text{ GHz} \leftrightarrow 50 \text{ mK} \\ 1 \text{ MHz} \leftrightarrow 50 \mu\text{K} \end{array}$$

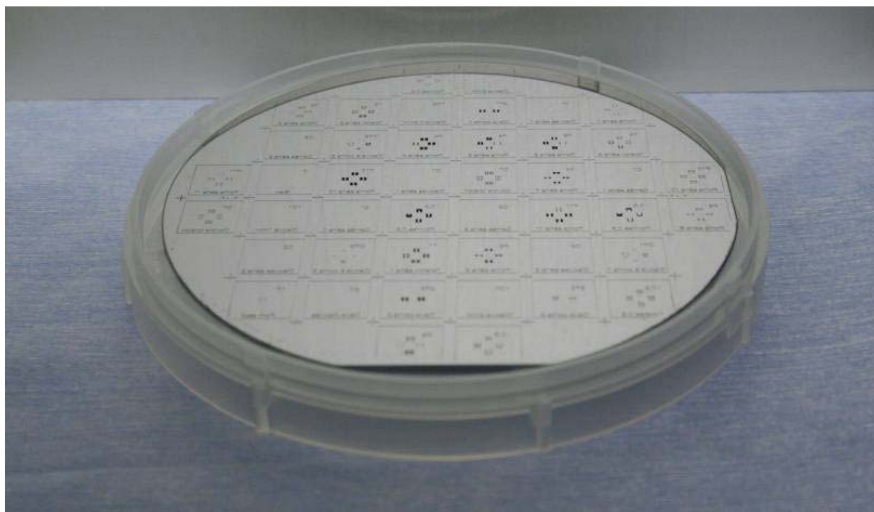
Cryogeny and laser cooling

Micro-resonator cavity

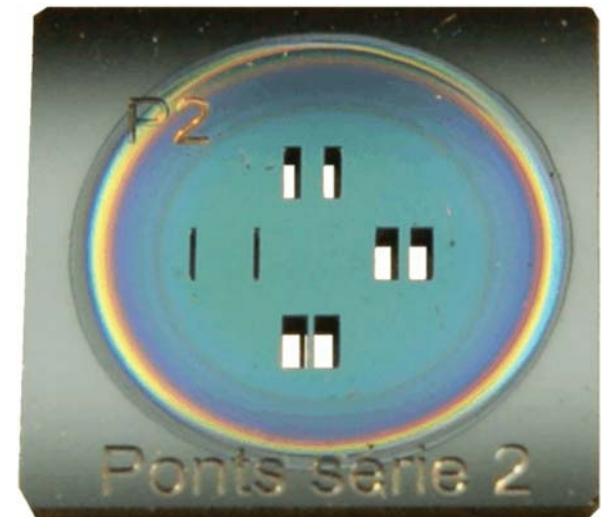


$1 \text{ mm} \times 400 \mu\text{m} \times 60 \mu\text{m}$
 $M \simeq 100 \mu\text{g}$

Micro-fabrication at ESIEE

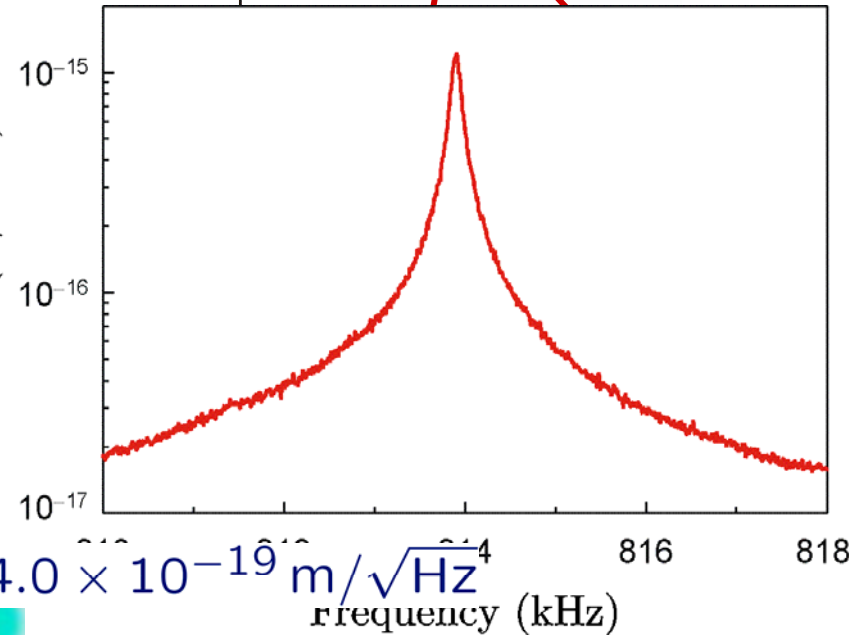
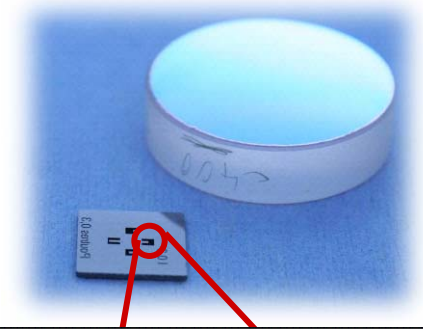
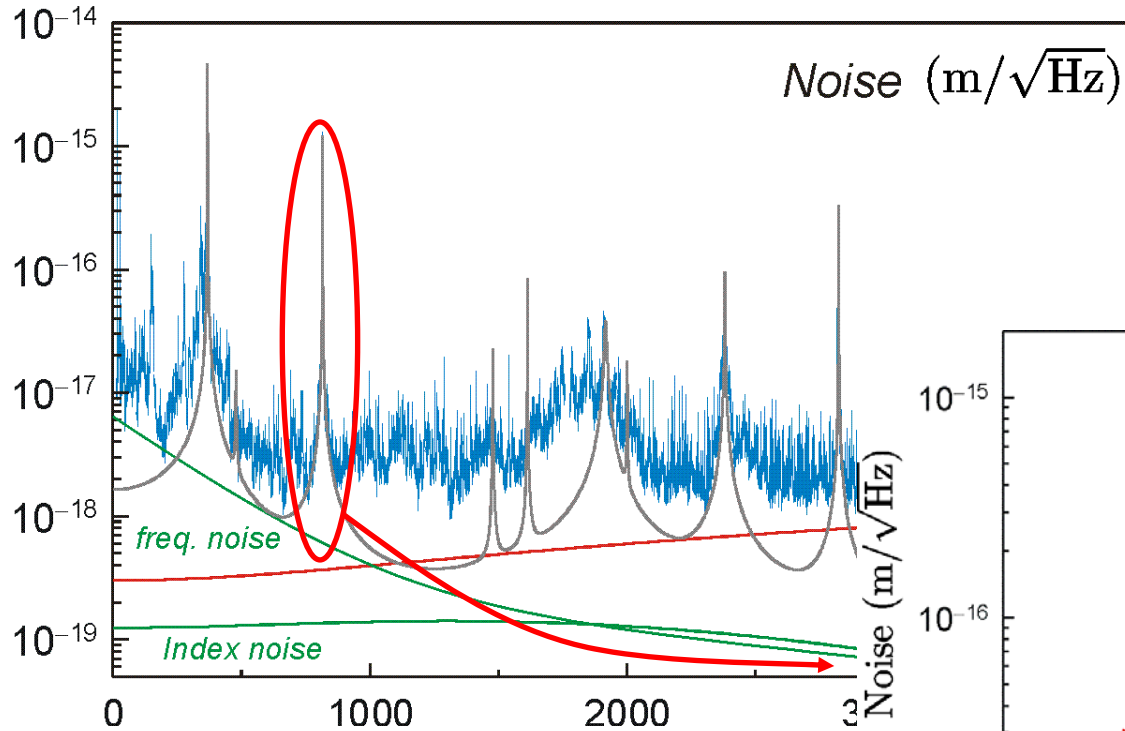


Optical coating at LMA (Virgo Lyon)
Optical metrology at ESPCI



Raw noise spectrum

Thermal noise at room temperature

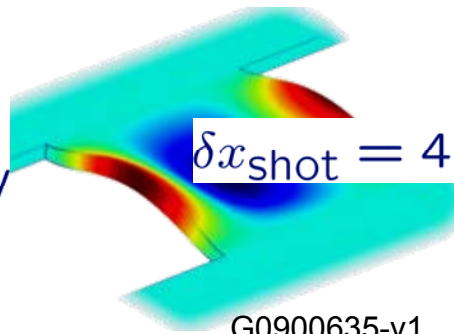


$$\Omega_m / 2\pi F \sim 814 \text{ kHz}$$

$$M = 30\,000$$

$$P_{in} = 1.5 \text{ mW}$$

$$Q =$$

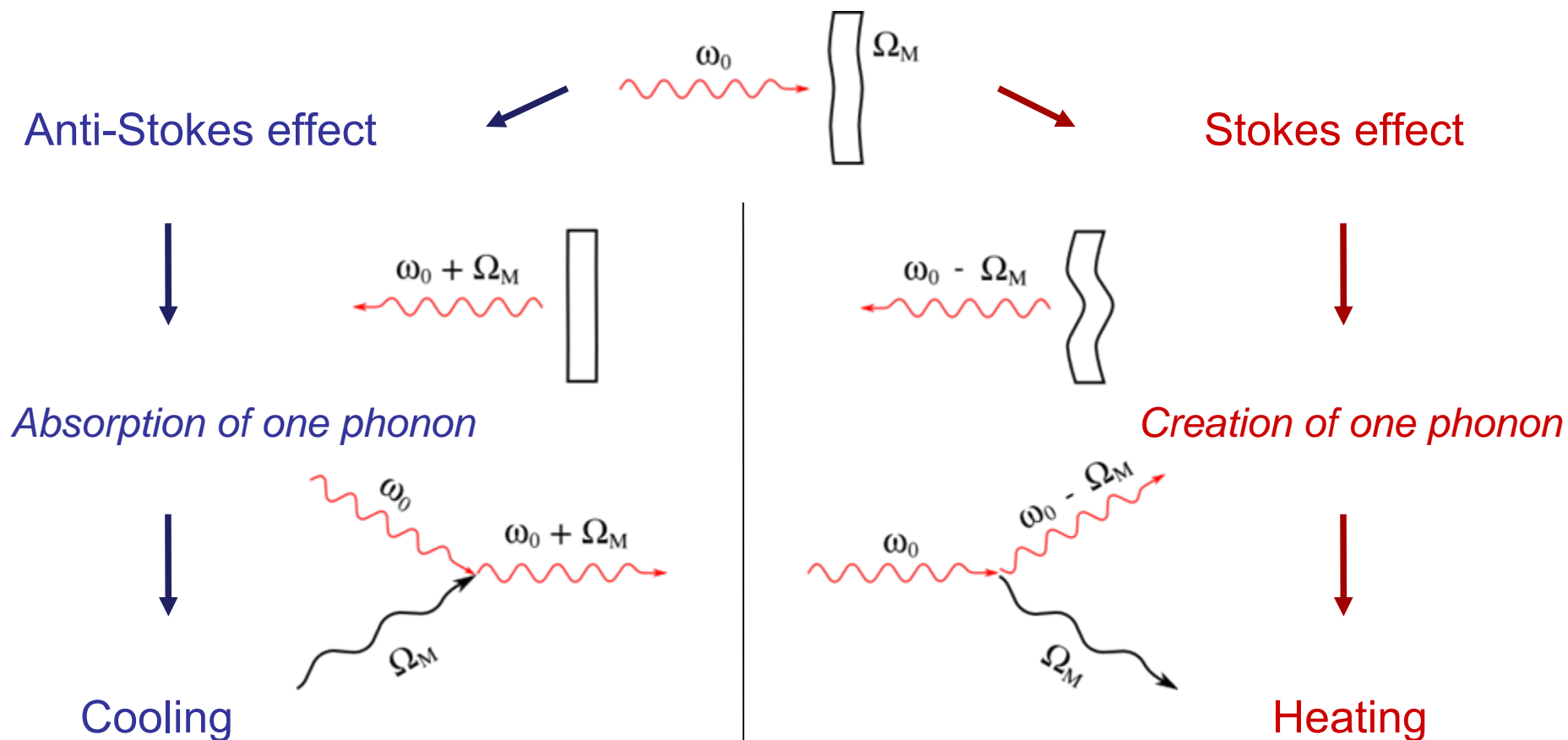


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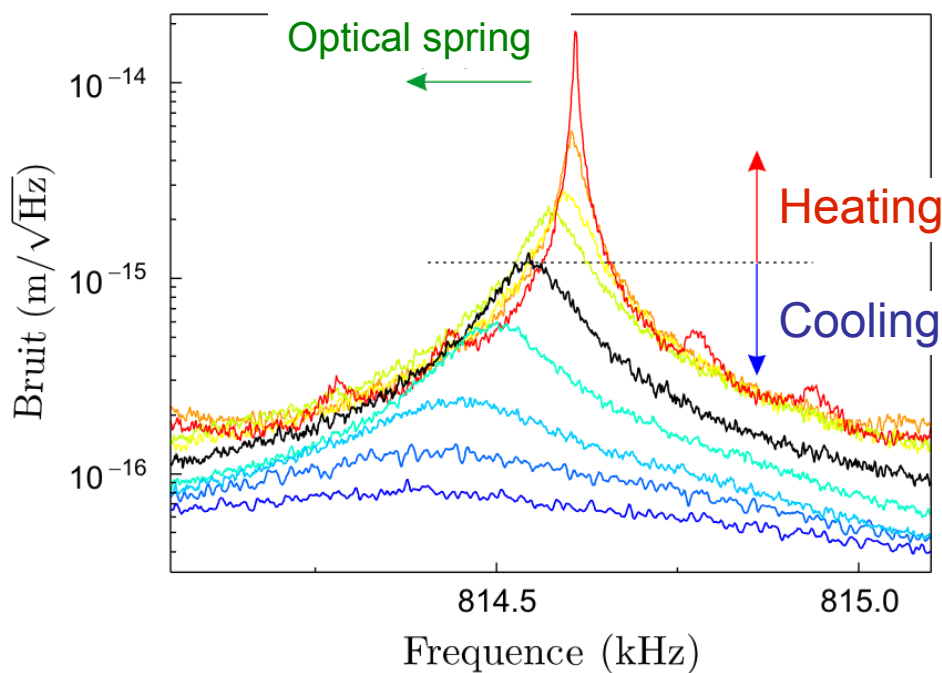
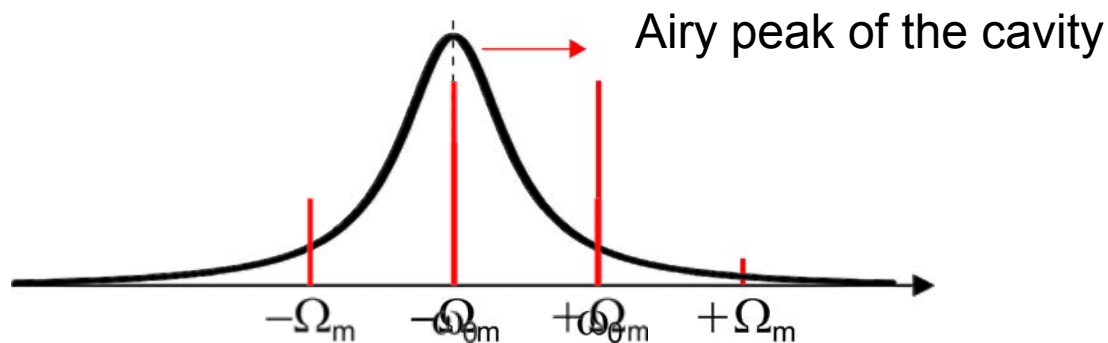
Phys. Rev. Lett. **97**, 133601 (2006)

Laser cooling effect

Energy transfer between optical and mechanical modes via the radiation pressure:



Laser cooling



Thermal noise spectrum

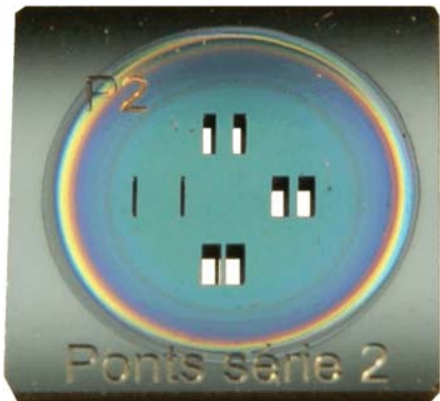
Negative detuning:
Anti-Stokes process amplified

Positive detuning :
Stokes process amplified

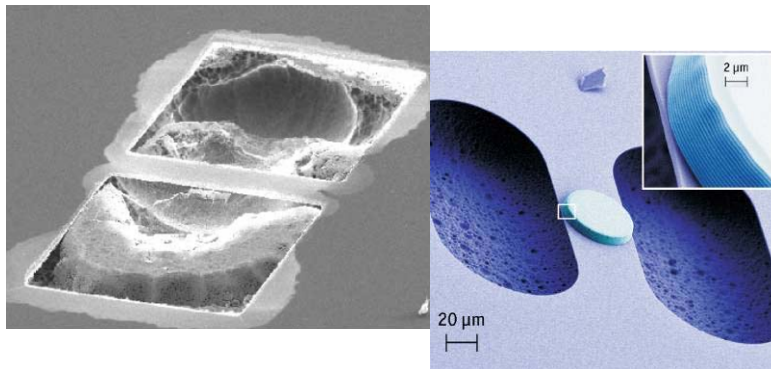
Cooling down to 10 K, heating up to 2000 K

Optomechanical system around the world

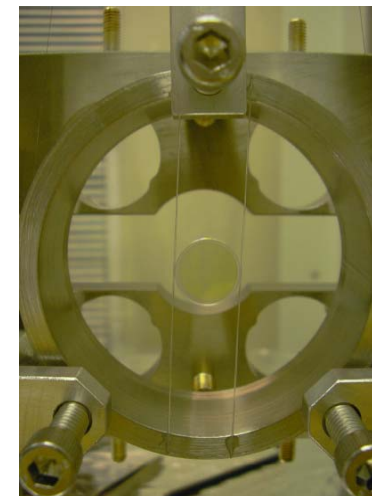
LKB



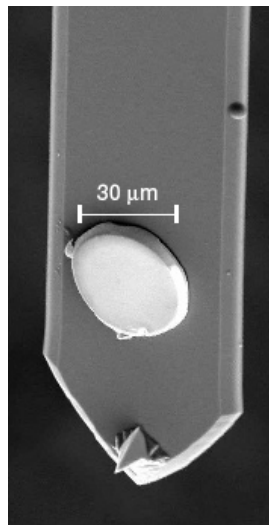
Vienna



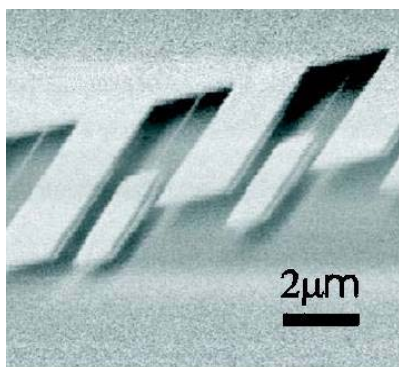
MIT - LIGO



UCSB



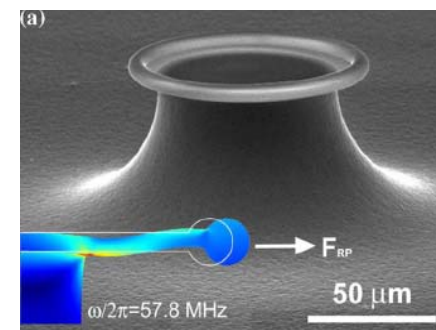
Munich



Yale



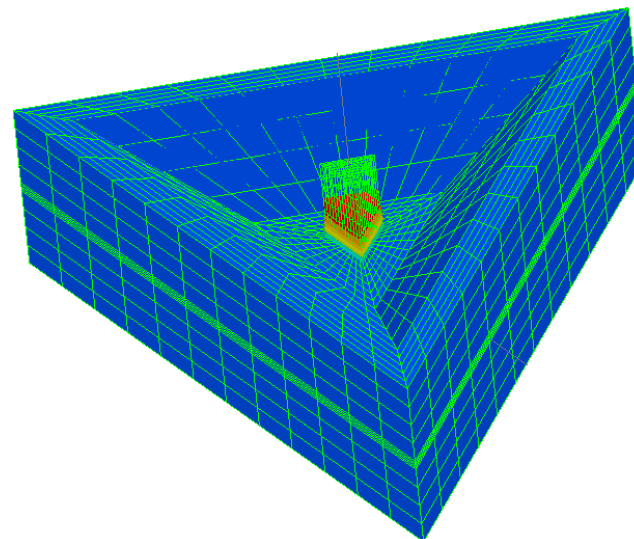
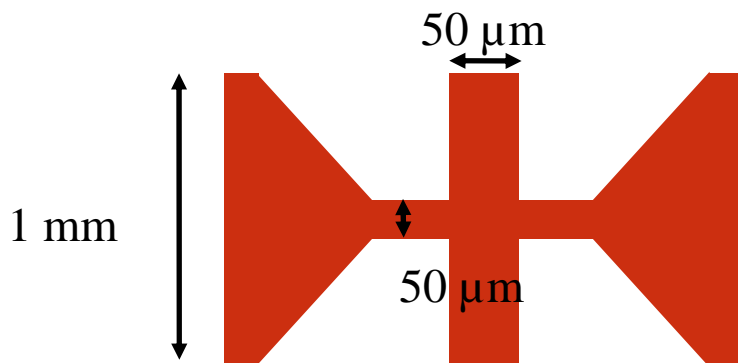
Garching / Caltech



Cooling down to $k_B T / \hbar \Omega_m < 100$ phonons

New generation of micro-mirrors

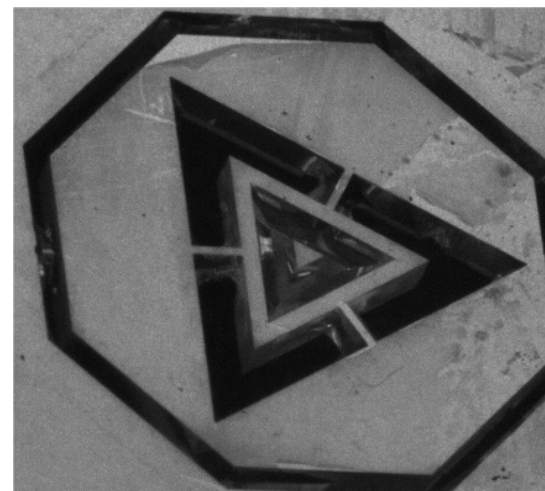
Symmetric pillar suspended by a thick membrane



Compression modes of the pillar

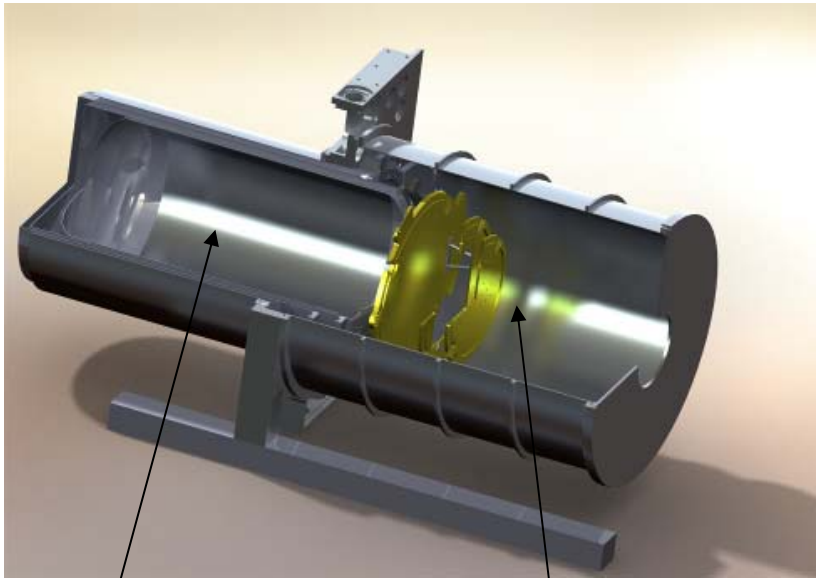
- *low mass, high mechanical isolation*
- *No stress in the coating area*
- *High mechanical Q factor*

Collaboration ANR with ONERA and LMA



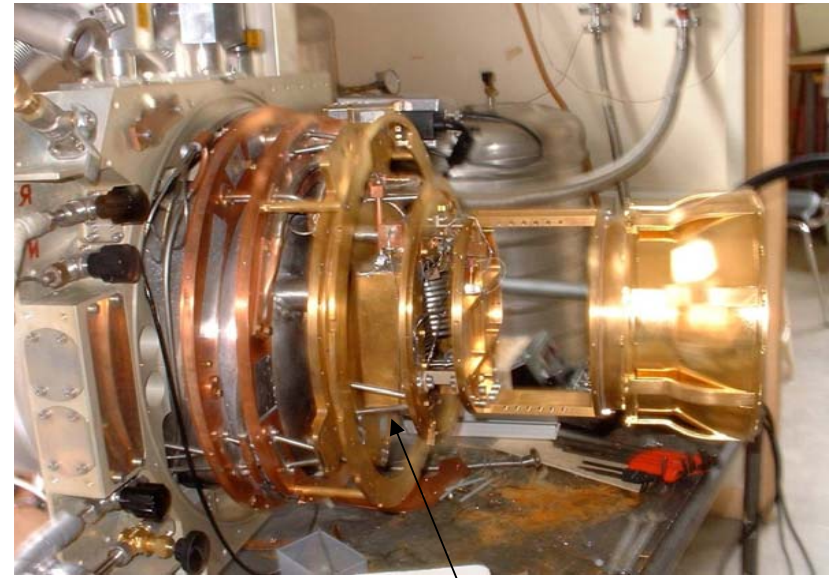
Cryogeny

Conception of a dilution He_3/He_4 cryostat
*limit temperature of 30 mK, horizontal configuration
to achieve a good mechanical stability*



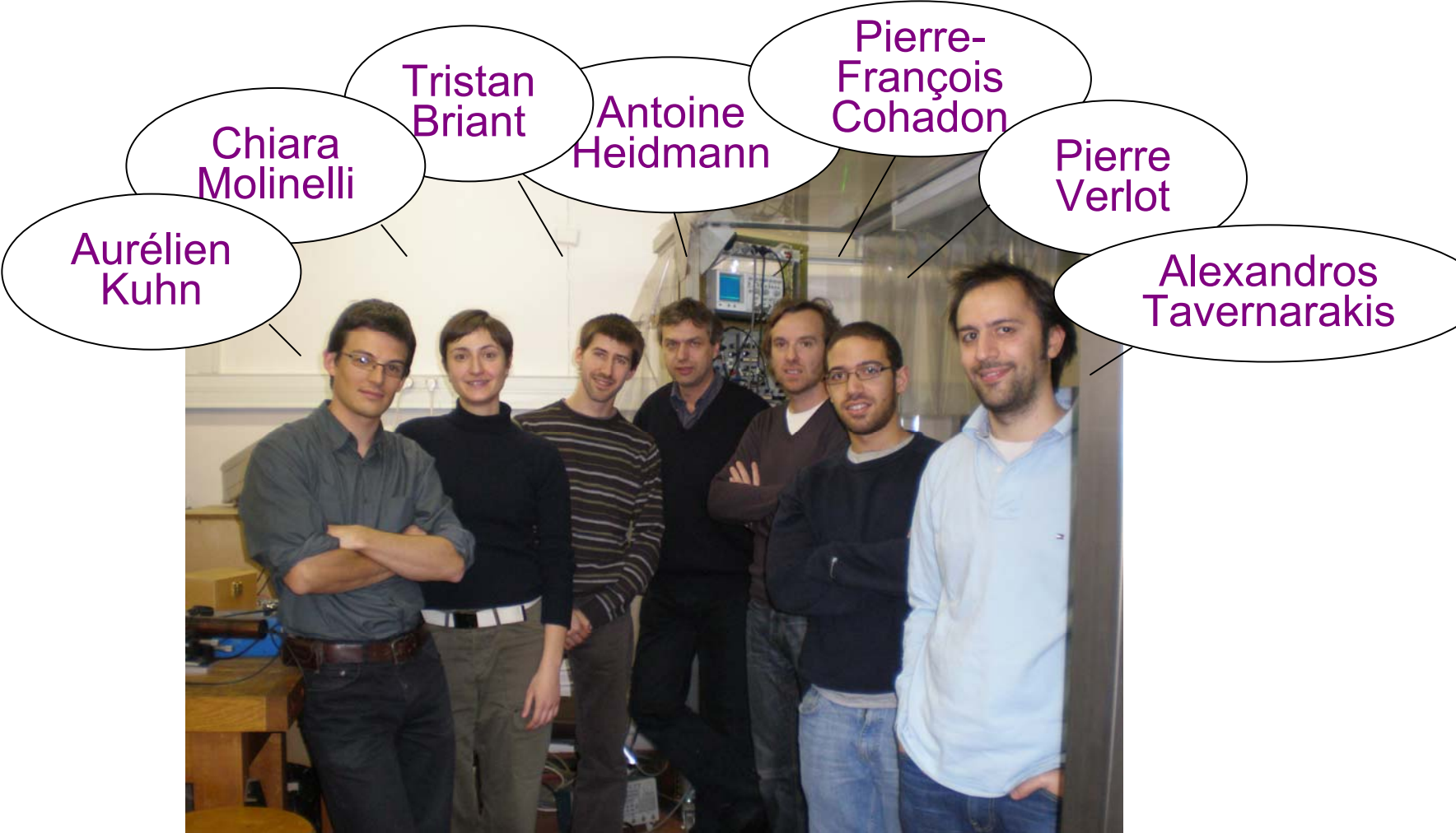
Helium tank

Sample chamber



Triangular suspensions

The « Mesure et bruits fondamentaux » team



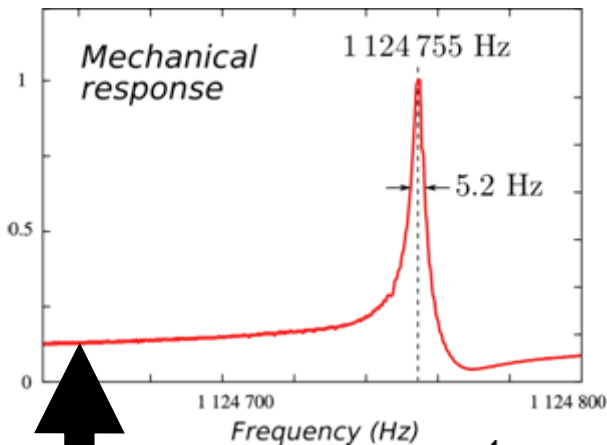
Detecting quantum correlations

For quantum radiation pressure noise: $\delta x_{\text{rad}} < \delta x_{\text{t}}$

but averaging should allow to uncover quantum correlations:

$$\langle \delta \varphi_m^{\text{out}} \cdot \delta I_s^{\text{out}} \rangle \simeq \frac{\mathcal{F}}{\lambda} \left(\underbrace{\langle \delta x_{\text{t}} \cdot \delta I_s^{\text{out}} \rangle}_{\rightarrow 0} + \langle \delta x_{\text{rad}} \cdot \delta I_s^{\text{out}} \rangle \right)$$

Experimental results

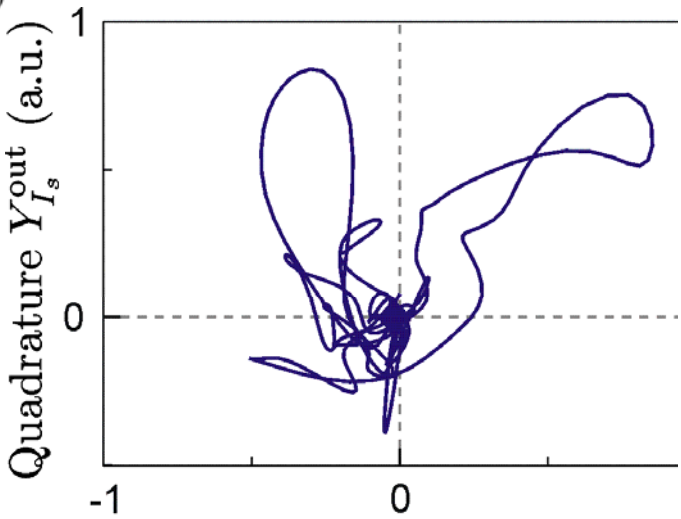


Intensity noise:

$$\delta I_s^{out}(t) = X_{I_s}^{out}(t) \cos(\Omega_c t) + Y_{I_s}^{out}(t) \sin(\Omega_c t)$$

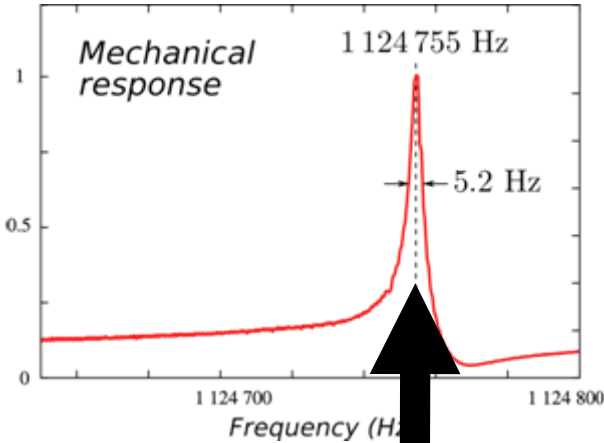
Phase noise:

$$\delta \varphi_m^{out}(t) = X_{\varphi_m}^{out}(t) \cos(\Omega_c t) + Y_{\varphi_m}^{out}(t) \sin(\Omega_c t)$$



$$\delta x_t \ll \delta x_{rad} \rightarrow C_{I_s, \varphi_m}^Q = \frac{|\langle \delta I_s^{out} \cdot \delta \varphi_m^{out*} \rangle|^2}{\langle |\delta I_s^{out}|^2 \rangle \langle |\delta \varphi_m^{out}|^2 \rangle} = 0.96$$

Correlations at resonance



The mechanical response has to be taken into account

